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## volume 42

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# analysis of units in electromagnetism 

F. PRIMDAHL

Abstract. To define a system of electromagnetic units uniquely, six basic quantities must be chosen. A suitable choice may include one basic unit and five constants, for example, or four basic units and two constants, Maxwell's equations are derived in a general form, independent of any particular choice of the six basic quantities. It is shown that the MKSA-formulation of the field equations involves three different unit systems.

In the relation $\overline{\mathrm{B}}=\mu_{0} \overline{\mathrm{H}}$, the symbols $\overline{\mathrm{B}}$ and $\overline{\mathrm{H}}$ are called a Giorgi-pair; other Giorgi-pairs are shown to exist in the MKSA-formulation of electromagnetic theory. Although of different dimensions, the members of a Giorgi-pair always describe the same physical phenomenon, and may thus be used arbitrarily, provided the Haines rule is observed. The general form of Maxwell's equations is derived for material bodies. It is shown that the MKSA-formulation uses two conflicting models for polarizable materials, leading to two electric and two magnetic fields, and the introduction of two units for each field in order to remove the constants from Maxwell's equations. Dimensional equations are replaced by more general expressions, called logometric formulas, including all six basic units and constants; they are used to analyze the existing unit systems.

## Introduction

For almost 100 years physicists have argued about units and unit systems in electromagnetism and the growing worldwide adoption of the SI†-units has revived this discussion (Rosser, 1969; Stopes-Roe, 1969; Temperly, 1969; Lovering, 1970).

One of the difficulties is, no doubt, that so many different terminologies exist and hence participants in the discussion do not use the same concepts in the same meaning. Much of the disagreement is thus believed to lie in the lack of proper means of communication.

The purpose of this paper is to provide a common denominator in the form of a set of electromagnetic equations written independently of any unit system, and to indicate the characteristic features of some of the existing systems. The equations are only derived as far as necessary to evaluate their general form and the selection is more or less arbitrary. It is, however, hoped that the examples cover a wide enough area to demonstrate the method and to indicate extensions.

The notation is very close to that of O'Rahilly (1965) whose treatment of electromagnetism, units, and dimensions has been the basic source of information. His viewpoint is that the symbols in the physical equations stand for pure numbers representing the ratios between the measured quantities (measure-ratios) and some chosen unit quantities. He replaces the dimensions by so-called logometric formulas giving the

[^0]Résumé. Pour donner une définition unique d'un système d'unités électromagnétiques, il faut choisir six quantités de base. On peut choisir, par exemple, une unité de base et cinq constantes ou quatre unités de base et deux constantes. Les équations de Maxwell ont été établies, sous une forme générale, indépendamment de tout choix particulier des six quantités de base. La présente étude démontre que dans le système M.K.S.A. la formulation des équations du champ électromagnétique fait intervenir trois systèmes d'unités différents,

Dans l'équation $\bar{B}=\mu_{0} \bar{H}$, les symboles $\bar{B}$ et $\bar{H}$ sont appelés paire de Giorgi; l'auteur démontre qu'il existe d'autres paires de ce genre dans la formulation en M.K.S.A. de la théorie électromagnétique. Bien que de dimensions différentes, les éléments d'une paire de Giorgi décrivent toujours le même phénomène physique et peuvent donc être appliqués de façon arbitraire, à condition d'observer la règle de Haines. La forme générale des équations de Maxwell est établie pour les corps matériels. L'auteur montre que la formulation selon le système M.K.S.A. emploie deux modèles contradictoires pour les matières polarisables, $d^{\prime}$ où deux champs électriques et deux champs magnétiques et l'introduction de deux unités pour chacun de ces champs afin d'éliminer les constantes des équations de Maxwell. Les équations de dimensions ont été remplacées par des expressions plus générales que l'auteur nomme formules logométriques, qui font intervenir les six unités et constantes de base; ce sont ces formules qui one été utilisées pour analyser les systèmes d'unités existants.
number by which a measure-ratio has to be multiplied if the basic units or constants are changed.

## Basic units

An earlier paper (Primdahl, 1970) has described, how two constants $\delta$ and $\gamma$ have to be included in Newton's second law and the mass attraction law to generalize them, and similarly how three constants $\alpha, \beta$, and $a$ are necessary to generalize the electromagnetic equations.

$$
\begin{array}{lll}
\mathrm{F}=\delta \mathrm{M} \frac{\mathrm{~d}^{2} \mathrm{r}}{\mathrm{dt}^{2}} & \text { Newton II } & \ldots .1 \\
\mathrm{~F}=\gamma \frac{\mathrm{MM}^{\prime}}{\mathrm{r}^{2}} & \begin{array}{l}
\text { Newton's law of gravitational } \\
\text { attraction }
\end{array} & \ldots .2 \\
\mathrm{~F}=\frac{\mathrm{qq}}{} \mathrm{qq}^{\prime} & \begin{array}{l}
\text { Coulomb's law for } \\
\text { electric charges }
\end{array} & \ldots .3 \\
\mathrm{~F}=\frac{\mathrm{mm}^{\prime}}{\alpha \mathrm{r}^{2}} & \text { for magnetic poles } & \ldots .4
\end{array}
$$

Electric current is the time-rate of charge transported through a cross-sectional area of the conductor

$$
\begin{equation*}
\mathrm{I}=\frac{\mathrm{dq}}{\mathrm{dt}} \tag{5}
\end{equation*}
$$

and magnetic field strength or field intensity is introduced as

$$
\mathrm{H}=\frac{\mathrm{F}}{\mathrm{~m}}
$$

the ratio between the force on a magnetic pole and its pole strength.

The magnetic field strength $\mathrm{d} \overline{\mathrm{H}}$ from a current element Ids at the distance $\mathrm{r}=\overline{\mathrm{r}} \stackrel{\rightharpoonup}{\mathrm{r}}$ is proportional to

$$
\frac{I \overrightarrow{d s} \times \hat{r}}{\mathbf{r}^{2}}
$$

so that the field strength at the centre of a circular current loop, radius $r$, carrying the current $I$ is by integration

$$
H=\frac{2 \| I}{a \cdot \frac{1}{i}}
$$

The constants of proportionality $\delta, \gamma, \alpha, \beta$, and $\varepsilon$ are basic in the same sense as the units for length, mass and time are basic, because they are necessary to uniquely determine the unit system. In mechanics we introduce a unit length, a unit mass, and a unit time. The value of one of the constants $\delta$ or $\gamma$ is then agreed upon internationally, and then the determination of the other is a matter of laboratory measurements. If both the constants $\delta$ and $\gamma$ were fixed by international agreement then only two basic units, e.g. mass and time, would be needed. Similarly, if $\alpha$ and $\beta$ are chosen in electromagnetism then $a$ and all the electromagnetic units may be determined experimentally, or if a fourth electromagnetic unit is introduced only one of the constants $\alpha, \beta$ or $a$ has to be chosen.

The seven equations (Equations 1 to 7) contain 13 unknowns so it is necessary to choose six of the 13 unknowns to solve the system. Thus we need, not three or four, but six basic "units" to define uniquely our unit system.

It is emphasized that the letter symbols in the algebraic Equations 1 to 7 represent pure algebraic numbers, e.g. the number $M$ in Equation 1 is thus obtained by comparing the mass in the acceleration experiment to a standard mass. Likewise, if the measure-ratio for one mass can be determined then the measure-ratio for all masses can be determined. Hence for the purpose of counting the number of equations and the number of unknowns all the measure-ratios for mass count for one unknown.

It is interesting to note that as there are only five constants ( $\delta, \gamma, \alpha, \beta$, and $a$ ) we cannot determine a unit system by fixing the values of the constants only; at least one actual physical sample, for example mass, is needed as a starting point. The six basic quantities cannot be chosen at random from the 13 unknowns; only a combination which does not violate any of the Equations 1 to 7 and 28 given below will be legal. An illegal choice will make the system indeterminate, as can be shown by solving for the remaining unknowns.

The claim ${ }^{\dagger}$ that the MKSA-system is defined uniquely by the choice of the four basic units metre, kilogram, second, and ampere is thus not justified. Equation 1 is always stated with $\delta=1$ giving a fifth basic "unit" and the definition of the ampere is written in a form tacitly stating $a=4$ | which then is our sixth basic "unit".

From Equations 1 to 7 the formula for the force between two current elements is derived to be

$$
\overline{d^{2} F}=\frac{\beta}{a^{2}} \cdot \frac{I_{1} \overline{d s_{1}} \times\left(I_{2} \overline{d s_{2}} \times \hat{r}\right)}{r^{2}}
$$

and it is seen that the unit for I may be fixed by specifying the force and the geometry in a standard experiment.

However, in the MKSA-system Equation 8 is normally stated in another form

$$
\overline{d^{2} F}=\frac{\mu_{0} I_{1} \overline{d s_{1}} \times\left(I_{2} \overline{d s_{2}} \times \hat{r}\right)}{4}
$$

where $\mu_{0}=\beta / a$, as will be shown later. Implicit in the form of Equation 8 a is thus the tacit assumption

$$
a=4
$$

and this is the sixth basic "unit".

## Electrostatics

Starting from Equation 3 electric field strength is defined as the force per unit charge

$$
\bar{E}=\frac{\bar{F}}{q}=\frac{q^{\prime}}{\alpha \cdot r^{2}} \hat{r}
$$

If we change the electrostatic constant in Equation 3 from $\alpha$ to $\alpha^{*}$ then E will change to $\mathrm{E}^{*}$ and q to $\mathrm{q}^{*}$. Here and in the following F is unchanged as we do not change the mechanical units.

$$
\mathrm{F}=\frac{\mathrm{q}^{*} \mathrm{q}^{\prime *}}{\alpha^{*} \mathrm{r}^{2}}=\frac{\mathrm{q} \mathrm{q}^{\prime}}{\alpha \mathrm{r}^{2}}
$$

and from this

$$
\frac{q^{*}}{q}=\sqrt{\frac{\alpha^{*}}{\alpha}}
$$

As

$$
\mathrm{F}=\mathrm{q} \cdot \mathrm{E}=\mathrm{q}^{*} \mathrm{E}^{*}
$$

[^1]we have
$$
\frac{E^{*}}{E}=\frac{q}{q^{*}}=\sqrt{\frac{\alpha}{\alpha^{*}}}
$$

The flux of electric field out through a sphere with radius $r$ centred around a charge $q$ is, by integration of Equation 9:

$$
\Psi=\int_{\text {sphere }} \bar{E} \cdot \overline{\mathrm{da}}=\int_{\text {sphere }} \frac{q}{\alpha r^{2}} d a=\frac{4 \|}{\alpha} q
$$

This is a special case of the more general Gauss' law:

$$
\Psi=\frac{4 \|}{\alpha} \int \rho d v
$$

Vol
or stated in differential form

$$
\nabla \cdot \bar{E}=\frac{4 \pi}{\alpha} \rho
$$

where $\rho$ is the measure-ratio for charge density.
Electric current in a conductor is introduced by Equation 5. If $\mathbf{A}$ is the cross-sectional area of the conductor then the current density is

$$
\mathrm{J}=\frac{\mathrm{I}}{\mathrm{~A}}
$$

and in general a current density vector is introduced as the current per unit area oriented perpendicularly to the direction of flow of charge.

As the current flowing out of a closed surface is equal to the decrease of charge inside the surface the following continuity equation is valid

$$
\nabla \cdot \overline{\mathrm{J}}=-\frac{\partial \rho}{\partial \mathrm{t}}
$$

If we change the electrostatic constant from $\alpha$ to $\alpha^{*}$ then J becomes J* and we have

$$
\frac{\mathrm{J}}{\mathrm{~J}^{*}}=\frac{\rho}{\rho^{*}}=\sqrt{\frac{\alpha}{\alpha^{*}}}
$$

The same transformation relation is valid for the current I

$$
\frac{I}{I^{*}}=\sqrt{\frac{\alpha}{\alpha^{*}}}
$$

## Magnetostatics

Despite intensive search for magnetic monopoles they have not been found (Fleischer, 1969), and they certainly do not
play any role in the magnetostatic effects upon which the theory of electromagnetism is based.

This is often stated as an argument against explicitly writing Equation 4. However, it must be realized that the (mathematical) concept of a magnetic pole is extremely useful in describing forces between magnets, and inevitably every textbook introciuces this concept when dealing with magnetized materials. So when the magnetic pole is introduced anyway, why not admit it openly by stating Equation 4 from the beginning taking advantage of its great pedagogic value:

$$
\mathrm{F}=\frac{\mathrm{mm}}{\beta \cdot \mathrm{r}^{2}}
$$

Changing the magnetostatic constant from $\beta$ to $\beta^{*}$ changes $m$ to $\mathrm{m}^{*}$ and we have the relation

$$
\frac{\mathrm{m}}{\mathrm{~m}^{*}}=\sqrt{\frac{\beta}{\beta^{*}}}
$$

Magnetic field strength is introduced as

$$
\mathrm{H}=\frac{\mathrm{F}}{\mathrm{~m}}
$$

which gives

$$
\stackrel{\mathrm{H}}{\mathrm{H}^{*}}=\sqrt{\frac{\beta^{*}}{\beta}}
$$

for a change of $\beta$ to $\beta^{*}$.
The flux of the magnetic field out through a sphere is

$$
\Phi=\int \overline{\mathrm{H}} \cdot \overline{\mathrm{da}}=0
$$

sphere
as magnetic poles always occur in opposite pairs. The differential form of this equation is

$$
\nabla \cdot \overline{\mathrm{H}}=0
$$

## Electromagnetics

The field at the centre of a circular conductor can be measured by magnetostatic experiments (Gauss' method) and it is found that

$$
\mathrm{H}=\frac{2 \pi}{\mathrm{a}} \cdot \frac{\mathrm{I}}{\mathrm{r}}
$$

where the factor $2 \pi$ is due to the geometry as stated in the explanation to Equation 7.

This offers a magnetostatic definition of current as opposed to the electrostatic definition in Equation 5:

$$
\mathrm{H}=2 \pi \frac{\mathrm{I}_{\mathrm{M}}}{\mathrm{r}}
$$

If $\alpha=1$ then $I=I_{E}$ is the measure-ratio in the electrostatic system and if $\beta=1$ at the same time then $I_{M}$ is the measure-ratio in the electromagnetic system; now, from a list of conversion factors between E.M.U. and E.S.U. (ASTM Metric Practice Guide; Maxwell, 1954, Art. 787) it can be verified that for the same current

$$
\frac{I_{E}}{I_{M}}=c
$$

where $c$ is equal to the speed of light.
If we want to use $I_{E}$ in Equation 26a we then have to write

$$
\mathrm{H}_{\mathrm{M}}=\frac{2 \boldsymbol{q}^{\mathrm{I}_{\mathrm{E}}}}{\mathrm{c}}
$$

where $H_{M}$ is the measure-ratio for the magnetic field when $\beta=$ 1.

For $\alpha=1$ and $\beta=1$ we are thus forced to put $a=c$, and this is the characteristic of the Gaussian system.

Changing $\alpha$ from 1 to $\alpha^{*}$ and $\beta$ from 1 to $\beta^{*}$ we will have to change $a$ from $c$ to $a^{*}$ and thus

$$
\mathrm{H}^{*}=\frac{2 \mathbb{1}}{\mathrm{a}^{*}} \cdot \frac{\mathrm{I}^{*}}{\mathrm{r}}
$$

Using Equations 20 and 23 with $I=I_{E}, \alpha=1$, and $\mathrm{H}=\mathrm{H}_{\mathrm{M}}, \beta=1$ we get

$$
H^{*}=\frac{H_{M}}{\sqrt{\beta^{*}}}=\frac{2 \rrbracket}{a^{*}} \cdot \frac{I^{*}}{r}=\frac{2 \Pi}{a^{*}} \cdot \frac{I_{E}}{r} \sqrt{\alpha^{*}}
$$

and from this

$$
\mathrm{H}_{\mathrm{M}}=\frac{\frac{2 ๆ \mathrm{I}_{\mathrm{E}} / \mathrm{r}}{\mathrm{a}^{*}}}{\sqrt{\alpha^{*} \mathrm{~b}^{*}}}
$$

By comparison to Equation 26b it is seen that the general limitation on the three constants $a, \alpha$, and $\beta$ is

$$
\frac{\mathrm{a}}{\sqrt{\alpha \beta}}=\mathrm{c}
$$

It must be remembered that $a, \alpha$, and $\beta$ stand for pure algebraic numbers and that $c$ is a number too as it is determined as the ratio between the two measure-ratios $I_{E}$ and $\mathrm{I}_{\mathrm{M}}$, themselves pure algebraic numbers.

The magnetic field at the centre of a circular conductor of radius $r$ carrying the current $I$ is, by Equation 7 or 26 c

$$
H=\frac{2 \phi}{a} \cdot \frac{I}{r}
$$

The force on a magnetic pole, $m$, would then be

$$
\mathrm{F}=\mathrm{H} \cdot \mathrm{~m}=\frac{2 ף}{a} \cdot \frac{\mathrm{I}}{\mathrm{r}} \cdot \mathrm{~m}
$$

and an equal, opposite force would exist on the conductor. This is the classical concept of 'action at a distance' between the magnetic pole and the current-carrying conductor. The force on the conductor may, however, also be considered a direct action from the field around it, in which case

$$
\mathrm{F}=\frac{2 \pi}{\mathrm{a}} \frac{\mathrm{l}}{\mathrm{r}} \cdot \mathrm{H}^{\prime} \cdot \beta \cdot \mathrm{r}^{2}=\frac{\beta}{\mathrm{a}} 2 \Pi \mathrm{I} \cdot \mathrm{H}^{\prime} \cdot \mathrm{r},
$$

where

$$
\mathrm{H}^{\prime}=\frac{\mathrm{m}}{\beta \mathrm{r}^{2}}
$$

is the field at the circular conductor from the magnetic pole placed at its centre. Equation 31 may be derived assuming that the force $\overline{\mathrm{dF}}$ on a current element $\overline{\mathrm{ds}}$ in a field $\overline{\mathrm{H}}$ is

$$
\mathrm{d} \stackrel{\rightharpoonup}{\mathrm{~F}}=\frac{\beta}{\mathrm{a}} \mathrm{I} \overline{\mathrm{ds}} \times \stackrel{\rightharpoonup}{\mathrm{H}}
$$

At the distance $r$ from a magnetic point-pole $m$ the field is

$$
\overrightarrow{\mathrm{H}}=\frac{\mathrm{m}}{\beta \mathrm{r}^{2}} \hat{\mathrm{r}}
$$

If this pole is at the centre of the current loop (current I, radius $r$ ) then the field is constant along the conductor and the current element I $\overline{\mathrm{ds}}$ is perpendicular to $\overline{\mathrm{H}}$; using $\mathrm{ds}=\mathrm{rd} \theta$ in Equation 33 we get

$$
F=\frac{\beta}{a} \cdot I \cdot \frac{m}{\beta r^{2}} \int_{0}^{2 \rrbracket} \mathrm{rd} \theta=\frac{2 \llbracket}{a} \frac{I}{r} \cdot m
$$

which is the same as Equation 30, i.e. Equation 33 is a correct form of the force equation between a current element and a magnetic field.

The field $\mathbf{H}$ in Equation 33 may be generated by another current element $I_{1} \overline{\mathrm{ds}}_{1}$ at the distance $\overline{\mathrm{r}}=\overline{\mathrm{r}} \cdot \mathrm{f}$ from I ds; using Equation 7 and the preceding remarks we get

$$
\mathrm{d} \overline{\mathrm{H}}_{1}=\frac{\mathrm{I}_{1}}{\mathrm{a}} \frac{\overline{\mathrm{ds}} \times \hat{\mathrm{r}}}{\mathrm{r}^{2}}
$$

which inserted into Equation 33 gives

$$
d^{2} \bar{F}=\frac{\beta}{a^{2}} \frac{\overline{\mathrm{ds}} \times\left(\mathrm{I}_{1} \overline{\mathrm{ds}_{1}} \times \hat{\mathrm{r}}\right)}{\mathrm{r}^{2}}
$$

This is Equation 8 where $\hat{f}$ is a unit vector along $\overline{\mathrm{r}}$.

## Electrodynamics

From the experiments of Faraday, Maxwell states the induction law as: (Maxwell, 1954, Art. 541)
"The total electromotive force acting round a circuit at any instant is measured by the rate of decrease of the number of lines of magnetic force which pass through it."

The "total electromotive force" is the line-integral of the electric field strength along the closed circuit and the "number of lines of magnetic force which pass through it" is the flux of the magnetic field vector through a surface bounded by the circuit. Stated in mathematical form this is

$$
\mathrm{V}=\int_{\begin{array}{l}
\text { closed } \\
\text { circuit }
\end{array}} \overline{\mathrm{E}} \cdot \overline{\mathrm{ds}} \text { proportional to }-\frac{\mathrm{d}}{\mathrm{dt}} \int_{\text {surface }} \overline{\mathrm{H}} \cdot \overline{\mathrm{da}} \ldots .38
$$

Using Equations 13 and 23 this can be written as

$$
\begin{aligned}
& \sqrt{\alpha} \int_{\begin{array}{l}
\text { closed } \\
\text { circuit }
\end{array}}=\overline{\mathrm{ds}}=-\mathrm{k} \cdot \sqrt{\beta} \frac{\mathrm{~d}}{\mathrm{dt}} \int \overline{\mathrm{H}} \cdot \overline{\mathrm{da}} \\
&
\end{aligned}
$$

where the proportionality-factor $k$ is independent of the unit system used, because $\sqrt{\alpha} \cdot \mathrm{E}$ and $\sqrt{\beta} \cdot \overline{\mathrm{H}}$ are independent of the units. (Throughout this treatment $F$ and the other mechanical units are assumed unchanged.)

The constant $k$ may be determined by experiments. For our purpose we put $\alpha=\beta=1$ and compare Equation 39 to Faraday's law in the Gaussian system. This gives $k=1 / c$ and from Equation 28 we get

$$
\int \overline{\mathrm{E}} \cdot \overline{\mathrm{ds}}=-\frac{\beta}{\mathrm{a}} \frac{\mathrm{~d}}{\mathrm{dt}} \int \overline{\mathrm{H}} \cdot \overline{\mathrm{da}}
$$

and the differential form is

$$
\nabla \times \overline{\mathrm{E}}=-\frac{\beta}{\mathrm{a}} \frac{\partial \overline{\mathrm{H}}}{\partial \mathrm{t}}
$$

Equation 40 may also be derived directly from Equation 33 by equating the mechanical and electric work involved in displacing a rigid, closed circuit in a static magnetic field (Slater and Frank, 1947, p. 210 f.).

## Maxwell's equations in general form

The field around a linear current I is calculated from Equation 36

$$
\mathrm{H}=\frac{2}{\mathrm{a}} \cdot \frac{\mathrm{I}}{\mathrm{r}}
$$

The field lines are concentric circles around I.
The line-integral of H along one of the closed circular field lines is

$$
\int_{\text {closed }} \overline{\mathrm{H}} \cdot \overline{\mathrm{ds}}=\frac{2}{\mathrm{a}} \mathrm{I} \int_{0}^{2 \pi} \frac{\mathrm{rd} \theta}{\mathrm{r}}=\frac{4 \|}{\mathrm{a}} \cdot \mathrm{I}
$$

curve

The general form of Equation 43 is Ampère law

$$
\int_{\text {closed }} \overline{\mathrm{H}} \cdot \overline{\mathrm{ds}}=\frac{4 \mathrm{I}}{\mathrm{a}} \Sigma \mathrm{I}
$$

curve
where $\Sigma$ I is the total encircled current. The differential form of Equation 44 is

$$
\nabla \times \overline{\mathrm{H}}=\frac{4 \pi}{\mathrm{a}} \overline{\mathrm{~J}}
$$

The Equations $41,16,25$, and 45 with an added term are the basic equations for the combined, time-varying magnetic and electric fields:

$$
\begin{gather*}
\nabla \times \overline{\mathrm{E}}=-\frac{\beta}{a} \frac{\partial \overline{\mathrm{H}}}{\partial \mathrm{t}} \\
\nabla \cdot \overline{\mathrm{E}}=\frac{4 \rrbracket}{\alpha} \rho  \tag{16}\\
\nabla \cdot \overline{\mathrm{H}}=0 \tag{25}
\end{gather*}
$$

and the incomplete equation

$$
\nabla \times \overline{\mathrm{H}}=\frac{4 \rrbracket}{\mathrm{a}} \mathrm{~J}
$$

Of course, the fact that the constant $c$ in Equation 28 is equal to the speed of light within the experimental error, inspired physicists to search for an electromagnetic theory of light. Maxwell saw that the electric and magnetic field vectors had to satisfy wave equations of the following form (Maxwell, 1954, Art. 784).

$$
\begin{align*}
& \nabla^{2} \overline{\mathrm{E}}-\frac{1}{\mathrm{c}^{2}} \frac{\partial^{2} \overline{\mathrm{E}}}{\partial \mathrm{t}^{2}}=\mathrm{f}(\mathrm{x}, \mathrm{y}, \mathrm{z}, \mathrm{t}) \\
& \nabla^{2} \overline{\mathrm{H}}-\frac{1}{\mathrm{c}^{2}} \frac{\partial^{2} \overline{\mathrm{H}}}{\partial \mathrm{t}^{2}}=\mathrm{g}(\mathrm{x}, \mathrm{y}, \mathrm{z}, \mathrm{t})
\end{align*}
$$

He could derive this from the four equations above if he added the term $\frac{\alpha}{a} \frac{\partial \overline{\mathrm{E}}}{\partial t}$ to the right-hand side of Equation 45 giving

$$
\nabla \times \bar{H}=\frac{4 \mathbb{I}}{a} \bar{J}+\frac{\alpha}{a} \frac{\partial \bar{E}}{\partial t}
$$

Applying $\nabla x$ and $\frac{\partial}{\partial t}$ to Equations 41 and 48 successively gives

$$
\begin{gather*}
\nabla x(\nabla \times \overline{\mathrm{E}})+\frac{\beta}{a} \frac{\partial}{\partial \mathrm{t}}(\nabla \times \overline{\mathrm{H}})=0 \\
\frac{\partial}{\partial \mathrm{t}}(\nabla \times \overline{\mathrm{E}})+\frac{\beta}{a} \frac{\partial^{2} \overline{\mathrm{H}}}{\partial \mathrm{t}^{2}}=0 \\
\nabla \mathrm{x}(\nabla \times \overline{\mathrm{H}})-\frac{\alpha}{\mathrm{a}} \frac{\partial}{\partial \mathrm{t}}(\nabla \times \overline{\mathrm{E}})=\frac{4 \|}{\mathrm{a}}(\nabla \times \overline{\mathrm{J}}) \\
\frac{\partial}{\partial \mathrm{t}}(\nabla \times \overline{\mathrm{H}})-\frac{\alpha}{\mathrm{a}} \frac{\partial^{2} \overline{\mathrm{E}}}{\partial \mathrm{t}^{2}}=\frac{4 \pi}{\mathrm{a}} \frac{\partial \overline{\mathrm{~J}}}{\partial \mathrm{t}}
\end{gather*}
$$

Substituting Equation 50 into Equations 51 and 52 into Equation 49 and using the vector-operator relation

$$
\nabla \times(\nabla \times \bar{A})=\nabla(\nabla \cdot \bar{A})-\nabla^{2} \overline{\mathbf{A}}
$$

cogether with Equations 16 and 25 gives the wave equations

$$
\begin{gather*}
\nabla^{2} \overline{\mathrm{H}}-\frac{\alpha \beta}{\mathrm{a}^{2}} \frac{\partial^{2} \overline{\mathrm{H}}}{\partial \mathrm{t}^{2}}=\frac{4 \|}{a}(\nabla x \overline{\mathrm{~J}})  \tag{54}\\
\nabla^{2} \overline{\mathrm{E}}-\frac{\alpha \beta}{\mathrm{a}^{2}} \frac{\partial^{2} \overline{\mathrm{E}}}{\partial \mathrm{t}^{2}}=\frac{4 \|}{\alpha} \nabla \rho+\frac{4 \llbracket \beta}{a^{2}} \frac{\partial \bar{J}}{\partial \mathrm{t}}
\end{gather*}
$$

where the constant in front of the time-derivatives of second order equals the reciprocal square of the speed of propagation in agreement with Equation 28.

Maxwell's modification of Equation 45 by adding the term $\frac{\alpha}{\alpha} \frac{\partial \overline{\mathrm{E}}}{\partial \mathrm{t}}$ is quite understandable as he knew exactly what he was looking for. It is a piece of ingenious mathematical intuition and it led to the prediction and discovery of electromagnetic waves. The modification has no measurable effect on the description of experiments with static and slowly varying electromagnetic fields from which the Equations $41,16,25$, and 45 were derived. Maxwell tried nevertheless after his successful accomplishment to explain and justify the modification in terms of the static electromagnetic concepts. This of course is impossible as it originates from an entirely different class of experiments. His attempt to explain $\frac{\partial \bar{E}}{\partial t}$ as "displacement current" is well known, and even in recent textbooks this notation is used, although it is clear that no current, i.e. transport of charge, is involved.

Lorenz (1867) suggested, two years after Maxwell, that the charge and current distributions in the Equations 15 and 44 should not be the instantaneous values, but the values r/c earlier where $r$ is the distance from the observed point to the charge or current. His suggestion also leads to a solution of Maxwell's equations.

Lorenz had no difficulties with the interpretation of the modification. In his paper (Lorenz, 1867) he says:
"But as the laws of induced currents, generally admitted and based on experiment, did not lead to the expected result, the question was whether it was not possible so to modify the laws assumed that they would embrace both the experiments on which they rest and the phenomena which belong to the theory of light......... It is at once obvious that the equations, which are deduced in a purely empirical manner, are not necessarily the exact expression of the actual law; and it will always be permissible to add several members or to give the equations another form, always provided these changes acquire no perceptible influence on the results which are established by experiment."

This is the introduction, in 1867, of the correspondence principle, which has proven so successful in the theory of relativity and in quantum mechanics. It states that any new theory must approach the classical theory asymptotically when dealing with classical phenomena. Nobody today maintains that the quantum mechanical equations can be understood entirely in terms of classical mechanics and yet Maxwell's "displacement current" is still defended in textbooks.

## Giorgi-pairs

The general form of Maxwell's equations independent of unit systems is

$$
\begin{gather*}
\nabla \mathrm{x} \overline{\mathrm{E}}+\frac{\beta}{\mathrm{a}} \frac{\partial \overline{\mathrm{H}}}{\partial \mathrm{t}}=0 \\
\nabla \cdot \overline{\mathrm{H}}=0 \\
\nabla \cdot \overline{\mathrm{E}}=\frac{4 \pi}{\alpha} \rho \\
\nabla \times \overline{\mathrm{H}}-\frac{\alpha}{\mathrm{a}} \frac{\partial \overline{\mathrm{E}}}{\partial \mathrm{t}}=\frac{4 \pi}{\mathrm{a}} \overline{\mathrm{~J}}
\end{gather*}
$$

If a new measure-ratio, $\overline{\mathbf{B}}$, for magnetic field is defined as

$$
\overline{\mathrm{B}}=\frac{\beta}{\mathrm{a}} \overline{\mathrm{H}}
$$

and a new measure-ratio for electric field

$$
\overline{\mathrm{D}}=\frac{\alpha}{\mathrm{a}} \overline{\mathrm{E}}
$$

then Equations 56 to 59 become

$$
\begin{array}{cc}
\nabla \times \overline{\mathrm{E}}+\frac{\partial \overline{\mathrm{B}}}{\partial \mathrm{t}}=0, & \nabla \cdot \overline{\mathrm{~B}}=0 \\
\nabla \times \overline{\mathrm{H}}-\frac{\partial \overline{\mathrm{D}}}{\partial \mathrm{t}}=\frac{4 \llbracket}{\mathrm{a}} \overline{\mathrm{~J}}, & \nabla \cdot \overline{\mathrm{D}}=\frac{4 \llbracket}{\mathrm{a}} \rho .
\end{array}
$$

This form of Maxwell's equations is independent of the constants $\alpha$ and $\beta$, but these are of course reintroduced by the Equations 60 and 61 and instead of the four equations (Equations 56 to 59) we now need the six equations (Equations 60 to 65 ).

The two relations (Equations 60 and 61) have been referred to as the Giorgi conditions (Stopes-Roe, 1969) and for purpose of the present discussion the two members of a Giorgi condition will be called a Giorgi-pair ${ }^{\dagger}$. In Equation 60 $\overline{\mathrm{B}}$ is the Giorgi-mate of $\overline{\mathrm{H}}$ and the process of transforming one to the other is called giorgization.

In discussing the effects of giorgization it is often necessary to distinguish between the two members of a Giorgi-pair; therefore if a Giorgi-pair is given

$$
\mathrm{G}_{2}=\frac{\beta}{\mathrm{a}} \cdot \mathrm{G}_{1}
$$

[^2]then $G_{1}$ is called the female member and $G_{2}$ the male member of the pair. ${ }^{\dagger}$ The same notation is used if the Giorgi-pair is related by
$$
\mathrm{G}_{2}=\frac{\alpha}{\mathrm{a}} \mathrm{G}_{1}
$$

Giorgization is not limited to the field vectors only. The magnetic moment of a current loop is (Stratton, 1941) introduced as

$$
\overline{\mathrm{i}_{\mathrm{m}}}=\mathrm{I} \cdot \mathrm{~A} \cdot \overline{\mathrm{n}}
$$

where I is the current, A the area of the loop, and $\overline{\mathrm{n}}$ a unit normal vector to A.

Others (Döring, 1948; and Bjerge, 1951) introduce the magnetic moment as

$$
\overline{m_{m}}=\frac{\beta}{a} \cdot I \cdot A \cdot \bar{n}
$$

Clearly $\overline{\bar{i}_{m}}$ and $\overline{m_{m}}$ are a Giorgi-pair as

$$
\overline{\mathrm{m}_{\mathrm{m}}}=\frac{\beta}{\mathrm{a}} \overline{\mathrm{i}_{\mathrm{m}}}
$$

Likewise magnetic poles, electric charges and all other electromagnetic measure-ratios may be giorgized.

An interesting feature of giorgization is that all formulas for force, torque, energy etc. contain both a male and female member of a giorgi-pair, side by side (both in numerator, or both in denominator). ${ }^{\dagger \dagger}$

The torque on a magnetic dipole moment in a magnetic field is

$$
\overline{\mathrm{T}}=\overline{\mathrm{m}_{\mathrm{m}}} \times \overline{\mathrm{H}}=\overline{\mathrm{i}_{\mathrm{m}}} \times \overline{\mathrm{B}}
$$

The force on an electric charge in an electric field is

$$
\overline{\mathrm{F}}=\mathrm{q} \cdot \overline{\mathrm{E}}=\mathrm{q}^{*} \cdot \overline{\mathrm{D}}
$$

where

$$
\mathrm{q}=\frac{\alpha}{\mathrm{a}} \cdot \mathrm{q}^{*}
$$

The work involved in moving a charge in an electric field is

$$
\mathrm{W}=\int \mathrm{q} \cdot \overline{\mathrm{E}} \cdot \mathrm{~d} \overline{\mathrm{r}}=\int \mathrm{q}^{*} \cdot \overline{\mathrm{D}} \cdot \mathrm{~d} \overline{\mathrm{r}}
$$

[^3]and the energy associated with a current
$$
\mathrm{P}=\mathrm{V} \cdot \mathrm{I}=\int_{\text {circuit }} \overline{\mathrm{E}} \cdot \mathrm{~d} \overline{\mathrm{~s}} \cdot \mathrm{I}=\int_{\text {circuit }} \overline{\mathrm{D}} \cdot \mathrm{~d} \overline{\mathrm{~s}} \cdot \mathrm{I} *
$$
where
$$
I=\frac{\alpha}{a} \cdot I^{*}
$$

In view of this the force formula (Coulomb's law) looks like a monstrosity, but replacing one of the charges by its Giorgi-mate overcomes this problem

$$
\mathrm{F}=\frac{\mathrm{q} \mathrm{q}^{\prime}}{\alpha \mathrm{r}^{2}}=\frac{\mathrm{q}^{*} \mathrm{q}^{\prime}}{\mathrm{a} \cdot \mathrm{r}^{2}}
$$

From these considerations it is clear that by giorgizing the proper measure-ratios according to the Haines male-female rule it is possible to completely eliminate the constants $\alpha$ and $\beta$ from all the electromagnetic formulas.

This elimination is of course only apparent as every quantity now is expressed by two measure-ratios related by one of the Giorgi conditions (Equation 66 or 67 ).

## Giorgi-transformation of a unit system

Starting from one unit system characterized by the constants $\alpha, \beta$, and $\alpha$ (the mechanical units are untouched) and consequently giorgizing all the measure-ratios will give two new unit systems characterized by $\alpha^{*}, \beta^{*}=\beta, a^{*}$ and $\alpha^{* *}=\alpha, \beta^{* *}, a^{* *}$.

## Coulomb's law for electric charges gives

$$
\mathrm{F}=\frac{\mathrm{q} \mathrm{q}^{\prime}}{\alpha \mathrm{r}^{2}}=\frac{\frac{\alpha}{\mathrm{a}} \mathrm{q}^{*} \cdot \frac{\alpha}{a} \mathrm{q}^{*^{\prime}}}{\alpha \mathrm{r}^{2}}=\frac{\mathrm{q}^{*} \mathrm{q}^{*^{\prime}}}{\frac{\mathrm{a}^{2}}{\alpha} \mathrm{r}^{2}}
$$

which means that

$$
\alpha^{*}=\frac{\mathrm{a}^{2}}{\alpha}=\mathrm{c}^{2} \beta
$$

using Equation 28. Similarly we get for $\beta^{* *}$

$$
\beta^{* *}=c^{2} \alpha
$$

and thus
and

$$
a^{* *}=\frac{a^{2}}{\beta}
$$

By giorgizing the original system

$$
\alpha, \beta, \underline{a}
$$

we thus express some of the formulas in the System (1)

$$
c^{2} \beta, \beta, \frac{a^{2}}{\alpha}
$$

and other formulas in the System (2)

$$
\alpha, c^{2} \alpha, \frac{a^{2}}{\beta}
$$

All three systems are proper unit systems as

$$
\frac{a^{2}}{\alpha \beta}=c^{2} \quad \text { Original system }
$$

$$
\begin{align*}
& \frac{a^{4} / \alpha^{2}}{c^{2} \beta \cdot \beta}=c^{2} \quad \text { System (1) } \\
& \frac{a^{4} / \beta^{2}}{\alpha^{2} c^{2} \alpha}=c^{2} \quad \text { System (2) }
\end{align*}
$$

If $\alpha, \beta$, and $a$ are the characteristic constants of the unit system of Equations 56 to 59 then $\alpha^{*}, \beta^{*}$, and $a^{*}$ given by Equation 84 are the constants of the unit system of Equations 64 and 65 , and $\alpha^{* *}, \beta^{* *}$, and $a^{* *}$ given by Equation 85 are the constants of the unit system of Equations 62 and 63. As the measure-ratio for current in Equation 64 is unchanged from that of Equation 59 it means that current in System (1) is defined by the magnetostatic units (e.g. Equation 7) rather than by Equation 5 using $a$ and not $a^{*}$.

The two new systems of course fulfil the conditions

$$
\frac{\alpha^{*}}{a^{*}}=\frac{\beta^{* *}}{a^{* *}}=1
$$

so Maxwell's equations appear with no constants in front of the time derivatives.

## Maxwell's equations in material bodies

The general form of Maxwell's equations is

$$
\begin{aligned}
& \nabla x \overline{\mathrm{E}}+\frac{\beta}{a} \frac{\partial \bar{H}}{\partial \mathrm{t}}=0 ; \quad \nabla \cdot \overline{\mathrm{H}}=0 \ldots .56,57 \\
& \nabla x \bar{H}-\frac{\alpha}{a} \frac{\partial \overline{\mathrm{E}}}{\partial \mathrm{t}}=\frac{4 \mathbb{I}}{a} \overline{\mathrm{~J}}, \quad \nabla \cdot \overline{\mathrm{E}}=\frac{4 \mathbb{T}}{\alpha} \rho \ldots . .59,58
\end{aligned}
$$

H.A. Lorentz assumed the validity of these equations inside material bodies provided $\rho$ and $\bar{J}$ included charges and currents from the atoms of the material bodies (Casimir, 1969).
$\rho$ is thus taken as

$$
\rho=\rho_{\mathrm{e}}+\rho_{\mathrm{p}}
$$

and $\overline{\mathrm{J}}$ as

$$
\overline{\mathrm{J}}=\overline{\mathrm{J}}_{\mathrm{e}}+\overline{\mathrm{J}}_{\mathrm{at}}
$$

The division in external and material contributions is, as pointed out by Casimir, to a certain extent arbitrary; and $\rho_{\mathrm{p}}$ and $\bar{J}_{a t}$ are statistical descriptions of the effect of the presence of matter.

For a small elementary volume, $\mathrm{dv}_{\mathrm{n}}$ containing a large number of atoms in order to make average values statistically meaningful, the electric dipole moment per unit volume, $\overline{\mathrm{P}}_{\mathrm{n}}$ is introduced as

$$
\overline{P_{n}}=\frac{1}{d v_{n}} \sum_{d v_{n}} \overline{m_{e}} i
$$

where $\bar{m}_{e}{ }^{i}$ is the $i^{\prime}$ th point-dipole inside $d v_{n}$. By a process of continuization (Knudsen, 1955) all the $\overline{\mathrm{P}}_{\mathrm{n}}$ - values assigned to the individual volume elements, $\mathrm{dv}_{\mathrm{n}}$, are replaced by a continuous vector field $\overline{\mathbf{P}}$ having the value $\overline{\mathbf{P}}=\overline{\mathbf{P}}_{\mathrm{n}}$ at some point inside each volume element $\underline{d v}_{\mathrm{n}}$.

This polarization vector field $\overline{\mathrm{P}}$ may be visualized as strings of dipoles starting with a negative charge and terminating with a positive. According to the Poisson-Thomson analysis (O'Rahilly, 1938, p. 37 ff ) $\overline{\mathrm{P}}$ is equivalent to a charge distribution $\rho_{\mathrm{p}}$ where

$$
\rho_{\mathbf{P}}=-\nabla \cdot \overline{\mathbf{P}}
$$

A positive $\nabla \cdot \overline{\mathrm{P}}$ means that more strings of dipoles are leaving the elementary volume than entering it, which in turn means that there are some negative ends of dipole strings inside the volume, hence the minus sign.

Equation 89 may be considered an "equation of continuity" following from the fact that the total charge of a collection of dipoles is zero.

The splitting into external and atomic contributions is arranged so that the external charges and currents satisfy the equation of continuity

$$
\nabla \cdot \overline{\mathrm{J}}_{\mathrm{e}}+\frac{\partial \rho_{\mathrm{e}}}{\partial \mathrm{t}}=0
$$

and the same holds for the atomic charges and currents
or

$$
\begin{gather*}
\nabla \cdot \overline{\mathrm{J}}_{\mathrm{at}}+\frac{\partial \rho_{\mathrm{p}}}{\partial \mathrm{t}}=0 \\
\nabla \cdot\left\{\overline{\mathrm{~J}}_{\mathrm{at}}-\frac{\partial}{\partial \mathrm{t}} \overline{\mathbf{P}}\right\}=0
\end{gather*}
$$

We may then write

$$
\overline{J_{a t}}=\frac{\partial \overline{\mathrm{P}}}{\partial \mathrm{t}}+\frac{a}{\beta} \nabla \mathrm{x} \overline{\mathrm{M}}
$$

or

$$
\begin{equation*}
\bar{J}_{\mathrm{at}}=\overline{\mathbf{J}}_{\mathrm{p}}+\overline{\mathrm{J}}_{\mathrm{amp}} \tag{93}
\end{equation*}
$$

where $\bar{J}_{p}$ is the current due to changes in polarization and $\bar{J}_{\text {amp }}$ are the amperean neutral currents.
$\bar{M}$ is the magnetization vector derived as a mathematical continuization of the magnetic moment per unit volume analogous to $\overline{\mathrm{P}}$.

The atoms contain small current loops originating in orbiting and spinning electrons and spinning nuclear particles. The actual description belongs to the quantum mechanics, but for our purpose it is sufficient to postulate an equivalent amperean current loop associated with every atom. The magnetic moment of the $i$ 'th current loop in an elementary volume $\mathrm{dv}_{\mathrm{n}^{\prime}}$, large enough to render average values statistically significant, is given by Equation 69

$$
\begin{equation*}
{\overline{m_{m}}}^{i}=\frac{\beta}{a} \cdot \mathbf{I}_{\mathbf{i}}{ }^{\circ} \mathbf{A}_{i} \cdot \bar{n}_{i} \tag{94}
\end{equation*}
$$

where $I_{i}$ is the current and $A_{i}$ the area of the current loop.
The magnetic moment per unit volume is

$$
\bar{M}_{\mathrm{n}}=\frac{1}{\mathrm{~d} v_{\mathrm{n}}} \sum_{\mathrm{i}} \bar{m}_{\mathrm{m}}^{\mathrm{i}}
$$

and the continuization of all the $\bar{M}_{n}$ 's is the vector field $\overline{\mathrm{M}} . \overline{\mathrm{M}}$, described by the equivalent current density distribution

$$
\overline{\mathrm{J}}_{\mathrm{amp}}=\frac{\mathrm{a}}{\beta} \nabla \times \overline{\mathrm{M}}
$$

and $\overline{\mathrm{P}}$, described by the equivalent charge density distribution

$$
\rho_{\mathrm{p}}=-\nabla \cdot \overline{\mathbf{P}}
$$

are two mathematical models representing the effects of the presence of matter.

Equation 91 follows from

$$
\nabla \cdot \bar{J}_{a m p}=0
$$

which means that the amperean currents are neutral.
Maxwell's Equations 56 to 59 , using Equations 86, 87, 92, 93 , and 89 become

$$
\begin{align*}
& \nabla x \bar{E}+\frac{\beta}{a} \frac{\partial \overline{\mathrm{H}}}{\partial \mathrm{t}}=0, \nabla \cdot \overline{\mathrm{H}}=0 \ldots 99,100 \\
& \nabla x \bar{H}-\frac{\alpha}{a} \frac{\partial \bar{E}}{\partial t}=\frac{4 \llbracket}{a} \bar{J}_{e}+\frac{4 \prod}{a} \frac{\partial \bar{P}}{\partial t}+\frac{4 \pi}{\beta} \nabla x \bar{M} \ldots 101 \\
& \nabla \cdot \stackrel{\rightharpoonup}{\mathrm{E}}=\frac{4 \pi}{\alpha} \rho_{\mathrm{e}}-\frac{4 \|}{\alpha} \nabla \cdot \overline{\mathrm{P}}
\end{align*}
$$

Equations 99 to 102 are Maxwell's equations for magnetic and electric fields inside material bodies. The contributions from the atoms of the present matter are accounted for by the space-average vectors $\overline{\mathbf{P}}$ and $\overline{\mathrm{M}}$, electric and magnetic dipole moment per unit volume. ${ }^{\dagger} \mathrm{J}_{\mathrm{e}}$ and $\rho_{\mathrm{e}}$ are the external current and charge densities.

To solve the equations we must know something about $\overline{\mathrm{P}}$ and $\overline{\mathrm{M}}$ besides $\bar{J}_{\mathrm{e}}$ and $\rho_{\mathrm{e}}$.

The solution to the 'external' problem, $\overline{\mathrm{H}}_{\mathrm{e}}$ and $\overline{\mathrm{E}}_{\mathrm{e}}$, is given by

$$
\begin{array}{r}
\nabla \times \overline{\mathrm{E}}_{\mathrm{e}}+\frac{\beta}{\mathrm{a}} \frac{\partial \overline{\mathrm{H}}_{\mathrm{e}}}{\partial \mathrm{t}}=0, \quad \nabla \cdot \overline{\mathrm{H}}_{\mathrm{e}}=0 \ldots 103,104 \\
\nabla \times \overline{\mathrm{H}}_{\mathrm{e}}-\frac{\alpha}{\mathrm{a}} \frac{\partial \overline{\mathrm{E}}_{\mathrm{e}}}{\partial \mathrm{t}}=\frac{4 \|}{\mathrm{a}} \overline{\mathrm{~J}}_{\mathrm{e}}, \quad \nabla \cdot \overline{\mathrm{E}}_{\mathrm{e}}=\frac{4 \|}{\alpha} \rho_{\mathrm{e}} \ldots .105,106
\end{array}
$$

[^4]$\overline{\mathrm{H}}_{\mathrm{e}}$ and $\overline{\mathrm{E}}_{\mathrm{e}}$ may be interpreted as the fields we would have if the material bodies were removed. Subtracting Equations 103 to 106 from Equations 99 to 102 and introducing
\[

$$
\begin{align*}
& \bar{H}_{\mathrm{I}}=\overline{\mathrm{H}}-\overline{\mathrm{H}}_{\mathrm{e}} \\
& \overline{\mathbf{E}}_{\mathrm{I}}=\overline{\mathrm{E}}-\overline{\mathrm{E}}_{\mathrm{e}}
\end{align*}
$$
\]

gives

$$
\begin{align*}
& \nabla x \overline{\mathrm{E}}_{\mathrm{I}}+\frac{\beta}{a} \frac{\partial \overline{\mathrm{H}}_{\mathrm{I}}}{\partial \mathrm{t}}=0, \quad \nabla \cdot \overline{\mathrm{H}}_{\mathrm{I}}=0 \quad \ldots .109,110 \\
& \nabla \mathrm{x} \overline{\mathrm{H}}_{\mathrm{I}}-\frac{\alpha}{\mathrm{a}} \frac{\partial \overline{\mathrm{E}}_{\mathrm{I}}}{\partial \mathrm{t}}=\frac{4 \llbracket}{\mathrm{a}} \frac{\partial \overline{\mathrm{P}}}{\partial \mathrm{t}}+\frac{4 ף}{\beta} \nabla \mathrm{xM} \quad \ldots .111  \tag{111}\\
& \nabla \cdot \overline{\mathrm{E}}_{\mathrm{I}}=-\frac{4 \llbracket}{\alpha} \nabla \cdot \overline{\mathrm{P}} \quad \ldots .112
\end{align*}
$$

where $\left(H_{I}, E_{I}\right)$ is the solution to the 'internal' problem, i.e. the field contributions from $\overline{\mathbf{P}}$ and $\overline{\mathrm{M}}$. The total fields $\overline{\mathrm{E}}$ and $\overline{\mathrm{H}}$ are thus made up of the partial fields $\overline{\mathrm{E}}_{\mathrm{e}}+\overline{\mathrm{E}}_{\mathrm{I}}$ and $\overline{\mathrm{H}}_{\mathrm{e}}+\overline{\mathrm{H}}_{\mathrm{I}}$.
$\overline{\mathrm{P}}$ and $\overline{\mathrm{M}}$ are normally dependent on the field vectors; but whether the 'primary' cause is $(\overline{\mathrm{E}}, \overline{\mathrm{H}}),\left(\overline{\mathrm{E}}_{\mathrm{e}}, \overline{\mathrm{H}}_{\mathrm{e}}\right)$ or $\left(\overline{\mathrm{E}}_{\mathrm{I}}, \overline{\mathrm{H}}_{\mathrm{I}}\right)$ is impossible to say as all three sets of vectors are interdependent. If $\overline{\mathrm{P}}$ and $\overline{\mathrm{M}}$ have constant parts unaffected by $\overline{\mathrm{E}}_{\mathrm{e}}$ and $\overline{\mathrm{H}}_{\mathrm{e}}$ it is reasonable to assume $\overline{\mathrm{E}}_{\mathrm{I}}$ and $\overline{\mathrm{H}}_{\mathrm{I}}$ to be the causes ${ }^{\dagger}$, but if $\overline{\mathrm{P}}$ and $\overline{\mathrm{M}}$ have parts dependent also on $\overline{\mathrm{E}}_{\mathrm{e}}$ and $\overline{\mathrm{H}}_{\mathrm{e}}$ these vectors as well (i.e. the total vectors $\overline{\mathrm{E}}$ and $\overline{\mathrm{H}}$ ) must be regarded as the causes.

The torque, $\overline{\mathrm{T}}$, on a magnetic dipole, $\overline{\mathrm{m}}_{\mathrm{m}}$, in a field, $\overline{\mathrm{H}}$, is

$$
\bar{T}=\overline{\mathrm{m}}_{\mathrm{m}} \times \overline{\mathrm{H}} \quad \text { or } \quad \mathrm{T}=\mathrm{m}_{\mathrm{m}} \cdot \mathrm{H} \cdot \sin \theta \ldots 113
$$

where $\theta$ is the angle between the directions of $\bar{m}_{m}$ and $\boldsymbol{H}$. The work involved in changing $\theta$ from $\theta_{1}$ to $\theta_{2}$ is

$$
\begin{align*}
& \mathrm{W}_{\mathrm{mag}}=\int_{\theta_{1}}^{\theta_{2}} \mathrm{~m}_{\mathrm{m}} \cdot \mathrm{H} \cdot \sin \theta \mathrm{~d} \theta= \\
& -\mathrm{m}_{\mathrm{m}} \mathrm{H}\left(\cos \theta_{2}-\cos \theta_{1}\right)
\end{align*}
$$

[^5]If $\theta_{1}=0$ is chosen then

$$
\begin{equation*}
\mathrm{W}_{\mathrm{mag}}=-\mathrm{m}_{\mathrm{m}} \mathrm{H}\left(\cos \theta_{2}-1\right) \tag{115}
\end{equation*}
$$

is the potential energy of a magnetic dipole $\bar{m}_{m}$ in a field $\bar{H}$ where the direction of the dipole has the angle $\theta_{2}$ to the field ${ }_{s}$ The zero level of the potential energy is arbitrary so we may express

$$
\mathrm{W}_{\text {mag }}=-\overline{\mathrm{m}}_{\mathrm{m}} \cdot \overline{\mathrm{H}}
$$

From this we have the potential energy of a volume element dv of a magnetized body

$$
\mathrm{dW}_{\text {mag }}=-\overline{\mathrm{M}} \cdot \overline{\mathrm{H}} \mathrm{dv}
$$

Normally there is also some mechanical energy associated with the magnetization so the total energy is

$$
d W_{\text {tot }}=-\bar{M} \cdot \bar{H} d v+d W_{\text {mech }} \quad \ldots .117 a
$$

If the mechanical potential energy $\mathrm{dW}_{\text {mech }}$ is independent of the direction of $\overline{\mathbf{M}}$ in the volume element then Equation 117a has a minimum when

$$
\mathrm{dW}_{\text {mag }}=-\overline{\mathrm{M}} \cdot \overline{\mathrm{H}} \mathrm{dv}
$$

is minimum. The directional independence of dW mech is the characteristic feature of the magnetically isotropic materials, in these materials $\overline{\mathrm{M}}$ is thus parallel to $\overline{\mathrm{H}}$ everywhere.

Anisotropic materials have $\mathrm{dW}_{\text {mech }}$ dependent on the orientation of $\bar{M}$ so that the total potential energy $\mathrm{dW}_{\text {tot }}$ is not necessarily minimum when $\bar{M}$ is parallel to $\bar{H}$, which means that in general $\overline{\mathrm{M}}$ and $\overline{\mathrm{H}}$ have different directions.

In some materials $\overline{\mathrm{M}}$ is a linear function of $\overline{\mathrm{H}}$. For isotropic materials

$$
\overline{\mathrm{M}}=\mathrm{k}_{\mathrm{m}} \cdot \overline{\mathrm{H}}
$$

where $\mathrm{k}_{\mathrm{m}}$ is the scalar proportionality factor between $\overline{\mathrm{H}}$ and $\overline{\mathbf{M}}{ }^{\dagger}{ }^{\dagger}$ In the case of anisotropy we have

$$
\bar{M}=\{k\} \cdot \bar{H}
$$

[^6]where $(k)$ is a $3 \times 3$ matrix.
For the ferromagnetic materials, however, the relation between $\bar{M}$ and $\overline{\mathrm{H}}$ is more involved than expressed by Equations 118 and 118a:
$$
\bar{M}=\sum_{n=0}^{\infty}\binom{+}{(-1)^{n-1}} m_{n} \bar{H}^{n}
$$
where + is taken if $H$ is decreasing and $(-1)^{\mathrm{n}-1}$ if H is increasing. Furthermore the coefficients $m_{n}$ are dependent on the immediately preceding maximum value of H . This is still the isotropic case where $\bar{M}$ is parallel to $\bar{H}$, so if anisotropy is introduced the relation between $\overline{\mathrm{M}}$ and $\overline{\mathrm{H}}$ becomes even more complicated.

Traditionally ${ }^{\frac{\dagger}{\dagger}}$, still another set of vector quantities is introduced in the treatment of magnetic and dielectric materials.

The basic Equations 101 and 102 are rearranged in the following manner

$$
\begin{equation*}
\nabla \mathrm{x}\left\{\overline{\mathrm{H}}-\frac{4 \Pi}{\beta} \overline{\mathrm{M}}\right\}-\frac{\alpha}{\mathrm{a}} \frac{\partial}{\partial \mathrm{t}}\left\{\overline{\mathrm{E}}+\frac{4 \Pi}{\alpha} \overline{\mathbf{P}}\right\}=\frac{4 \Pi}{a} \overline{\mathrm{~J}}_{e} \ldots \tag{119}
\end{equation*}
$$

and

$$
\begin{equation*}
\nabla \cdot\left\{\overrightarrow{\mathrm{E}}+\frac{4 \|}{\alpha} \overrightarrow{\mathrm{P}}\right\}=\frac{4 \Pi}{\alpha} \rho_{\mathrm{e}} \tag{120}
\end{equation*}
$$

Two new vectors are then introduced

$$
\begin{align*}
& \overline{\mathrm{K}}=\overline{\mathrm{H}}-\frac{4 \llbracket}{\beta} \overline{\mathrm{M}} \\
& \overline{\mathrm{G}}=\overline{\mathrm{E}}+\frac{4 \llbracket}{\alpha} \overline{\mathrm{P}}
\end{align*}
$$

and inserted into Equations 99 to 102

$$
\begin{gathered}
\nabla x \overline{\mathrm{G}}+\frac{\beta}{a} \frac{\partial \overline{\mathrm{~K}}}{\partial \mathrm{t}}=\frac{4 \Pi}{\alpha} \nabla \mathrm{x} \overline{\mathrm{P}}-\frac{4 \Pi}{a} \frac{\partial \overline{\mathrm{M}}}{\partial \mathrm{t}} \\
\nabla \cdot \overline{\mathrm{~K}}=-\frac{4 \Pi}{\beta} \nabla \cdot \overline{\mathrm{M}} \\
\nabla x \overline{\mathrm{~K}}-\frac{\alpha}{\mathrm{a}} \frac{\partial \overline{\mathrm{G}}}{\partial \mathrm{t}}=\frac{4 \|}{\mathrm{a}} \overline{\mathrm{~J}}_{\mathrm{e}}
\end{gathered}
$$

$$
\nabla \cdot \overline{\mathrm{G}}=\frac{4 \Pi}{\alpha} \rho_{\mathrm{e}}
$$

[^7]There are two mathematical models of polarized media in existence. The Poisson-Thomson model replaces a polarized dielectric by an equivalent charge density distribution

$$
\begin{equation*}
\rho_{\rho}=-\nabla \cdot \overline{\mathbf{P}} \tag{97}
\end{equation*}
$$

and the amperen model replaces a magnetized medium by an equivalent current density distribution

$$
\overline{\mathrm{J}}_{\mathrm{amp}}=\frac{\mathrm{a}}{\beta} \nabla \mathrm{xM}
$$

Maxwell's equations for material bodies Equations 99 to 102 contain the terms $\nabla \mathrm{x} \overline{\mathrm{M}}, \nabla \cdot \stackrel{\rightharpoonup}{\mathrm{P}}$ and $\frac{\partial \overline{\mathrm{F}}}{\partial \mathrm{t}}$ because in the derivation we used the amperean model for magnetic materials and the Poisson-Thomson model for dielectrics. In the Equations 123 to 126 we have the reverse situation as the terms $\nabla \mathrm{x} \overline{\mathrm{P}}$, $\nabla \cdot \bar{M}$ and $\frac{\partial \bar{M}}{\partial t}$ indicate the amperean model for dielectrics and the Poisson-Thomson model for magnetic materials.

The two models give the same field outside the polarized bodies, but in predicting the internal fields they differ. The Poisson-Thomson model is, however, often used to calculate the field around a magnetized body because of its analogy to similar problems already solved in electrostatics, but for calculating the internal magnetic fields this model fails to explain the experimental results and must be rejected. The self-induction of an air-cored coil increases when the coil is filled with magnetic material, indicating an increased internal field according to the amperean model. The $\overline{\mathrm{K}}$-field is thus a hypothetical field based on a wrong model for magnetized materials.

Similarly the $\overline{\mathrm{G}}$-field is a hypothetical field based on the amperean model for dielectrics. This model fails to explain experiments with the internal fields in dielectrics. The capacity of a condenser increases if the empty space between the plates is filled with a dielectric indicating a decreased field as predicted by the Poisson-Thomson model.

The question of $\overline{\mathrm{K}}$-field vs. $\overline{\mathrm{H}}$-field and $\overline{\mathrm{G}}$-field vs. $\overline{\mathrm{E}}$-field is closely related to the question of the existence of a free magnetic pole. In Equation 124 the term $-\nabla \cdot \overline{\mathrm{M}}$ is equivalent to a magnetic charge density

$$
m=-\nabla \cdot \bar{M} \quad \ldots .97 a
$$

and in Equation 123 the terms $\frac{a}{\alpha} \nabla_{x} \bar{P}$ and $\frac{\partial \bar{M}}{\partial t}$ are equivalent to a density of "magnetic current"

$$
\overline{\mathrm{J}}_{\mathrm{m}}=\frac{\partial \overline{\mathrm{M}}}{\partial \mathrm{t}}-\frac{\mathrm{a}}{\alpha} \nabla \times \overline{\mathrm{P}} \quad \ldots 996 \mathrm{a}
$$

In the section on Giorgi-pairs it is shown that by introducing two units for electric field and two units for magnetic field it is possible to remove the constants in Maxwell's equations. To justify this, the MKSA-formulation simultaneously adopts both models for dielectrics and for magnetic materials, assigning different units to the resulting two electric and two magnetic fields. The $\overline{\mathrm{D}}, \overline{\mathrm{E}}, \overline{\mathrm{B}}$ and $\overline{\mathrm{H}}$-fields in the MKSA-formulation are thus related to the $\bar{G}, \bar{E}, \overline{\mathbf{H}}$ and $\overline{\mathrm{K}}$-fields in the notation used here by

$$
\begin{aligned}
& \overline{\mathrm{D}}_{\mathrm{MKSA}}=\frac{\alpha}{\mathrm{a}} \overline{\mathrm{G}} \\
& \overline{\mathrm{E}}_{\mathrm{MKSA}}=\overline{\mathrm{E}} \\
& \overline{\mathrm{~B}}_{\mathrm{MKSA}}=\frac{\beta}{\mathrm{a}} \overline{\mathrm{H}} \\
& \overline{\mathrm{H}}_{\mathrm{MKSA}}=\overline{\mathrm{K}}
\end{aligned}
$$

## Static fields in material bodies

For static and slowly varying fields where the timederivatives may be neglected the magnetic and electric fields can be separated. This leads to

$$
\begin{array}{ll}
\nabla x \overline{\mathrm{G}}=\frac{4 \prod}{\alpha} \nabla \mathrm{x} \overline{\mathrm{P}} ; & \nabla \cdot \overline{\mathrm{G}}=\frac{4 \|}{\alpha} \rho_{\mathrm{e}} \ldots 127,128 \\
\nabla \times \overline{\mathrm{K}}=\frac{4 \prod}{\mathrm{a}} \overline{\mathrm{~J}_{\mathrm{e}}} ; & \nabla \cdot \overline{\mathrm{K}}=\frac{4 \prod}{\beta} \nabla \cdot \overline{\mathrm{M}} \ldots 129,130
\end{array}
$$

Considering the magnetostatic part (Equations 129 and 130) we see that if the magnetization vector $\bar{M}$ is divergencefree then $\overline{\mathrm{K}}$ is the solution to the external problem. An infinitely long cylinder magnetized uniformly along the axis is a case where $\nabla \overline{\mathrm{M}}=0$ and thus $\overline{\mathrm{K}}=\overline{\mathrm{H}}_{\mathrm{e}}$. A toroid magnetized uniformly along its crrcular axis is another example of a body with divergence-less magnetization having $\overline{\mathrm{K}}=\bar{H}_{\mathrm{e}}$.

For isotopic materials $\overline{\mathrm{M}}$ and $\overline{\mathrm{H}}$ are collinear and proportional (Equation 118). From the definition (Equation 121) it then follows that $\overline{\mathrm{K}}$ is proportional to and collinear with $\overline{\mathrm{H}}$ which gives the following interpretation of $\bar{K}$.

A volume element dv, with magnetization $M$ and the total field $\overline{\mathrm{H}}$ inside a body of arbitrary geometrical shape, has a vector $\overline{\mathrm{K}}$ equal to the external field $\mathrm{H}_{\mathrm{e}}^{\mathrm{c}}$ that applied axially to an infinite cylinder of the same material would produce the same magnetization $\overline{\mathrm{M}}$ and the same total field $\overline{\mathrm{H}}$.

For the volume element we have

$$
\overline{\mathrm{H}}=\overline{\mathrm{H}}_{\mathrm{e}}+\overline{\mathrm{H}}_{\mathrm{I}}=\overline{\mathrm{K}}+\frac{4 \mathrm{I}}{\beta} \overline{\mathrm{M}}
$$

and for the hypothetical cylinder

$$
\begin{equation*}
\mathrm{H}=\overline{\mathrm{H}}_{\mathrm{e}}^{\mathrm{c}}+\overline{\mathrm{H}}_{\mathrm{I}}^{\mathrm{c}}=\overline{\mathrm{K}}+\frac{4 \prod}{\beta} \overline{\mathrm{M}} \tag{132}
\end{equation*}
$$

$\mathrm{H}_{1}^{\mathrm{c}}$ is the field from the distribution of magnetic moment per unit volume in the cylinder which may be calculated from Equations 110 and 111

$$
\bar{H}_{\mathrm{I}}^{\mathrm{c}}=\frac{4 \|}{\beta} \overline{\mathrm{M}}
$$

In the body of arbitrary shape the distribution of $\bar{M}$ in general gives a field $H_{I}$ different from ${ }_{\bar{\beta}}^{49} \bar{M}$, e.g. for uniformly magnetized sphere we have

$$
\overline{\mathrm{H}}_{\mathrm{I}}=\frac{2}{3} \cdot \frac{4}{\beta} \overline{\mathrm{M}}
$$

and in the general case

$$
\overline{\mathrm{H}_{\mathrm{I}}}=\frac{1}{\beta} \int \nabla^{\prime} \mathrm{x}\left[\overline{\mathrm{M} x} \nabla\left(\frac{1}{\mathrm{r}}\right)\right] \mathrm{dv}
$$

## Vol

where $d v$ is at $(x, y, z), \bar{H}_{I}$ at $\left(x^{\prime}, y^{\prime}, z^{\prime}\right), \bar{M}$ at $(x, y, z)$ and $\bar{r}=$ $\left\{\left(x^{\prime}-\mathrm{x}\right),\left(\mathrm{y}^{\prime}-\mathrm{y}\right),\left(\mathrm{z}^{\prime}-\mathrm{z}\right)\right\}$. The operator $\nabla^{\prime}$ works only on $\left(\mathrm{x}^{\prime}, \mathrm{y}^{\prime}, \mathrm{z}^{\prime},\right)$, and $\nabla$ only on $(x, y, z)$.

Equations 132 and 133 give $\mathrm{H}_{\mathrm{e}}^{\mathrm{c}}=\overline{\mathrm{K}}$ and Equation 131 gives

$$
\overline{\mathrm{K}}=\overline{\mathrm{H}}_{\mathrm{e}}\left\{\frac{4 \mathbb{I}}{\beta} \overline{\mathrm{M}}-\overline{\mathrm{H}}_{\mathrm{I}}\right\}
$$

but as $\mathrm{H}_{\mathrm{I}}$ from Equation 135 is dependent on the geometry it is seen that $\overline{\mathrm{K}}$ is dependent on the shape of the body.

$$
\overline{\mathrm{K}}_{\mathrm{D}}=\frac{4 \|}{\beta} \overline{\mathrm{M}}-\overline{\mathrm{H}}_{\mathrm{I}}
$$

is normally referred to as the demagnetizing force.
From Equations 118 and 121 we may deduce

$$
\overline{\mathrm{H}}=\overline{\mathrm{K}}+\frac{4 \pi}{\beta} \overline{\mathrm{M}}=\overline{\mathrm{K}}+\frac{4 \prod}{\beta} \cdot \mathbf{k}_{\mathrm{m}} \cdot \overline{\mathrm{H}} \ldots 137
$$

and from this

$$
\begin{align*}
& \bar{H}=\frac{1}{1-\frac{4 \eta}{\beta} k_{m}} \bar{K} \\
& \bar{M}=\frac{k_{m}}{1-\frac{4 \|}{\beta} k_{m}} \bar{K}
\end{align*}
$$

The factor $k_{m}=1 /\left(1-\frac{4 d}{\beta} k_{m}\right)$ is normally called the magnetic permeability and $\chi_{m}=k_{m} /\left(1-\frac{4 \pi}{\beta} k_{m}\right)$ the suscepticeptibility of the material.
$\kappa_{\mathrm{m}}$ and $\chi_{\mathrm{m}}$ preassumes the introduction of the geometrydependent, hypothetical vector $K$; which the paremeter $k_{m}$ does not, Stratton (1941, p. 12) remarks that $\mathrm{k}_{\mathrm{m}}$ would be a more logical way to describe the magnetic materials although he abstains from using this notation due to the traditionally adopted parameters $k_{\mathrm{m}}$ and $\chi_{\mathrm{m}}$.

Anisotropic materials are normally investigated by cutting long cylinders out in the directions of the anisotropy axes and measuring $\kappa_{\mathrm{m}}$ or $\chi_{\mathrm{m}}$ in these directions. From these measurements the matrix $\{\mathrm{k}\}$ in Equation 118 a may be constructed and used in further calculations.

The ferromagnetic materials present a special problem. An approximate solution is sometimes possible by assuming $\overline{\mathrm{M}}$ to consist of a constant part $\overline{\mathrm{M}}_{0}$ and a part $\overline{\mathrm{M}}_{\mathrm{H}}$ proportional to $\overline{\mathrm{H}}$.

If Equation 118 and its analog for electric polarization

$$
\overline{\mathbf{P}}=\mathbf{k}_{\mathrm{e}} \cdot \overline{\mathbf{E}}
$$

are introduced in Maxwell's Equations 99 to 102 we get

$$
\begin{gather*}
\nabla x \bar{E}+\frac{\beta}{a} \frac{\partial \bar{H}}{\partial \mathrm{t}}=0 ; \quad \nabla \cdot \overline{\mathrm{H}}=0 \\
\nabla x \overline{\mathrm{H}}-\frac{\alpha}{\mathrm{a}} \frac{\partial \overline{\mathrm{E}}}{\partial \mathrm{t}}=\frac{4 \Pi}{\mathrm{a}} \overline{\mathrm{~J}} \\
\mathrm{e}
\end{gather*}+\frac{4 \|}{\mathrm{a}} \frac{\partial}{\partial \mathrm{t}}\left(\mathrm{k}_{\mathrm{e}} \cdot \overline{\mathrm{E}}\right)+\mathrm{t}
$$

$$
\nabla \mathrm{x} \overline{\mathrm{E}}+\frac{\beta}{\mathrm{a}} \frac{\partial \overline{\mathrm{H}}}{\partial \mathrm{t}}=0 ; \quad \nabla \cdot \overline{\mathrm{H}}=0
$$

$$
\begin{array}{r}
\nabla x\left\{\left(1-\frac{4 \llbracket}{\beta} k_{m}\right) \bar{H}\right\}- \\
\frac{\alpha}{a} \frac{\partial}{\partial t}\left\{\left(1+\frac{4 \Psi}{\alpha} \mathrm{k}_{\mathrm{e}}\right) \overline{\mathrm{E}}\right\}=\frac{4 \Pi}{a} \bar{J}_{\mathrm{e}}
\end{array}
$$

$$
\nabla \cdot\left\{\left(1+\frac{4 \|}{\alpha} \mathrm{k}_{\mathrm{e}}\right) \overline{\mathrm{E}}\right\}=\frac{4 \|}{\alpha} \rho_{\mathrm{e}}
$$

These equations assume isotropy so $\mathrm{k}_{\mathrm{m}}$ and $\mathrm{k}_{\mathrm{e}}$ are scalars; if we also assume homogeneous materials, i.e. $\mathrm{k}_{\mathrm{m}}$ and $\mathrm{k}_{\mathrm{e}}$ are constants inside the material bodies, we have for interior points

$$
\begin{align*}
& \nabla \times \vec{E}+\frac{\beta}{a} \frac{\partial \bar{H}}{\partial t}=0, \quad \nabla \cdot \bar{H}=0 \\
& \nabla \times \bar{H}-\frac{\left(1+\frac{4 \Phi}{\alpha} k_{e}\right)}{\left(1-\frac{4 \rrbracket}{\beta} k_{m}\right)} \cdot \frac{\alpha}{a} \frac{\partial \bar{E}}{\partial t}= \\
& \frac{1}{\left(1-\frac{4 \llbracket}{\beta} k_{m}\right)} \cdot \frac{4 \pi}{a} \bar{J}_{e} \\
& \nabla \cdot \overline{\mathrm{E}}=\frac{1}{\left(1+\frac{4 \|}{\alpha} \mathrm{k}_{\mathrm{e}}\right)} \frac{4 \mathbb{1}}{\alpha} \rho_{\mathrm{e}}
\end{align*}
$$

By introducing three new constants $\alpha^{\prime}=\left(1+\frac{41}{\alpha} \mathrm{k}_{\mathrm{e}}\right) \alpha, \beta^{\prime}=$ $\left(1-\frac{4 \text { 茜 }}{\beta} \mathrm{k}_{\mathrm{m}}\right) \beta$ and $a^{\prime}=\left(1-\frac{4 \text { I }}{\beta} \mathrm{k}_{\mathrm{m}}\right) a$ the equations are given the form

$$
\begin{gather*}
\nabla \times \bar{E}+\frac{\beta^{\prime}}{a^{\prime}} \frac{\partial \overline{\mathrm{H}}}{\partial \mathrm{t}}=0, \quad \nabla \cdot \overline{\mathrm{H}}=0 \\
\nabla \mathrm{x} \overline{\mathrm{H}}-\frac{\alpha^{\prime}}{\mathrm{a}^{\prime}} \frac{\partial \overline{\mathrm{E}}}{\partial \mathrm{t}}=\frac{4 \Pi}{a^{\prime}} \overline{\mathrm{J}_{\mathrm{e}}} \\
\nabla \cdot \overline{\mathrm{E}}=\frac{4 \mathbb{4}}{\alpha^{\prime}} \rho_{\mathrm{e}}
\end{gather*}
$$

so that a change of constants formally accounts for the presence of material bodies.

The effective speed of propagation is thus changed from c to $c^{\prime}$.

$$
c^{\prime}=\frac{a^{\prime}}{\sqrt{\alpha^{\prime} \cdot \beta^{\prime}}}=c \sqrt{\frac{\left(1-\frac{4 \pi}{\beta} k_{m}\right)}{\left(1+\frac{4 \pi}{\alpha} k_{e}\right)}}
$$

as a result of a complicated interaction between the electromagnetic wave and the atoms of the present matter.

## Unit systems

On the preceding pages it is shown that a unit system is completely determined by six basic "units" including the constants $\delta, \alpha, \gamma, a$, and $\beta$ in this concept. Two sets of mechanical units are in common use, the cm , the sec., the gram, and $\delta=1$ called the c.g.s.system, and the metre, the kilogram and the sec. also with $\delta=1$ called the MKS-system. The reason for including $\delta$ in the analysis is that other unit systems having $\delta \neq 1$ exist and so this constant is necessary to make the equations fully general.

Specifying c.g.s. or MKS and tacitly assuming $\delta=1$ then determines the unit for force in the two systems. If a measure-ratio for force is $F_{\text {c.g.s. }}$ in the c.g.s.s.system and $F_{\text {MKS }}$ in the MKS-system we have

$$
\mathrm{F}_{\mathrm{MKS}}=10^{-5} \cdot \mathrm{~F}_{\text {cogs }}
$$

and the speed of light in the two systems is

$$
\mathrm{c}_{\mathrm{MKS}}=10^{-2} \cdot \mathrm{c}_{\mathrm{cog}, \mathrm{~s}}
$$

The electromagnetic units are then specified by choosing two of the three constants $\alpha, \beta$, and $a$. The values of these constants are characteristic for the unit system and once they have been stated no need really exists for any names of the units. This is the reason for the common practice of stating E.M.U. or E.S.U. after measure-ratios when using the equations of the absolute electromagnetic system of the electrostatic system.

Table I gives the values of the constants in the three c.g.s.-systems, in the Practical system, in the MKS-system and in the three versions of the giorgized, rationalized MKSAsystem, which is the SI presently being adopted internationally.

The constant $c$ is the measure-ratio for the speed of light using the mechanical units of each particular system.

The absolute electromagnetic system is referred to as E.M.U. and so is the magnetostatic part of the Gaussian system. Maxwell's electrostatic system and the electrostatic part of the Gaussian system are called E.S.U.

The absolute electromagnetic system is in a sense the basic unit system as both the practical system and the MKS-system are derived from it.

The practical system has $\alpha=\left(\frac{10}{c}\right)^{2}$ and $\mathrm{a}=10$ which make the unit of current equal to the technical unit, ampere. (1 E.M.U. $=10$ amperes). The practical unit for potential difference then becomes 10 times bigger than the E.M.U. for potential (1 E.M.U. $=1 \sigma^{1}$ pra-volts). In the practical system Equation 40 is

$$
\mathrm{V}=\int \overline{\mathrm{E}} \cdot \overline{\mathrm{ds}}=-\frac{1}{10} \frac{\mathrm{~d}}{\mathrm{dt}} \int \overline{\mathrm{H}} \cdot \overline{\mathrm{da}}
$$

Table I Characteristic constants of electromagnetic unit systems

| Unit System |  | $\alpha$ | $\beta$ | a | Mechanical units ( $\delta=1$ ) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Gaussian |  | 1 | 1 | c | c.g.s. |
| Absolute <br> Electromagnetic |  | $\frac{1}{c^{2}}$ | 1 | 1 | c.gss |
| Maxwell's <br> Electrostatic |  | 1 | $\frac{1}{c^{2}}$ | 1 | cogss |
| Practical (ampere) |  | $\frac{100}{c^{2}}$ | 1 | 10 | c.g.s. |
| MKS <br> (volt, ampere) |  | $\frac{.107}{c^{2}}$ | $10^{-7}$ | 1 | MKS |
| Giorgized, Rationalized MKSA-System (Giorgi-Syst, or SD) | Basic | - $\frac{10^{7}}{c^{2}}$ | $(4 \\|)^{2} \cdot 10^{-7}$ | 4【 |  |
|  | Subsyst. <br> (1) | $(4 \\| c)^{2} \cdot 10^{-7}$ | $(4 \llbracket)^{2} \cdot 10^{-7}$ | $(4 \pi c)^{2} \cdot 10^{-7}$ | MKS |
|  | Subsyst. <br> (2) | $\frac{10^{7}}{c^{2}}$ | $10^{7}$ | $10^{7}$ |  |

substituting N for $\int \overline{\mathrm{H}} \cdot \overline{\mathrm{\sigma a}}$ and introducing volts by dividing both sides by $10^{7}$ gives ( 1 volt $=10^{8}$ E.M.U.):

$$
\mathrm{V}^{\prime}=\frac{\mathrm{V}}{10^{7}}=-10^{-8} \frac{\mathrm{dN}}{\mathrm{dt}}
$$

which is the familiar form of Faraday's law in the practical system. As $\beta=1$ the magnetostatic measure-ratios are in E.M.U., V is in pra-volts and $\mathrm{V}^{\prime}$ in volts. Because the volt is not the "natural" practical unit for potential difference it became necessary to state explicitly " V ' in volts" and to include the conversion factor $10^{7}$.

This conversion factor of $10^{7}$ between volts and pra-volts was considered impractical so a search for a new unit system based on the volt and the ampere began.

Because of a confusion between conversion factors and constants of nature in the equations the idea came up that by choosing a "proper" unit system any factor in the equations could be eliminated.

In E.M.U. Maxwell's Equations 56 to 59 are

$$
\nabla \times \overline{\mathrm{E}}+\frac{\partial \overline{\mathrm{H}}}{\partial \mathrm{t}}=0, \quad \nabla \cdot \overline{\mathrm{H}}=0
$$

$$
\nabla x \bar{H}-\frac{1}{c^{2}} \frac{\partial \overline{\mathrm{E}}}{\partial \mathrm{t}}=4 \llbracket \cdot \overline{\mathrm{~J}}, \quad \nabla \cdot \overline{\mathrm{E}}=4 \llbracket \mathrm{c}^{2} \rho \ldots .164,165
$$

and in the Gaussian system

$$
\nabla \times \overline{\mathrm{E}}+\frac{1}{\mathrm{c}} \frac{\partial \overline{\mathrm{H}}}{\partial \mathrm{t}}=0, \quad \nabla \cdot \overline{\mathrm{H}}=0
$$

$$
\nabla \mathrm{x} \overline{\mathrm{H}}-\frac{1}{\mathrm{c}} \frac{\partial \overline{\mathrm{E}}}{\partial \mathrm{t}}=\frac{4 \pi}{\mathrm{c}} \cdot \overline{\mathrm{~J}}, \quad \nabla \cdot \overline{\mathrm{E}}=4 \llbracket \cdot \rho \ldots .168,169
$$

The $\frac{1}{c}$ and $\frac{1}{c} 2$ constants and especially the 49 -factors annoyed people. Oliver Heaviside considered the 49 's "irrational" and suggested the equations "rationalized" by simply removing the $4 \pi$-factors. Now, the only way to remove the $4 \pi$ 's is to choose $a=4 \|$ and multiply the two other constants $\alpha$ and $\beta$ by $4 \pi$. Obviously the units then change by factors like $\sqrt{4 \Pi}$ or $1 / \sqrt{4 \Pi}$ and the $4 \Pi$ 's will emerge in other equations, but this did not seem to bother Heaviside. In fact very few people seem to realize what "rationalization" is, and even in recent literature the confusion exists (Avčin, 1961, pp. 5 and 10).

The choice of the values of $\alpha, \beta$, and $a$ is, of course, a matter of taste, and it has as such been discussed violently. No real physical arguments can be put forward in favour of one choice over the other; the only thing to be said is that there is no reason for choosing a set of values that will give grossly impractical constants in the equations, or complicated conversion factors to other unit systems.

The statement that, for instance, $\alpha=1, \beta=1$, and $a=\mathrm{c}$ cause 49 -factors to appear where "they have nothing to do with the geometry" is purely emotional; who can, anyway, say where 4 -ffactors really "ought to" be? Maybe Newton's law for mass-attraction really "ought to" be

$$
\mathrm{F}=\frac{\gamma}{4 \prod} \frac{\mathrm{MM}^{\prime}}{\mathrm{r}^{2}}
$$

and Newton's second law

$$
F=\frac{1}{\sqrt{4 \eta}} \vec{M} \frac{d^{2} r}{d t^{2}}
$$

by rationalizing the mass unit?
However, a new unit system was desired and the conditions it had to satisfy were:

1) 1 Volt $=10^{8}$ E.M.U. should be the unit for potential difference.
2) 1 ampere $=10^{-1}$ E.M.U. should be the unit for current.
3) No constants in Maxwell's equations.

As will be shown later 3) is contradictory to 1) and 2), but by the technique called giorgization the constants have been removed from Maxwell's equations and put into the Giorgiconditions. It thus appears as if 3 ) is fulfilled; but it is not, and the manipulation has caused great confusion in electromagnetic theory.

## Logometric formulas

To analyze the problem of changing the E.M.U. to a system having volt and ampere as the units for potential difference and current, we have to investigate the effects of changing also the mechanical units including the constant $\delta$.

In the following the unmarked symbols stand for measureratios in the absolute electromagnetic system defined by gram, second, centimetre, $\delta=1, a=1, \beta=1$, and thus $\alpha=\frac{1}{c} 2$. The symbols marked with a star stand for measure-ratios in some new unit system whose basic units for length, time, and mass and characteristic constants $\delta^{*}, \alpha^{*}, \beta^{*}$, and $a^{*}$ we are going to evaluate.

The general form of Newton's second law is

$$
\mathrm{F}=\delta \mathrm{M} \frac{\mathrm{~d}^{2} \mathrm{~L}}{\mathrm{dT}^{2}}
$$

and changing to the starred system we get

$$
\frac{\mathrm{F}}{\mathrm{~F}}=\frac{\delta}{\delta^{*}} \cdot \frac{\mathrm{M}}{\mathrm{M}^{*}} \cdot \frac{\mathrm{~L}}{\mathrm{~L}^{*}} \cdot \frac{\mathrm{~T}^{* 2}}{\mathrm{~T}^{2}}
$$

Coulomb's law for electric charges

$$
F=\frac{Q \quad Q^{\prime}}{\alpha \cdot L^{2}}
$$

and

$$
\frac{F}{F^{*}}=\left(\frac{Q}{Q^{*}}\right)^{2} \cdot \frac{\alpha^{*}}{\alpha} \cdot\left(\frac{L^{*}}{L}\right)^{2}
$$

Electric potential is

$$
V=\frac{Q}{\alpha L}
$$

and

$$
\frac{V}{V^{*}}=\frac{Q}{Q^{*}} \cdot \frac{\alpha^{*}}{\alpha} \cdot \frac{L^{*}}{L}
$$

Electric current

$$
\mathrm{I}=\frac{\mathrm{dQ}}{\mathrm{dT}}
$$

and

$$
\frac{\mathrm{I}}{\mathrm{I}^{*}}=\frac{\mathrm{Q}}{\mathrm{Q}^{*}} \cdot \frac{\mathrm{~T}^{*}}{\mathrm{~T}}
$$

The formulas (Equations 172a to 175a) are the so-called logometric formulas introduced by $O^{\prime} R a h i l l y$, except for a small change in notation ${ }^{\dagger}$. These logometric formulas, of course, perform much the same function as dimensional equations, and except for the inclusion of the constants $\delta$ and $\alpha$ etc. the logometric expressions are identical to the dimensions.

The reason for including $\delta, \alpha$, and other characteristic constants is that we are completely free to choose and change these independently of the basic units for length, mass, and time. The logometric formulas are thus more general than the dimensional equations.

The four equations (172a to 175a) contain the following nine unknown transformation-ratios
$\frac{\mathrm{M}}{\mathrm{M}^{*}} ; \frac{\mathrm{L}}{\mathrm{L}^{*}} ; \frac{\mathrm{T}}{\mathrm{T}^{*}} ; \frac{\delta}{\delta^{*}} ; \frac{\mathrm{F}}{\mathrm{F}^{*}} ; \frac{\alpha}{\alpha^{*}} ; \frac{\mathrm{Q}}{\mathrm{Q}^{*}} ; \frac{\mathrm{V}}{\mathrm{V}^{*}}$ and $\frac{\mathrm{I}}{\mathrm{I}^{*}} \ldots 176$
$\dagger_{\text {O'Rahilly }}$ uses $[\mathrm{L}]=\frac{\mathrm{L}}{\mathrm{L}},[\alpha]=\frac{\alpha}{\alpha^{*}}$ etc. to symbolize the trans-formation-ratios between the equivalent measure-ratios in the unstarred and the starred systems. To avoid introducing new symbols, the transformation ratios are used directly here.
which means that we are free to choose five of the trans-formation-ratios.

The aim of this investigation is to find out how the volt and the ampere can be incorporated in a unit system, so the first two choices are

$$
\frac{\mathrm{I}}{\mathrm{I}^{*}}=10^{-1}
$$

and

$$
\frac{V}{V^{*}}=10^{8} \quad \ldots \ldots 178
$$

Then we choose

$$
\frac{\delta}{\delta^{*}}=1
$$

to keep Newton's second law free from constants and

$$
\frac{\mathrm{T}}{\mathrm{~T}^{*}}=1
$$

so that the time-unit is unchanged.
If we, as the last choice, put $M / M^{*}=1$ then by solving the Equations 172 a to 175 a we get $L / L^{*}=10^{7}$ which is a rather crastic change. More acceptable is

$$
\frac{\mathrm{L}}{\mathrm{~L}^{*}}=10^{2}
$$

which means that the unit for length is changed from cm to metre. By solving the equations we get

$$
\frac{\mathrm{M}}{\mathrm{M}^{*}}=10^{3}
$$

so that the unit for mass in system (*) is the kilogram instead of the gram: a very acceptable change.

The transformation-ratio for $\alpha$ is then

$$
\begin{equation*}
\frac{\alpha}{\alpha^{*}}=10^{-11} \tag{183}
\end{equation*}
$$

or

$$
\alpha^{*}=10^{11} \alpha=\frac{10^{11}}{c^{2}}
$$

The definition of a speed is

$$
\mathrm{v}=\frac{\mathrm{dL}}{\mathrm{dT}}
$$

so

$$
\frac{\mathrm{v}}{\mathrm{v}^{*}}=\frac{\mathrm{L}}{\mathrm{~L}^{*}} \cdot \frac{\mathrm{~T}^{*}}{\mathrm{~T}}
$$

and

$$
\frac{c}{c^{*}}=\frac{L}{L^{*}}=10^{2}
$$

so we get

$$
\alpha^{*}=\frac{10^{11}}{10^{4} c^{* 2}}=\frac{10^{7}}{c^{* 2}}
$$

which is the value of the constant $\alpha$ in the MKS-system and in the basic Giorgi-system.

## MKS-systems

In the preceding section it has been shown that using kg, metre, second, and $\delta=1$ as the mechanical units it is possible to construct a unit system with the volt and the ampere as units for potential difference and for current if we at the same time take

$$
\alpha=\frac{10^{7}}{c^{2}}
$$

We are still free to choose one of the constants $\alpha$ or $\beta$, and it would have been tempting to take $\beta=10^{-1}$ so the magnetostatic unit for field strength would have been equal to the E.M.U. for magnetic field. The constant $a$ would then have been $a=10^{3}$ using Equation 28.

However, the historical fact is that $a$ was chosen as

$$
a=1
$$

and thus

$$
\beta=10^{-7}
$$

These values characterize the unrationalized MKS-system, and Maxwell's equations in this system are

$$
\nabla x \overline{\mathrm{E}}+10^{-7} \frac{\partial \overline{\mathrm{H}}}{\partial \mathrm{t}}=0, \quad \nabla \cdot \overline{\mathrm{H}}=0 \quad \ldots .192,193
$$

$\nabla x \bar{H}-\frac{10^{7}}{c^{2}} \frac{\partial \overline{\mathrm{E}}}{\partial \mathrm{t}}=4 \pi \cdot \overline{\mathrm{~J}}, \quad \nabla \cdot \overline{\mathrm{E}}=\frac{4 \pi \cdot \mathrm{c}^{2}}{10^{7}} \cdot \rho \quad \ldots .194,195$

By giorgization, as shown earlier, it is possible to get rid of the constants in front of the two time derivatives. But to cancel the $4 \|$ 's we have to choose $a=4 \|$ additionally. This means that $\beta=(4 \|)^{2} \cdot 10^{-7}$ as we can not change $\alpha$ if we still want the volt and the ampere.

The magnetostatic units then become badly "rationalized" so the conversion factors to E.M.U.'s include 4 4 -factors.

The rationalized MKS-system thus has the following characteristic constants

$$
\alpha=\frac{10^{7}}{c^{2}}, a=4 \pi, \text { and } \beta=(4 \pi)^{2} \cdot 10^{-7} \ldots 196
$$

and Maxwell's equations are

$$
\begin{array}{r}
\nabla \times \overline{\mathrm{E}}+4 \pi \cdot 10^{-7} \cdot \frac{\partial \overline{\mathrm{H}}}{\partial \mathrm{t}}=0 ; \nabla \cdot \mathrm{H}=0 \quad \ldots .197,198 \\
\nabla \mathrm{x} \overline{\mathrm{H}}-\frac{10^{7}}{4 \| \cdot \mathrm{c}^{2}} \cdot \frac{\partial \overline{\mathrm{E}}}{\partial \mathrm{t}}=\bar{J} ; \nabla \cdot \overline{\mathrm{E}}=\frac{4 \prod \cdot \mathrm{c}^{2}}{10^{7}} \rho \ldots 199,200
\end{array}
$$

In the giorgized, rationalized MKS-system the equations are

$$
\begin{array}{lll}
\nabla \times \bar{E}+\frac{\partial B}{\partial t}=0 ; & \nabla \cdot \bar{B}=0 & \ldots .201,202 \\
\nabla \times \bar{H}-\frac{\partial D}{\partial \mathrm{t}}=\overline{\mathrm{J}} ; & \nabla \cdot \overline{\mathrm{D}}=\rho & \ldots .203,204
\end{array}
$$

together with the Giorgi-conditions

$$
\begin{align*}
& \overline{\mathrm{B}}=4 \| \cdot 10^{-7} \cdot \mathrm{H} \\
& \overline{\mathrm{D}}=\frac{10^{7}}{4 \pi \cdot \mathrm{c}^{2}} \cdot \overline{\mathrm{E}}
\end{align*}
$$

As shown in the section on Giorgi-transformation of a unit system, the giorgization means that we use two different unit systems in Equations 201, 202 and 203, 204, and that 205 and 206 are the necessary transformation rules between these systems.

Referring to Table I, Equations 201, 202 are in Giorgisubsystem (2) and Equations 203, 204 are in subsystem (1). The basic system is used when potential difference and current simultaneously enter the equations, e.g. in Kirchhoff's equations involving resistance, self-induction and capacitance in AC-circuits.

The two transformation rules Equations 205 and 206 are, by a misinterpreted analogy to the Equation 138 and the corresponding equation for dielectrics, stated to be the relations between 'magnetic induction' and 'magnetizing force', 'electric induction', and 'polarizing force', respectively, in free space, the two constants are concealed behind the symbols

$$
\mu_{0}=4 \pi \cdot 10^{-7}
$$

and

$$
\epsilon_{0}=\frac{10^{7}}{4 \pi \cdot c^{2}}
$$

where $\mu_{0}$ is called the "permeability of free space" and $\epsilon_{0}$ the "permittivity of free space".

The original aim of all these manipulations was to include the volt and the ampere in an absolute unit system; but this has long been lost in the discussions about "rationalization" and a "fourth unit".

Heaviside's suggestion of rationalization has truly been disastrous; we are now stuck with $\mu_{0}$ and $\epsilon_{0}$, two sets of electromagnetic units belonging to three unit systems, and a stubborn confusion about magnetic and dielectric materials.

Life was simpler when the only conversion factors to remember were

$$
\begin{aligned}
& 1 \text { volt }=10^{8} \text { E.M.U. } \\
& 1 \text { ampere }=10^{-1} \text { E.M.U. }
\end{aligned}
$$

and only one magnetic and one electric field existed.

## Conclusions

It is possible to develop an electromagnetic theory independent of any unit system, and this formulation is extremely useful in distinguishing the features inherent in the theory from the features imposed by the different existing unit systems.

Inherent in the theory is thus the necessity of constants in the equations including the occasional occurrence of 4 ाfactors. One system in particular, the MKSA-system or the SI, contains a duality of dimensionally different units for the physical phenomena.

The problems in the MKSA-system can be traced back to Maxwell's "displacement current" which caused him unnecessarily to introduce two different electric field concepts, to

Heaviside's "removal" of 4 П-factors from Maxwell's equations, and to the simultaneous adoption of two conflicting models in the theory of polarizable media. The "brute force" removal of constants from Maxwell's equations by giorgization has resulted in two sets of units with the conversion factors $\mu_{0}$ and $\epsilon_{0}$, which, of course, have nothing to do with permeability or permittivity.

Once this is realized all the ambiguity about B - or H -units, about I•A or $\mu_{0} \cdot I \cdot A$ being the "real" magnetic moment, etc. disappears, and we are free to use which one we please, as long as the formulas are consistent.

The magnetostatic E.M.U.'s can then be converted to SI-units using the following power-of-ten conversion factors.

Magnetic field strength:

$$
1 \text { oersted }=10^{-4} \text { tesla }
$$

Magnetization intensity:

$$
1 \frac{\text { E.M.U. of mag. moment }}{\mathrm{cm}^{3}}=10^{3} \frac{\mathrm{amp}}{\mathrm{~m}}
$$

In this way we are, of course, avoiding the "rationalized" SI-units and leaving it to the user in SI to rationalize or to work his problem out in a consistent set of unrationalized SI-equations.

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The author is greatly indebted to Prof. Alfred O'Rahilly who, in his book, among other things pointed out the need for a third constant in electromagnetism, the existence of two units for magnetic field in the MKSA-formulation, and who reintroduced reality into dimensions by stating them as ratios between measures of the same quantity in different unit systems.

Special thanks are given to G.V. Haines for his contributions to the analysis of Giorgi-pairs, to E.I. Loomer and to P.H. Serson for many clarifying discussions and for encouragement during the work; also E. Irving is thanked for discussions on the units in paleomagnetism.

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## Appendix 1 - Units in the MKSA-subsystems and application of the Haines rule

Because of the existence of two sets of units in the MKSA-system it is necessary to state the names of the units together with the measure-ratios in order to avoid inconsistency. However, once this is done it is always possible to go back and forth between the subsystems by giorgization of the measure-ratios observing the Haines male-female rule.

The MKSA-notation is used

$$
\begin{align*}
& \epsilon_{0}=\frac{\alpha}{a} \\
& \mu_{0}=\frac{\beta}{a}
\end{align*}
$$

where $\alpha, \beta$, and $a$ belong to the basic MKSA-system (see Table I). The symbols used in the following two tables are not completely consistent with international practice nor with the earlier notation but no misunderstandings should arise from this.

The force on an electric charge $Q$ in the field $E$ is:

$$
\overrightarrow{\mathrm{F}}=\stackrel{\delta}{\mathrm{Q}} \cdot \stackrel{\underline{\mathrm{E}}}{\mathrm{E}}=\stackrel{\stackrel{\delta}{\mathrm{Q}}}{\mathrm{Q}} \cdot \frac{\mathrm{\delta}}{\mathrm{D}}
$$

Power is:

$$
\mathrm{P}=\begin{gather*}
\% \\
\mathrm{~V}
\end{gathered} \delta^{*} \mathrm{I}=\mathrm{V}^{*} \cdot \begin{gathered}
申 \\
\mathrm{I}
\end{gather*}
$$

Work:

$$
\begin{align*}
& \text { it or of } \\
& W=V \cdot Q=V^{*} \cdot Q^{*}
\end{align*}
$$

Torque on an electric dipole in the field $\mathbf{E}$

$$
\overline{\mathrm{T}}=\frac{\delta}{\mathrm{m}_{\mathrm{e}}} \times \frac{\%}{\overline{\mathrm{E}}}=\frac{\%}{\mathrm{~m}_{\mathrm{e}}^{*}} \times \frac{\delta}{\mathrm{D}}
$$

Force between two electric charges (Coulomb's law):

Table II. Electrostatic part of the MKSA-system

| Name | Symbol, Name of unit, gender | Symbol, Name of unit, gender | $\begin{aligned} & \text { Giorgization rule } \\ & e_{0}\left[\frac{\text { Coulomb }}{\text { valtom }}\right] \end{aligned}$ |
| :---: | :---: | :---: | :---: |
|  | Basic system | Sub system (1) |  |
| Charge | $\begin{gathered} \text { Q } \\ \text { Coulomb, } \\ \text { ó } \end{gathered}$ | $\begin{aligned} & \mathrm{Q}^{*} \\ & \text { volt•m, } \end{aligned}$ | $\mathrm{Q}=\epsilon_{0} \cdot \mathrm{Q}^{*}$ |
| Electric field intensity | $\underset{\text { volt } / \mathrm{m},}{\mathrm{E}} \quad \text { 甲 }$ | $\begin{aligned} & \text { D } \\ & \text { Coulomb } / \mathrm{m}^{2}, \delta^{2} \end{aligned}$ | $\mathrm{D}=\epsilon_{0} \cdot \mathrm{E}$ |
| Electric flux | voltom, $\%$ | Coulomb, ơ | $\Psi=\epsilon_{0} \cdot \Psi^{*}$ |
| Potential difference | $\begin{array}{cc} \text { V } \\ \text { volt, } \end{array}$ | Coulomb/m, ${ }^{\text {o }}$ | $\mathrm{V}^{*}=\epsilon_{0} \cdot \mathrm{~V}$ |
| Polarization | P <br> Coulomb/m ${ }^{2}$, $\delta$ | $\begin{gathered} \mathrm{p}^{*} \\ \mathrm{volt} / \mathrm{m}, \end{gathered}$ | $P=\epsilon_{0} \cdot{ }^{*}$ |
| Electric dipolemoment | $\overline{\mathrm{m}}_{\mathrm{e}}$ <br> Coulombem, ot | $\begin{aligned} & \overline{\mathrm{m}}_{\mathrm{e}}^{*} \\ & \text { volt• } \mathrm{m}^{2} \quad q \end{aligned}$ | $\overline{\mathrm{m}}_{\mathrm{e}}=\epsilon_{0} \cdot \overline{\mathrm{~m}}_{e}^{*}$ |
| Current | $\text { ampere }=\frac{\text { Coulomb }}{\text { sec }}, \delta$ | $\begin{gathered} \begin{array}{c} \text { I* } \\ \text { volt } * \mathrm{~m} \end{array} \\ \frac{\mathrm{sec}}{} \end{gathered} \text {, ㅇ, }$ | $\mathrm{I}=\epsilon_{0} \cdot \mathrm{I}^{*}$ |
| Time derivative of flux | $\begin{gathered} \frac{\mathrm{d} \Psi^{*}}{\mathrm{dt}} \\ \frac{\mathrm{volt} \cdot \mathrm{~m}}{\mathrm{sec}}, \quad \text { ㅇ } \end{gathered}$ | $\begin{gathered} \frac{\mathrm{d} \Psi}{\mathrm{dt}} \\ \frac{\text { Coulomb }}{\sec }=\mathrm{amp}, \sigma^{t} \end{gathered}$ | $\frac{d \Psi}{d t}=\varepsilon_{0}, \frac{d \Psi^{*}}{d t}$ |

Table III. Magnetostatic part of the MKSA-system

|  | Symbol, Name of unit, gender | Symbol, Name of unit, gender |  | Giorgization rule $\mu_{0}\left[\frac{\text { Webers }}{\text { amp }}\right]$ |
| :---: | :---: | :---: | :---: | :---: |
| Magnetic pole strength | Basic system <br> m <br> Webers, $\delta^{7}$ | Sub. system $\begin{gathered} \mathrm{m}^{*} \\ \mathrm{amp} \cdot \mathrm{~m}, \end{gathered}$ | $\dagger$ | $\mathrm{m}=\mu_{0} \cdot \mathrm{~m}^{*}$ |
| Magnetic field strength | $\begin{gathered} \overline{\mathbf{H}} \\ \mathrm{amp} / \mathrm{m}, \end{gathered}$ | $\begin{aligned} & \quad \overline{\mathbf{B}} \\ & \text { Webers } / \mathrm{m}^{2}, \quad \\ & =\text { tesla } \end{aligned}$ |  | $\overline{\mathbf{B}}=\mu_{0} \cdot \overline{\mathrm{H}}$ |
| Magnetic flux | $\text { amp.m, } \quad \text { ¢ }$ | Webers, ${ }^{\circ}$ |  | $\Phi=\mu_{0} \cdot \Phi^{*}$ |
| Magnetization | Webers/m ${ }^{2}$, ठ́ | $\begin{gathered} \overrightarrow{\mathrm{J}} \\ \mathrm{amp} / \mathrm{m}, \end{gathered}$ | $\dagger \dagger$ | $\overline{\mathrm{M}}=\mu_{0} \cdot \overline{\mathrm{~J}}$ |
| Magnetic dipolemoment | $\bar{m}_{m}$ <br> Webers.m, ó | $\begin{gathered} \overline{\mathrm{m}}_{\mathrm{m}}^{*} \\ \mathrm{amp} \cdot \mathrm{~m}^{2}, \quad \text {, } \end{gathered}$ |  | $\bar{m}_{m}=\mu_{0} \cdot \overline{m_{m}^{*}}$ |
| Timederivative of flux | $\frac{\mathrm{d} \Phi^{*}}{\mathrm{dt}}$ $\mathrm{amp} \cdot \mathrm{~m} / \mathrm{sec}, \quad \text { 甲 }$ | $\begin{gathered} \frac{\mathrm{d} \Phi}{\mathrm{dt}} \\ \frac{\text { Webers }}{\sec }=\text { volt, } \delta \delta \end{gathered}$ |  | $\frac{\mathrm{d} \Phi}{\mathrm{dt}}=\mu_{0} \cdot \frac{\mathrm{~d} \Phi^{*}}{\mathrm{dt}}$ |

† Volt and ampere change gender according to whether they are members of a magnetic or an electric Giorgi-pair. $\dagger \dagger$ Not to be confused with the symbol for current density.

If we want to avoid the constant $\epsilon_{0}$ in the formula, Haines rule has to be observed.

The force on a magnetic pole in a magnetic field

$$
\overline{\mathrm{F}}=\begin{gather*}
\delta^{*} \\
\mathrm{~m}
\end{gather*} \cdot \stackrel{i}{\mathrm{H}}=\stackrel{\circ}{\mathrm{H}} \mathrm{~m}^{*} \cdot \frac{\mathrm{o}^{2}}{\mathrm{~B}}
$$

Torque on a magnetic dipole:

$$
\overline{\mathrm{T}}=\frac{\delta}{\mathrm{m}_{\mathrm{m}}} \times \frac{\frac{q}{\mathrm{H}}}{\mathrm{H}}=\frac{\frac{q}{\mathrm{~m}_{\mathrm{m}}} \times \frac{\delta}{\mathrm{B}}}{\frac{\delta}{2}}
$$

Force between poles:

$$
\mathrm{F}=\frac{\begin{array}{c}
\delta \sigma^{\prime} \\
\mathrm{a} \cdot \mu_{0} \cdot \mathrm{r}^{2}
\end{array}}{\mathrm{~m}}=\frac{\% \%}{\mathrm{a}} \cdot \frac{\mu_{0}}{\mathrm{~m}^{*} \mathrm{~m}^{* \prime}} \mathrm{r}^{2}=\frac{\mathrm{mm}^{*}{ }^{\prime}}{\mathrm{a} \cdot \mathrm{r}^{2}}
$$

Again the constant $\mu_{0}$ disappears if the Haines rule is followed.
In magnetic materials the following general formula is given (Equation 121):

$$
\overline{\mathrm{H}}=\overline{\mathrm{K}}+\frac{4 ף}{\beta} \overline{\mathrm{M}}
$$

if all the terms are giorgized we get

$$
\bar{B}=\mu_{0} \bar{K}+\bar{M}
$$

as

$$
\mu_{0}=\frac{\beta}{a} \text { and } a=4 \pi
$$

By giorgizing $\overline{\mathrm{M}}$ according to Table III then Equation A1.12 becomes

$$
\overline{\mathrm{B}}=\mu_{0}(\overline{\mathrm{~K}}+\overline{\mathrm{J}})
$$

In Equation A1.11 the three measure-ratios $\bar{H}, \bar{K}$, and $\bar{M}$ all belong to the basic system of Table III. Equation A1.12 thus contains measure-ratios belonging to two different unit systems as $\overline{\mathrm{B}}$ is the magnetic field strength in the subsystem. The same is the case in Equation A1.13, $\overline{\mathrm{B}}$ and $\overline{\mathrm{J}}$ belong to the subsystem in Table III and $\overline{\mathrm{K}}$ to the basic system. The factor $\frac{4 \pi}{\beta}$ is thus eliminated in the two MKSA-versions of Equation A1.11 by mixing the units; but this elimination is, of course, only apparent as it must have been included earlier in the definition of $\overline{\mathrm{M}}$ or of $\overline{\mathrm{B}}$.

Maxwell's equations in the giorgized, rationalized MKSAsystem are (Equations 201 to 204)

$$
\begin{array}{ll}
\nabla \times \overline{\mathrm{E}}+\frac{\partial \overline{\mathrm{B}}}{\partial \mathrm{t}}=0 ; & \nabla \cdot \overline{\mathrm{B}}=0 \\
\nabla \times \overline{\mathrm{H}}-\frac{\partial \overline{\mathrm{D}}}{\partial \mathrm{t}}=\overline{\mathrm{J}} ; & \nabla \cdot \overline{\mathrm{D}}=\rho
\end{array}
$$

The unit for $\nabla x \bar{E}$ is [volt $/ \mathrm{m}^{2}$ ] so $\overleftarrow{\mathrm{E}}$ belongs to the basic system of Table II. $\frac{\partial \bar{B}}{\partial t}$ is in [ $\frac{\text { Webers }}{m^{2} \cdot \sec }$ ] or [tesla/sec] so this term belongs to subsystem (2) of Table III.
$\nabla \mathbf{x} \bar{H}$ is in [ampere $/ \mathrm{m}^{2}$ ] belonging to the basic system and $\frac{\partial \bar{D}}{\partial t}$ is in $\left[\frac{\text { Coulom } b}{m^{2} \cdot \sec }\right]$ belonging to subsystem (1).

Now, subsystem (1) and the magnetic part of the basic system form a consistent unit system, and subsystem (2) together with the electric part of the basic system also constitute a unit system. These are the two systems referred to as (1) and (2) in Table $I$, and they are both different from the basic MKSA-system, Maxwell's Equations 201 to 204 are thus given in two different unit systems and the conversion factors from these systems to the basic MKSA-system are

$$
\overline{\mathrm{B}}=\mu_{0} \cdot \overline{\mathrm{H}}
$$

and

$$
\overline{\mathrm{D}}=\epsilon_{0} \cdot \overline{\mathrm{E}}
$$

Appendix 2 - Units, dimensions and logometric expressions

A unit is a name attached to a measure-ratio to state which unit system it belongs to. Units like volt, ampere, coulomb, etc. and compounded units such as volt-sec, ampere $\cdot \mathrm{m}$, etc. are used to ensure that the formulas we use are correct or that the measure-ratios are in the same unit system.

The equation

$$
\nabla \overline{\mathrm{xE}}+\frac{\partial \overline{\mathrm{B}}}{\partial \mathrm{t}}=0
$$

is stated in a unit system having volt/m as the unit for electric field strength $E$ and tesla as the unit for magnetic field strength. If the measure ratio for magnetic field strength has been given in ampere/m we would immediately recognize either the formula in Equation A2.1 as wrong or the measure-ratio as belonging to another unit system. We may then use the corresponding formula in the other system

$$
\nabla \times \overline{\mathrm{E}}+4 \pi \cdot 10^{-7} \frac{\partial \bar{H}}{\partial t}=0
$$

or, which amounts to the same thing, convert the measureratio for magnetic field from ampere/m to tesla by using the conversion factor $\mu_{0}$

$$
\overline{\mathrm{B}}=\mu_{0} \overline{\mathrm{H}}
$$

where

$$
\mu_{0}=4 \pi \cdot 10^{-7}\left[\frac{\text { Webers }}{\text { amp } m}\right]
$$

The unit attached to $\mu_{0}$ is of the same kind as the unit metres/inch attached to the conversion factor between inches and metres
$\mathrm{L}[$ metres $]=0.0254\left[\frac{\text { metres }}{\text { inch }}\right] \cdot \mathrm{L}^{*}[$ inches $]$,
i.e. it is a mnemotechnical help to remember whether it is the measure-ratio in inches or in metres we have to multiply by the conversion factor.

Also, if we change the unit of a measure-ratio to a subunit, i.e. from volts to millivolts, microvolts, kilovolts etc., then the units are useful to derive the conversion factors. If $\vec{E}$ is the measure-ratio for electric field in volts/m and $\bar{E}^{*}$ is the measure-ratio for the same field in microvolts/cm we have
$\overline{\mathrm{E}}\left[\frac{\text { volts }}{\mathrm{m}}\right]=\overline{\mathrm{E}^{*}}\left[\frac{\text { microvolts }}{\mathrm{cm}}\right] \cdot \mathrm{k}\left[\frac{\mathrm{cm}}{\mathrm{m}} \cdot \frac{\text { volts }}{\text { microvolts }}\right] \ldots \mathrm{A} 2.6$
where k is the conversion factor. It is easily derived that

$$
\mathrm{k}=10^{2} \cdot 10^{-6}=10^{-4}
$$

and thus

$$
\overline{\mathrm{E}}^{*}=10^{4} \cdot \overline{\mathrm{E}}
$$

Dimensions are the units stated in terms of the chosen basic units, but ignoring the basic constants. In the c.g.s. systems the basic units are cm , gram, and second normally represented by $\mathrm{L}, \mathrm{M}$, and T and the basic constants are $\delta=1$, $\beta=1$ or $\frac{1}{c^{2}}$, and $\alpha=\frac{1}{c^{2}}$ or 1 .

The dimension of force is

$$
[F]=\left[\frac{\mathrm{ML}}{\mathrm{~T}^{2}}\right]
$$

which states how the measure-ratios for force change if we change the units, and thus the measure-ratios, for mass, length, and time. Comparing to Equation 172a we see that tacitly we have limited ourselves to $\delta=1$, unchanged, as this constant is not included in Equation A2.9. It is well known that the three-unit dimensions lead to contradictions in the electromagnetic part of the C.G.S.-systems.

The MKSA-systems have four basic units - metre, kilogram, second, and ampere, symbolized by $L, M, T$, and $I$, and the two constants $\delta=1$ and $a=4 \pi$. The use of four units in the dimensions removes the double-dimensions in electromagnetism, but as $\delta$ and $a$ are not included we are restricted to unit systems having $\delta=1$ and $a=4 \pi$. The change from the unrationalized MKS-system to the rationalized MKSA-system cannot be analyzed by dimensions as the rationalization is equivalent to a change from $a=1$ to $a=4 \pi$. Neither can the change from the absolute electromagnetic system to the unrationalized MKS-system be analyzed by dimensions as it involves a change of the constant $\alpha$ from $\alpha=\frac{1}{c^{2}}$ to $\alpha=\frac{10^{7}}{c^{2}}$ and of $\beta$ from $\beta=1$ to $\beta=10^{-7}$.

Logometric formulas are the fully general expressions including all six basic units and constants. The logometric expression for force is (Equation 172a)

$$
\frac{\mathrm{F}}{\mathrm{~F}^{*}}=\frac{\delta}{\delta^{*}} \cdot \frac{\mathrm{M}}{\mathrm{M}^{*}} \cdot \frac{\mathrm{~L}}{\mathrm{~L}^{*}} \cdot\left(\frac{\mathrm{~T}^{*}}{\mathrm{~T}}\right)^{2}
$$

where $\mathrm{F}, \delta, \mathrm{M}$, etc. are measure-ratios and constants in system (1) and $F^{*}, \delta^{*}, M^{*}$, etc. belong to system (2). Using O'Rahilly's notation $[\mathrm{F}]=\mathrm{F} / \mathrm{F}^{*},[\delta]=\delta / \delta^{*}$, etc., we have

$$
[\mathrm{F}]=\left[\frac{\delta \mathrm{ML}}{\mathrm{~T}^{2}}\right]
$$

and it is seen that the logometric formula reduces to the dimension of force if $[\delta]=\delta / \delta^{*}=1$.

The expression "logometric" is also O'Rahilly's. According to him it is derived from Greek "logos" = ratio and "metron" = measure and means "ratio between measures".

As an example of the use of logometric formulas we will derive the logometric expressions for the constants $\alpha$ and $\beta$ in the MKSA-system.

The MKSA-system is defined by metre, kilogram, second, $\delta=1$, ampere, and $a=4 \uparrow$. The logometric expression for force is Equation A2.11

$$
[\mathrm{F}]=\left[\frac{\delta \mathrm{ML}}{\mathrm{~T}^{2}}\right] \quad \ldots . \mathrm{A} 2.11
$$

The definition of the ampere is based on Equation 8

$$
d^{2} F=\frac{\beta}{a^{2}} \frac{I_{1} d s_{1} \times\left(I_{2} d_{s_{2}} \times r\right)}{r^{2}} \quad \ldots .8
$$

which gives the following logometric formula

$$
[F]=\left[\frac{\beta}{a^{2}} \cdot I^{2}\right]
$$

From Coulomb's law for two electric charges we get

$$
[\mathrm{F}]=\left[\frac{\mathrm{Q}^{2}}{\alpha \mathrm{~L}^{2}}\right]
$$

and from Equation 5

$$
[\mathrm{I}]=\left[\frac{\mathrm{Q}}{\mathrm{~T}}\right]
$$

Combining Equations A2.13 and A2.14 and equating [F] to [F] in Equations A2.11 and A2.12 we have

$$
[\mathrm{F}]=\left[\frac{\delta \mathrm{ML}}{\mathrm{~T}^{2}}\right]=\left[\frac{\beta}{\mathrm{a}^{2}} \cdot \mathrm{I}^{2}\right]=\left[\frac{\mathrm{I}^{2} \mathrm{~T}^{2}}{\alpha \mathrm{~L}^{2}}\right]
$$

From this we may derive

$$
\left[\frac{\mathrm{a}^{2}}{\alpha \beta}\right]=\left[\frac{\mathrm{L}}{\mathrm{~T}}\right]^{2}
$$

which is the logometric expression corresponding to Equation 28. Further we have

$$
[\alpha]=\left[\frac{\mathrm{I}^{2} \cdot \mathrm{~T}^{4}}{\delta \cdot \mathrm{M} \cdot \mathrm{~L}^{3}}\right]
$$

and

$$
[\beta]=\left[\frac{\delta \cdot \mathrm{a}^{2} \mathrm{M} \cdot \mathrm{~L}}{\mathrm{I}^{2} \cdot \mathrm{~T}^{2}}\right]
$$

From the section on Giorgi-pairs we have

$$
\epsilon_{0}=\frac{\alpha}{a}
$$

and

$$
\begin{equation*}
\mu_{0}=\frac{\beta}{a} \tag{A 2.20}
\end{equation*}
$$

The logometric expressions are then

$$
\epsilon_{0}\left[\frac{I^{2} \cdot T^{4}}{\delta \cdot a \cdot M \cdot L^{3}}\right]
$$

and

$$
\mu_{0}\left[\frac{\delta \cdot a \cdot M \cdot L}{I^{2} \cdot T^{2}}\right]
$$

If we choose $\delta=\delta / \delta^{*}=1$ and $a=a / a^{*}=1$ we get the four-unit dimensions

$$
\begin{equation*}
\epsilon_{0}\left[\frac{\mathrm{I}^{2} \mathrm{~T}^{4}}{\mathrm{M} \cdot \mathrm{~L}^{3}}\right] \tag{A2. 23}
\end{equation*}
$$

and

$$
\mu_{0}\left[\frac{\mathrm{M} \cdot \mathrm{~L}}{\mathrm{I}^{2} \cdot \mathrm{~T}^{2}}\right]
$$

If we replace $M$ by kg , L by metre, T by second, and I by ampere and use the relations

$$
\frac{\mathrm{kg} \cdot \text { metre }}{\sec ^{2}}=\text { newton }
$$

$$
\frac{\text { Newton } \cdot \text { metre }}{\text { Coulomb }}=\text { volt }
$$

$$
\text { Volt-sec }=\text { weber }
$$

$$
\text { ampere } \cdot \mathrm{sec}=\text { coulomb }
$$

we get the units for $\mu_{0}$ and $\epsilon_{0}$

$$
\begin{align*}
& \mu_{0}\left[\frac{\text { Webers }}{\text { amp } \cdot \mathrm{m}}\right] \\
& \epsilon_{0}\left[\frac{\text { Coulomb }}{\text { volt } \cdot \mathrm{m}}\right]
\end{align*}
$$



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# gravity measurements in canada january 1, 1967 to december 31, 1970 

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| Flexural rigidity, thickness and viscosity of the lithosphere |  |
| Gravity interpretation methods |  |
| Physical geodesy |  |
| Polar studies |  |
| Bedford Institute (Atlantic Oceanographic Laboratory) |  |
| Detailed gravity surveys |  |
| Hydrographic-geophysical survey of the eastern |  |
| Canada Continental Shelf |  |
| Grand Banks |  |
| Gulf of St. Lawrence |  |
| Western Arctic |  |
| Regional geophysical surveys |  |
| Mid-Atlantic Ridge |  |
| Bay of Fundy |  |
| Hudson Strait |  |
| North American Basin |  |
| Hudson '70 |  |
| Environmental tests |  |
| Satellite navigation cruise (CSS Baffin 022-69) |  |
| Laboratory tests |  |
| Memorial University of Newfoundland |  |
| Nova Scotia Research Foundation |  |
| University of New Brunswick |  |
| McGill University |  |
| University of Manitoba |  |
| University of Alberta |  |
| University of Calgary |  |
| University of Saskatchewan |  |
| University of British Columbia |  |
| Petroleum Industry |  |
|  | Bibliography |

# gravity measurements in canada january 1, 1967 to december 31, 1970 

## Introduction

This report has been compiled at the request of the International Union of Geodesy and Geophysics (IUGG) for presentation at the Fifteenth General Assembly on behalf of the Associate Committee of Geodesy and Geophysics (ACGG), the National Committee representing Canada in the international union. Annual reports published by the subcommittee on Gravity of the ACGG in the Canadian Geophysical Bulletin (C.M. Carmichael, Editor) form the basis for this compilation. The gravity subcommittee includes representatives from universities, from government institutions and from the mineral industry. The present membership is:

| A.E. Beck | University of Western <br> Ontario |
| :--- | :--- |
| D.E.T. Bidgood | Nova Scotia Research <br> Foundation |
| W.C. Brisbin | University of Manitoba <br> E.R. Deutsch <br> Memorial University <br> of Newfoundland |
| R.M. Ellis | University of British <br> Columbia |
| R.A. Gibb | Earth Physics Branch, <br> Secretary |
| R.T. Haworth | Atlantic Oceanographic <br> Laboratory, Bedford |
| E. Krakiwsky | Institute <br> University of |
| T.H. Pezarro | New Brunswick <br> Voyager Petroleums <br> Ltd. |
| J.G. Tanner | Earth Physics Branch, |
| H.D. Valliant | Chairman <br> Earth Physics Branch |

The largest contributor to this report is the Earth Physics Branch (formerly the Dominion Observatory) of the Department of Energy, Mines and Resources, the federal agency responsible for mapping the gravity field in Canada and its
coastal waters. Allied responsibilities include maintenance of gravity standards for Canada, operation of a gravity data bank, instrumental development and the application of gravity to geologic and geodetic problems in Canada.

A major contribution comes from the Atlantic Oceanographic Laboratory, Bedford Institute of the Marine Sciences Branch, Department of Energy, Mines and Resources. This institute is involved with surface gravity measurements at sea.

Several provincial agencies and several Canadian Universities are increasingly active in a diversity of gravity investigations as reported here.

## Earth Physics Branch

## Gravity standards

National primary net. An extensive series of pendulum and gravimeter measurements were carried out on the national primary net between 1967 and 1970. This network (Figure 1) consists of 64 stations interconnected by 1,500 LaCoste and Romberg gravimeter ties and six pendulum intervals.

The first full scale field evaluation of the rebuilt Canadian bronze pendulum apparatus was carried out over the North American calibration line between Mexico City and Fairbanks in 1967. The results of these measurements (Valliant, 1969) when compared with earlier Gulf and Cambridge pendulum measurements and with gravity values derived from combined adjustments of all existing gravimeter and pendulum measurements on the NACL, showed that an accuracy better than $\pm 0.2 \mathrm{mgal}$ could be achieved with two sets of measurements in opposite directions on any interval. In 1969, pendulum measurements were carried out at Ottawa, Winnipeg, Vancouver, Edmonton, Yellowknife, Fairbanks and Resolute. Environmental problems at Resolute and logistic dif-

J. G. TANNER and R. A. GIBB

ficulties in the initial Fairbanks - Resolute and Resolute - Ottawa ties caused large discrepancies between the incoming and outgoing legs. Satisfactory results were obtained on the repeated Ottawa - Resolute measurements but transportation difficulties have prevented a remeasurement of the Resolute - Fairbanks interval. An analysis of these measurements (Valliant, 1970, in press) indicates that an accuracy better than 0.2 mgal has been achieved. Comparisons with absolute measurements at Fairbanks, Denver and Boston carried out by Air Force Cambridge Research Laboratories, Bedford, Mass., using Faller's apparatus show that the Canadian pendulums agree with the absolute measurements to about 1 part in 20,000.

In order to minimize errors due to excentre corrections at points in the primary network nearly all excentre networks were reobserved or strengthened with new measurements. A large proportion of the 270 excentre stations in the network were reobserved during 1968 to 1970 and each excentre network readjusted. The standard errors of the adjusted excentre stations are generally less than 0.02 mgals.

During the period under review about 700 long range measurements with LaCoste and Romberg gravimeters were added to the 800 older LaCoste and Romberg measurements, the Canadian pendulum measurements, and the absolute measurements at Fairbanks and Boston to form the basis for adjusting the Canada net. During the adjustment, a larger dispersion in the gravimeter measurements carried out before the installation of vibration insulators in 1966, led to the development of a weighting system based on the elapsed time between successive readings of the gravimeters. Pendulum and absolute measurements were weighted according to their respective estimated variances.


Figure 1. The Canadian primary net (1970).

The analysis of the primary network adjustment (R.K. McConnell, Earth Physics Branch, personal communication) indicates that gravity values in the primary net are accurate to $\pm 0.05$ mgals relative to the datum defined by the absolute measurements.

Adjustment of the secondary networks comprising some 17,000 ties between 3,000 control stations has been underway for some time. In order to reduce, adjust, and analyze this rapidly expanding file of data quickly and efficiently, considerable emphasis has been placed upon computer filing, retrieval and data reduction systems. These are described briefly in a subsequent paragraph.

World gravity net The Earth Physics Branch has continued its participation in the work of Special Study Group 5 of the International Association of Geodesy. In 1967, C.T. Whalen of the 1381st Geodetic Survey Squadron, Cheyenne, Wyoming visited Ottawa to carry out preliminary adjustments of the world net using all available gravimeter and pendulum data. In 1968, R.K. McConnell of the Earth Physics Branch collaborated again with Mr. Whalen using the computing facilities of Aerospace Corporation in San Bernardino, California. In September of 1970 J.G. Tanner and R.K. McConnell presented the results of an adjustment of a world gravity net consisting of 270 stations to the Special

Study Group 5 meeting held in Paris and participated in the development of plans for the final adjustment to be accomplished in 1971.

A few additional measurements on the world net were made by Earth Physics Branch personnel in 1969, Direct ties between absolute sites at Fairbanks, Boston and Bogota were carried out using three LaCoste and Romberg meters. Additional ties were made between South America and South Africa in co-operation with Professor Baglietto of the Institute of Geodesy, University of Buenos Aires.

Gravimeter tilt calibrator. A gravimeter tilt calibrator built at the Earth Physics Branch from plans supplied by Texas

Instruments Ltd., was used extensively by A.C. Hamilton to investigate dial nonlinearaties in Worden type gravimeters. Discrepancies between calibrations of the same meter on the Earth Physics Branch tilt table and one at Texas Instruments led to an investigation of the table design. Precise angle measurement carried out by E. Greene of the National Research Council of Canada, Ottawa showed that the knife edge surface and the surface on which the Johannsen blocks rest were not sufficiently coplanar to eliminate erratic tilt angles due to slight horizontal movements of the table. As a result R.K. McConnell and J. Geuer designed a new tilt calibrator using a cast iron table tilted on precision steel balls. Automated lifting and tilting features were incorporated into the new design. Construction of the new table was completed late in 1970 and an extensive series of evaluation tests will be carried out in 1971. If the new design proves satisfactory, it will provide an efficient means of calibrating quartz type gravimeters before and after each field survey.

## Gravity storage and retrieval system

In 1965, it became apparent that the existing punch card storage and retrieval system would soon be inadequate to handle the increasing number of new observations and the increasing requirement for plotting and other computer processing of the output file. Consequently, in that year, a study was made of the feasibility of a new storage and retrieval system using data files on magnetic tape and disk. This study inciuded the preparation and documentation of the computer hardware requirements, system flow charts, program specifications, and program flow charts. Although some preliminary experimental programming was done, the project had to be postponed for two years because there was no access to a large computer suitable for use with such a system.

In 1967, with the installation of an IBM 360 Model 65 computer at the Computer Bureau in Ottawa and with the acquisition by the Division of a new X-Y data plotter which used magnetic tape as input, the development of the planned storage and retrieval system was begun. By the spring of 1969, the new system
was operational. The present version of the system operates on an IBM 360 Model 85 computer at Systems Dimensions Limited in Ottawa. Its main components are a principal facts file of approximately 120,000 gravity observations stored on an IBM 2316 disk pack, and a suite of programs to store, update, and retrieve data from this file. Provision is made for output on the data plotter, the computer printer, punched cards, and magnetic tape.

Six major programs are used in this system. The gravity traverse reduction program is used to process the new observations, to detect errors in these observations, and to produce output records suitable for inclusion in the disk file. The general program produces maps at any scale on one of four different map projections showing the positions and values of selected gravity observations within a specified geographic area. Input in any combination from punched cards, card-image magnetic tape, and the disk file is possible. The plotting program can also select and display data within a specified range of any of the 14 data fields. Complete listings of the observations plotted on each map are provided automatically. The general utility program uses the disk file as input and produces punched cards, a card-image magnetic tape file, or a printer listing of selected observations within a specified geographical area. Given the latitude and longitude of the end points of a profile, the profile plotting program will select observations within a band of specified width along this line, interpolate them to the line, and plot a profile to the specified scale. The file updating program and the file reorganization program are used to update the disk file by the correction, deletion, or addition of data records. The former is used to process a small number of update records, while the latter is run whenever a large number of observations must be added to the file.

Using this system, the Division has been able to satisfy the needs of not only its own field officers and scientists but also those of universities, research institutions and the exploration industry. During the past year, the Division has
processed approximately 100 requests for data from external agencies, involving the production of approximately 1,000 special maps and associated printer listings.

During the past year, work has progressed on the adjustment of the world gravity network and the Canadian gravity network and new values of gravity for the control stations in these networks will probably be adopted in the near future. In this same period, certain agencies in Canada such as the Bedford Institute and the Nova Scotia Research Foundation have offered their data for the file. Also, the subcommittee on gravity has recommended that this file will become a national repository for gravity data. These developments will require the recomputation of the input data during the coming year and some redesign of the system. The result of this redesign and recomputation will be a more complete and compact data record, a new file indexing system which will allow the addition of data from any part of the world, and a suite of more modular and more flexible programs. It is expected that this new system will be operational sometime in 1972.

## Network processing and adjustment system

Concurrent with the development of the gravity storage and retrieval system, a compatible system for the processing, editing, and adjustment of observations taken at control stations in the Canadian gravity network has been developed. This system consists of four data files and eight major computer programs.

The control station file, which is the primary source for all control station information required by the system, consists of approximately 3,200 data records stored on a direct access file on an IBM 2316 disk pack, and a backup file on punched cards which provides the records necessary for the updating of this file. The gravimeter file consists of the conversion tables, calibration constants, and other parameters for approximately 50 instruments, and is stored as a direct access file on the same disk pack. The network observation file contains approximately 15,000 observations which have
been taken at control stations in Canada and throughout the world, and is stored on punched cards. The network tie file is an intermediate file which is computed from the network observation file and is stored on magnetic tape with a backup file on punched cards.

The control station file updating program is used to modify the control station file by correction, deletion, or addition of data records. The control station utility program can select data records based on a number of different parameters and conditions, sort the output in various ways, and produce punched cards, a card-image tape file, or a printer listing of the selected and sorted control station records. All requests for control station descriptions are accompanied by a current printer listing from this program. The tie processing program uses the control station and gravimeter files to process the new network observations to produce network tie records on punched cards and a listing of these new ties. The tie file updating program uses punched card input to update the network tie file on magnetic tape by correction, deletion, and addition of these records. Using a file of control stations such as is produced by the control station utility program, the network selection program will select the gravimeters and network ties required for the adjustment of a particular network. This selected network can be plotted using the network plotting program to show the positions of the control stations, their names or identification numbers, and the gravity ties observed. The colour and type of line indicate the type of instrument used for a particular gravity tie. The gravity difference and the number of ties observed are also given. These network diagrams are very useful for editing a network and determining its structure. The network editing program is then used to edit and check the selected observations, set up the observation and fixing equations, apply various weighting functions, and produce an output file of the results. The network adjustment program uses this output file to form and solve the normal equations, list the adjusted observations, punch new control station cards, and perform statistical analysis on the results.

The solution of the normal equations may be carried out either by matrix inversion for systems of less than 550 unknowns or by the Seidel iteration method for systems up to 3,500 unknowns.

Future development of this system will include the creation of a new network observation file on magnetic tape or disk, eliminating the intermediate network tie file, and the modification of the tie processing and network selection programs so that all computations and selections will be performed on a single file.

## Regional gravity surveys

During the period under review emphasis continued to be given to the completion of the regional gravity mapping of Canada (gravity stations spaced at intervals of $10-15 \mathrm{~km}$ ). Approximately 85 per cent of the regional measurements during the past four years were made by large helicopter supported field parties. Table I summarizes the observations by region and Figures 2 and 3 show the geographical coverage of the measurements.

Within the Canadian Shield and south of the Arctic Circle (latitude $66^{\circ} 30^{\prime} \mathrm{N}$ ) regional gravity observations are now complete. The first of the large systematic, helicopter supported regional mapping surveys was commenced in the southern Cordillera of British Columbia in 1968 using locations especially surveyed by the Surveys and Mapping Branch of the Department of Energy, Mines and Resources and by the Mapping and Charting Establishment, Department of National Defence. Gravity observations
were made at elevations of up to 3,000 metres above sea level during this survey. In 1970 an Armed Forces survey party from the Mapping and Charting Establishment carried out gravity observations in conjunction with establishing horizontal and vertical control for topographical mapping.

During 1969 the Polar Continental Shelf Project moved from Mould Bay on Prince Patrick Island to its present site on the Mackenzie River Delta. The gravity coverage in the Beaufort Sea is shown in Figures 2 and 3.

Detailed surveys have been made over various geological features, of which the Morin Anorthosite is an example. Detailed studies of this type have shown the need for a more rapid and accurate means of obtaining vertical control. An elevation meter acquired in 1969 will provide a means of increasing both accuracy and density of elevation control in those areas with an adequate road network.

## Regional gravity interpretation

Gulf of St Lawrence. The underwater gravity survey of the Gulf of St. Lawrence was completed in 1967. Three important conclusions emerged from the study of these data (Goodacre, Brule and Cooper, 1969). The Bouguer anomaly field over the northern portion of the Gulf is similar to that of the adjacent Precambrian Shield, but a distinct change in anomaly level from negative in the north to more positive in the south occurs in the Gulf and is believed to mark the boundary between the Grenville and Appalachian geological provinces. Basic intrusive rocks characteristic of this boundary are out-

Table I. Regional Gravity Mapping by the Earth Physics Branch
$\left.\begin{array}{lrc}\hline & \text { Region } & \text { Area (sq. mi) }\end{array}\right)$ No. of observations



Figure 3. Additional maps published by the Earth Physics Branch to April, 1971.
lined by a series of gravity highs extending from Gaspe Peninsula to Port au Port Peninsula, Newfoundland. A gravity low of -60 mgal near the Magdalen Islands is attributed to Carboniferous sediments of low density or to Devonian granite or alternatively their combined effect.

Scotian Shelf. In 1970 the east coast underwater gravity survey was extended to cover Cabot Strait, the Laurentian Channel, and parts of St. Pierre Bank and Scotian Shelf (Stephens, Goodacre and Cooper, 1971). The gravity anomalies between southwestern Newfoundland and Cape Breton Island suggest a structural continuity between these regions. On the shelf the dominant feature of the gravity field is the Orpheus anomaly, a linear gravity low, first described by Loncarevic and Ewing (1967). Loncarevic and Ewing attribute the low to a trough filled with Carboniferous deposits including evaporites and younger sediments of low density. A broad gravity low south of the Orpheus anomaly resembles anomalies underlain by granite batholiths in Nova Scotia and may have a similar source. Positive anomalies on the Shelf are believed to be related to dense preCarboniferous metamorphic rocks (Stephens et al., 1971).

## Canadian Shield

Quebec. The major gravity anomalies of Quebec were described by Tanner (1969). Three major anomalies, the Cape Smith high, the Labrador Trough low and the Grenville Front low, are associated with the boundaries between the Superior Province and younger structural provinces of the Shield. The Cape Smith high is believed to be caused by a fold belt of dense Proterozoic volcanic, sedimentary and basic intrusive rocks. Flanking gravity lows probably result from local crustal thickening which compensates the crustal load of the fold belt. The negative anomalies associated with the Labrador Trough and the Grenville Front are interpreted as edge effects between continental blocks of differing density and thickness which are in relative isostatic equilibrium. In both cases the crust of the younger provinces are denser and thicker than the Superior nucleus.

Another set of major anomalies described by Tanner occurs over the anorthosite masses of the eastern Grenville Province. Interpretation of these anomalies suggests that the anorthosites extend to considerable depth in the crust. Tanner and McConnell (1970) noted a correlation between gravity highs and occurrences of granulites in northern Quebec. They suggest the possibility of a 'granulite layer' throughout the Superior Province of northern Quebec.

Northern Ontario. Innes, Goodacre, Weber and McConnell (1967) presented evidence which strengthens the hypothesis previously proposed by Innes that the Kapuskasing gravity high marks an ancient zone of crustal rifting. The Kapuskasing anomaly, a major feature of the gravity field of northern Ontario, cuts across the characteristic east-west trends of the Superior Province. Several carbonatite complexes, some as old as 1.7 m.y., are aligned along the Kapuskasing structure and may place an upper limit on the age of the rift.

Studies of the geology and geophysical results in northern Ontario have also led to formulation of two new hypotheses concerning the early structural history of the Canadian Shield. These hypotheses assume that plate tectonics operated in Precambrian time. Gibb (1971) suggests that the Slave and Superior cratons were once contiguous forming a single Archean craton. Rupture and sea-floor spreading caused them to separate with formation of an early Proterozoic ocean. This hypothesis is based on the remarkable morphological fit of the Slave Province and eastern Hudson Bay obtained by rotating the Slave Province about a pole at $75^{\circ} 45^{\prime} \mathrm{N}\left( \pm 15^{\prime}\right)$, $51^{\circ} \mathrm{W}\left( \pm 1^{\circ}\right) . \mathrm{Gibb}$ and Walcott (1971) further suggest that closure of this ocean was responsible for formation of the now intervening Churchill Province mainly by accretion and coalescence of crustal fragments during the Hudsonian period of orogeny. Remnants of ancient oceanic deposits and oceanic crust juxtaposed with ancient continental margin deposits may still be preserved in suture zones within the Churchill Province. The most readily recognized probable suture is the
circum-Superior belt which includes the Setting-Moak Lakes structure, the Fox River structure, and Cape Smith Belt, and Labrador Trough.

Northern Manitoba. Gibb (1968a and b) completed a study of the gravity anomalies adjacent to the ChurchillSuperior boundary in northern Manitoba. Density determinations of some 2,000 Precambrian rock samples provided a basis for interpretation of the Bouguer anomalies in terms of relatively nearsurface mass distributions in the upper crust. In some parts of the area there is excellent correlation between the surface rocks, their densities, and the Bouguer anomalies. The Nelson River gravity high outlines a belt of dense granulites. To the northwest three gravity lows are interpreted as the gravity effects of three granitic intrusions of which one is largely exposed at Split Lake and the others are largely buried although their presence is supported by the occurrence of numerous stocks of intrusive granite within the gravity lows. The Nelson River high is separated from these lows by a steep gravity gradient which marks a boundary between rocks of predominantly different ages (Hudsonian and Kenoran) between latitudes $54^{\circ}$ and $56^{\circ} \mathrm{N}$.

Northern Saskatchewan. A study of the gravity anomaly field of northern Saskatchewan and part of northeastern Alberta was completed by Walcott (1968). The principal feature of the Bouguer anomaly field is a belt of intense anomalies parallel to the northeast structural trend of the crystalline basement of the region, bounded on the northwest and southeast by regions of comparatively low gravity relief. This belt comprises the Fond du Lac low, a linear anomaly at least 500 km long, about 70 km broad and with an amplitude of about -30 mgal , and the smaller Lisgar Lake and Stony Rapids highs with amplitudes of about +20 mgal . The Fond du Lac low defines a belt of low density rocks which geological mapping of one area suggests are granites. If the change in load due to the crustal density changes is compensated, as implied by studies of earth deformation due to unloading of

Pleistocene lakes, then the crust is about 5 km thinner beneath the low than in adjacent areas. A three dimensional model based on postulates of complete compensation and lateral changes in crustal density can explain the major features of the anomaly field.

Northwest Territories. A gravity map of the Coppermine region, Northwest Territories has been published by Hornal (1968). A large gravity high is related to the Coppermine basalt flows, the Muskox ultrabasic intrusion and the diabase dyke swarms in the area. Secondary features include (i) gravity highs along the north shore of Great Bear Lake and south of the Muskox intrusion, and (ii) gravity lows attributed to granites, in the vicinity of the Dismal Lakes and Coronation Gulf. A detailed gravity survey over the Muskox intrusion showed a smoother gravity field than expected, probably because a considerable portion of the dense olivine layers of the intrusion have been altered to less dense serpentine.

Interior Plains. In northern Alberta the gravity field is dominated by the gradual decrease in Bouguer anomaly towards the Rocky Mountains; this decrease reflects the isostatic compensation for the increasing topographic load (Walcott and Boyd, 1970). Other major anomalies indicate changes in lithology within the upper part of the Precambrian basement. The MacDonald fault is well defined gravitationally in the area of its exposure as far southwestward as Pine Point. The Peace River Uplift of northern Alberta may be isostatic in origin. Walcott (1970b) has discussed this interpretation in terms of differential loading by sediments on originally compensated basement topography. If the wavelength of topography is large, differential vertical movements can occur causing amplification of the original topography and growth of an arch with sediments thicker and the load greater on either side of the arch.

Prior to interpreting the major gravity anomalies of the sedimentary basin in the southern Interior Plains, Dr. J. Maxant, a postdoctorate fellow, has undertaken an intensive study of the densities of the sedimentary rocks. Gamma-gamma logs
from about 450 wells distributed throughout the basin are the main source of density information. Densities, formation tops and lithological descriptions, made available through the co-operation of numerous oil companies in Canada, are now stored on cards and preliminary analysis of these data has commenced.
Canadian Cordillera. A Bouguer anomaly map (scale 1:1,000,000) covering the continental shelf, Vancouver Island, the Queen Charlotte Islands and the fiords of the west coast of British Columbia has been published by Stacey, Stephens, Cooper and Brule (1969). More detailed gravity, magnetic and bathymetric maps are available for the Strait of Georgia and the Strait of Juan de Fuca (Stacey and Steele, 1970). The major features of the gravity field are: (1) a positive Bouguer anomaly along the western edge of the area, which is associated with the change from continental to oceanic crust, and (2) a negative anomaly along the Coast Mountains, which is attributed to the thickening of the continental crust below these mountains. On the eastern side of the Queen Charlotte Islands, Hecate Strait, Queen Charlotte Sound, and Vancouver Island, the average Bouguer anomaly is approximately zero, with local anomalies superimposed on a fairly flat gravity field. Several of these local anomalies are related to density variations in the surface rocks. A crustal model for the southern part of the Canadian Cordillera has been developed on the assumption that isostatic compensation is complete and local. The area included in the model lies between $49^{\circ}$ and $51^{\circ} \mathrm{N}$ and extends from the Plains of southern Alberta to the vicinity of the Juan de Fuca Ridge. In the model, the thickness of the crust below the Plains, below the mountains of British Columbia and below the ocean west of Vancouver Island appears to be in good agreement with the depth of the M-discontinuity derived from seismic data. The results are ambiguous over Vancouver Island due to the very strong gravity anomaly related to the thinning of the crust west of the Island towards the ocean. However, the results suggest that the crust below the Island may be 70 km thick, which would be in reasonable agreement with seismic and magnetotel-
luric results, and with the requirements of plate tectonics (Berry, Jacoby, Niblett and Stacey, in press).

Hudson Bay. Weber and Goodacre (1968) have completed an analysis of the crustmantle boundary in Hudson Bay from gravity and seismic observations. A study of the results of the gravity and seismic surveys in Hudson Bay in 1965 showed that the gravitational effect of a two-layer crustal model based on the seismically determined depths has no correlation with the observed gravity anomalies (Innes et al., 1968). On the profile from Churchill to Povungnituk the gravity and seismic observations could be reconciled by postulating lateral variations of the acoustic compressional wave velocity within the crust. A crustal model was calculated, consistent with the seismic and gravity observations for which the crustal velocity varies from 6.15 to 6.56 $\mathrm{km} / \mathrm{sec}$ and the postulated depths were almost entirely within the confidence limits of the original model.

The postulated velocity variations were compared with the lower refractor velocities of the shallow seismic survey on the hypotheses that the crustal velocities are systematically higher than the crystalline surface velocities and that there is a correlation between variations in crustal and surface velocities. The test was inconclusive because bottom refractor velocities were higher than crustal velocities in two areas where volcanic flows and high-velocity sediments might be present.

The case of linearly related velocity (V) and density ( $\rho$ ) variations was analyzed and it was shown that the gravitational effect of the crust-mantle boundary undulations might be completely masked or even over-balanced by density changes in the crust if $\frac{d \rho}{d V} \geq 0.11 \mathrm{~g} \mathrm{~cm}^{-4} \mathrm{sec}$. The crust could be characterized by having dominant velocity variations (in which case the gravity anomaly reflects the undulations of the crust-mantle boundary) or dominant density variations (in which case the gravity anomaly inversely reflects the crust-mantle boundary undulations) depending on the relationship between average crustal density and average crustal velocity.

Arctic Canada. Two Bouguer anomaly maps at a scale of $1: 1,000,000$ covering the area bounded by latitudes $74^{\circ} \mathrm{N}$ and $82^{\circ} \mathrm{N}$ and longitudes $60^{\circ} \mathrm{W}$ and $141^{\circ} \mathrm{W}$ have been compiled from about 8,800 gravity observations made in the period 1960-68 (Sobczak and Weber, 1970). On land, relationships between gravity anomalies and sedimentary facies changes and thickness of sediments have been established. Models of crustal structure have been derived from gravity, density, magnetic and seismic measurements. The regional free air anomaly map shows a series of positive elliptically-shaped anomalies aligned along the Polar Continental Margin. These anomalies, with amplitudes in excess of 100 mgal and with horizontal gradients of up to $2.5 \mathrm{mgal} / \mathrm{km}$, are explained by the combined effect of sedimentary thickening (to 10 km ) and crustal thinning (to 20 km ) at the margin (Sobczak and Weber, in press).

A paper on the densities of crystalline, carbonate and clastic rocks from the Queen Elizabeth Islands has also been published (Sobczak, Weber and Roots, 1970).

A study of the gravity field over Somerset, Prince of Wales, and northern Baffin Islands has been presented by Berkhout (1970). Major negative anomlies occur on Borden and Brodeur peninsulas, in the area east of Agu Bay, on northeastern Somerset Island, and on northwestern Prince of Wales Island. These lows are explained by the presence of Upper Proterozoic metasedimentary rocks. An important conclusion is that during Upper Proterozoic time vast basins existed which were the sites of accumulation of clastic sediments. The observed gravity field outlines these basins and suggests that they may be interconnected.

A northerly trending gravity high is associated with the Boothia Uplift and two parallel highs occur to the west of it, all three being separated by gravity lows. The density contrast between crystalline rocks of the uplift and the adjacent Paleozoic rocks is not sufficient to explain the change of gravity over the Boothia Uplift. It is suggested that three northerly trending basement uplifts exist, separated by graben in which Upper Proterozoic quartzitic rocks occur. The

Boothia Uplift became active again in Paleozoic time and overthrusts the quartzitic rocks in the west; this is reflected by observed negative anomalies along its western flank.

The gravity high over Prince Regent Inlet may reflect a basemant fault block beneath the Paleozoic rocks, whereas adjacent gravity lows represent the depressed areas occupied by thick deposits of Upper Proterozoic quartzitic rocks. The northerly and northeasterly trends of the two systems of basement fault blocks cut across the generally easterly (Archean) trend of basement structures, as on Baffin Island. Similar observations have been made in the Canadian Shield. Berkhout concludes that these unusual trends may possibly originate along ancient orogenic zones with northerly and northeasterly trends.

Three Bouguer anomaly maps at a scale of $1: 1,000,000$ and contoured at 5 mgal intervals have been prepared from 6,100 gravity observations made in the northern Interior Plains and on the Beaufort Sea from latitude $60^{\circ} \mathrm{N}$ to $72^{\circ} \mathrm{N}$ (Hornal, Sobczak, Burke and Stephens, 1970). The major features of the gravity field are: a gravity low over the Mackenzie Mountains which is attributed to a thickened sedimentary sequence and a deeper crust-mantle boundary; a relatively positive anomaly of 50 mgal striking north from Trout Lake to Great Bear Lake which reflects a ridge of mafic rock within the Precambrian basement; a negative anomaly over the Mackenzie River Delta of 55 mgal which results from the deposition of more than 21,000 feet of Cretaceous and Tertiary sediments; and a circular positive anomaly of 130 mgal situated south of Darnley Bay which is explained by a cone-shaped basic intrusion. Smaller variations in the gravity field in the Interior Plains may be attributed to changes in the depth to the Precambrian basement and density variations within the sedimentary column.

## Detailed gravity investigations

Alexandria area, Ontario. Sobczak (1969) has completed a study of the gravity field in the Alexandria area of eastern Ontario. Negative Bouguer anomalies are correlated with the Chatham-Grenville
syenite stock and a similar intrusion at Mount Rigaud on the southern border of the Grenville-A subprovince. It is postulated that the negative anomaly near Plaisance indicates the presence of a similar intrusion below the Paleozoic cover. The Alexandria high, a positive residual Bouguer anomaly which extends from Lunenburg to Pointe aux Chênes, may be explained by the presence of a basic lenticular body of thickness varying from 6,000 to 9,000 feet and width of 50,000 feet at a depth varying from 3,000 to 5,000 feet. The approximate thickness of the Grenville Series is 11,000 to 12,000 feet along the crest of the Alexandria high. The regional gravity gradient which increases from -30 milligals in the northwest to +10 milligals in the southeast of the area is correlated with a rise of over 3 kilometres $(10,000$ feet) of the Mohorovicic discontinuity.

Bancroft area, Ontario. W.R. Jacoby has completed a detailed gravity study of the Bancroft area, Ontario. The correlation between surface geology and gravity is excellent and there is enough density information to calculate the sub-surface mass distribution with considerable confidence. The low density granite gneiss, outcropping in large domes, batholiths and smaller plutons, seems to be extensive under a rather shallow metasedjmentary cover $1-4 \mathrm{~km}$ thick. This indicates that the granite may represent partly pre-Grenville basement, remobilized or anatectically melted, and partly Grenville deposits, intensely metamorphosed and granitized. The granites and the gravity field show a distinct waveform over several wavelengths ( 20 to 30 km and 5 to 6 km ). This wavelength is used to study the mechanics of granite emplacement. No vertical variation of the base of the granitic layer was indicated for the region.

Preparation of a comprehensive paper on this study was nearing completion at the end of 1970.

Timmins - Senneterre area, OntarioQuebec. A study of the gravity field in the Timmins Senneterre mining belt was completed by Gibb, van Boeckel and Hornal (1969). The area is studded with many granite batholiths of variable com-
position which are outlined by intense negative gravity anomalies. The whole region was regarded as one great roof pendant and on this assumption model studies show that the volcanic belts extend to depths ranging from 3 to 5 km . Variations in anomaly level within the batholiths were correlated with compositional and density differences in the granites which have a compositional range which includes granodiorite and diorite. One of these batholiths, the Round Lake batholith, was the subject of a separate study (Gibb and van Boeckel, 1970). Two possible three-dimensional models of the batholith were presented which depend on different assumptions. The first model involves normal faulting of the batholith to explain the variations in anomaly level within the batholith. In this model the granite is assumed to be homogeneous in density and extends to a maximum depth of 10 km . Alternatively density variations corresponding to a facies change within the pluton may be the major cause of the local internal anomaly variations. In this interpretation the true thickness of the granite connot be evaluated as the whole region is assumed to be underlain by granite, but the maximum thickness of the surrounding basic volcanic rocks is 5 km.

Piercement structures in the Arctic Islands. Reconnaissance gravity surveys over three evaporite piercement domes in the Canadian Arctic Islands have been interpreted by Spector and Hornal (1970). Each dome was considered as a right-vertical cylinder divided into two homogeneous regions, a high density anhydrite zone ( $2.9 \mathrm{~g} / \mathrm{cm}^{3}$ ) overlying a low density gypsum and/or rock salt zone $\left(2.3 \mathrm{~g} / \mathrm{cm}^{3}\right)$. The cylinder is surrounded by a sedimentary sequence which has a uniform density of $2.4 \mathrm{~g} / \mathrm{cm}^{3}$. A leastsquares approach was used to estimate the thickness of the anhydrite and gypsum-rock salt zones. The three sets of estimates gave a range of 200 to 550 m for the anhydrite thickness and a range of 700 to $5,500 \mathrm{~m}$ for the vertical extent of domes. In each case the depths were less than expected on the basis of estimates from seismic and geological data. Possible explanations for this are: (a) the crosssectional area of each dome decreases
with depth; (b) the existence of a transition zone where a gradation occurs between the high and low density zones; and (c) the effective density contrast of the low density zone is less than 0.1 $\mathrm{g} / \mathrm{cm}^{3}$.

Darnley Bay, Northwest Territories. The largest isolated gravity anomaly (130 mgal) discovered in Canada so far occurs at Darnley Bay, N.W.T. This anomaly was described by Hornal et al, (1970) who suggested that it is caused by a basic intrusion with the shape of an inverted cone and a thickness of crustal dimensions ( -40 km ). Stacey (in press) has completed a further study of this anomaly and concludes that a coneshaped basic intrusion with or without an ultrabasic core can explain the anomaly equally well. He compares his models with lopoliths having similar gravity anomalies, with Tertiary igneous centres in Scotland, and with present day sea-mounts.

Crater investigations. The investigation of Canadian structural and topographic features for evidence of origin by hypervelocity impact of cosmic bodies began in 1950. By 1966 twelve Canadian sites had been shown to have the approximately circular outline, strong fracturing and brecciation and megascopic and microscopic evidence for shock metamorphism which are the main characteristics of eroded but otherwise undisturbed impact structures. Most of the sites had been investigated by gravity, magnetic and, in some cases, seismic methods. These studies showed the structures to have moderate to weak gravity anomalies consistent with their being underlain by rocks of low density, generally weak magnetic susceptibility and low seismic velocity to depths no greater than their radius at the surface.

Since 1966, a further six sites have been shown to contain shock metamorphosed rocks. Two of these, Steen River, Alberta and Lake St. Martin, Manitoba have weak surface expression, being buried by later sediments to a large extent. Two others, Mistastin Lake, Labrador, and Lake Wanapitei, Ontario closely resemble craters such as those at Clearwater Lake and Deep Bay. The
remaining two, Charlevoix, Quebec and Sudbury, Ontario have been eroded and also deformed to some extent by tectonic events subsequent to their formation.

Geophysical data acquired to 1966 included gravity and magnetic surveys of eight craters and seismic surveys of five. Magnetic data mainly airborne are now available for an additional five sites and gravity for eight. A gravity Bouguer anomaly map has been published for Nicholson Lake crater (Dence et al, 1968) while detailed maps by Dr. J. Popelar for Sudbury and Lake Wanapitei are in an advanced stage of preparation. Detailed gravity data are also available for Manicouagan and have been included in the regional gravity map series. Altogether of the eight, only Nicholson Lake and Lake Wanapitei have clearly expressed negative gravity anomaly fields. The rest all show indications of gravity lows, but lie within complex regional fields which appear to obscure or distort the crater anomalies. More detailed data are required to define clearly the anomalies associated with these structures.

## Earth tides and crustal loading

Both the Earth Physics Branch and Dalhousie University have been concerned with this subject. Theoretical and experimental work has been directed mainly to the problem of correcting for the perturbing effect of the ocean tide on measurements of the earth tide. Until this correction can be made with high accuracy the original purpose of earth-tide measurements, the determination of the Love numbers, cannot be realized. A technique for estimating the correction has been developed by the Earth Physics Branch on the assumption of a given global distribution of ocean tides loading a Gutenberg-model earth. However, the Love numbers are presently better known than is the global distribution of ocean tides or the response of the lithosphere to surface loading. Consequently, this technique has been used only to explain the general features of the global variation in earth-tide measurements and, in a reverse sense, to identify definite regional anomalies due either to incorrect ocean tide data or to anomalous response of the lithosphere to surface loading. One such anomaly has been revealed by the dis-
agreement between theoretical results obtained by the Earth Physics Branch with earth-tide measurements made at several locations across the United States by Columbia University. Measurements in the western half of the United States show a loading effect due to the tides in the eastern Pacific Ocean which is smaller than that expected on the basis of published ocean-tide data. The Earth Physics Branch intends during the next two years to make a series of earth-tide gravity measurements throughout Canada to identify and investigate other anomalies. These will be fairly short observations beginning in the north at Alert (lat. $83^{\circ} \mathrm{N}$ ) and proceeding south along a mid-continental line to link with similar measurements in the United States.

On a regional scale the ocean tide is sometimes accurately known and the feasibility of using it to probe the upper layers of the earth has been investigated by Bower (1969) with measurements in England and by Lambert (1970) and Beaumont and Lambert with measurements in the Bay of Fundy area. This type of investigation, which relies principally on precise tilt measurements, will continue with a view to improving both the experimental and the analysis techniques available. At the Earth Physics Branch D. Bower is developing a long watertube tiltmeter which can be precisely calibrated and which is expected to be zero stable. Also at the Earth Physics Branch data analysis techniques such as the "response method" are being applied by A. Lambert in order to isolate the tidal component of tilt from coherent "noise" effects. C. Beaumont at Dalhousie University is constructing a finiteelement crustal model of the Bay of Fundy area which will permit a generalized theoretical approach allowing for multilayers, lateral homogeneities and discontinuities.

The underground recording station near Ottawa was closed early in 1970 after approximately four years of recording both gravity and tilt earth-tide measurements. A new site in the same area is being prepared as a permanent station and will be equipped with both pendulum and hydrostatic type tiltmeters.

Flexural rigidity, thickness and viscosity of the lithosphere

In a series of recent studies Walcott (1970b) has modelled the earth's lithosphere and asthenosphere as a thin sheet and a fluid substratum respectively. The flexural rigidity of the lithosphere was deduced from observations of the wavelength and amplitude of bending in the vicinity of supercrustal loads. Data from Lake Bonneville given by M.D. Crittenden, Jr. were reinterpreted to give a value for the flexural rigidity of the lithosphere in the Basin and Range province of the western United States of $5 \times 10^{22}$ Newton meters. Observations of loading in Canada give values for the flexural rigidity greater than $3 \times 10^{23} \mathrm{~N} \mathrm{~m}$ for the Caribou Mountains in Northern Alberta (Walcott, 1970a); about $4 \times 10^{23} \mathrm{~N} \mathrm{~m}$ for the topography over the Interior Plains (Walcott, 1970a); about $10^{23} \mathrm{~N} \mathrm{~m}$ for the Boothia uplift in arctic Canada (Walcott, 1970b); and about $10^{25} \mathrm{~N} \mathrm{~m}$ for the bending of the beaches of Pleistocene Lakes Agassiz and Algonquin. The flexure of the lithosphere at Hawaii and the bending of the oceanic lithosphere near island arcs give values of about $2 \times 10^{23} \mathrm{~N}$ m (Walcott, 1970c). For short-term loads ( $10^{3}-10^{4}$ years) the flexural rigidity of the continental lithosphere is almost two orders of magnitude larger than for long. term loads, indicating nonelastic behaviour of the lithosphere with a viscous (about $10^{23} \mathrm{~N}$ sec $\mathrm{m}^{-2}$ ) as well as an elastic response to stress. From the values of the flexural rigidity the thickness of the continental lithosphere is inferred to be about 110 km and that of the oceanic lithosphere about 75 km or more. The anomalously low flexural rigidity of the lithosphere of the Basin and Range province may be due to a very thin lithosphere, only about 20 km thick, with hot, lower crustal material acting as an asthenosphere.

## Gravity interpretation methods

Jacoby (1970) has published sets of diagrams of the normalized peak gravity effect of exposed rock bodies which can be used to determine the depth to which the bodies extend. The method is straightforward and is applicable to rock bodies of any shape.

An accurate method of computing the first vertical derivatives at different elevations from two-dimensional gravity profiles has been published by Paul (1970). He has shown that the accuracy of the computed first vertical derivative values depends significantly on a remainder term due to the finite length of the anomaly profile. Paul has also completed the development of a quantitative method to interpret gravity anomalies with circular symmetry. In this method the radial profile is first transformed to a vertical profile using the upward continuation principle, direct interpretation of the physical and geometrical parameters of the local causative body is then possible.

A weighted summation method for upward continuation of gravity data from a plane has been developed by Paul and Nagy (in press) under the assumption that the observations are available at regular intervals. The upward continued value has been expressed as the sum of individual gravity values and the corresponding theoretical coefficients. Besides the usual parameters involving horizontal and vertical distances, these theoretical coefficients have been generalized to be dependent also upon (i) the order of a low order polynomial assumed to represent the gravity variation around a grid point and (ii) the weights assigned to the gravity values at the nearest four points used for least square determination of the polynomial. The method has been tested with theoretical models and field gravity data and a paper has been submitted for publication.

## Physical geodesy

Graphic representation. For the purpose of correlating various types of data (gravimetric, geodetic) and selecting areas to test various hypotheses, graphic representation of data is essential. The following developments are mentioned:

1. Compilation of an average free air gravity anomaly map of Canada. Using piecewise surface fitting technique, representative values over surface elements are obtained. The selection of a grid separation of about 55 km resulted in 2,923 surface elements on
which basis the free air map has been compiled. A paper describing the details is forthcoming.
2. Development of a special plotting package by which deflections of the vertical (input data represented as vector), geoidal height changes calculated from these reflection values can be plotted in the desired map projections and scales.

Computation of changes in the deflections of the vertical from gravity data. Programming of a method using local plane co-ordinate system and integrating out to a few hundred km around the computation point has been compiled. For checking the procedure see paragraph on model studies.

Model studies. The basic element for model studies is a right rectangular parallelopiped for which the gravity, the deflection of the vertical, the potential, and other quantities can be calculated with high precision. By combinations of elements, various potential fields can be computed to simulate practical situations satisfactorily. The model gravity field can then be used as a basis for upward continuation, computation of the deflections of the vertical, and other operations. Comparison of computations using the model field with those values obtained directly from the mass model serve not only to check the computations but also to provide a basis to specify requirements in the practical situation.

Upward continuation of gravity data from a plane, A method of upward continuation of potential fields has been developed assuming that the input data is regularly distributed over a plane. The computational procedure has been verified on a model for various elevations. A paper on this study by M. Paul and D. Nagy has been submitted for publication.

Upward continuation from an irregular surface. This is an extension of the above work and is being carried out by M. Paul. This method recognizes that the observations are made on actual topographic surface. The computational procedure is an iterative one which involves the integral for downward continuation from a plane.

Data representation. Y. Hagiwara, postdoctorate fellow, has investigated various methods of obtaining representative values from point distribution and techniques for predicting values in unsurveyed areas. Spherical harmonics expansion requires too many terms for adequate short wavelength representation to render its use feasible at present. The method accepted is that based on double Fourier series expansion.

Computation of geoid and the deflection of the vertical. Y. Hagiwara has also investigated techniques of using surface gravity data to provide the detail lacking in satellite measurements. The large wavelength structures for both the geoid and the deflection of the vertical have been computed from the spherical harmonics representation of the potential and gravity as determined by the Smithsonian Astrophysical Observatory 1967. More detailed computations of the geoid and the deflection values have been made using representative values from surface gravity data in surveyed regions and extrapolated values for unsurveyed regions within Canada. Co-ordinate transformation of the surface gravity data was also made for compatibility with satellite data. A publication giving the details of the various methods used and results obtained is under preparation.

Singularity. The singularities of the Stokes' and Vening-Meinesz's functions at the origin and their treatments are well known. In other cases when Fourier techniques or the methods of Molodenskii and Bjerhammer are used for the calculation of geoidal heights or the deflections of the vertical, the treatments of the singularities are more involved. M. Paul has examined this problem from the standpoint of practical computations.

## Polar studies

In May 1967 and in April 1969 the Earth Physics Branch in co-operation with the Polar Continental Shelf Project carried out multidisciplinary geophysical studies in the vicinity of the North Pole. The expeditions under the leadership of J.R. Weber included participants from private industry and universities. The original objective was to establish a
gravity traverse from Ellesmere Island to the North Pole. The biggest problem facing the project was precise navigation. Drift of the pack ice and atmospheric refraction results in accuracy of position fixes in the polar region obtained from conventional sun observations that is no better than a few kilometres. The problem was solved by R.L. Lillestrand from the Research Division of Control Data Corporation in Minneapolis who developed techniques involving sighting on various celestial targets during daytime and improved methods to solve for ice drift by computer. The computer was programmed to convert time of observations and zenith angles of the celestial target into position and drift velocity. A communication link for data transmission between the expedition and the computer in Minneapolis was established with the help of radio amateurs in Alert and Ottawa (Lillestrand, Grosch and Vanelli, 1967).

For logistical reasons it was not possible in 1967 to obtain aircraft suitable for making spot landings between Ellesmere Island and the Pole. Instead the expedition was airlifted to the Pole with a Bristol Freighter aircraft. The scientists drifted with the pack ice a distance of 30 km over a seven-day period during which time gravity observations were taken and the experimental navigational techniques were tested. These tests included ranging to an acoustic transponder dropped to the ocean floor.

Tilt measurements carried out on Fletcher's Ice Island (T-3) by Browne and Crary (1959)* more than a decade earlier, prompted an attempt to measure the tilt of the fluid surface of the ocean. Three holes were drilled through the ice and by levelling from water surface to water surface a tilt of eight seconds of arc was observed. It was realized that if such tilts persist over long distances along atmospheric pressure gradients (as Browne and Crary's observations indicated) it would imply sea level changes of a magnitude which would significantly affect the gravity measurements. Accordingly J.R. Weber developed a hydrostatic levelling

[^8]system capable of measuring the tilt of the fluid ocean surface to an accuracy of about $\pm 0.01$ second of arc. Spot observations with this instrument in the vicinity of the North Pole in 1969 and in the Gulf of St. Lawrence in 1970 indicated tilts of up to about one second of arc (Weber and Lillestrand, 1971). Instrumentation is presently being developed with the aim of setting up an array of automatic tilt recording meters during the Arctic Ice Deformation Joint Experiment (AIDJEX) in the Arctic Ocean in 1973 in order to determine the deformation of the ocean surface with time.

During the 1969 expedition some 40 gravity stations were established between the Lincoln Sea and the North Pole, across the Lomonosov Ridge and in the vicinity of the North Pole using navigational techniques developed during the earlier expedition. The expedition established a base camp 50 km from the North Pole and over a period of 26 days drifted a distance of 80 km with the transpolar current. Advanced navigational techniques involving some 400 star observations, the use of satellite transit observations, and sonar trilateration from a number of acoustic transponders on the ocean floor were used to determine the path of the ice floe. An Omega VLF receiver was also used as a navigational aid, but because of unusually poor radio propagation conditions the system was inoperative most of the time. The relative agreement between the sonar drift path and the positions determined from the celestial observations is excellent, being of the order of 70 m . Evaluation of the satellite data has been delayed because the unique geometric configuration of satellite observations in the polar areas requires a different method for the reduction of the data than in more southerly latitudes. It is hoped to apply the results of the satellite data, the astronomic observations and the sonar trilateration to determine the absolute deflection of the plumbline. In addition to these geodetic observations continuous current measurements 2 m and 100 m below sea level and wind measurements 3 m above the ice surface as well as a number of hydro-casts were made.

Bedford Institute (Atlantic Oceanographic Laboratory)

## Detailed gravity surveys

Hydrographic-geophysical survey of the eastern Canada Continental Shelf. Since 1966, the Atlantic Oceanographic Laboratory at the Bedford Institute has greatly increased its geophysical coverage of the eastern continental margin of Canada. This has been largely due to the collaboration existing between the Marine Geophysics Section and the Hydrographic Section of the Institute. The prime responsibility of the A.O.L. Hydrographic Section is charting all navigable waters within the Atlantic Region, as applicable to navigation requirements. The Region is defined as Canada's Atlantic Seaboard, the Gulf of St. Lawrence east of Pointe-des-Monts, Hudson Bay and the eastern Arctic. The surveys conducted by the Section satisfy requirements in navigation, fisheries and mineral exploration. All positioning of the ship is done by Lambda (low ambiguity decca) in the range/range mode, thus providing the most accurate navigation available in the areas surveyed so far. After a mutual study of each group's surveying techniques, it was decided that the two disciplines could be combined to produce a highly effective multi-disciplinary survey operation covering the Canadian east coast continental margin with measurements of bathymetry, gravity and magnetics.

The method of operation now existing is that the hydrographers carry out an initial survey of their proposed survey area at a line spacing of 2 or 4 miles, depending upon the density of measurements required to give good geophysical control. With the completion of this multidisciplinary portion of the survey, the hydrographers continue surveying the same area at a reduced line spacing, this being $1 / 2$ or 1 mile line spacing at water depths less than 50 fathoms. During this latter portion of the cruise geophysical studies are carried out as opportunity and manpower permits.

The data collection and reduction operation has now passed into the hands of the Hydrographic Section and a series
of natural resources charts* are to be produced by them, with editions covering bathymetry, gravity (free air anomaly) and magnetics (total field). At present only the three editions of sheet 14956 are available (covering Marsden Squares 14956 and 14957: latitude $45^{\circ}-46^{\circ} \mathrm{N}$, longitude $46^{\circ}-48^{\circ} \mathrm{W}$ ). Four sheets covering the Tail of the Bank area (latitude $42^{\circ}-44^{\circ} \mathrm{N}$, longitude $48^{\circ}-52^{\circ} \mathrm{W}$ ) are expected to be published before spring 1971. Geophysical data from the Grand Bank of Newfoundland and the Gulf of St. Lawrence is undergoing final processing at the Institute, and will be turned over to the cartographers at about the same time. The feasibility of extending natural resources charts to cover all Canadian offshore is presently being investigated by the Canadian Hydrographic Service.

While the routine data collection, reduction and chart production are in the hands of the Hydrographic Section, responsibilities for the initial planning of the geophysical aspects of the multidisciplinary cruises and their data interpretation still lie with the Marine Geophysics Section. This development is still in its infancy to the extent that the Hydrographic Section is still learning the techniques of geophysical surveying and data reduction. Meanwhile, Marine Geophysics is still attempting to exploit the positioning facilities provided by the surveys, in increasing the accuracy of sea surface gravity measurements as limited by the calculation of the Eotvos correction. The seismic group is also investigating the possibility of adding seismic reflection profiling to the functions of the survey.
Grand Banks. The area surveyed in 1966 and 1967 lies approximately between longitude $53^{\circ} \mathrm{W}$ and $44^{\circ} \mathrm{W}$ and latitude $45^{\circ} \mathrm{N}$ and $48^{\circ} \mathrm{N}$. The most interesting features of the gravity charts reveal:

1. Steep horizontal gradients (up to 12 mgals per km).
2. A large "low" near the central portion of the survey area (minimum of -35 mgals with general low area extending over approximately $1^{\circ} \times 1^{\circ}$ ).

[^9]3. An extensive "high" in the north central portion of the survey area (maximum of +136 mgals with general high area extending over approximately $1^{\circ} \times 1^{\circ}$ ).
4. A positive zone of +60 to +80 mgals associated with the Flemish Cap.
5. A belt of circular positive features with amplitudes from 20 to 100 mgals lying within and parallel to the 100 and 1,000 fathoms contour lines.
The top of the Grand Banks, especially within the 50 fathom contour is remarkably flat; therefore the steep gradients of the gravity field are due to major variations in the density distribution and/or structure of the subsurface rocks. This, coupled with the fact that the magnetic field in the same area is very smooth, indicates that the density variations are due to changes in structure within the sedimentary rock section. The gravity "lows" that are relatively small in areal extent are believed to be due to salt structures, while the large low in the central portion of the survey area is believed to be a basinal type feature with a total sedimentary rock thickness probably in excess of 6 km . In the area of survey, two 30 -mile and one 150 -mile refraction seismic lines were shot. Six distinct refraction layers were mapped with the following velocities: $1.67,1.84$, $2.69,4.59,5.40$ and $6.03 \mathrm{~km} / \mathrm{sec}$. The highest velocity probably identifies cristalline basement rock in this area. As expected from previous investigations, a thickness of sedimentary rock in excess of 3 km was found in the vicinity of the long profile near $45^{\circ} \mathrm{N}$ and $49^{\circ} \mathrm{W}$.

Gulf of St. Lawrence. In 1968 and 1969 a multidisciplinary survey was carried out in the Gulf of St. Lawrence. In surveying the Gulf east of $62^{\circ} \mathrm{W}$ and north of $47^{\circ} \mathrm{N}$ approximately $55,000 \mathrm{~km}$ of bathymetry, magnetics and gravity data were obtained. In the northeastern areas, surveyed in 1968, the gravity map covering part of the western flank of the Canadian Appalachians is featureless when compared with the gravity map of the Grand Banks which comprise part of the eastern flank. In the southeast Gulf, the gravity field is more complex and is dominated by a large negative free-air anomaly of
-100 mgals (Bouguer anomaly of -60 mgals) to the northeast of Magdalen Islands. The analysis of this gravity information has only recently been started.

The surveyed area of the Gulf has been covered previously with sea-bottom gravity measurements made by the Gravity Division of Earth Physics Branch. The data in the eastern Gulf of St. Lawrence covering the areas of both the 1968 and 1969 A.O.L. surveys are being analyzed with the intention of determining whether this type of survey with greater concentration of survey lines (1or 2 -mile intervals), speed of data collection, and higher resolution of gravity anomalies is a better investment of money and manpower than the 8 -mile grid bottom gravimeter survey providing more accurate gravity values. Initial comparison of the data yields a mean difference of 2.1 mgals between A.O.L. and E.P.B. over the 1969 survey area with the E.P.B. measurements being higher. Separating the E.P.B. measurements into different years of operation, there also appears to be a temporal variation in the underwater measurements. This is suspected to be the result of using different depth transducers in each of those years ${ }^{\text { }}$ operations. These and further results derived from the analysis will provide a basis for planning future complementary surveys by the two agencies.

Western Arctic. In response to the requirement for better navigation charts in the north the locale of the mapping program was shifted to the western Arctic for the 1970 field season. In the Beaufort Sea, bathymetry, gravity, and total magnetic field were measured at ${ }^{1} / 4$ mile line spacing over 1,500 square miles. The area surveyed was centred on the Admiral's Finger, a shoal located approximately 50 miles north of Atkinson Point, and discovered in 1969 by S.S. Manhattan during her passage to Prudhoe Bay, Alaska.

During the course of the survey, about 80 additional shoals were discovered, some rising to within 17 metres of the surface. Observed gravity in the area was dominated by the shelf anomaly, exceeding 80 mgal at its maximum value,
and paralleling the 100 -metre contour. Except for the northeast corner of the survey area, there was no indication of shallow disturbances to the earth's magnetic field.

In conjunction with the western Arctic program, ships' passages from Victoria to the Beaufort Sea and then to Halifax provided additional opportunities for the collection of geophysical data, especially in Baffin Bay. Eight thousand km of gravity data were obtained by CSS Hudson and CSS Baffin between Resolute and Funk Island, Newfoundland. About one half of the data were collected during a survey of Baffin Bay in an attempt to ascertain its crustal structure.

Future plans. The proposed hydro-graphic-geophysical survey for 1971 will complete the surveying of Flemish Cap and then proceed northward along the continental shelves of Newfoundland and Labrador. At the present rate of coverage, and if priorities do not change, it is hoped to complete the survey up to Cape Chidley within the next five years.

## Regional geophysical surveys

Mid - Atlantic Ridge. In 1968, the third Institute expedition to the Mid-Atlantic Ridge continued the comprehensive geophysical survey of the area between $45^{\circ}$ and $46^{\circ}$ which began with the voyage of R.R.S. Discovery II in 1960. Two ships were used in this survey to provide a shooting and receiving ship for a seismic experiment carried out on the eastern flanks of the ridge. Satellite navigation provided absolute positioning for the survey and radar transponder buoys were moored to provide accurate navigation within the survey area. Nine thousand km of bathymetric, magnetic and gravity measurements were made at a spacing of less than two miles to complete the detailed survey of the western flank of the ridge. In addition some $4,000 \mathrm{~km}$ of surveying were completed on the eastern flank. The total coverage is now approximately between $45^{\circ} \mathrm{N}$ and $46^{\circ} \mathrm{N}$ from $26^{\circ} 30^{\circ} \mathrm{W}$ to $30^{\circ} \mathrm{W}$. All the gravity data obtained during the three expeditions have now been compiled and the data adjusted. Free air and Bouguer anomalies have been calculated for the entire region
and interpretation is proceeding. The associated seismic refraction data will be used in model studies to be made on the crustal structure of the $3^{\circ}$ by $1^{\circ}$ area. Preliminary gravity results from the combined surveys were included in a paper presented at the 50th Annual General Meeting of the American Geophysical Union (A.G.U.).
Bay of Fundy. Three thousand seven hundred kilometres of gravity, magnetic and bathymetric data acquired in the Bay of Fundy (between $66^{\circ} \mathrm{W}$ and $67^{\circ} 10^{\prime} \mathrm{W}$ from $44^{\circ} 10^{\prime} \mathrm{N}$ to $45^{\circ} 10^{\prime} \mathrm{N}$ ) have been processed and reduced to free air and Bouguer gravity anomalies and total magnetic field. An interpretation of the data has been made and a paper is being prepared for publication.
Hudson Strait. Gravity data on two tracks to and from Hudson Bay have been reduced and are being used in an interpretation of the structure of Ungava Bay and Hudson Strait based on all geophysical observations in this area. This work has been published by Grant and Manchester (1970).
North American Basin. A series of N-S traverses on which geophysical data are collected is in progress in the western North Atlantic. For this program, CSS Baffin and CSS Hudson were used on an opportunity basis as they travelled to and from the Caribbean on hydrographic training and geological research cruises. Magnetic and gravity coverage now extends between $45^{\circ} \mathrm{N}$ and $20^{\circ} \mathrm{N}$ along meridians at $2^{1 / 2^{\circ}}$ intervals between $55^{\circ} \mathrm{W}$ and $70^{\circ} \mathrm{W}$. Gravity data have also been collected along meridians $55^{\circ} \mathrm{W}$, $57^{1 / 2}{ }^{\circ} \mathrm{W}, 64^{\circ} \mathrm{W}$ and $70^{\circ} \mathrm{W}$. A graduate student at Queen's University is examining the combined data.

Hudson '70. As a Canadian contribution to the Oceanographic Decade, CSS Hudson undertook a one-year oceanographic expedition named Hudson '70 comprising a circumnavigation of North and South America. An extensive marine geophysical program has been carried out as part of the expedition. Upon the departure of CSS Hudson for the Arctic from Victoria, British Columbia, 35,000 km of bathymetry, gravity and magnetic
field data had been collected. This had been supplemented with $1,670 \mathrm{~km}$ of continuous seismic profiling, a major seismic refraction experiment, 13 heat flow measurements, 14 dredge hauls and the collection of two cores during detailed surveys in selected areas.

In the Atlantic, the track of CSS Hudson from Halifax to Rio de Janeiro provided gravity, magnetic and bathymetry data to add to that collected by CSS Hudson and CSS Baffin on long traverses from Nova Scotia to Europe, the Caribbean and the Arctic. These regional data will assist in our investigation of the northwest Atlantic-North America plate.

In the Pacific the geophysical investigation, while providing similar regional data to that obtained in the Atlantic, included the survey of an area adjacent to the contact between the Juan de Fuca, North America and Pacific plates. Seven thousand kilometres of gravity and magnetic data and $9,500 \mathrm{~km}$ of bathymetry data extended the previously surveyed section of the Juan de Fuca Ridge (the western boundary of the Juan de Fuca plate) towards the Queen Charlotte Island fault. Detailed station work was also carried out in the Explorer Trench which may be the last expression of the East Pacific Rise before its termination at the Queen Charlotte Island fault.

Regional studies of the Gulf of Alaska are also planned as a result of bathy. metry, gravity and magnetic field data collected on five adjacent tracks of CSS Hudson, CSS Baffin and CSS Parizeau in the area while en route to and from the Arctic.

In the southeast Pacific, a geophysical profile was made over a feature which may be associated with the southern portion of the East Pacific Rise. A deep trench and adjacent peak (with a vertical separation of 3 km ) were found in an area previously thought to exhibit few tectonic features. It appears that the feature may be part of a long fracture of the East Pacific Rise and it is hoped to name it the Hudson Fracture Zone.

The gravity data collected along latitude $150^{\circ} \mathrm{W}$ from the Antarctic ice field to the Alaska Shelf are being used in a geodetic program in ultimate support of a proposed oceanographic satellite. Deter-
mination of the difference in height between the isobaric sea surface and the geoid gives the change in potential of an isobaric surface. From this can be calculated the potential of all other isobaric surfaces, wherein lies the key to ocean current transport. Orbital perturbation analysis of satellite track observations provides the low order harmonics of the geoid. At present the higher order harmonics may only be obtained at the sea surface. In order to determine the high harmonics of the geoid along the path of a polar orbiting satellite, a gravimetric determination of the geoid was made along $150^{\circ} \mathrm{W}$ between $63^{\circ} \mathrm{S}$ and $57^{\circ} \mathrm{N}$ on the assumption that variations in the gravity are independent of longitude. Future satellite altimeter profiling of the sea surface with reference to this geoidal section will enable an absolute dynamic section to be made.

En route home to Dartmouth, CSS Hudson and CSS Baffin carried out a geophysical program in Baffin Bay. Previous work in the Labrador Sea has indicated the presence of a ridge structure buried beneath the sea floor. This ridge may have been the focus for the ancient separation of Greenland from Canada. Whether this proposed ridge extends into Baffin Bay is not known. The few days spent by the two ships in Baffin Bay were intended to provide the answer to one fundamental question: is the crust of Baffin Bay oceanic or continental? The main evidence for concluding that the crust was oceanic came from a seismic refraction experiment conducted along the axis of the Bay. In support of this, seismic reflection profiling together with bathymetry, gravity and magnetic surveying was carried out. The results of this activity will be used for planning subsequent cruises to areas of Baffin Bay requiring detailed investigation.

## Environmental tests

Satellite navigation cruise (CSS Baffin 022-69). Extensive trials and comparisons between the ITT and Magnavox satellite navigation receivers were carried out on this cruise. Because of the excellent navigation facilities available (incorporating positioning by automatically recorded D.R., satellite
fixes, Decca, Hi-fix, Omega and VLF) it was hoped to isolate some of the errors involved in the measurement of gravity at sea. Our two Askania sea gravimeters were operated on the same Anschutz gyrostabilized platform, each gravimeter being connected to a separate crosscoupling analog computer. Unfortunately the weather was so good and the ship motion so limited that the errors encountered were very small.
Laboratory tests. The extension of the laboratory wing of Bedford Institute in 1969 has included the provision of two laboratories dedicated solely to gravity studies. One is used as a "quiet laboratory" with a floor level platform isolated from the building. Another platform, provided for seismic studies, is coupled directly to bedrock and is also isolated from the building. No vibration testing has yet been performed on either of these platforms to determine the extent of their isolation. When this has been done, consideration will be given to setting up a gravity reference station on each of these platforms.

While the two Askania sea gravimeters have been land based, work has been carried out to determine some of the torsional parameters of the measuring system, and in particular linearity. This work was necessary on two counts. A proposal has been made to produce a completely digital processing system for the sea gravimeter. To do this, the digital filter employed must be tailored precisely to the linearity of the gravimeter measuring system. Secondly, the investigation of cross-coupling errors in gravity measurements at sea suggested that there might be an asymmetry in these errors and that this might be attributed to the nonlinearity of the meter. The investigation demonstrated a non-linearity in the system which will have to be compensated for in the proposed digital processing system.

The cross-coupling computer originally built in 1965 has been modified, redesigned and completely rebuilt. It underwent extensive sea trials in its revised form early in 1969 and has been employed in correction of gravity data in the field ever since. With the continuous
computation and logging of crosscoupling error data, on line correction for these errors is now feasible.

## Memorial University of Newfoundland

## Trans-Newfoundland gravity profile

An $800-\mathrm{km}$ gravity profile, with 0.8 km station spacing, has been established along the Trans-Canada Highway between Port-aux-Basques and Come-by-Chance, Newfoundland. About one-third of the elevations were obtained from precise levelling, the remainder from an improved "one-base" barometric method which yielded a standard deviation less than half as large as that associated with the traditional "one-base" method. A total of 144 rock samples was collected along or near the profile to aid in the interpretation.

A qualitative profile interpretation has suggested the presence of unmapped gypsum deposits in southwestern Newfoundland, and intrusive bodies at several locations along the route. A detailed model study between Notre Dame Junction and Traytown shows the Ackley batholith to be a funnel shaped lopolith; it also shows this region to be underlain by an intermediate to basic layer, which may be a continuation of the layer inferred at 5.10 km depth from a gravity survey in eastern Notre Dame Bay (Miller, 1970).

## Notre Dame Bay gravity investigation

A gravity survey covering $2,500 \mathrm{~km}^{2}$ at 2.5 km spacing was conducted on islands and the coast of Notre Dame Bay near the eastern boundary of the Paleozoic Mobile Belt of Newfoundland. The Bouguer anomaly field shows good correlation with dominant features of the surface geology: (1) a strong northeasterly structural trend; (2) the Luke's Arm fault; (3) several extensive granitic bodies; however, no significant anomalies were observed over sedimentary areas. Preliminary qualitative interpretation of the published total-intensity aeromagnetic maps indicates some overall correlation with gravity and surface geology.

A satisfactory fit to the Bouguer field was obtained from three-dimensional model studies, dividing the area by geo-
logical criteria into 13 blocks, each with a mean density derived from rock samples. From the model results, two new features may be proposed:

1. A structural discontinuity near Change Islands, suggested also on the aeromagnetic maps, separating the eastern (Fogo-Change Islands) and western parts of the survey area.
2. A basic to ultrabasic layer at $5-10 \mathrm{~km}$ depth to explain the overall positive character of the Bouguer anomalies. This layer appears to be a landward continuation of the intermediate layer of Sheridan and Drake (1968).*

## Nova Scotia Research Foundation

During the past four years some 15,000 gravity stations have been observed by the Nova Scotia Research Foundation in Nova Scotia and adjacent regions. A program of regional gravity surveying in Nova Scotia is underway. Particular emphasis is given to areas underlain by Lower Mississippian rocks which may contain diapiric salt structures. Many detailed surveys have been made to investigate possible deposits of barite, celestite, manganese and fluorite. Future plans include the extension of the regional gravity surveys in northern and eastern Cape Breton, the production of a new series of gravity maps for Nova Scotia including both Bouguer and residual anomaly maps, and a detailed study of the Chedabucto fault which runs eastwest across the province and may continue seaward into the Atlantic.

During the last few years a computer oriented data handling system has been developed and is now in routine use. Data reduction, sort, merge, update, search and retrieval programs are in use. Plotting and interpretation programs are also available and a contouring package is presently being tested. All existing gravity data in Nova Scotia are gradually being incorporated in the data file.

Precise levelling methods used at present will be supplemented in 1971 by a hydrostatic levelling device currently

[^10]under development. This device should find practical application in surveys involving loops or closures of distances up to a few miles.

## University of New Brunswick

The Department of Surveying Engineering at the University of New Brunswick has completed a regional gravity survey of the province of New Brunswick and published eight Bouguer anomaly maps with 5 mgal contours at a scale of $1: 250,000$. Listings of 4,000 stations are also available. Professor K.B.S. Burke has commenced a geological interpretation of these results. Additional gravity observations have since been made as part of a program of the New Brunswick Department of Mines to map gravity lows associated with evaporite deposits in the Plumweseep-Penobsquis area.

Free-air anomaly maps have also been compiled and were used to calculate gravimetric deflections of the vertical at four triangulation stations in the province. These deflections were compared with astro-deflections. E.J. Krakiwsky has analyzed existing astrogeodetic deflection data in Canada. The objective of this analysis is to compute geoidal profiles using gravity data to interpolate deflection values between astrogeodetic stations.

Krakiwsky also reports that the satellite geodesy team at the University has made significant progress in defining the geodetic positioning of Canada's vast and remote land and sea areas. A satellite observing experiment was organized in November, 1970 in eastern Canada where seven satellite receivers (five on land, two at sea) simultaneously observed the dop. pler shift to five satellites in polar orbit. Simultaneous data was achieved for approximately 30 passes in a few days. The amount and type of data collected may be second only to that obtained in the U.S.A. The project was a joint program with Shell Canada Ltd. and Bedford Institute. The 60,000 feet of punched paper tape containing the data is now at the University for analysis. A mathematical model for the solutions of the positioning problem has been developed and programmed on an IBM 360/50 computer. Datum shift components be-
tween the geometric centre of the N.A.D. 1927 ellipsoid and the centre of gravity of the Earth will be determined from the data obtained in the experiment.

## McGill University

At the Department of Mining, Engineering and Applied Geophysics, McGill University, four theses on different aspects of gravity have been completed in the four-year period 1967-1970. Theoretical formulae for the gravity effect of multiple horizontal semi-infinite blocks, truncated by a dipping plane, have been developed (B. Sharma, unpublished thesis, 1968; Sharma and Geldart, 1968) and the results checked over several twodimensional faults in the St. Lawrence lowlands.
M. Vyas (unpublished thesis, 1969) has studied gravity anomalies over semiinfinite tilted slabs. The effect of tilt angle on semi-infinite blocks was calculated. It was necessary to terminate the block at finite depth. Extension of the results to calculate the effect of twodimensional anticlinal and synclinal features was carried out by dividing the cross-section into several horizontal and tilted slabs.
H.P. Parsneau (unpublished thesis, 1970) studied two dimensional digital operations for filtering potential field data. The collection and manipulation of gravity and magnetic data in applied geophysics can be described in terms of sampling and filtering of continuous twodimensional waveforms. Use of filter theory and modern processing techniques allows a more accurate approximation of potential field operations. The inverse Hankel transform and a wavelength filter were used for derivation of zero phase two-dimensional field operations.

A new approach for making terrain corrections using terrain profiles was described by W.B. Chang (unpublished thesis, 1970). The method is based on a simple formula for a three-dimensional shell in cylindrical co-ordinates. The terrain effect is calculated by superimposing a special graticule upon the terrain profiles and counting graticule elements. Results obtained were compared with results obtained by conventional methods and agreed within 0.1 mgal. The new
approach is faster than previous methods employing graticules.

## University of Manitoba

Gravity studies at the University of Manitoba have been concentrated mainly in the Rice Lake area of Manitoba. These investigations cover an area of some $2,000 \mathrm{~km}^{2}$ and form part of Project Pioneer a joint geophysical-geological study by the Manitoba Mines Branch and the University.

The southern part of this area is underlain by granitic gneisses of the English River gneissic belt which appear to be in fault contact with rocks of the Rice Lake greenstone belt lying to the north. The Rice Lake volcanic-sedimentary belt has been intruded by several igneous bodies, only one of which, southeast of Gold Lake, is completely surrounded by greenstone. The rocks of the gneissic belt exhibit a completely different metamorphic history to those of the greenstone belt and also have entirely different structural characteristics. The juxtaposition of the two-rock types undoubtedly indicates some major dislocation.

A total of 1,260 gravity stations has now been established in the Rice Lake area. The gravity station distribution is not uniform and depends on a combination of accessibility and identification of critical areas. All of the gravity data observed to date have been reduced to Bouguer anomalies using a density of $2.67 \mathrm{~g} / \mathrm{cm}^{3}$.

Determination of densities of surface rocks forms an important phase of the work. Two methods are being used; determination from surface samples, and short detailed gravity traverses across outcrops with good relief to determine the average density of major rock units.

Interpretation of anomalies and preparation of final Bouguer anomaly maps is now underway. Some of the results have been published by Brown (1968) and by Hall and Hajnal (1969).

All available gravity data in Manitoba have been compiled at the University and a preliminary draft of a new gravity map of the province is in the editorial stage.

## University of Alberta

The University of Alberta completed a gravity survey of an area of about $40,000 \mathrm{~km}^{2}$ centred near Brooks in southern Alberta. Seismic reflectionrefraction studies have led to the discovery of a rift valley, bounded by faults, at depths between 30 and 50 km in the lower crust (Kanasewich, 1966, 1968). This feature strikes nearly east-west. Gravity and magnetic surveys were used to follow the structure beyond the area of the detailed seismic study. Recently mapped magnetic anomalies show that it continues under the Rocky Mountains into British Columbia. The gravity anomalies have been shown to support the seismically-discovered rift structure, on a two-dimensional calculation.

A gravity survey made by the Dominion Observatory in the Stoney Rapids area of northern Saskatchewan is described by Agarwal and Kanasewich (1968). A major positive anomaly is underlain by a norite intrusion with an estimated anomalous mass of $10^{16} \mathrm{~kg}$. A simple three-dimensional model was constructed for this mass distribution. In this model the norite outcrop in the northwest is gently dipping under the sandstone, and the main norite body is about 7 km thick in the centre with a sandstone layer almost 1 km thick on top of it. Considering the occurrence of economic minerals in the exposed part of the noritic rocks, it is suggested that several drill-holes in the sandstone area would enhance the geophysical interpretation of the main norite body and its economic importance for future development.

A method for automatic computer determination of geological or geophysical trends has been developed at the university using cross-correlation techniques. The trend direction is obtained by scanning cross-correlation coefficients and fitting a third degree polynomial equation to the selected contiguous maxima. The degree of correlation and the direction is obtained in a computer program that makes extensive use of logic statements and involves an interesting example of the possibility for programmed decision making. This study is described by Agarwal (1968).

Potential field data have been analyzed in a two-dimensional wave number domain to obtain the ratio of intensity of magnetization to the density ( $\mathrm{J} / \rho$ ) (Kanasewich and Agarwal, 1970). A twodimensional fast Fourier transform was used to obtain auto-correlations, crosscorrelations, convolution, upward continuation, vertical and horizontal derivatives and reduction of the total field to the pole. A coherency test was used on the two sets of data to evaluate the validity of the calculated J/م ratio for each wavelength. A high coherency value was assumed to arise if the gravity and magnetic anomalies are caused by the same body. A theoretical prismatic model and a field example from northern Saskatchewan were used to illustrate the techniques.

## University of Calgary

At the University of Calgary F. Syber and P.E. Gretener are investigating the postulate that gravity anomalies are associated with deep seated reed structures. This project should be completed in 1971.

## University of Saskatchewan

Gendzwill (1968, 1969a and b) completed a detailed survey and interpretation of gravity and density data in the Amisk Lake-Flin Flon region which covers an area of about $750 \mathrm{~km}^{2}$ in east-central Saskatchewan. The main results include a Bouguer anomaly map, a density map and several new interpretation techniques (see also Gendzwill, 1970). The Bouguer anomalies correlate well with the densities of the Precambrian surface rocks and interpretation suggests that the surface density distribution must extend to depths of between 3 and 5 km to explain the gravity anomalies.

## University of British Columbia

The University of British Columbia has published the results of a gravity survey of southwestern British Columbia covering an area of some $50,000 \mathrm{~km}^{2}$ (Walcott, 1967). The Bouguer anomalies were divided into first- and second-order anomalies. Despite the obscuring effect of second-order anomalies the first order
anomalies could be isolated to allow quantitative analysis. A positive anomaly over Vancouver Island and a negative anomaly over the Olympic Peninsula together define a linear anomaly pattern which was named the Coastal Anomaly. Using geological, seismic and gravity information, and the assumption of hydrostatic equilibrium, this feature was interpreted as the edge effect between two crustal blocks of different thickness and density. The model demonstrates that isostatic anomalies may arise through lateral variations in crustal density and thickness and need not indicate departures from equilibrium.

At the University of British Columbia the design and analysis of linear filters for the enhancement of potential field data have also been studied. Standard techniques such as regional/residual separation, second derivative computation and upward and downward continuation have been considered from the linear filter viewpoint. The effects of improved filters were examined (Clarke, 1969a and b, 1971; Ulrych, 1968, 1969).

## Petroleum industry

The use of gravity surveying as a reconnaissance tool for petroleum exploration in Canada has recently increased significantly. During the last four years the average number of crew months has been 128 per year. This increased activity can be directly correlated with the shift in exploration to new frontier areas which include the Northwest Territories, the Arctic and the continental shelves. Large land holdings and difficult working conditions have stimulated the need for effective reconnaissance survey methods. Considerable effort is being made to solve logistical and operational problems in these remote areas.

Significant progress has been made in the use of computer-oriented data handling systems. Computers are now in routine use to reduce and interpret gravity data. More surveys completed by industry are being tied to the national gravity net established by Earth Physics Branch of the Department of Energy, Mines and Resources. Widespread use of gravity standards established by the Earth

Physics Branch ensures the long term value of oil company data.

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General distribution of ultramafic rocks in Canada (compiled by T.N. Irvine from Smith (1962), Scoates (1970) and other sources. Generalized structural boundaries are given as dotted lines. The sizes of individual bodies are necessarily exaggerated. Better known localities and areas numbered as follows: (1) Kluane Range intrusions; (2) Nahlin complex; (3) Blue River intrusion; (4) Cassiar asbestor body; (5) Polaris complex; (6) Middle River bodies; (7) Shylaps complex; (8) Tulameen complex; (9) Giant Mascot complex; (10) Muskox intrusion; (11) Manitoba Nickel Belt; (12) Fox River Sill; (13) Bird River Sill; (14) Kakagi Lake Sill; (15) Quetico-Sherbandowan intrusions; (16) Dundonald Sill and associated lenses; (17) Abitibi Sills; (18) Cape Smith-Wakeham Bay Sills; (19) Labrador Trough Sills; (20) Eastern Townships complexes; (21) Mount Albert intrusion; (22) Bay of Island complex; (23) Hare Bäy complex; (24) Burlington Penninsula complexes and (25) St. Stephen complex.


This illustration intends to show, in a wide diagrammatic fashion, one of the ways in which oceanic lithosphere may become trapped within the continental crust. Above, the single plate tectonic model is shown. In the centre, a fragment of continental crust is imagined to be situated in the downgoing slab of lithosphere. When the two continents collide, a sliver of oceanic lithosphere may become trapped between them.


# the ancient oceanic lithosphereidentification within the present continents statement of the problem 

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The theory of plate tectonics has been very successful in explaining the observations relating to the later Mesozoic and Cenozoic history of the earth. Its applicability to earlier times is uncertain. According to this theory oceanic lithosphere is produced at the axis of a mid-ocean ridge by accretion from the mantle. It then spreads laterally (acting approximately as a rigid spherical shell or olate) passing finally beneath one of the deep ocean trenches. During its passage seneath the trench, fragments of the ridge-generated oceanic lithosphere may become trapped, and eventually incorporated into the continental crust (a greatly oversimplified scheme is given in the Frontispiece) so that one of the interesting consequences of plate tectohics is that fragments of old oceanic crust should occur, not invariably perhaps, but at least occasionally, at the sites of old trenches. Should such occurrences never be found, then the theory is perhaps not applicable to Paleozoic and earlier times. If, on the other hand, definite identification of ridge-generated oceanic fragments within present day continents can be made, it would strengthen the case for extending concepts of plate tectonics back into the more remote history of the earth. In fact such identifications would
constitute one of the most powerful means of testing whether or not it is reasonable to extend this dynamic view of the earth into more remote times. This is why the subject of this symposium is so relevant to the Geodynamics Project.

There are two parts to this task of identification. Firstly, there is the "rock problem" which requires comparisons to be made of the geological, chemical, and physical properties of the rocks of present-day ridges, with their possible older equivalents now within the continents. Secondly, there is the "kinematic problem" which requires that the present sites of possible old oceanic lithosphere must be shown to have been zones of lithosphere convergence. There will be no satisfactory discussion until the kinematic framework of at least some of the older fold belts has been established quantitatively, through the application of a whole range of geological, geochemical, and geophysical techniques.

The relevance of these ideas to the origin of mineral deposits should not be overlooked. Rich deposits are being formed today in the hot brine pools of the deep axial parts of the Red Sea which is a constricted juvenile rift. In the open ocean ridge systems disseminated metallic sulphides occur ubiquitously in pillow
basalts. Asbestos is produced by the alteration of ultrabasic rock which may, on these ideas, originally have had an oceanic source. Thus, the very important mineralization of many such ultrabasic and basic rocks, at least insofar as the original source of metals is concerned, may become explicable in terms of volcanic and tectonic processes currently active.

The purpose of this short symposium was not to even attempt to cover the entire field, or even to answer specific questions, but rather to draw attention to an important general problem of particular significance to the earth sciences in Canada where there are such splendid displays of mafic and ultramafic rocks of all ages (see Frontispiece).

The subcommittee wishes to express its thanks to Carleton University for the use of a meeting room, Professor W. Tupper of Carleton University who made the accommodation arrangements, and to Professor A. Goodwin of the University of Toronto who very kindly chaired the meeting with grace and good humour. Finally, we would like to acknowledge the very great help given by Dr. G. Skippen of Carleton University in reviewing these papers prior to their publication.

# the oceanic crust of the mid-atlantic ridge at $45^{\circ} \mathrm{N}$ 

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Abstract. Detailed geological and geophysical investigations on the crest and High Fractured Plateaus of the Mid-Atlantic Ridge at $45^{\circ} \mathrm{N}$ have permitted the synthesis of a clear picture of the structure, petrography, geochemistry and geochronology of a section through a modern, slowly spreading oceanic ridge. This paper does not dwell on the methods of data acquisition and processing which were essential to the synthesis, nor does it enter into many of the controversies which have arisen from the data; these have been described by Aumento 1967, 1968, 1969. It is emphasized that the active, slowly spreading ridge described may show significant differences from a repidly spreading ridge (e.g. the East Pacific Rise) and may, by nature of its youth, bear little obvious resemblance (especially geochemically) to old, deformed, altered and metamorphosed oceanic remnants found on the continents.

## Structure

The oceanic crust near the crest of the Mid-Atlantic Ridge consists of discontinuously layered sequences of igneous and metamorphic rocks 5 km thick, overlain by a veneer of sedimentary material (Figure 1) (Keen and Tramontini, 1970; Barrett and Aumento, 1970). The layering is disrupted by steep normal faults roughly parallel to the axis of the ridge; their $45^{\circ}$ scarp slopes generally face the axis, and have vertical throws of up to 2 km (Keen and Manchester, 1970; Barrett and Aumento, 1970). These faults are responsible for much of the topographic relief found on the ridge. This rugged relief has been subsequently moderated by rapid sedimentation (Keen and Manchester, 1970). Sedimentary thicknesses increase with distance from the axis, such that at distances of 100 km from the axis intermontane valleys are buried under many hundreds of metres of sediments, resulting in an apparent smoothing out of the bottom topography. This observation is consistent with the hypothesis of an actively spreading ocean floor (Keen and Manchester, 1970).

The mean crustal thickness is approximately 5 km , but shows local variations of up to 3 km (Keen and Tramontini, 1970). These variations are presumably the result of block faulting and the variable nature of the Mohorovicic dis-
continuity beneath the oceanic crust. The oceanic crust can be subdivided into three main layers, with a fourth beneath representing the top of the upper mantle.

Layers 1, 2, 3 and 4 have been correlated with specific rock types as shown in tabular form below: (Barrett and Aumento, 1970)

Layer 1, varying in thickness from 0 km at the axis, to many thousands of metres in the abyssal plains, is a lowvelocity sedimentary layer. Layer 2 , with a mean thickness of 1.6 km , thickens to 2 km near the axis, and layer 3 , with a mean thickness of 3.4 km , thins to 1.3 km near the axis. Layer 2 can be subdivided further into two discontinuous
layers with velocities of 3.8 and 4.7 km $\mathrm{s}^{-1}$ for the upper and lower layers respectively. Layer 4, the uppermost upper mantle beneath the Mohorovicic discontinuity, consists of a thick sequence of high-velocity rocks ( $8.1 \mathrm{~km} \mathrm{~s}^{-1}$ ) exhibiting a velocity anisotropy of some 0.25 $\mathrm{km} \mathrm{s}^{-1}$ (Keen and Tramontini, 1970).

The serpentinites which appear in the table do not belong to any one layer, but rather occur as diapiric intrusions cutting through the igneous/metamorphic layering of the mafic rocks. Ultramafic diapiric intrusives are characteristic of slowly spreading ridges, but may be absent on rapidly spreading ridges (Aumento and Loubat, 1971).

Layers 2, 3 and 4 apparently originate beneath the axis of the ridge in the following way: large, discontinuous, totally liquid lopoliths of mafic magma are emplaced beneath the axis of the ridge following a phase of major lateral fracturing due to the forces responsible for ocean-floor spreading. The floors of these lopoliths lie at depths of less than

| Oceanic Layer | Thickness km | Velocity <br> $\mathrm{km} \mathrm{s}^{-1}$ |  |
| :---: | :---: | :---: | :---: |
| 1 | 0 | 2.2 | Foraminiferal sand and ooze |
|  | to |  |  |
|  | 1.0 | 2.8 | Highly weathered material and compacted sediment |
| 2 | 1.6 | 3.8 | Weathered pillow basalt and weathered serpentinite |
|  | to |  |  |
|  | 2.0 | 4.7 | Massive basalt, diabase and fresh serpentinite |
| 3 | 1.3-3.4 | 5.8-6.8 | Meta-basalt, gabbro and metargabbro |
|  | Mohorovicic | discontinuity |  |
| 4 | uncertain | 8.1 | Ultramafics (layered peridotites and dunites) |

Figure 1. Schematic cross-section through the oceanic crust beneath the Mid-Atlantic Ridge at $45^{\circ} \mathrm{N}$.

24 km below sea level, while their roofs may be within $1-2 \mathrm{~km}$ of the ocean floor hence these bodies encroach upon the uppermost levels of the upper mantle and the base of the crust (Aumento and Loubat, 1971). Magmatic differentiation by gravity crystal settling takes place after emplacement under quiescent conditions, producing igneous layering with an upward dunite-peridotite-gabbroextrusives stratigraphy. The gabbros and extrusives accrete to the base of the crust, whereas the ultramafics beneath them accrete to the top of the upper mantle. The gabbro-peridotite interface so formed represents the local Mohorovicic discontinuity between layers 3 and 4 , which, by nature of its origin, exhibits considerable variations in depth from lopolith to lopolith.

Metamorphism (Aumento and Loncarevic, 1968) due to burial, subsequent intrusions and extrusions and generally high heat flow affects these rocks in a manner approaching that of continental regional metamorphism, transforming gabbros and diabases into reenstones and amphibolites. This pwardly encroaching metamorphic horizon is thought to represent the junction between layers 2 and 3, layer 2 consisting of the unmetamorphosed mafic rocks, and layer 3 their metamorphosed equivalents (Barrett and Aumento, 1970).

The final complete crystallization and solidification of these lopoliths restricts further plastic stress release, and contributes to a new cycle of tensional stress build up, resulting in renewed fracturing beneath the axis. A new generation of totally liquid bodies is then intruded into the voids formed, while the solid rocks formed during the previous cycle are deformed cataclastically as they are moved apart; however, these rocks may often succeed in repairing the tectonic damage by renewed, solid-state recrystallization under a hot, high stress environment. Cataclasism is followed by amphibolitization through the action of juvenile water hydration. Rodingitizing metasomatism appears contemporaneous with the last stages of amphibolitization, and heralds incipient serpentinization. The bulk of the serpentinization results from
later, more extreme, periods of hydration. Diverse physical conditions are evident here: initially the result of very hot juvenile waters, the final phases are produced under tensional stress, by the hydrating effects of cooler meteoric waters possibly contemporaneous with diapiric emplacement through the oceanic crust.

## Magnetics

The magnetic anomaly pattern of the oceanic crust at $45^{\circ} \mathrm{N}$, as elsewhere on the axes of ridge systems, is dominated by a strong positive lineation (over $800 \gamma$ ) coincident in position with the Median Valley (Loncarevic et al, 1966). On either side of this central anomaly the detailed pattern is confused, but is characterized nevertheless by numerous elongate anomalies of short continuity parallel to the central anomaly. Some 120 km west of the axis there appears a continuous anomaly of +350 y maximum amplitude, corresponding to an anomaly which is readily identifiable over other axial regions, and which has been designated as oceanic anomaly 5 . The relative position of anomaly 5 with respect to the axis (anomaly 1) indicates that the ocean floor has probably been spreading at an overall average rate of $1.28 \mathrm{~cm} / \mathrm{y}$ over the last 10 m.y. (Aumento, 1969 and Aumento et al, 1970).

Paleomagnetic tests on the rocks from the area have shown that only the eruptives belonging to the uppermost part of oceanic layer 2 are likely contributors to the regular magnetic anomaly pattern over the ridge (Irving, Robertson and Aumento, 1970; Irving, Haggerty, Aumento and Loncarevic, 1970). These eruptives have an average n.r.m. (natural remanent magnetization) of $78 \times 10^{4}$ $\mathrm{cm}^{-3}$ cgs over the Crest Mountains, decreasing to $50 \times 10^{4}$ over the High Fractured Plateaus, whereas the gabbros and diabases beneath have an average of only $1.2 \times 10^{4}$, and their metamorphic equivalents $0.3 \times 10^{4} \mathrm{~cm}^{-3} \mathrm{cgs}$. In contrast, serpentinites average $40 \times 10^{4}$ $\mathrm{cm}^{-3} \mathrm{cgs}$; such high intensities of n.r.m. for the serpentinites produce substantial disruptions of the magnetic anomaly lineations in the surface anomaly patterns
coincident with diapiric intrusions of serpentinized ultramafics. These high n.r.m. intensities also suggest that the oceanic layer 3 is not composed primarily of serpentinites (Aumento et al., 1970; Irving, Robertson and Aumento, 1970).

## Geochronology

Radiometric ages (potassium-argon and fission track) show that the spreading rate of the ocean floor may have changed from $1 \mathrm{~cm} / \mathrm{yr}$. over the High Fractured Plateau for the period 3-16 m.y. to 4 $\mathrm{cm} / \mathrm{yr}$. over the Crest Mountains for the period $3 \mathrm{~m} . \mathrm{y}$. to the present (Fleischer et al, 1968; Aumento, Wanless and Stevens, 1968; Aumento, 1969). The change in rate cannot be detected in the magnetic anomaly patterns due to their confused nature (they give the average rate of 1.28 $\mathrm{cm} / \mathrm{yr}$. only), but shows a remarkable coincidence with the physiographic boundary between the Crest Mountains and the High Fractured Plateaus and possibly also with increased sedimentary thicknesses and in the thickness of ferromanganese encrustations on rocks at that boundary. Similar changes in spreading rate have been suggested for other oceanridge systems.

A number of geochemical and geophysical parameters vary with distance from the axis of the ridge, and hence with time: among these are the intensities of remanent magnetization (Irving, Robertson and Aumento, 1970), $\mathrm{Fe}_{2} \mathrm{O}_{3}$ $/ \mathrm{FeO}$ ratios, $\mathrm{H}_{2} \mathrm{O}$ and U contents, and $\delta 0^{18} / \mathrm{O}^{16}$ and $\mathrm{Sr}^{87} / \mathrm{Sr}^{86}$ ratios of basalts (Aumento, 1971). An understanding of these variations with time is important if we are to anticipate the characteristics of rocks from ancient oceanic crusts outcropping on the continents relative to those we know are characteristic of fresh rocks collected over modern ridge systems.

## Igneous and metamorphic rocks

Mafic rocks: these vary in texture from glassy, sometimes spherulitic pillow basalts, to more massive, diabasic and gabbroic rocks. Pillow lavas are often vesicular, the vesicles showing no correlation with the depth of water under
which the extrusion occurred. Resorbed calcic plagioclase xenocrysts, indicative of gravity crystal differentiation in lopoliths beneath the axis, are characteristic of many of the pillow basalts (Muir and Tilley, 1964; Aumento, 1968; Aumento and Loncarevic, 1968).

Mafic rocks vary in composition from quartz-normative tholeiites to nephelinenormative alkali basalts. Many of these rocks fall into the low olivene-normative field, with a smaller concentration occupying the field of incipient normative nepheline (Muir and Tilley, 1964; Aumento, 1968; Aumento and Loncarevic, 1968). Table I lists the average compositions of the main types of rocks at $45^{\circ} \mathrm{N}$.

Meta-basites: zeolite facies metamorphism of basalts and diabases takes place under very shallow burial conditions, possibly of the order of a few tens of metres. Plagioclase phenocrysts are altered to analcite, and the groundmass to other zeolites. In the greenschist facies the mafic rocks still retain their igneous textures; here calcic plagioclase alters to albite, augite to actinolite, olivine and glass to chlorite. In the higher grades epidote, tremolite, quartz, calcite, talc, titanomaghemite and green hornblende also occur (Aumento et al., 1970).

Amphibolite facies meta-basites occur at greater crustal depths (well into layer 3). These rocks have lost all igneous textures and most relict minerals, and exhibit strong fabric lineations. Minerals include (a) lower grade assemblages of quartz, plagioclase (oligoclase-andesine), biotite, hornblende, epidote, sericitized orthoclase, magnetite and sphene; (b) a higher grade assemblage of homblende, diallagic diopside, plagioclase (oligoclaseandesine), sericitized orthoclase and minor biotite (Aumento et al., 1970).

Serpentinized ultramafics: these rocks include dunites, harzburgites, lherzolites, peridotites, amphibole peridotites, wehrlites and troctolitic gabbros (Aumento et al., 1970; Aumento and Loubat, 1971). Many show evidence of gravity crystal cumulate layering, of subsequent mylonitization, and other mechanical deformations, as well as metasomatic changes
such as amphibolitization and rodingitization, and ubiquitous, almost total serpentinization. In these features, as well as textures, they are comparable to the classical stratiform massifs of the continents, the mediterranean ultramafic massifs and the alpine-type ophiolites. However, these affinities are never clear cut: important discrepancies always appear. Oceanic ultramafics may represent an intermediate stage between the large layered massifs and the smaller, highly deformed alpine bodies. Indeed, oceanic ultramafics may offer unique opportunities to solve problems encountered in the more disturbed continental environments.

Sialic intrusives: hornblende-rich quartz diorites grading into trondhjemites or albite granites occur as small pockets in intimate association with the ultramafic rocks. They contain xenoliths of basalt, serpentinites and metabasites. These rocks are reminiscent of the albitized diorites characteristic of the late stages of alpine intrusive complexes (Aumento, 1969).

## Conclusions

A modem oceanic crust consists of a layered sedimentary sequence of variable thickness underlain by 5 km of systematically layered igneous and metamorphic rocks. The latter consist of a thin upper "layer" of pillow lava underlain by massive basalts, diabases and gabbros. These rocks show increasing metamorphism with depth, and reach the equivalent of the amphibolite facies near the base of the crust. Layered ultramafic bodies make up the top of the upper mantle beneath the amphibolites. On the slowly spreading ridges the hydrated equivalents of these ultramafics (the serpentinites) pierce through the crustal layering; however, under rapidly spreading ridges they may be unable to do so, since vertical tectonic movements are less characteristic of rapid spreading.

At present only the gross features described above may be used in the preliminary identification of ancient oceanic crusts on the continents. The geochemical parameters which are characteristic of modern ridges (Table I) appear
to be too dependent on time variations to permit direct comparisons to be made. It is possible, however, that in the near future we may find parameters that are independent of geological time for use in the unequivocal identification of ancient oceanic crusts.

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## Legend for Table I

Column 1. Average of 15 analyses of almost totally serpentinized ultramafic rocks (pro-serpentinization rock types include peridotites, lherzolites, harzburgites and dunites).
Column 2. Average of two analyses of gabbros, both showing incipient greenstone metamorphism.
Column 3. Average of 10 analyses of extremely fresh tholeiitic basalts from the Median Rift Valley floor.
Column 4. Average of 10 analyses of fresh tholeiitic basalts from the Median Valley scrap showing incipient weathering (note higher $\mathrm{Fe}_{2} \mathrm{O}_{3}$ / FeO ratio and $\mathrm{H}_{2} \mathrm{O}$ content relative to analysis in column 3).
Column 5. Average of 10 analyses of basalts showing alkaline affinitives. These basalts characteristically show more advanced weathering than do the associated tholeiites. This may be due to the particular susceptibility of alkali basalts to weathering, to their initially higher oxydation state, or both.
Column 6. Average of 10 analyses of basalts and diabases showing incipient or complete greenstone metamorphism
Column 7. Average of five analyses of quartzdiorites and trondhjemites.

Table I. Average major, minor and trace element compositions of rocks from the Crest Mountains of the Mid-Atlantic Ridge at $45^{\circ} \mathrm{N}$.

|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | SERPE | GABBR | THOLE | THOLE | ALKAL | GREEN | DIORI |
| $\mathrm{SiO}_{2}$ | 37.65 | 47.55 | 50.24 | 50.19 | 48.09 | 49.33 | 65.76 |
| $\mathrm{Al}_{2} \mathrm{O}_{3}$ | 2.45 | 16.02 | 15.77 | 16.77 | 16.19 | 15.23 | 14.95 |
| $\mathrm{Fe}_{2} \mathrm{O}_{3}$ | 7.71 | 1.47 | 1.24 | 2.66 | 4.55 | 3.08 | 2.97 |
| FeO | 0.56 | 5.02 | 8.12 | 6.50 | 4.75 | 7.07 | 3.18 |
| CaO | 0.20 | 12.64 | 11.45 | 11.65 | 9.80 | 9.15 | 2.86 |
| MgO | 36.94 | 11.16 | 8.18 | 6.55 | 7.61 | 7.18 | 1.85 |
| $\mathrm{Na}_{2} \mathrm{O}$ | 0.18 | 1.70 | 2.55 | 2.75 | 3.68 | 3.22 | 5.35 |
| $\mathrm{K}_{2} \mathrm{O}$ | 0.02 | 0.04 | 0.23 | 0.44 | 0.88 | 0.14 | 0.76 |
| $\mathrm{TiO}_{2}$ | 0.06 | 0.64 | 1.34 | 1.40 | 1.72 | 1.42 | 0.77 |
| $\mathrm{PiO}_{5}$ | 0.02 | 0.04 | 0.11 | 0.14 | 0.26 | 0.17 | 0.21 |
| $\mathrm{H}_{2} \mathrm{O}$ | 12.67 | 2.66 | 0.48 | 0.77 | 2.23 | 3.03 | 1.00 |
| MnO | 0.12 | 0.15 | 0.14 | 0.14 | 0.18 | 0.39 | 0.10 |
| S | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| NiO | 0.13 | 0.02 | 0.01 | 0.0 | 0.01 | 0.01 | 0.0 |
| $\mathrm{CrIO}_{3}$ | 0.24 | 0.01 | 0.02 | 0.01 | 0.03 | 0.01 | 0.0 |
| $\mathrm{CO}_{2}$ | 0.18 | < 0.10 | < 0.10 | 0.15 | 0.15 | 0.37 | < 0.05 |
| TOTAL | 99.13 | 99.24 | 99.98 | 100.12 | 99.98 | 100.80 | 99.86 |
| Q | 0.0 | 0.0 | 0.0 | 0.24 | 0.0 | 0.54 | 22.80 |
| Or | 0.14 | 0.24 | 1.37 | 2.62 | 5.32 | 0.86 | 4.55 |
| Ab | 1.76 | 14.89 | 21.68 | 23.42 | 30.66 | 28.15 | 45.81 |
| An | 0.0 | 37.25 | 31.06 | 32.33 | 25.60 | 27.58 | 12.65 |
| Ne | 0.0 | 0.0 | 0.0 | 0.0 | 0.62 | 0.0 | 0.0 |
| Ag | 0.0 | 21.34 | 20.07 | 19.38 | 16.84 | 12.75 | 0.0 |
| Hy | 34.81 | 13.22 | 16.25 | 14.78 | 0.0 | 21.42 | 6.99 |
| Ol | 50.21 | 9.23 | 4.69 | 0.0 | 9.88 | 0.0 | 0.0 |
| Mt | 2.38 | 2.21 | 1.81 | 3.88 | 6.74 | 4.61 | 4.36 |
| Il | 0.13 | 1.26 | 2.56 | 2.68 | 3.34 | 2.79 | 1.48 |
| Hm | 7.28 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| Ap | 0.05 | 0.10 | 0.26 | 0.33 | 0.62 | 0.41 | 0.49 |
| C | 2.47 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.76 |
| Cr | 0.41 | 0.01 | 0.03 | 0.01 | 0.04 | 0.01 | 0.0 |
| La | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| Cc | 0.36 | 0.24 | 0.23 | 0.34 | 0.35 | 0.87 | 0.11 |
| TOTAL | 100.00 | 100.00 | 100.00 | 100.00 | 100.00 | 100.00 | 100.00 |
| Sr | 20 | 75 | 97 | 120 | 274 | 195 | 120 |
| Ba | 25 | 14 | 61 | 94 | 142 | 24 | 226 |
| Cr | 2450 | 160 | 200 | 125 | 328 | 84 | <20 |
| Zr | <30 | 116 | 120 | 342 | 208 | 116 | 468 |
| V | 57 | 140 | 392 | 360 | 351 | 348 | 37 |
| Ni | 1300 | 163 | 131 | 56 | 104 | 95 | 35 |
| Cu | 120 | 19 | 91 | 73 | 124 | 150 | 25 |
| Co | 136 | 31 | 41 | 42 | 39 | 33 | $<20$ |
| Sc | <10 | 33 | 47 | 42 | 38 | 30 | $<10$ |
| Zn | nd | 87 | 91 | 99 | 81 | 102 | 25 |
| Pb | nd | 1.4 | 1.6 | 2.3 | 3.0 | 3.4 | 2.1 |
| Ga | nd | 20 | 35 | 27 | 12 | 19 | 30 |
| B | nd | <5 | $<5$ | 5.5 | 2.4 | <1 | 1.8 |
| Rb | nd | $<5$ | <5 | 5 | <30 | < 5 | <5 |
| U | 0.45 | 0.17 | 0.25 | 0.42 | 0.85 | 0.41 | 0.66 |
| La | nd | ndd | 5.29 | 7.52 | nd | nd | nd |
| Sm | nd | nd | 3.13 | 3.55 | nd | nd | nd |
| Eu | nd | nd | 0.98 | 1.09 | nd | nd | nd |
| Tb | nd | nd | 0.53 | 0.60 | nd | nd | nd |
| Lu | nd | nd | 0.42 | 0.39 | nd | nd | nd |
| Hf | nd | nd | 1.85 | 2.12 | nd | nd | nd |
| Yb | nd | nd | 2.25 | 2.29 | nd | nd | nd |



# mesozoic and tertiary volcanism of the western canadian cordillera 

Mbstract. No Mesozoic or Tertiary rocks with the characteristics of oceanic crust are known in the Fanadian Cordillera. The early Mesozoic was dominated by the successive formation and erosion of Sland arcs situated near the continent, whereas volcanism during the late Mesozoic and Tertiary was entirely continental. Spatial and temporal changes in the style of volcanism and the fomposition of lavas is believed to reflect changes in the interaction between Pacific crust and the fontinental margin.

## Introduction

The record of Mesozoic and Tertiary Folcanism in the Cordillera is a record of fontinental and island arc volcanism, for mowhere in western Canada do rocks of this age exhibit the characteristics of oceanic crust. Nevertheless, the changing styles of Cordilleran volcanism must reflect changes in the interaction between Pacific crust and the continental margin. In our present state of knowledge any ittempt to interpret this record requires What certain assumptions be made. Foremost of these concerns is the amount and fiming of transcurrent movement between the various tectonic belts of the western Cordillera for clearly, variations in magma type are significant only if their original spatial relationships are known. Pre-Tertiary right lateral movement has been suggested for several northwesterly trending lineaments, particularly the Yalakom and Tintina trenches, and parts of the Rocky Mountain Trench. Morepover, Permian and Triassic faunas in central British Columbia are similar to faunas in the southwestern United States, wgesting that large-scale translation may have continued into late Triassic or early Jurassic time. Conversely, the stratigraphic record in many parts of British Columbia suggests that Upper Triassic and younger clastic sediments were derived from immediately adjacent source areas, and that structures related to Mesozoic tectonic events may be traced across, as well as along, the Cordilleran structural trend. The latter evidence is sufficiently strong, in the writer's opinion, to justify the view that the Insular

Belt, the Coast Crystalline Belt, and the western part of the Intermontane Belt have been in their present positions rela. tive to one another since late Triassic time. The possibility remains that this entire segment of the Cordillera may be allochthonous with respect to Triassic rocks farther east. The present paper is restricted to a discussion of this most westerly segment of the Cordillera and adjacent parts of the Pacific Basin. The larger problem of relating this region to global plate motion, and to the southern Cordillera, is dealt with in a more comprehensive paper now in preparation.

## Distribution of volcanic rocks

Both the Insular Belt of western British Columbia and the Intermontane Belt of central British Columbia contain great thicknesses of Mesozoic and Tertiary volcanic rocks. These two belts are separated by the tectonically high Coast Mountains, consisting mainly of crystalline rocks that were emplaced in a series of pulses, approximately synchronous with the major volcanic episodes.

The two distinct belts of Triassic and early-to-middle Jurassic outcrops in the Intermontane Belt (Figure 1) may be more apparent than real since the interior of this belt is largely covered by younger sediments and Tertiary plateau lavas. Conversely, the outcrop distribution of Early Tertiary volcanics (Figure 2) is misleadingly small since most of this material is poorly indurated subaereal ash-flows that were rapidly eroded. Very thick sections preserved in small downfaulted blocks within and adjacent to the

Coast Mountains indicate that the early Tertiary volcanism was a more important and more widespread event than the present outcrop distribution suggests. Similarly, the presence of Miocene basaltic dyke swarms thoughout the Coast Mountains suggest that the plateau lavas may originally have extended much farther west. Only the Pleistocene and younger volcanoes are sufficiently well preserved to permit recognition of individual vents. With few exceptions these are aligned in north-south and east-west trending linear belts.

## Sequence of volcanic events

During Late Triassic (Karnian) time volcanism in the Intermontane Belt was dominated by the eruption of clastic, augite andesite lava from both submarine and subaerial vents. These are interbedded with rapidly deposited eugeosynclinal sediments that exhibit abrupt facies changes and numerous local unconformities. Contemporaneous volcanism farther west, in the Insular Belt, produced thick piles of tholeiitic pillow lavas, aquagene tuffs and breccias. Despite their submarine origin these Triassic lavas, unlike those of Permo-Carboniferous age, are not associated with ultramafic rocks or chert and are therefore not typical of deep oceanic basalts of the ophiolite suite.

The quiet effusion of tholeiite in the Insular Belt ended in earliest Jurassic time and was followed by sporadic eruption of clastic andesite from subaerial as well as submarine vents. Similar early Jurassic, andesitic volcanism continued in the southern part of the Intermontane Belt but diminished northward, and, north of Stikine River, the entire Lower and Middle Jurassic succession is represented by clastic sedimentary rocks locally containing piles of pillow basalt and


Figure 1. Distribution and chemistry of Mesozoic volcanic rocks.
peperites that formed isolated seamounts within the sedimentary basin.

By late Jurassic time large segments of the Cordillera had become emergent and thick sections of clastic sediments were deposited in successor basins within the central part of the Intermontane Belt. Regional uplift, particularly of the Coast Geanticline, was accompanied by plutonism, but volcanic activity did not resume until the late Cretaceous. By that time the Cordillera was almost completely emergent, and profound uplift of the Coast Geanticline during the late Creataceous and early Tertiary was accompanied by extensive high-level plutonism, block faulting, and explosive, subaerial eruption of enormous volumes of thyolite, rhyodacite, and dacite ash-flows and ignimbrites. Their close spatial relation-
ships and similar chemistry suggest that these lavas are genetically related to plutons and to north-south trending dyke swarms of the same age. Acid volcanism reached its climax in the Eocene, declined rapidly, and was followed in the Oligocene by a period of quiescence that lasted until the Miocene. At that time a flood of alkali-olivine basalt issued from a multitude of vents and fissures to form the plateau lavas of central British Columbia. This activity culminated in the late Miocene but intermittent eruption of similar lava continued from belts of central vents thoughout Pleistocene and into Recent time.

## Chemistry

Very few chemical analyses are available of early Mesozoic or early Tertiary
volcanic rocks and, although a largy number of Miocene and younger lavas, have been analyzed, they are mostly from small, intensively studied areas and are not a regional sample. However, even these few analyses indicate several important trends. Both Triassic and Jurassic volcanics exhibit a distinct east-west polarity with respect to potash, those in the Intermontane Belt having an appreciable higher $\mathrm{K}_{2} \mathrm{O}$ content than equivalent rocks in the Insular Belt (Figure 1).

The early Tertiary volcanics, as one would expect from their explosive origin, are relatively high in silica. The random/ scatter of both silica and alkali values is, also significant, and contrasts markedly with the narrow range of compositions exhibited by the Miocene alkali-olivind basalt of the plateau lavas (Figure 2).

Most Pleistocene and Recent volcanoes consist of similar alkali-olivine basalt however a few of the larger centres such as Edziza and Garibaldi have produced highly differentiated lava series. In most cases these show a direct line of descent from primary alkali-olivine magma similar to that of the plateau lavas (Figure 2).

## Discussion

If the initial assumption of this paper is accepted, namely that the three most westerly tectonic subdivisions of the Cordillera have maintained their present relative positions since late Triassic time, then the changing pattern of volcanism through time and space becomes mean-
ingful within the framework of plate tectonic theory. According to this concept (Hamilton, 1969) the underflow of spreading oceanic crust into a trench and down an inclined subduction zone beneath the continental margin is the driving mechanism of tectonic processes including volcanicity. Empirically,


Figure 2. Distribution and chemistry of Tertiary and Quaternary volcanic rocks.
andesitic volcanism of the island arc type is confined to belts above such subduction zones and lavas erupted farthest from the trench are more alkaline, particularly more potassic, than those closer to it (Dickinson, 1968). Similarly, the basaltic rocks derived deep within the mantle have an alkaline affinity while those of shallower origin tend toward tholeiite (Kuno, 1966).

Applying this model to the western Cordillera, the late Triassic volcanics of the Intermontane Belt are considered to represent a series of volcanic arcs that formed above a gently inclined subduction zone. Contemporaneous submarine volcanism in or near the trench produced the great elongate piles of less potassic lavas found in the Insular Belt. Westward migration of andesitic arcs in the early Jurassic may reflect steepening of the subduction zone in response to the development of a deep root of granitic rocks beneath the arcs.

The termination of andesitic, arc-type volcanism in the late Jurassic may reflect a change in the direction of relative motion between the Pacific and North American crustal plates, resulting in cessation of underflow. The profound late Jurassic regional uplift is thus explained by rebound of the gravitationally unstable granitic root zone that lay beneath the arcs and which is now exposed in the Coast Mountains.

This block, formed by partial or complete melting of heterogeneous plutons, neared the surface, and block foundering and cauldron subsidence
accompanied the explosive volcanics of central British Columbia (Souther, 1967). This activity persisted until mid-Tertiary when isostatic equilibrium was restored. Uplift of the Coast Mountain belt declined, and the present stable, aseismic continental margin emerged. Late Miocene and younger activity, dominated by effusion of mantle-derived alkali-olivine basalt, is characteristic of interplate continental volcanism, unrelated to crustal underflow (Souther, 1970). The eastwest, north-south alignment of Pleistocene and younger volcanic centres suggests that the magma rose along gash fractures related to right lateral shear between the Pacific plate and the continent along the northwesterly trending Queen Charlotte-Fairweather Fault system.

Until further data are available, this, or any other comprehensive model of Cordilleran tectonism must be at best highly speculative. However, it provides the nucleus of a mechanistic theory of tectonism that relates the continental margin to the adjacent ocean basin and provides a basic framework within which the cause and effect of many different tectonic processes may be tested. Viewed in this light, it can serve a useful function in giving direction to further research, both in the field and in the laboratory.

## Future research

A better understanding of the relative positions of the various tectonic segments of the Cordillera during Mesozoic and Tertiary time is essential. Until this has
been established no confident interpretations can be drawn from any body of data pertaining to the regional distribution of rock properties. Particular emphasis should therefore be placed on the following:

1. stratigraphic studies designed to identify the source of clastic sediments in Mesozoic and Tertiary basins to establish stratigraphic ties between those parts of the Cordillera that have not undergone large scale relative displacement,
2. paleomagnetic study of Mesozoic and Tertiary volcanic rocks in several different tectonic domains and comparison of their pole positions, and
3. regional geochemistry of volcanic rocks to identify individual volcanic eras and establish their chemical polarity.

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# oceanic crust in the canadian cordillera 



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Abstract. Analysis of available information on the distribution of lithologies of the upper Paleozoic in the western Canadian Cordiliera leads to the conclusion that, by analogy with modern examples, elements of both ancient oceanic basins and island arcs are represented. A westernmost upper Paleozoic arc along the present site of the Coast Mountains is succeeded eastward by upper Paleozoic oceanic rocks in the modern Intermontane Belt, a Permian (?) arc in the modern Cassiar-Omineca-Columbia Mountains and, eastern most, Mississippian oceanic rocks on the east flank of these mountains.

## Introduction

Possible representations of extensive ancient oceanic rocks in the Canadian Cordillera are some of the upper Paleozoic (Mississippian, Pennsylvanian and Permian) volcanic and sedimentary assemblages. In places these assemblages contain the association of basalt, ultramafic rock and chert, that is commonly regarded as being characteristic of rocks formed in deep ocean basins. The only other assemblage of a similar nature in the Canadian Cordillera is represented by the small area of Tertiary basalt on southernmost Vancouver Island that is the northerly extension of the "oceanic" Olympic Mountains province. This paper is a preliminary attempt to identify the location of possible ancient oceanic rocks within the Canadian Cordillera by briefly reviewing the distribution of lithologies and the stratigraphic character of these upper Paleozoic rocks.

The following review is largely compiled from reconnaissance data in regional mapping reports of the Geological Survey of Canada, and a few local detailed studies. These data are summarized with references in a recent paper by Monger and Ross (in press, Table II). The writer is personally familiar from detailed mapping only with upper Paleozoic rocks in southwestern British Columbia (Localities 1 and 2, Figure 1) and northwestern British Columbia (Localities 4 and 9, Figure 1), and the conclusions drawn here are therefore influenced strongly by the writer's work in these areas.

## Distribution of upper Paleozoic rocks in the western Cordillera

The distribution of upper Paleozoic rocks in the western Cordillera is shown on the Index Map (Figure 1) in relation to (1) present physical features, (2) older stratigraphic units and (3) time-equivalent, non-volcanic shelf rocks to the east. Noteworthy is the absence of any known pre-upper Paleozoic rock in the central Intermontane Belt and Coast Mountains. Oldest known rocks are Lower to mid-Mississippian strata from Locality 9 (Figure 1), although the possibility exists that some rocks from Locality 2 may be as old as Devonian (H.W. Tipper, pers. comm.). Some of the outcrop areas in the Intermontane Belt (e.g. Locality 9, Figure 1) are extensive and contain strata that commonly dip steeply (thus exposing great thicknesses) and this absence of older rocks may therefore not be fortuitous.

## Distribution of upper Paleozoic magmatic rocks

The distribution of the upper Paleozoic volcanic assemblages shown in Figure 2A is provisional owing to the scarcity of information on composition from most localities. This scarcity is partly because of the reconnaissance nature of many reports but also is because the primary nature of these rocks is obscured by low-grade metamorphism, mainly of the sub-greenschist, pumpellyite-chlorite or pumpellyite-actinolite facies of Seki
(1969). Chemical analyses of these rocks come from only four areas (Locality 9, Aitken, 1959; Monger, 1969; Locality 10, Sutherland Brown, 1957; K.V. Campbell, pers. comm.; Locality 13, Gabrielse, 1963; Locality 14, Tempelman-Kluit, in press) and all are of basalts and thus not a representative sample of all upper Paleozoic volcanic rocks. In addition, stratigraphic information is insufficient to show distribution of the volcanic rocks by geological systems, and lumping all together under the heading of upper Paleozoic probably blurs some distinctions that could otherwise be made. Nevertheless, sufficient data are available to divide the volcanic rocks into two groups: (a) basalts with relatively little associated pyroclastic material and (b) mixed volcanic rocks, comprising basalts, andesites, and acid lavas, with abundant pyroclastic rocks.

Four belts of volcanic rocks can be recognized (Figure 2A). Westernmost are mainly andesite and pyroclastic rocks with some basalt. Acid volcanic rock has been reported from Localities 1,3 and 5 (Monger, 1970a, J.K. Rigby, pers. comm., Buddington and Chapin, 1929) and latite from Locality 6 (Muller, 1967). These rocks are apparently of Mississippian and Permian age. In the Intermontane Belt basalts are of Mississippian, Pennsylvanian and Permian age. Texturally these rocks are typical tholeiites, although it is not possible to characterize the type of basalt from the chemical data available, as the potassium content is widely variable, possibly as the result of later metasomatism. To the east of this is Permian and Pennsylvanian (?) pyroclastic rock and acid volcanic rock (Localities 11, 12, Lord, 1948; H. Gabrielse, pers. comm.). Finally, the easternmost belt consists mainly of basalts of Mississippian age in


Figure 1. Index map of upper Paleozoic rocks in the western Cordillera.


Figure 2. Distribution of upper Paleozoic lithologies.
the south, Mississippian and younger in the north.

Most ultramafic rocks of Alpine-type in the western Cordillera are spatially associated with upper Paleozoic rocks in the central belt, although some are in the easternmost belt. They vary in size from small dyke-like masses to the enormous Nahlin body of northwestern British Columbia (Locality 9) that is more than 60 miles long and 4 miles wide. In composition they range from serpentinite to variably serpentinized peridotite, with minor dunite and pyroxenite (e.g. Leech, 1953). In many places they are associated with gabbros, diabases and altered basalts, although nowhere has the stratified association characteristic of the ophiolite suite (e.g. Aubouin, 1965, p. 153) been reported.

The ultramafic bodies are extremely difficult to date. This problem is exemplified by the Shulaps body (Locality 2, Figure 1) that is enclosed partly by upper Paleozoic and partly by Triassic rocks (Leech, 1953). The serpentine phase of this body clearly intrudes Upper Triassic rocks but with no contact metamorphism. Chromite, probably derived from the body is found in late Lower Jurassic clastic rocks in the area and these in tum are intruded by ultramafic rocks. It is evident therefore that at least two phases of intrusion are represented but typically there is no information about time of cooling and crystallization of the body. In general, the lithological and common spatial association of the ultramafic rocks indicate a late Paleozoic age but, locally, they have been remobilized during Mesozoic deformation and have intruded postPaleozoic rocks.

## Distribution of upper Paleozoic clastic rocks

The distribution of upper Paleozoic clastic rocks in the Cordillera follows the same pattern as the volcanic rocks. Abundant sandstones and pelites and some conglomerates occur in the westernmost belt and along the western side of the Cassiar-Omineca-Columbia Mountains (Figure 2B). Ribbon-chert with radiolaria, indicative of a very slow influx of finegrained clastic material, characterizes assemblages in the Intermontane Belt
where it occurs with pelitic rocks. The easternmost belt consists of a lower clastic sequence overlain by abundant ribbon cherts (and therefore is shown as a 'mixed' pattern on Figure 2B).

The clastic sedimentation can be linked closely with the nature of the upper Paleozoic volcanism but also probably reflects differences in the tectonic behaviour of the belts. Detritus in the western and eastern belts has a two-fold source. Some was contributed directly to the basin by explosive pyroclastic activity reflecting the intermediate and acidic nature of the volcanism. In contrast, basaltic volcanism in the central belt produced relatively little clastic material. Secondly, other clastic material results from erosion of previously consolidated rocks, mainly volcanic rocks and carbonates. Evidence that landmasses were available for erosion in the eastern and western belts is provided by terrestrial plant fossils and conglomerates containing well-rounded cobbles at several localities (Figure 2B). These landmasses presumably resulted from the building-up of volcanic piles above sea level or from local tectonic uplift.

## Distribution of the upper Paleozoic carbonates in the western Cordillera

Marked differences between the nature of the carbonates in the central belt and those in the eastern and western belts cannot be related solely to the greater amount of clastic material in the eastern and western belts. Carbonate in the central belt (Localities 7, 8, 9 , Figure 1) is pure and forms enormous linear masses up to 6,000 feet thick that appear to have been deposited in shallow water as banks, reefs and tidal flats over a considerable length of time (the body at Locality 9 contains Upper Mississippian, Pennsylvanian and Permian fossils). Carbonate in the eastern and western belts is impure in many places, is nowhere as extensive as that in the central belt although locally it may be up to 2,000 feet thick, and it is generally restricted in time to a single system or part of a system. Much appears to have been deposited in a lower energy environment than carbonate in the central belt.

## Tectonic behaviour of upper Paleozoic depositional sites

Preliminary stratigraphic evidence suggests that the tectonic behaviour of the central belt differed from that of the eastern and western belts. The central belt appears to have undergone more or less continuous subsidence in upper Paleozoic time as shown by the Upper Mississippian to Upper Permian shallow water carbonate. Some stages, such as the Virgilian and Missourian (Upper Pennslyvanian) are missing from this carbonate (Link, 1965; Monger and Ross, 1971, Table D, but no physical break has been recognized apart from a postUpper Permian unconformity. In addition, the scarcity of coarse clastic rocks in the central belt indicates that there was no local erosion and redeposition in this belt. By contrast, stratigraphic breaks that at least in places record uplift are known from the western and possibly the eastern belt. At Locality 4, Permian strata sit with angular unconformity on Mississipian beds (Monger, 1970b). The only Pennsylvanian strata known from the eastem belt belong to the very top of that system (Monger and Ross, 1971). Many of the clastic rocks in the eastern and western belts that were derived from previously consolidated rock could well result from uplift and erosion, although all detritus known is derived from essentially surficial rock, indicating that if uplift took place it was relatively minor. These scarce data suggest that in the upper Paleozoic there was more or less continuous subsidence in the central, Intermontane Belt, whereas deposition was broken by uplift in the eastern and western belts.

## Conclusions

The above distribution of upper Paleozoic rocks can be explained in terms of oceanic basins and island arcs if criteria such as those outlined by Hamilton (1969, pp. 2410-2412) from modern examples are used.
(1) The westem belt of volcanic rocks of variable composition, clastics and carbonates on the site of the modern Insular Belt and Coast Mountains was an active arc in at least Mississippian
and Permian time. It may have developed, at least partly, on old continental crust formed during the time of the lower and mid-Paleozoic orogenic activity, which has been reported from southeastern Alaska by Brew et al. (1966).
(2) The central belt of basalts, cherts, ultramafic rocks (?) and carbonates of Mississippian, Pennsylvanian, and Permian age in the modern Intermontane Belt was an oceanic basin during the upper Paleozoic. This inference is supported by the lack (in contrast with adjacent belts) of a recognizable base to the succession, and the apparently continuous subsidence of this belt through late Paleozoic time. The presence of shallow-water carbonate seems incompatible with the requirements of isostacy if this is old oceanic crust, but it should be noted that very similar carbonate accumulations occur elsewhere in the world in close proximity to rocks of oceanic type. For example, carbonate of the Bahama Banks, believed by Dietz et al. (1970) to be underlain by oceanic crust, is of similar lithology and areal extent, and has formed in shallow water on a surface that has subsided for about 135 million years at an average rate of about $28 \mathrm{~m} / \mathrm{m}$ yr. (Lynts, 1970). Also, Upper Triassic to Eocene shallow-water carbonate in the Alpine mountain chains of Greece, is associated with radiolarites and ophiolites, and subsided for a similar length of time at a rate of approximately $28 \mathrm{~m} / \mathrm{m}$ yr. (calculated from Aubouin, 1965; Temple, 1968, Figure 5). Comparable figures for the carbonate accumulations at Locality 9 (Figure 1) are 90 million years at $22 \mathrm{~m} / \mathrm{m}$ yr. Reinhardt (1969) has reported Upper Permian to Lower Jurassic shallow-water carbonates in association with ophiolites in the Oman, and suggested that these formed on an ocean ridge. Perhaps, due to some as yet unexplained cause, this type of thick relatively localized carbonate accumulation characterizes oceanic crust.
(3) The eastern belt along the Cassiar-Omineca-Columbia Mountains, is poorly known, but contains at least Permian and probably Pennsylvanian mixed volcanics, suggesting that an arc existed there at least in younger late Paleozoic time.
(4) The easternmost belt, on the east flank of the Cassian-Omineca-Columbia Mountains consists of basalt, chert and some ultramafics. These are Mississippian in the south and Mississippian and younger in the north. They overlie a thick clastic sequence, that in turn lies on older shelf deposits. J. Dercourt (pers. comm.) has suggested that these rocks may be allochthonous and have overridden an eastward continental plate, in a situation somewhat analogous to that in Papua described by Davies (1968).

These data can be used to construct various plate tectonic models (e.g. Monger and Ross, in press) that will not be discussed here except to say that if the rules are followed the conclusion seems inescapable that the Coast Range, Insular, and Intemontane Belts are allochthonous with respect to the continent. The available information has been exploited to a maximum in the present paper, and before these models can be more than speculative, far more basic data is needed, along the following lines:
(a) Detailed stratigraphic studies of all upper Paleozoic localities are fundamental for any future work.
(b) Arising from the above, a knowledge of the composition of dated volcanic rocks is basic to any understanding of plate tectonics and can be used to interpret the polarity of the arcs (see Dickinson and Hatherton, 1967) and thus restrict the number of possible models.
(c) Detailed work on ultramafic bodies and their surrounding rocks to see if any "classical ophiolite" complexes are, in fact, present in the Cordillera.
(d) Detailed paleontological studies may be able to suggest, but will probably not confirm, some upper Paleozoic paleogeographic patterns.
(e) Finally, upper Paleozoic rocks should be tested for their suitability for paleomagnetic studies. Most of these rocks appear too metamorphosed and complexly deformed for this to be of much value, but so far no systematic testing has been carried out.

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# ophiolites of southern quebec* 

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Abstract. The Eastern Townships ultramafics of southern Quebec are of great economic importance, for they host numerous chromite occurrences and all of the asbestos deposits exploited in the Asbestos and the Thetford-Black Lake areas.

Preliminary results from a systematic field study recently conducted by the writer in the Thetford-Black Lake area suggest close spatial, temporal, and genetic associations of the ultramafics (mainly peridotite, pyroxenite, and dunite) with one another and with other coarse-grained igneous rocks of gabbroic, dioritic, syenitic, and granitic compositions, as well as with mafic to intermediate massive, pillowed, and fragmental volcanics. Hence, all these igneous rocks are interpreted as being part of so-called alpine-type ultramafic complexes, herein referred to as ophiolitic complexes or simply as ophiolites.

The ophiolites of southern Quebec are interpreted as being Lower Ordovician in age, for they occupy a constant stratigraphic position between the Caldwell group of Lower Ordovician or older age, on which they rest unconformably, and the St. Daniel wildflysch-type sediments of pre-Normanskill age.

Field evidence suggests that these ophiolitic complexes were extruded on a eugeosynclinal ocean floor, through a major zone of distensional fractures running along the northwestern margin of the complexes, as testified locally by a wide zone of amphibolitized Caldwell metagreywackes.

Natural features strongly suggest that liquid immiscibility is the sole process responsible for the magmatic differentiation that took place under a self formed roof of mafic volcanics in the submarine ophiolites of southern Quebec. Podiform chromites are hence interpreted as primary features resulting from the coalescent growth of chromite-rich immiscible liquid droplets in an ultramafic melt.

## Introduction

Most previous workers interpreted the phanerites (coarse-grained igneous rocks) of the ophiolites of southern Quebec (Figure 1) as intrusive into the mafic to intermediate volcanics**, near the contact between what are herein considered the Caldwell metasediments and the St. Daniel wildflysch-type sediments (Adams, 1880-81-82; Ells, 1887; Dresser, 1913; Harvie, in Knox, 1916; Cooke, 1937; Riordon, 1954; and St. Julien, 1965). Of these, Dresser was the first to venture farther into the genesis of these phanerites by suggesting that the pyroxenites, gabbros, and granites of the ThetfordBlack Lake district were derived, through gravitative differentiation after intrusion, from the same magma as that which gave rise to the serpentinized ultramafics. Likewise, most writers succeeding Dresser

[^11]have considered at least some of the coarse-grained igneous rocks of the district, and especially those of mafic and ultramafic compositions, as being comagmatic intrusives.

The interpretation proposed by the writer differs from those offered previously in that all of the spatially and temporally related ultramafic to felsic phanerites and the mafic to intermediate aphanerites (fine-grained igneous rocks) of southern Quebec are interpreted as comagmatic differentiates within ophiolitic complexes. These complexes are believed to have been extruded on a eugeosynclinal ocean floor during the Lower Ordovician epoch; thereby reviving, but in a modified form (Figure 2), Brunn's $(1956,1960)$ and Aubouin's (1959, 1965) classic hypothesis of ophiolite genesis, which has been rather unpopular in recent years.

## Distribution

All of the ophiolitic complexes of southern Quebec lie within the Serpentine tectonic belt, east of the axis of the Green Mountain-Sutton Mountain anticlinorium (also known as the Sutton-

Bennett belt in Quebec) and west of the Stoke Mountain anticlinal track (Cady, 1969). From the St. Magloire area (Béland, 1957), some 50 miles eastsoutheast of Quebec City, they extend southwestward for 175 miles, through the Thetford-Black Lake, Asbestos, and Orford areas, entering Vermont just west of Lake Memphremagog (Figure 1).

Several small, sill-like, masses of serpentinized (and locally carbonatized) peridotite, apparently intrusive in nature, are also found at various levels within the highly schistose rocks of the SuttonBennett belt. The most prominent of these is the Pennington sill, just north of Thetford Mines (not shown on Figure 1). The relationship between these ultramafic masses emplaced in the Sutton-Bennett schists and the main ophiolitic complexes is still unclear.

## General lithology and contact relations

The various lithological units present in the ophiolites of southern Quebec are: spilitized mafic to intermediate volcanics (fragmental, pillowed, and massive), serpentinized dunite and peridotite (mainly harzburgite) with local chromitite concentrations, pyroxenite, doleritic and gabbroic rocks, diorite, syenite, and granitic rocks. Some pyroxenites, gabbros, and diorites have locally suffered various degrees of rodingitization (Marshall, 1911; Grange, 1927).

The lower volcanic member of the ophiolites rests unconformably on schistose and folded eugeosynclinal metasedimentary rocks of the Caldwell group and are locally separated from them by interformational pelitic or cherty sedimentary rocks which are also typical of a eugeosynclinal environment (Figure 2).

The peripheral volcanics (including the lower volcanic member) of these ophiolites grade inward from a pillowed


Figure 1. Tectonic map of the Appalachian region of southern Quebec, showing alpine-type ophiolite complexes,


Figure 2. Synoptic cross-section of the Thetford-Ham submarine ophiolite flow, showing irregular globules of the various rock types, differentiated through liquid immiscibility (modified after Aubouin, 1959, fig. 17). The size of most globules has been exaggerated, due to the scale of the section. Originat NW-SE width of this flow may have exceeded 20 km .
or agglomeratic facies to more massive and somewhat coarser-grained doleritic and gabbroic rocks. Locally, phanerites from within the complexes were brought in direct and cold contact with the adjacent metasedimentary rocks through overthrust or underthrust faulting, especially along the well lubricated serpentinized ultramafics, close to the northwestern margin of the complexes.

Intrusive contacts showing remarkable metamorphic effects grading from the greenschist to the garnet-amphibolite facies were observed locally, but only where ultramafic feeders or apophyses from the main feeders are in contact with rocks of the underlying Caldwell. This contact metamorphism is nowhere found in any of the surrounding volcanics, however.

The ultramafic to felsic phanerites are texturally either massive or layered and show local brecciation. As is generally the case in ophiolitic complexes the world over (Thayer, 1967), phanerites of various compositions are disposed in a rather chaotic way, without showing the cumulate sequence usually found in classic examples of layered intrusions such as the Skaergaard, the Stillwater, and the Bushveld (Wager and Brown, 1968).

Furthermore, even though most contacts between any two phanerites are sharp, they are far from being geometrically simple. Indeed they show complicated contact relations, with numerous examples of contradicting "intertonguing" and so-called "inclusions" (e.g. "tongues" or "inclusions" of pyroxenite in peridotite and vice versa), without chilled margins or contact metamorphic effects.

## Stratigraphy and age

In the Serpentine belt, the ophiolite complexes of southern Quebec occupy a constant stratigraphic position between the Lower Ordovician or older Caldwell metasediments, (on which they rest (Lamarche, 1969, in press)), and the preNormanskill St. Daniel wildflysch-type sediments (St. Julien, 1968). The St. Daniel is unconformably overlain by the basal beds of the Beauceville formation of
the Magog group. These beds are well dated as Normanskill from their abundant graptolite fauna, particularly from the Castle Brook locality on the west side of Lake Memphremagog (Berry, 1962). The Caldwell metasediments are usually to the northwest of these ophiolites, whereas the wildflysch-type sediments lie to the southeast.

The basal part of the volcanic member of the ophiolites rests either directly over the Caldwell metasedimentary rocks, with a marked angular unconformity, or conformably on pelitic eugeosynclinal rocks* which, themselves, overlie the Caldwell unconformably (Figure 2).

Several sills, dykes, and lenticular masses of peridotite cutting through the underlying Caldwell metasedimentary rocks are believed to be subsidiary feeders or aphophyses from the main feeders to the ophiolitic complexes, for they show some evidence of contact metamorphism from a few feet to a few tens of feet and grade from the greenschist to the garnetamphibolite facies. The contact metamorphic effects bordering the main zone of feeders along the northwestern margin of the Thetford-Ham complex, on the other hand, are visible over widths exceeding 3,000 feet and also grades inward from the greenschist to the garnetamphibolite facies (Figure 2).

Hence, on a purely stratigraphic basis, all rocks of the ophiolitic complexes of southern Quebec are considered post Caldwell and pre-Normanskill, or, in all probability, of Lower Ordovician age. Moreover, the $\pm 480$ m.y. K-Ar dates (Poole et al., 1963) obtained on granitic rocks that are here considered as comagmatic differentiates within the ThetfordHam ophiolitic complex are interpreted as a minimum radiometric age for the whole complex and, by correlation, for the other ophiolites of southern Quebec. This determination also points to a Lower Ordovician age, according to Kulp's (1961) and Holme's (1959) time scales.

[^12]
## Origin

As reviewed by Moores (1969), four possible origins of ophiolitic complexes are worthy of consideration.

1. Giant submarine extrusions, differentiated under a self formed roof of mafic volcanics, as proposed by Brunn (1956, 1960) and Aubouin (1959, 1965), and herein modified by the writer.
2. Allochthonous sheets of oceanic crust and mantle, formed at mantle upwellings or ridges and subsequently thrust onto the continental margin (de Roever, 1956; Gass and Masson-Smith, 1963; Irwin, 1964; Hess, 1965; Davies, 1968; Church, 1969).
3. Stratified peridotite-gabbro complexes, differentiated in the mantle (Thayer, 1969) or in basic magma chambers high in the crust (McTaggart, 1971), by crystal settling from fluid magma, broken up and modified during re-mplacement as crystal mushes.
4. A partial combination of all three an origin by partial fusion of mantle material and for its emplacement as a deforming and differentiating solidliquid mass on the ocean floor (Hess, 1962; Ringwood, 1966; Moores, 1969).

In the light of field observations made on the ophiolitic complexes of southern Quebec and in view of the fact that the lower volcanic member of these complexes rests unconformably (Lamarche, 1969) on schistose and folded eugeosynclinal metasedimentary rocks, locally separated from them by interformational pelitic or cherty metasediments which are also typical of a eugeosynclinal environment, the writer favours the first of the four origins and therefore interprets all of the spatially and temporally related ultramafic to felsic phanerites and the mafic to intermediate volcanic aphanerites of the Serpentine belt of southern Quebec, as being comagmatic within ophiolitic complexes, believed to have been extruded as a simatic (ultramafic) fluid magma on a sialic eugeosynclinal ocean floor during the Lower Ordovician epoch (Figure 2).

Liquid immiscibility is believed to be the sole process responsible for the magmatic differentiation of the ophiolitic complexes of southern Quebec (Figure 2) for many reasons, some of which are:

1. Contacts between the various phanerites are sharp rather than gradational.
2. Lack of chilling and lack of contact metamorphism between the various phanerites.
3. Contradictory "intertonguing" and "inclusions", herein considered as embayments and globules of one liquid in another (e.g. pyroxenite in peridotite and vice versa).
4. Globules of the lighter liquid often have a tail pointing one way whereas the tails of the heavier globules point the opposite way.
5. The smaller the globules, the better the sphericity.
6. Coalescent features arrested at various stages between globules that have come in contact.
Hence, podiform, nodular, and orbicular features in chromite deposits, universally associated with ophiolitic complexes, are interpreted as primary features resulting from the coalescent growth of chromite-rich immiscible liquid droplets in an ultra-mafic melt.

Because of their great number and similarity to the ophiolites of southern Quebec, other well known ophiolitic complexes such as those of western Newfoundland, Canyon Mountain of Oregon, New Caledonia, Oman, Sesia Lanzo zone of the western Alps, Troodos of Cyprus, and Vourinos of northem Greece (regardless of their respective ages and sizes) are also believed to have been extruded as huge submarine ophiolite flows on ocean floors and to have undergone differentiation through liquid immiscibility in this relatively fast cooling submarine environment.

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# ophiolite: its definition, origin as oceanic crust, and mode of emplacement in orogenic belts, with special reference to the appalachians 

No. 6


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#### Abstract

Alpine-type ophiolites are allochthonous stratiform complexes composed of complete or partial sequences of peridotite, pyroxenite-troctolite-gabbro, "sheeted diabase', and pillow lava, Such sequences are probably generated at 'oceanic' ridges. The peridotite component of ophiolite is a cumulate derived from an ultramafic liquid which crystallized at some depth within the mantle, whereas the gabbros and associated pyroxenites and troctolites are cumulates formed at a relatively high level in fissures below ridges. The peridotites were deformed during their emplacement as solid material and have nonconformable contacts with the overlying gabbro cumulates.

Alpine ophiolites are also characterized by the presence, when preserved, of basal contact aureoles of pyroxene-gamet-amphibole-plagioclase granofels and amphibolite. In contrast ophiolites of the Circum-Pacific region are underlain by blueschist metamorphic rocks. The time span between the origin of ophiolite at an oceanic ridge and its emplacement as an allochthonous sheet may be quite short, and some ophiolites may have been directly emplaced over their adjacent continental margins as thick sheets of 'hot', yet crystalline, oceanic lithosphere.

The Appalachian geosyncline was initiated on a Precambrian sialic crust. Oceanic crust of the northern Appalachians may not have appeared as a significant component of the geosyncline until early Ordovician time. There is no evidence to suggest that the ocean basin ever achieved the dimensions of the present Atlantic or Pacific. In the southern Appalachians, where alpine-type ophiolites appear to be absent, crustal distension during the early Phanerozic may have been too limited to allow the development of recognizable oceanic crust. The appearance in the northern Appalachians of ophiolites during the early Ordowician may reflect a stage in the evolutionary change from Precambrian-type tectonism to that associated with the large-scale plate motions characterizing the late Phanerozoic.


It is the purpose of this paper to outline the origin and subsequent use of the term "ophiolite", and the several theories pertaining to the origin of rocks denoted by this term; secondly, to show that the ultramafic-mafic associations of the Newfoundland Appalachians and possibly also those of Quebec and Maine are comparable to ophiolites of the Alpine fold belt, and that the Appalachian system is therefore an alpine-type rather than cordilleran-type mountain chain; thirdly, to point out that, of the various ultramafic-mafic complexes referred to as alpine-type, those resembling true Alpine ophiolites are most likely to represent complete sections of oceanic lithosphere; and fourthly, to suggest that some ophiolite complexes may have been emplaced during periods of ocean formation rather than ocean closure.

Definition and origin of the term "ophiolite"

Steinmann $(1905,1927)$ in describing the ophiolite zone of the Mediterranean Mountain Chain states (1927, p. 637) that "as ophiolite one should designate only the consanguineous association of chiefly ultrabasic rocks, the most important component of which consists of peridotite (serpentinite) the more subordinate of gabbro, diabase, spilite or norite and related rocks". Steinmann pointed out that the peridotite (serpentinite) gabbro, diabase-spilite members of the ophiolites were ordered in stratigraphic sequences in which the peridotite was always the lowermost member.

Benson (1926, pp. 6, 68) referred to the ophiolites as "Green Rocks of the Alpine Type" noting that their special character lay in the intimate association of coarse-grained peridotite and gabbro,
clearly plutonic in nature, with finergrained diabase, spilite, and pillow lava. On this basis they were to be distinguished from another group of more or less stratiform or sill-like masses of peridotite and gabrro which he referred to as 'sill-and-batholith' or 'cordilleran type' complexes. These rocks were considered by Benson to represent parts of differentiated mafic intrusives that had been separated during periods of 'great lateral pressure' (cf. Bowen, 1920, 1927; Mc'Taggart, 1971), and which were invaded subsequently by less regular batholiths of diorite and granite. Cordil-leran-type complexes include uiltramafic and mafic rocks of the Ivrea zone the Harz Mountains, the Highlands of Scetland, and, apparently (Benson, 1926, p. 76) the Great Serpentine Belt of New South Wales. Such complexes have also been referred to as orogenic or orogenotype (cf. Green, 1964, p. 185; Den Tex, 1965, 1969; Rost, 1968; Forestier, 1968).

It is suggested that use of the term "ophiolite" should be restricted to those ultramafic-mafic sequences which are comparable in petrography and structure to the Mesozoic layered plutonic-effusive rock associations of the Mediterranean Alpine system (cf. Vuagnat, 1968). The term should not be used for such patently intrusive ultramafic sheets or diapirs as those of the Lizard (Green, 1964) Beni Bouchera (Komprobst, 1969) Lherz (Ravier, 1959) La Ronda (Herna-dez-Pacheco, 1967) Tinaquillo (MacKenzie, 1960) the Caribbean (Bowin, 1966; Kozary, 1968) Japan (Igi, 1953; Yoshino, 1961, 1964; Myashiro, 1966) Dun Mountain-Red Hills (Challis,

1965, 1969; Challis and Lauder, 1966) Darvel Bay (Hutchison and Dhonau, 1969) Blue River (Wolfe, 1965) and California (Ragan, 1963; Raleigh, 1965; Irwin, 1964).

## Theories of the origin of ophiolite

## Early theories

Most theories are based on either an affirmation or denial of the consanguinity of the plutonic and effusive components of ophiolite. The simplest explanation for their origin was advanced by Steinmann (1927) who considered all the components of ophiolite, including pillow lava, to have crystallized from ophiolite magma intruded into a thick section of Mesozoic deep-sea sediments. He proposed that ophiolites represent abyssaltype mafic magmatism as opposed to hyperbyssal magmatism represented by spilitic rocks (also considered by Steinmann to be intrusive) and neritictype magmatism represented by effusive rocks such as the volcanic rocks of the Andes (cf. Rocci and Juteau, 1968). In opposition to Steinmann, Suess (1909) considered the ophiolites to have been intruded during Tertiary main-phase orogenic movements. Benson (1926) supported the views of Suess. He attempted to reconcile the association of plutonic and effusive rocks in ophiolites, and also explain their location within fold belts, by suggesting that "basic magma rising along a plane of shearing (is) pressed out at the surface in front of an advancing overthrust anticline or crust flake, and may consolidate in the form of volcanic rocks, .... (which) may be overridden by the advancing sheet; the magma passing along the thrust plane may now be injected into the previously formed volcanic rocks, thus (forming) a plutonic series of intrusions". It has now been established however (Gannser, 1959; Trumpy, 1960; Karamata, 1970; Abbate et al, 1970) that the ophiolites of the Mediterranean Alpine system were emplaced relatively early in the Alpine tectonic cycle; much earlier than the main orogenic movements of Tertiary age. Consequently the association of plutonic and effusive rocks in ophiolites has remained an enigmatic and unsolved
problem (Anonymous, 1968, 1969; Wyllie, 1967).

## Current theories

The main hypotheses for the origin of ophiolite are those of:
(1) Routhier $(1946,1953)$ Bailey and McCallien (1953) Brunn (1954, 1960) Dubertret (1955) Borchert (1961) (Aubouin, 1964) and Lamarche (1971) who consider ophiolites to be products of gravitational differentiation within a large submarine mafic lava flow.
(2) Maxwell (1969) who states that Alpine ophiolites perhaps resulted from diapiric up-welling and partial melting of mantle material during an early, possibly tensile, stage in the Alpine orogenic cycle; lavas were extruded into deep troughs and residual ultramafic rocks, perhaps lubricated by intragranular melt, moved plastically beneath the volcanic carapace. The resulting ophiolite complex is thus a composite subsea laccolith.
(3) Moores (1969) who suggested that ophiolite complexes may represent the closest existing approach to ultramafic extrusives, and may originate by partial fusion of mantle material and its emplacement as a deforming and differentiating solid-liquid mass on the ocean floor.
(4) Peters (1969) Decandia and Elter (1969) Abbate et al. (1970) Bortolami and Dal Piaz (1970) and Bezzi and Piccardo (1971) who consider ophiolites of the Alpine region to be allochthonous fragments of an "ophiolitic window" formed during attenuation and disruption of continental crust. The ophiolites are therefore composed of mantle and lower crust and were emplaced during reconvergence of the separated crustal blocks. Avariation of this view is given by Hsu (1970) for the Jurassic ophiolites of the Franciscan of California.
(5) Dietz (1963) Hess (1964) Gass (1968) Laubscher (1969) Reinhardt (1969) who have suggested that Alpine ophiolites may represent allochthonous fragments of oceanic floor emplaced, according to Hess and Reinhardt, by
gravity sliding from a mid-ocean ridge. As a variant of this hypothesis, and of hypothesis (4) Church and Stevens (1970(a) and (b), 1971) put forward the possibility that some ophiolites of the Appalachians, although formed at a 'mid-ocean' ridge in the manner suggested by Reinhardt, may have been emplaced as 'hot' layered complexes directly over sialic crust at the time of inception of an oceanic ridge within a continental plate during the development of an intrasialic small ocean basin (cf, Church, 1971).
(6) Davies (1968) Dewey and Bird (1970) Hamilton (1969) Moores (1970) Stevens (1970) Coleman (1971) Dickinson (1971) propose that ophiolites are overthrust segments of 'cold' oceanic lithosphere emplaced as a result of continent-ocean collision.

Hypotheses (4), (5) and (6) are in agreement in interpreting ophiolite as oceanic lithosphere, but differ with respect to the relative age and manner of ophiolite emplacement within eugeosynclinal sequences. Opinions also vary concerning the mechanism by which the gross compositional layering of ophiolites is produced. Gass (1968) postulates that the Troodos ophiolite complex of Cyprus represents oceanic lithosphere formed at a mid-ocean ridge by fusion of the upper mantle. Melting of the upper mantle was sufficient to allow gravity fractionation at depth, thus producing the gross compositional layering of the oceanic crust, and provision of a liquid phase to be injected as dykes and poured out as lava flows. Reinhardt (1969) however considers ophiolite to be a polygenetic assemblage, the peridotitic component of which may have formed in an independent, highly contrasted environment to that of the gabbro, diabase and spilite. The peridotite component of ophiolite was, according to Reinhardt (1969, p. 26), formed deep within the mantle and brought to near surface by mantle convection cells, whereas the gabbro, diabase and spilite components of ophiolite crystallized from basaltic magma at different levels in the fissures below oceanic ridges. Maxwell's hypothesis, although an attractive one, does not explain the formation of
'sheeted diabase' units (cf. Reinhardt, 1969), such as those of the Oman, Troodos, and Appalachian ophiolites, as well as does the 'oceanic lithosphere' hypothesis as illustrated by Reinhardt (1969, fig. 17). On the other hand the presence of a basal high-temperature contact aureole in some ophiolite complexes (Karamata, 1968; Bilgrami, 1963; Ricou, 1971; Church and Stevens, 1971) is a feature which is not in accord with their interpretation as 'cold' sheets of oceanic lithosphere.

## Ultramafic-mafic associations of the Appalachians

## Distribution

The first comprehensive description of the belt of ultramafic intrusions extending the length of the Appalachians was given by Pratt and Lewis (1905) who considered that "the principal period of intrusion was closely associated with the great orogenic movements of the revolution at the close of the Ordovician period The late Appalachian disturbance at the close of the Carboniferous would account for the widespread lamination developed in the peridotites," (quoted by Benson, 1926, p. S6). This view of the ultramafic rocks as synorogenic intrusives was echoed by Hess who showed the Appalachian ultramafic rocks distributed in two belts which he considered to define the axis of the Appalachian system. It is now known however that in the Newfoundland Appalachians there are four belts of ultramafic rocks (Figure 1): the Bay of Islands-Hare Bay belt; the Baie Verte belt; the Betts Cove belt; and the Gander Lake belt. The first three ultramafic occurrences are formed of layered ultramafic-gabbro-diabase-spilite sequences which are structurally and petrographically identical to Mesozoic Alpine ophiolite complexes (Church and Stevens, 1970, 1971).

The Gander Lake belt, along with other minor occurrences of ultramafic rock in the Central Mobile belt of the Newfoundland Appalachians, represent cordilleran-type ultramafic-mafic rocks related to Acadian (mid-Devonian) igneous and tectonic activity (cf. Chapman, 1968).

Extrapolation of major tectonic structures of the Newfoundland Appalachians to the southwest (Figure 1) suggests that the Baie Verte and Betts Cove ophiolite belts of Newfoundland may be lateral equivalents of the ultra-mafic-mafic complexes of the Eastern Townships of Quebec and the Chain Lakes region of southwestern Maine, respectively (Boudette, 1970). In each case the ophiolite sequence overlies deformed and metamorphosed rocks of Late Proterozoic to Cambrian age-the Fleur de Lys of Newfoundland, the Sutton-Bennet-Caldwell Schists of Quebec, and metamorphic rocks of the Chain Lakes Massif of southwest Maine (Figure 1). In the British Caledonides, the equivalents of the Baie Verte and Betts Cove ophiolite belts would be those of the Highland Boundary fault zone and the Ballantrae complex of the Girvan region of Scotland, respectively (Church, 1969, fig. 12; Church and Stevens, 1970(b)). The above correlations are supported by the existence of a belt of pre-ophiolite basalt-rhyolite-porphyry volcanic rocks (Paquet Harbour-Grand Cove-Cape St. John volcanic groups of Newfoundland, and the Stoke Mountain belt of Quebec) between both the Baie Verte-Betts Cove ophiolites and the Eastern Townships-Chain Lakes ophiolites. In both regions the volcanic rocks are the loci of $\mathrm{Cu}-\mathrm{Zn}$ mineralization typified by deposits of the Eustis Mine of the Eastern Townships and the Rambler Mine of the Burlington Peninsula, Newfoundland. As a point of metallogenic interest it may therefore be noted that in the Appalachians ophiolites do not represent the earliest phase of volcanic activity associated with base metal mineralization (cf. Hutchinson et al, 1971).

Pre-ophiolite ultramafic rocks of the Appalachians

Ultramafic bodies occurring within the Cambro-Ordovician (?) rocks of Vermont (Chidester, 1968) and areas to the south (Piedmont ultramafics) may represent parts of ophiolites dismembered and reintruded during the Acadian orogeny, or, alternatively and more likely, cordilleran-type ultramafic rocks intro-
duced directly as solids or crystal mushes from a deep crustal or mantle source. Such an origin seems most plausible for the clearly sheet-like ultramafic rocks intrusive into the Caldwell formation west of the Thetford Mines area. Such rocks also form part of the pre-ophiolite Fleur de Lys metamorphic complex of the Burlington Peninsula, Newfoundland (Church, 1969) and of the mid-Cambrian metamorphic rocks of the northern part of the Piedmont zone of the southern Appalachians (Southwick, 1970). The complexity of the ultramafic associations of the Eastern Townships region may therefore be the result of the presence of both ophiolitic and cordilleran-type ultra-mafic-mafic complexes (cf. Lamarche, this volume) as in New Caledonia (Routhier, 1953; Avias, 1967; Guillon, 1969).

## Post-ophiolite flysch and calc-alkaline volcanism

The ophiolite sequence of the Eastern Townships of Quebec is overlain by a flysch sequence which includes olistostrome units (St. Daniel 'argilles à blocs', St. Julien, 1968). Analogous rocks to the diatostromes may be represented in the Baie Verte ophiolite belt of Newfoundland by a black-slate conglomerate (containing granodiorite and peridotite debris) which overlies pillow lavas of the Baie Verte ophiolite. The ophiolites of the Betts Cove-Chain Lakes belt are overlain by greywackes (containing chromite), slates, and volcanic rocks (pyroxene and amphibole andesites; keratophyres) indicative of post-ophiolite calc-alkaline volcanic activity (Snooks Arm Group and parts of the Lushs Bight Group of the Notre Dame Bay region of Newfoundland; unnamed formations and Ammonoosac volcanic rocks of Maine and New Hampshire, Boudette, 1970).

## Ophiolites of the Newfoundland Appalachians

A composite section of the Newfoundland ophiolites of the Bay of Islands, Baie Verte, and Betts Cove regions is shown in Figure 2. The ophiolites are characterized by the following features:
(1) they are thick (c. $7-10 \mathrm{~km}$ ), (Smith, 1958, p. 78) stratiform bodies composed of a lower unit of ultramafic tectonites overlain by pyroxenite-gabbro or dunite-troctolite-gabbro cumulate sequences, 'sheeted diabase' units, and pillow lavas. On a gross scale the sequences are comparable to ophiolite complexes of the Alpine system (cf. Reinhardt, 1969; Bezzi and Piccardo, 1971).
(2) the presence of ultramafic debris in dated underlying and overlying flysch sediments shows that the ophiolites were emplaced prior to mid-Arenigian (early Ordovician) time, but after the late Cambrian (?) metamorphism of the underlying Fleur de Lys metasediments (Church, 1969; Stevens et al., 1969; Stevens, 1970; Church and Stevens, 1971). The ophiolites were therefore not intruded during the mid-late Ordovician Taconic orogeny, and in common with the Mesozoic Alpine ophiolites their emplacement is demonstrably not 'syntectonic'.
(3) where the lower contact of the ophiolites are exposed a high-temperature contact aureole may be observed (Smith, 1958). At Trout River in the Bay of Islands the contact aureole immediately adjacent to the peridotite is composed of a pyroxene-garnet-amphibole-plagioclaseilmenite granofels. The contact aureole is superposed on mafic schists with a pre-existing regional metamorphic fabric. The thickness (less than one metre) and distribution of the garnet-pyrabole relative to the base of the ophiolite makes it clear that the aureole was formed by contact metamorphism induced by emplacement of a high-temperature solid. In the Hare Bay region garnets in the contact aureole are helicitic and contain relicts of the earlier regional polymetamorphic fabric.
(4) high-pressure mineral assemblages have been recorded in the basal part of the lherzolitic member (Figure 2, zone B) of the peridotite at Trout River (Church and Stevens, 1971, fig. 2) indicating that at least part of the peridotite crystallized at depth within the mantle.

Mineral assemblages include:
(a) olivine-orthopyroxene-clinopyroxenespinel.
(lherzolite spec. Tr6932) $\mathrm{Al}_{2} \mathrm{O}_{3}$ in spinel c. 45 weight per cent; $\mathrm{Al}_{2} \mathrm{O}_{3}$ in clinopyroxene c. 5 weight per cent.
(b) clinopyroxene-orthopyroxene-spinel. (normal ariegite spec. Tr6932)
(c) olivine $\left(\mathrm{Fa}_{2}\right)$-kaersutite-orthopyro-xene-clinopyroxene-ceylonite.
(kaersutite-lherzolite spec. Tr6813)
(d) kaersutite-clinopyroxene (c. 8 weight per cent $\mathrm{Al}_{2} \mathrm{O}_{3}$ ) - garnet ( $\mathrm{FeO} / \mathrm{MgO}$ mole ratio - $1.0 ; \mathrm{CaO}$ weight per cent - 5.5) - ceylonite.
(garnetiferous amphibole ariegite spec. Tr6813)
(e) kaersutite - Ti-phlogopite $\left(\mathrm{TiO}_{2}\right.$ weight per cent - c. 5)
(Iherzolite spec. Tr6920)

Mineralogically and chemically the ariegites at Trout River are comparable to the kaersutite-bearing ariegites occurring as dykes and veins in the lherzolite of the type locality at Uherz in the French Pyrênées (Ravier, 1959, 1964; Church, 1966, 1968; Avé Lallemant, 1967; Conquéré, 1971). Of particular interest is the occurrence in the Trout River ariegites of grass-green spinel (ceylonite) with rims of garnet, a texture which is particularly characteristic of the ariegites at Lherz (Church, 1966, 1968, p. 784) and also of some gamet-ariegites occurring as inclusions in basalts of Hawaii (Jackson and Wright, 1970, p. 417). Gamet-ariegites also occur in association with ultramafic rocks of the Ballantrae ophiolite at Girvan, Scotland. The latter occupies a structural position analogous to the Betts Cove complex of Newfoundland. The ariegites are NOT eclogites and are in no way related to the post-ophiolite blueschist metamorphism of the Cirvan area (Bloxam and Allen, 1959).
(5) podiform chromite associated with clinopyroxenite occurs towards the top of the peridotite of the Bay of Islands ophiolite. At Blow Me Down Mpuntain chromite is relatively rich in alumina $\left(\mathrm{Al}_{2} \mathrm{O}_{3} / \mathrm{Cr}_{2} \mathrm{O}_{3}\right.$ weight ratio - $1.0 ;$ Smith, 1958, p. 103).
(6) cumulate and tectonite fabrics may be found in both the peridotite and pyroxenite-troctolite-gabbro components of the ophiolites. Graded beds of pyroxenite have been observed within the peridotite tectonite at Betts Cove, as have also websterite layers with a laminated cumulate fabric and euhedral clinopyroxenes. Anhedral pyroxenes and olivines in adjacent bands of wehrlite may however show a strong preferred crystallographic orientation. The associated grey pyroxenite and gabbro cumulates (Figure 2, zone D) which intrude the above rocks are not deformed. However in the Bay of Islands at Trout River (Church and Stevens, 1971, fig. 2) both the peridotite and gabbro have strong deformation fabrics. Gabbros contain irregularly shaped plagioclases with a strong preferred crystallographic orientation, and pyroxenes are concentrated in parallel but discontinuous layers. The gabbros show no signs of diaphthoresis other than the development of rims of brown amphibole about some pyroxenes. The preferred orientation of the plagioclase is probably a piezocrystalline deformation fabric formed at elevated temperatures (Den Tex, 1965, 1969).
(7) the contact relations of the peridotite and pyroxenite-gabbro units (Figure 2, Zones C and D) are well displayed at Betts Cove where grey clinopyroxenite, representing the basal unit of the gabbro, and also the gabbro, cut in the form of dykes, sheets, and veins the underlying peridotite, websterite and wehrlite. Ultramafic xenoliths are also common in the pyroxenite and gabbro. At Trout River, although ultramafic xenoliths may also be observed in the gabbro, the transition zone is marked by the presence of feldspathic dunites, troctolites and anorthosite. Where deformation has been strong the contact relations between these transition-zone rocks and the underlying peridotite are not clear. However, in association with the troctolite zone of the Lewis Hills region of the Bay of Islands, Cooper (1936, p. 31) recorded the presence of selvages of picotite up to four inches thick separating layers of anorthosite and feldspathic dunite. This rela-


Figure 1. Tectonic zonation, trends of anticlinorial and synclinorial fold axial traces, and distribution of Ordovician ophiolites and Acadian ultramafic-mafic layered intrusives in the northern Appalachians.


SEDIMENTS

PILLOW LAVA

G．BASALT－SPILITE ZONE

＇SHEETED＇DIABASE

玉゙き2 QUARTZ DIORITE
ニ～～～
GABBRO


Not to scale
Figure 2．Idealized composite section of an early Ordovician ophiolite based on the Trout River and Betts Cove ophiolites of western Newfoundland and the Burlington Peninsula，respectively（Church and Stevens，1971， fig．2）．Thickness of the section is about 10 km ．
tionship has also been observed by Bezzi and Piccardo (1971, figures 13 and 14) where gabbroic and peridotitic rocks are interbanded in the ophiolites of eastern Liguria. Such rocks are considered by Bezzi and Piccardo (1971) to be cumulates related to the gabbro.
(8) 'sheeted diabase' units separate the gabbro and spilite components of the ophiolites at Betts Cove (Church and Stevens, 1970, 1971) Flatwater Pond in the Baie Verte belt, and Blow Me Down Mountain in the Bay of Islands ( $F$. Graham, personal communications). At Trout River, the gabbro, according to Smith (1958) metamorphoses the overlying pillow lavas. However as Smith notes (p. 20-21) the contact relations between gabbro and volcanic rocks are difficult to define and their true relationship is at present not known.
(9) satellitic bodies of quartz diorite and trondjemite are associated with the ophiolites (Smith, 1958).
(10) volcanic rocks associated with the ophiolite at Betts Cove are low K tholeiites.

The presence of an "ophiolite stratigraphy", the nonconformable relationship between peridotite and gabbro, the upper mantle origin of some of the peridotite, the presence of sheeted diabase, their pretectonic emplacement, their age relative to the development of the Appalachian flysch basins of Ordovician age, all combine to suggest that the Newfoundland ultramafic-mafic complexes are true alpine-type ophiolites, and that the northern Appalachians at least in part developed in a similar manner to the Alpine orogen of the Mediterranean region.

## Ophiolite as oceanic lithosphere

The main difficulty in comparing ophiolite complexes with oceanic lithosphere is the absence of detailed petrographic and structural descriptions of actual sections of oceanic crust. Any comparison between oceanic lithosphere and ophiolite must of necessity be circumstantial.

Layered nature of ophiolites and oceanic lithosphere

Seismic evidence and deep-sea dredging show that the ocean crust is formed of three layers, the uppermost two of which are composed of sediments and basaltic submarine volcanic rocks, respectively, pierced by serpentine intrusions (Cann and Funnell, 1967; Barret and Aumento, 1970). There is less agreement as to the constitution of the third oceanic layer, and it is usual to consider it as formed of either gabbro, serpentine, or amphibolite. Comparison with ophiolites suggests that it is made up of gabbro and 'sheeted diabase', both of which rock types have seismic velocities comparable to those of the third layer. Lesser amounts of brown homblende-bearing gabbro and amphibolite may also be present since these have been recorded by Reinhardt (1969, p. 6) in the Oman ophiolite, Smith (1958, p. 47) in the Bay of Islands, and T. Schroeter and L. Riccio (personal communication) in gabbros and diabases of the Betts Cove ophiolite. Myashiro et al. (1970) point out that brown homblende occurs in many gabbros from the Mid-Atlantic Ridge, but is not common in tholeiitic gabbros on the continents and in island arcs. Brown amphibole in ophiolites occurs as an alteration, and sometimes total recrystallization product of pyroxene, its formation representing the relatively high-temperature hydrous metamorphic conditions attained in the regions below ocean ridges. The occurrence of clinopyroxene rimmed by clear tremolite-actinolite and orthopyroxene pseudomorphed by talc, in ultramafic rocks of the Betts Cove ophiolite of Newfoundland (L. Riccio, personal communication) and in samples dredged from the Mid-Alantic Ridge (Aumento and Loubat, 1971, p. 637, 644) further emphasizes the identity of the alteration processes which have affected both ophiolites, and mafic rocks formed at ocean ridges.

## 'Sheeted' diabases

One of the more potent reasons for considering ophiolites as oceanic lithosphere is that the mechanism for their formation at an ocean ridge as outlined
by Reinhardt (1969) explains in a very satisfactory manner the structural and stratigraphic relationships of the various cumulate units, and also of the gabbros and 'sheeted diabases'. The latter have now been recorded in ophiolites in Cyprus (Gass, 1968) the Oman (Reinhardt, 1969) Kizil Dagh, Turkey (Vuagnat and Cogulu, 1968) Newfoundland (Church and Stevens, 1970, 1971) and the Vardar zone of Yugoslavia (S. Karamata, personal communication, 1970). At Betts Cove in Newfoundland the 'sheeted diabases' form a discrete unit between the gabbro and the overlying pillow lava sequence. In places the unit is composed entirely of diabase dykes intrusive into one another, and inclined at a high angle to the gross layering of the ophiolite (Figure 2). The presence of 'sheeted diabase' units within any ophiolite sequence may be one of the best criteria for considering it as oceanic lithosphere. However the actual sequence present in any section of oceanic lithosphere will depend on the spreading rate and the availability of basaltic magma. Thick sections of gabbro may imply periods of slow or no spreading.

## Peridotite-gabbro boundary and the Mohorovicic discontinuity

The boundary between peridotite and gabbro in ophiolites represents the Mohorovicic discontinuity. The boundary is a nonconformity as is indicated by the kind of intrusive and migmatitic contacts observed between gabbro and peridotite in many ophiolites (e.g. Oman, Reinhardt, 1969, p. 7; Kizil Dagh, Vuagnat and Cogulu, 1968; Newfoundland, Church and Stevens, 1970; northern Appenines, Elter in Bezzi and Piccardo, 1971, p. 59). The independence of the peridotite and gabbro may also be marked by the presence of a deformation fabric in the former and a lack of such in the overlying gabbro, diabase and spilite. Aumento and Loubat (1971, p. 655) state in their description of the ultramafic rocks collected from the Mid-Atlantic Ridge near $45^{\circ} \mathrm{N}$ that "whereas all the dredged ultramafics have been deformed and altered there is an absence of volcanic and diabasic dredged specimens which
have undergone similar mechanical and chemical action".

Dunite-harzburgite and Iherzolite components of ophiolite as mantle-derived material

Bonatti, Honnorez, and Ferrara (1970) suggest on the basis of strontium isotopic studies of peridotite, and the analogy of ophiolite with oceanic lithosphere, that a boundary should exist within the upper part of the mantle separating depleted 'residual' mantle with high Sr87/Sr86 from primary mantle typified by the lherzolite inclusions commonly found in basalts. Since the kaersutite-bearing high-pressure mineral assemblages occurring as layers in the basal lherzolite (Figure 2, Zone B) of the ophiolite section at Trout River closely resemble mineralogically and chemically the kaersutite-bearing ariegites associated with mantle lherzolites of the type locality at Lherz in the French Pyrenées, and also the ariégites occurring as inclusions in basalt (Ravier, 1964; Church, 1968, p. 783; Jackson and Wright, 1970, p. 417; Beeson and Jackson, 1969) it is conceivable that the lherzolite/harzburgite boundary within the peridotite at Trout River represents the primary peridotite-residual peridotite boundary judged to exist within the upper mantle of oceanic regions by Bonatti et al. However, petrographic studies, in particular the identification of cumulate textures, indicate that the harzburgitic and dunitic rocks of the peridotite component of the ophiolites of Newfoundland are deformed cumulate igneous rocks rather than residual primary mantle material. The deformation fabric of the peridotites, and also the sometimes complex distribution of rock types within it, were presumably induced during vertical flowage of the peridotite below the mid-ocean ridge (cf. de Roever, 1957) and lateral flowage during sea-floor spreading. At higher levels in the oceanic crust the peridotite may have formed the walls and floors of the magma chamber in which crystallized the gabbro component of the ophiolites. In turn, the basal "high-pressure" lherzolite at Trout River may have formed part of a wall or floor
of a magma chamber in which the harzburgite and dunite crystallized.
'High-pressure' lherzolite and ariegites occur as inclusions in basalts, as intrusive sheets or diapirs in metamorphic complexes (Green, 1964; Kornprobst, 1969) as allochthonous blocks in explosion breccias (Ravier, 1959) and as basal units of some Alpine ophiolites (Nicolas, 1967, 1969; Bezzi and Piccardo, 1971). Although tectonism has largely obscured their primary textures, chemical data and the rare preservation of what can be interpreted as relict cumulate textures suggest that these rocks may also have originated as differentiates of a silicate melt.

The layered lherzolite bodies at the type locality of Lherz (and also Beni Bouchera, Komprobst, 1969) are not homogeneous but vary in composition from layer to layer due to changes in the proportions of olivine, pyroxenes, and spinel, and also changes in the chemical composition of the pyroxenes and spinels. $\mathrm{Al}_{2} \mathrm{O}_{3}$ in clinopyroxenes varies from 3 to 6 weight per cent, and $\mathrm{Cr}_{2} \mathrm{O}_{3}$ in spinels from 2 to 15 weight per cent (Collée, 1962; Conquéré, 1971; Church. and O'Hara and Mercy, unpublished data). Concentration of the pyroxenes and spinels in layers produces pyroxenites ranging from bright-green diopsidic pyroxenite to the typical ariégite (2-pyroxene spinel rock) which most clearly identifies the lherzolite assemblage as having formed at high pressures (cf. Green, 1964; Church, 1968, p. 781).

The pyroxene compositions, bulk alumina content of lherzolite, and the composition of olivine ( $\mathrm{Fa}_{7-10}$, Collée, 1962; Conquéré, 1971) imply, following the arguments of Carter (1970) whereby it is assumed that primary mantle material has an alumina content of 6 to 8 weight per cent, that lherzolites are either the refractory residuum following partial melting of aluminous-peridotite (e.g. garnet-"Iherzolite' spec. 66SAL-1, Jackson and Wright, 1970, p. 417) or early cumulates from an aluminous peridotitic liquid. Although the lherzolites from Lherz have been strongly tectonized (Avé Lallemant, 1967) euhedral to subhedral inclusions of spinel in olivine, of spinel
and olivine in orthopyroxene (Conquéré, 1971, p. 297) and subhedral grains of clinopyroxene in contact with spinel are sometimes still preserved in the pyroxenites. Such textures as well as the rhythmic and chemical layering of the lherzolite suggest that it was originally formed as an igneous cumulate. The occurrence of garnetiferous ariégites and lherzolites as dykes and veins (Avé Lallemant, 1967) and the presence of garnet reaction coronas about spinel (Church, 1966) indicate that these rocks are also the products of crystal fractionation of a silicate melt at high pressure.

Clinopyroxenes of ariégites are much richer in alumina compared with clinopyroxenes from websterites associated with dunite-harzburgite suites such as those of New Zealand (1.0-1.7 weight per cent, Challis, 1965) and Betts Cove (1.7 weight per cent, L. Riccio, personal communication) and correspondingly lower in iron and magnesium. It is the higher alumina content of pyroxenes in lherzolites and ariégites (Figure 2, zone B) compared with that of pyroxenes from harzburgites and websterites (Figure 2, zone C) which forms the basis for the separation of these suites of rocks into 'high-pressure' and 'low-pressure' associations; and also for the assumption that the lherzolite-ariégite and harzburgite-dunite-websterite components of ophiolite peridotite must have formed in very different environments, and are therefore not comagmatic. The different compositions of pyroxenes in lherzolite and harzburgite could be reconciled with their origin from a common body of magma, however, if it is assumed that the magma chamber in which they crystallized migrated upwards during differentiation of the magma beneath an active oceanic ridge. The pyroxenes may also have crystallized from the same melt under the same high-pressure conditions, the difference in pyroxene compositions merely reflecting the change in composition of the magma, in particular its depletion in alumina, during its progressive differentiation.

Which explanation, if any, is correct has yet to be resolved.

## Emplacement of ophiolite

Primary and secondary emplacement
Alpine-type ophiolites are allochthonous sheets which have been emplaced by subhorizontal thrust movements. Their movement history can be divided into two phases:
(1) primary emplacement as large strati. form sheets overthrust onto, or underthrust by, sialic continental rocks (as a result of sea-floor spreading);
(2) secondary emplacement in association with the formation of olistostromes (argille scagliose) due to vertical uplift and gravity sliding of segments of the ophiolite sheets into a migrating flysch basin or basins.

In the Dinaric-Hellenic mobile belt of the Eastern European Alpine system, the ophiolite-bearing sub-Pelagonian and Vardar zones appear to be independent eugeosynclinal systems separated during their development by a shelf area of crystalline rocks (the Pelagonian Massif) which in places is also overlain by ophiolite (Vourinos, Moores, 1969). The ophiolites of the Vardar zone (Milovanovic and Ciric, 1968; Karamata, 1968, 1970) presently occur as dissected sheets overlying or within Jurassic eugeosynclinal rocks (the diabase-hornstein formation) which overlie in turn Paleozoic basement and its mantle of early Mesozoic shelf carbonates. This situation is strongly reminiscent of that of the ophiolites of western Newfoundland (Stevens, 1970). In both cases the ophiolites represent gravity slides which have slid into a migrating flysch trough (Stevens, 1970). Consequently, ophiolites associated with olistostromes are commonly disrupted and often only part of the full ophiolite sequence is preserved. Such ophiolites have been interpreted as blocks of oceanic lithosphere incorporated into trench mélanges (Dewey and Bird, 1970). However, stratigraphic relations preclude such an interpretation for the ilistostromes of the Alps and the Appalachians (e.g. the Dunnage Formation of Newfoundland, Horne and Helwig, 1969; the St. Daniel Formation, St. Julien, 1968). Further-
more, within both the Appalachian and Dinaride ophiolite zones, blueschist metamorphic rocks associated with mélanges, an association considered by Dewey and Bird to indicate that the mélanges are trench deposits, are absent. Even in areas such as Turkey and the Sesia Lanzo zone of the Western Alps where ophiolite and glaucophane schists occur together, it has been shown that the ophiolite was emplaced prior to the onset of blueschist metamorphism and nappe formation (Nicolas, 1967; Van der Kaaden, 1970). Andesitic volcanism, the appearance of which is considered to mark the development of a subduction zone and initiation of destruction of oceanic crust beneath an island arc, also makes its appearance in the Dinarides (Upper Cretaceous-Miocene) much later than the emplacement (Jurassic) of ophiolite. Similarly, in the Appalachians, calc-alkaline volcanism was initiated later than the emplacement of ophiolite, and continued until late Middle Ordovician time. It therefore seems unlikely that ophiolite emplacement marks subduction zone activity as is potentially represented by the serpentine and eclogite bearing Franciscan mélange of California, or continental collision marked by orogenic events late during the tectonic cycle. (It should perhaps be stated that it is not entirely clear whether the ophiolite components in the Franciscan mélange are really primary trench material derived from oceanic lithosphere being subducted in the immediate vicinity of the trench as in the Dewey and Bird 1970 interpretation - or parts of an olistostrome composed of material derived from an easterly terrain of older ophiolite and blueschist metamorphic rocks (cf. Hsu, 1971).)

In the Mediterranean Alpine system, ophiolites preserved relatively near to their sites of primary emplacement may be present on the Isle of Elba and in the Sesia Lanzo zone of the Western Alps (Nicolas, 1967). In the Circum-Pacific region, ophiolites preserved in their positions of primary emplacement overlying blueschist metamorphic rocks occur in Papua (Davies, 1968; Coleman, 1971, p. 1216) and New Caledonia (Routhier,

1953, fig. 22; Avias, 1967; Guillon, 1969). It is probable that the CircumPacific ophiolites represent overthrust sheets of 'cold' oceanic lithosphere derived from an adjacent major ocean basin (Pacific). However ophiolites of the intrasialic Alpine and Appalachian systems generally have, where preserved, high-temperature basal contact aureoles, and the origin of ophiolite as overthrust plates of 'cold' oceanic lithosphere emplaced during the closing of a major ocean basin is therefore not entirely satisfactory.

Significance of the basal contact aureoles of ophiolites

The high-temperature, yet narrow, contact aureoles of ophiolites record their primary emplacement history. The contact aureoles indicate that the ophiolites were emplaced as high-temperature solids, the narrowness of the aureoles precluding their intrusion as liquids. In places the contact minerals have undergone granulation and serpentinization, and their formation is therefore independent of any process involving the formation of serpentine. The two most viable explanations for the formation of the aureoles are:
(1) the aureoles formed as a result of frictional heating produced during overthrusting of oceanic lithosphere (or underthrusting of a continental plate).
(2) the heat for the metamorphism is inherent, the ophiolites having been emplaced relatively soon after their formation at the oceanic ridge. This may have been accomplished either by the ridge having migrated into a position marginal to the continental plate during a phase of ocean closing, or, by the ridge having originated within a continental sialic plate such that 'hot' ophiolite sheets were emplaced directly onto the continental margins during an early stage in the formation of an ocean basin. Evaluation of these hypotheses is at an early stage and requires further reasearch both in the field and laboratory, and theoretical evaluation of the frictional heating hypothesis.

Models for the origin of Appalachian ophiolites

With regard to the specific mode of formation and emplacement of the Appalachian ophiolites a number of alternatives can be considered:
(1) The ophiolites are the dissected remains of a large single sheet which, during the early Ordovician, following the deformation of the marginal clastic wedge represented by the Fleur de Lys, Caldwell and Chain Lakes metamorphic complexes, covered a large part of the Appalachians between Newfoundland and Vermont, and possibly farther south (Stevens, Church, and St. Julien, 1969).
(a) the ophiolites were emplaced as a result of underthrusting of continental margin and adjacent oceanic crust beneath oceanic lithosphere during the closing of a Cambrian oceanic basin along a southeasterly (present geographic co-ordinates) dipping subduction zone. The source area of the ophiolites is now delineated by the Lukes Arm or Dildo fault zones, and the contact aureoles were formed as a result of frictional heating during thrusting. The Ordovician calc-alkaline volcanic activity of the Burlington Peninsula-Notre Dame Bay region of Newfoundland, New Brunswick (Tetagouche volcanic rocks), Maine and Vermont, is related to subduction of oceanic crust beneath oceanic lithosphere now represented by the ophiolites.
(b) the ophiolites of western Newfoundland (Bay of Islands-Hare Bay) were emplaced during the formation of an early Ordovician ocean basin. The contact aureoles were formed as a result of the migration of hot peridotite and gabbro from an oceanproducing ridge directly onto the continental margin. The Baie Verte and Betts Cove ophiolites (also the Ballantrae ophiolite of Scotland) may have been emplaced in a similar manner, or alternatively, emplaced as 'cold' oceanic crust at a slightly later date. In the latter case the emplacement could be related to the development of a southeasterly dipping subduction zone which brought Arenig
age oceanic lithosphere over previously emplaced Tremadocian oceanic rocks now represented by the allochthonous ophiolites of the Bay of Islands. Ordovician calc-alkaline volcanism of the Appalachian eugeosyncline is related to this event.
(2) The ophiolites of the Bay of Islands Hare Bay, Baie Verte-Eastern Townships, and Betts Cove-Chain Lakes belts represent independent small ocean basins formed within a distending sialic plate.
(a) all three ophiolite belts were formed and emplaced during a phase of early Ordovician ocean formation.
(b) the ophiolites of western Newfoundland (Bay of Islands-Hare Bay) were emplaced as "hot' oceanic lithosphere at the time of formation of an early Ordovician small ocean basin of Japan Sea-type within the Fleur de Lys metamorphic complex, now delineated by the White Bay fault zone, during the closing of a major Cambrian ocean basin east of the Fleur de Lys as in case (1a).

## Early history of the Appalachian geosyncline

The distribution on both sides of the Appalachian-Caledonide orogen of rock types which uniquely characterize certain periods of the Proterozoic and early Phanerozoic of the North Atlantic region (Figure 3) clearly indicates that the Appalachian system was initiated on a Precambrian sialic basement. This view is supported by the proven existence of Precambrian basement beneath thick late Proterozoic-Cambrian clastic sequences in the Appalachians and the British and Norwegian Caledonides. The clastics were probably deposited in several faultbounded linear troughs or rifts. Evidence of rapid distension of the basement is provided by the existence of a latest Proterozoic-early Cambrian mafic dyke swarm within the Precambrian of the Long Range Peninsula of western Newfoundland (Williams and Stevens, 1969). (This event may correlate with the late Proterozoic-Cambrian Pan African and Cadomian orogenies of Africa and Western Europe.) However, the recent discovery of late Cambrian? (post-Fleur
de Lys Supergroup-pre-Ordovician) peralkaline granite and subalkalicperalkaline volcanic rocks in the Burlington Peninsula (Cockburn, 1971) and the distribution of peralkaline granites in the North Atlantic region (Figure 3) suggest that rifting of the continent had, by late Cambrian times, not exceeded a stage represented at the present time by the Red Sea rift. The existence of similar age (c. $500 \mathrm{~m} . y$. ) peralkaline silicic rocks in the vicinity of the East African-Middle East rift system also suggests that Cambrian crustal distension and development of a system of major crustal fractures was not a local phenomenon but may have reflected a major though largely abortive attempt at continental fragmentation. This view is supported by the apparent absence of oceanic lithosphere in the form of ophiolite from the southern Appalachians, implying that distension of continental crust in this region was of limited magnitude. Oceanic lithosphere may therefore have been developed only in the northern Appalachians, and the first appearance of recognizable oceanic crust may not have taken place until early Ordovician (Tremadocian) time (Bay of Islands Ophiolite). Whether the ophiolites were emplaced directly onto the margin of the basin of deposition, as is suggested by the existence of contact aureoles welded onto the base of the ophiolites, or were emplaced significantly later than their formation at an oceanic ridge, or whether both types of ophiolite exist (hypothesis 1b) is not at present resolved. However, the continuity of sedimentation throughout the Ordovician, and even into the Silurian in the region south of the Lukes Arm fault (cf. Kay, 1969) can only be explained by assuming that the 'North American' (Long Range - Fleur de Lys) plate was subducted beneath the ophiolites (that is, the continental plate underthrusts the oceanic crust) rather than vice versa as in the Bird and Dewey 1969 model in which the Newfoundland ophiolites are not interpreted as oceanic lithosphere.

## Conclusions

The stratiform ultramafic-mafic complexes of the northern Appalachians may


Figure 3. Sketch map showing the pre-Mesozoic distribution in the North Atlantic of various rock rypes which characterize the early and middle Proterozoic, and the late Proterozoic-early Phanerozoic, relative to the proposed line of closure of the intrasialic early Ordovician 'Proto-Atlantic Ocean' of the Appalachian-Caledonide gyetom- Distribution of anorthosite after Herz. (1969).
represent not only the oldest but pos sibly the only true alpine-type ophiolites in eastern North America. The apparent absence of ophiolites in North American Precambrian orogens such as the presently intra-continental circumSuperior Province fold belts (Penokean Labrador Trough - Cape Smith - Belcher Island - Setting Lake - Moak Lake) should also be taken into consideration in any attempt to apply plate tectonic theory to the Precambrian (cf. Church, 1971; Gibb and Walcott, 1971).

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# paleomagnetism and the kinematic history of mafic and ultramafic rocks in fold mountain belts 

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#### Abstract

Mafic and ultramafic rocks commonly occur in orogenic belts, and some can be regarded as remnants of oceanic lithosphere trapped in a subduction zone at the edge of oceanic plate. If this is so, then the opposing plate edges must have moved towards one another. The initial (pre-movement) positions of the plate margins can be calculated if there are paleomagnetic results from both margins pertaining to at least two different periods (different field configurations) prior to the movements. Only a few paleomagnetic results relevant to Canadian ultramafic complexes are available. However, the kinematic framework of most Phanerozoic examples could be studied using existing paleomagnetic techniques, and, as an illustration, results from the Pacific Ocean and the Pacific rim of North America are described. These results do not yet meet the full technical requirements, so accurate reconstructions cannot be made, but nevertheless they indicate that since the Triassic the crust of the Pacific Ocean and the western margin of the Cordillera were displaced northwards by several thousand kilometres relative to the main body of North America, and hence that the ultramafic rocks of the Cordillera could be fragments of intervening oceanic lithosphere driven into the continent from the south. Data are insufficient for comparisons relevant to Canadian ultramafic complexes older than late Paleozoic to be made, but a review of the problems allows two conclusions to be made. The first is that the problem of determining the kinematic framework of the Appalachian ophiolites is experimentally accessible and could be readily obtained; such a study could be a test case of the hypothesis of plate tectonics for the Lower Paleozoic. The second conclusion is that in order to determine the kinematic framework of Precambrian occurrences it will almost certainly be necessary to make general use of late orogenic secondary magnetization.


## Introduction

The purpose of this paper is to discuss the ways in which paleomagnetism may be used to determine the kinematic framework of some ultramafic and mafic rocks with particular reference to Canadian occurrences (see Frontispiece).

In the application of the hypothesis of plate tectonics to orogenic belts many mafic and ultramafic complexes (particularly those that have associated submarine extrusive rocks) have been interpreted as fragments of ridge-generated oceanic lithosphere which have been trapped in an orogen as an oceanic lithospheric plate passes down a subduction zone into the mantle (for example Temple and Zimmerman 1969; Moores, 1970; Dewey and Bird, 1970). If this hypothesis is accepted, then the
under-riding plate must have moved a great distance relative to the over-riding plate. Therefore, a necessary condition for this tectonic interpretation of such mafic and ultramafic occurrences, is that paleomagnetic directions from rocks which predate the period of movement should show large differences between plates. Discrepancies (expressed as differences between paleomagnetic poles) of $30^{\circ}$ to $90^{\circ}$ have been observed between either side of Tethys in late Paleozoic and Mesozoic sequences on the present-day fragments of Gondwanaland and Laurasia, so that for the Alpine ophiolites this condition is fulfilled. However, before plate tectonics can be applied with any confidence to the interpretation of preAlpine mafic and ultramafic rocks there is a need for similar quantitative evidence,
independent of the hypothesis itself, of motions between opposed plates of lithosphere. The geometrical and magnetic requirements are given first, followed by a discussion of how paleomagnetism may be applied to the ultramafic occurrence within the orogenic belts of Canada.

Two hypothetical ways in which oceanic lithosphere may be emplaced into orogenic belts are shown in Figure 1. On the left (after Moores, 1970) the subduction zone dips away from the continent Y . The continent is buoyant and cannot descend, so movement ceases and a further cycle of sinking commences at another site. Fragments of oceanic crust (X) together with deformed sediments become part of continent $Y$. On the right the subduction zone dips under the continent $C$, and oceanic lithosphere becomes incorporated into the trench and later into the continent perhaps as huge slivers as Dewey and Bird (1970) have shown in their diagrams. Similar displacements between opposed plates could occur in both models, but the displacement between trapped oceanic lithosphere and continent depends on the direction of dip of the subduction zone, and the method of incorporation of oceanic material into the continental margins. In principle, this feature could be a means of determining the direction of dip of subduction zones.

Should no paleomagnetic discrepancies be observed, then plate models requiring large displacements can be discounted. However, if discrepancies are found, then the past arrangement of


Figure 1. Models for the emplacement of oceanic crust within a continent. On the left (modified after Moores, 1970) the down-going plate dips away from the continent ( $Y$ ). The continent is prevented from descending by its buoyancy, and oceanic crust ( $X$ ) may become incorporated in the marginal zone. On the right the down-going plate dips beneath the continent $(\mathrm{C})$ and oceanic crust from it is incorporated into the inner wall of the trench, and eventually becomes incorporated into new continental crust.
plates needs to be determined. In order to do this it is necessary to obtain from each plate, paleomagnetic poles which can be referred to at least two different field configurations prior to the period of movement. Suppose that we wish to determine the relative movement of localities $R$ and $S$ (Figure 2) from which paleomagnetic poles A to D have been obtained (A and C from S, and B and D from $R$ ) then the movement of $S$ relative to $R$ (which is assumed fixed) is described by a rotation about a point (called a pivot point) on the earth's surface. Thus the technical problem in paleogeographic reconstructions is to determine the pivot points and rotations appropriate to each plate (Runcorn, 1956). If only one pair of contemporaneous poles are known (say only A and B) then the pivot point lies anywhere on a line PX equidistant from $A$ and $B$, but it is determined uniquely by the intersection of a second line PY defined by a second pair of poles (C and D) assigned to a later field configuration, provided the observing localities ( R and S ) have not moved relative to one another between the two
periods of time. Once the pivot point is determined, the angle (SPS') through which $S$ must be rotated to bring the poles into agreement can be calculated, and the position ( $\mathrm{S}^{\prime}$ ) prior to movement determined.

Paleomagnetic evidence can be obtained in either of two ways. The first and usual way is to study the directions at primary magnetization (magnetization acquired when the rock was formed) of undeformed, chemically unaltered rocks which lie superficially on the earth's crust. This method is generally applicable to the study of the tectonic framework of ultramafic and mafic occurrences in Phanerozoic fold mountain belts, because it is commonly possible to obtain the primary magnetization of late Procambrian and younger rocks; but this is probably not so for most Archean rocks whose presently detectable magnetization was acquired long after formation. If their magnetization (secondary magnetization) was acquired during cooling (say by uplift after a period of deep burial) then it will be a type of thermoremanent magnetization. If it was acquired during
recrystallization of the iron minerals at temperatures below the Curie temperature, then it will be a chemical remnant magnetization. The age of such secondary magnetization probably corresponds, to a first approximation, to the apparent K-Ar age reset at the time regional heating ceased. In the Phanerozoic many examples of primary magnetization being replaced by stable secondary magnetiration during some identifiable later regional process are known. For example, the Silurian Bloomsburg formation in the Valley and Ridge Province of the Appalachians has a strong stable secondary magnetization acquired at the close of the Appalachian orogeny (late Carboniferous or Permian) presumably as a result of cooling during uplift following a time of deep burial and regional heating (Roy et al, 1968). Thus the only source of paleomagnetic information in very old altered rocks is stable secondary magnetization of known age; instead of applying the usual paleomagnetic method of studying the primary magnetization of unaltered superficial rocks, it will be necessary, in order to determine the


Figure 2. Geometrical requirements for determining past relative position of two sampling localities $R$ and $S$. Poles $A$ and $C$ are observed from $S$, and $B$ and $D$ from $R$. The poles $A, B$ refer to the same time period (field configuration). The poles C,D also refer to the same field configuration as each other but different from that of $A, B$. In order to bring $B$ and $D$ into agreement with $A$ and C locality S is rotated about a pivot point P by and angle $\mathrm{SPS}^{\prime}$. The past position of $\mathbf{S}^{\prime}$ relative to $\mathbf{R}$ is then fixed uniquely. For convenience $\mathbf{P}$ is taken to be at the centre.
tectonic history of ultramafic rocks in Precambrian orogenic belts, to study the stable secondary magnetization acquired during uplift or metamorphism of basement complexes.

The paleomagnetic requirements for determining the kinematic history of preAlpine mafic and ultramafic orogenic complexes may now be summarized: (1) remnant magnetization directions of known age from both margins of an orogen, and, if possible, from supposed remnants of oceanic lithosphere within it, and (2) sufficient data to furnish at least two pole pairs pertaining to two different field configurations prior to the movements.

Through lack of study, the paleomagnetic data do not yet fully satisfy these requirements for any Canadian examples. The youngest ultramafic rocks (late Paleozoic and early Mesozoic) in Canada are in the Cordillera (localities 1 to 9 of the Frontispiece) and the following discussion is concerned mainly with paleomagnetic data from the Pacific rim of North America which is relevant to them. However, in the long term, the main challenge will be the study of the kinematic history of older ultramafic and mafic rocks, particularly those of the Canadian Shield, because they are economically so important, and because they span such an enormous length of time, and hence provide an excellent opportunity for the application of plate tectonics to the remote history of the earth. Therefore, although the data relevant to them
are few, a discussion is also given of how paleomagnetism may be applied to older examples.

## Previous work from the Pacific Ocean and the Pacific Rim of North America

Magnetic surveys of Cretaceous seamounts from a wide area of the Pacific have given paleomagnetic poles near northern Europe with a mean at $016 \mathrm{E}, 61 \mathrm{~N}$ (error $(P=0.05)=8^{\circ}$; Francheteau et al, 1970). The seamounts typically have declinations near zero or $180^{\circ}$, and inclinations that are consistent with a position south of their present position. The good agreement among seamount poles and the presence of reversals indicates that the magnetization is stable. The mean Cretaceous pole for the main body of North America is at $176 \mathrm{~W}, 69 \mathrm{~N}$ (error $(P=0.05)=3^{\circ}$ ), and differs from the Pacific seamount poles by $49^{\circ}$.

Paleomagnetic studies of the Pacific rim of mainland North America began with the work of Cox (1957) on the Siletz River Volcanic Series of Oregon (locality $S$ of Figure 3), which is of Eocene age. These rocks have easterly declinations with a pole in the Atlantic (mean direction 070, +55 ; error $(P=0.5)$ $=7^{\circ}$; pole $050 \mathrm{~W}, 37 \mathrm{~N}$ ). Cox studied samples from eight sites spaced over a distance of about 60 km and a stratigraphic thickness of about 1000 m . The original attitude of each flow was determined from bedding in associated sediments, and thermal demagnetization
studies and the application of Graham's bedding tilt test (Graham, 1949) showed the magnetization to be stable.

Some years later, results were reported by Grommé and Gluskotter (1965) from three large bodies of pillow basalt and diabase in the Franciscan Formation (late Jurassic to late Cretaceous; locality $F_{1}$ of Figure 3). These bodies were sampled over a distance of about 20 km just north of San Francisco. Directions were obtained (mean 078,+47 based on seven collecting localities; error $(P=0.05)=14^{\circ}$; pole $\left.050 \mathrm{~W}, 26 \mathrm{~N}\right)$ with large easterly declinations, strongly discordant with results from rocks of comparable age from North America (Table 1). The original attitudes of the beds were determined from the shape of the lava pillows. The stability of magnetization was established by demagnetization studies.

More recently Saad (1969) has studied Franciscan ultramafic rocks from Red Mountain to the southeast of San Francisco. He found three distinct groups of directions. Saad's group 3 (mean direction $090,+11$; error $(P=0.05)=$ $27^{\circ}$; pole $036 \mathrm{~W}, 03 \mathrm{~N}$ ) which he considers to have been acquired "during or immediately after emplacement", gave a pole in the Atlantic, not far from that just described from Franciscan pillow basalt and diabase. Saad's group 2 directions (mean $350,+75$; error $(P=0.05)=6^{\circ}$; pole $132 \mathrm{~W}, 66 \mathrm{~N}$ ) occurred in dunite "emplaced and magnetized at a much later time". They gave a pole in Alaska in good


Figure 3. Paleomagnetic sampling localities from the Mesozoic and Paleogene of North America. Localities giving concordant results for the same geological period are indicated by stars and labelled LT (Paleogene), K (Cretaceous), J (Jurassic) and TR (Triassic). Localities giving discordant results (Table I) are indicated by arrows.

Table I
Differences between poles from the Pacific rim and the main body of North America

|  |  | Rock Unit |
| :--- | :--- | :---: |
| S | Siletz volcanics (Eocene) | $\Delta^{\circ}$ |
| F $_{1}$ | Franciscan spilites and diabase <br> (Upper Jurassic or Cretaceous) | 57 |
| $\mathbf{F}_{2}$ | Franciscan ultramafics <br> (Upper Jurassic or Cretaceous) | 89,84 |
| K | Karmutsen (Upper Triassic) | 55 |

$\Delta$ is the difference in degrees between the corresponding poles for the rock unit and that for stable North America. The error associated with these values is about $10^{\circ}$, on average, and never exceeds $20^{\circ}$. In entries $F_{1}$ and $F_{2}$ two values are given, which refer to Jurassic and Creataceous poles respectively. The results in $F_{2}$ refer to Saad's group 3.
agreement with Cretaceous poles from elsewhere in North America. Saad's group 1 directions occurred in the main peridotite body (mean 045, +59 ; error $(P=$ $0.05)=4^{\circ}$; pole $050 \mathrm{~W}, 56 \mathrm{~N}$ ). They gave a pole intermediate between those for groups 3 and 2. Saad considered the group 1 directions to have been acquired after the magnetization of group 3. The Red Hill intrusion is thought to have the form of a sill or laccolith folded into a syncline; original attitudes were calculated by Saad from the regional geology by an interpolation technique. The method seems to be justified in that after correction the directions within each group are, with few exceptions, in good agreement.

## New results from Vancouver Island

The Karmutsen Volcanic Group (locality $K$ of Figure 3) of Vancouver Island comprises over 4000 m of mainly basaltic and andesitic flows (some pillowed), diabase sills, pyroclastic recks; and sediments. Upper Triassic fossils (late Karnian, Tozer, 1967) occur in the upper part. The sequence is intruded by Jurassic and younger granitic plutons. The Karmutsen has been sampled in the Buttle Lake area $\left(125.6^{\circ} \mathrm{W}, 49.7^{\circ} \mathrm{N}\right)$ at 11 sites, (three in diabase ( D specimens) and eight from lavas (L specimens)) spanning much of the exposed thickness.

Reliable "bedding" attitudes are not easily obtained at the sampling sites, because of the massive nature of most flows and diabases, the abundance of minor faults and joints, and the absence of easily recognizable interlava sediments. At those sites where structural attitudes could not be gained from local sedimentary bedding, pillow lava configurations or flow boundaries, local attitudes were interpolated from regional geological maps.

The magnetization directions after thermal and alternating field (a.f.) cleaning are plotted in Figure 4. There are two distinct sets. The first set (group $A$ comprising most samples), even after cleaning, shows high within-site dispersion, all except one site having Fisher (Fisher, 1953) precision indices ( $k$ ) less than 3. The site mean directions are also poorly grouped ( $k=12$ ). The overall mean


Figure 4. Directions of remanent magnetization in the Karmutsen samples after magnetic cleaning at 150 oersted and thermal cleaning (TH) at $500^{\circ} \mathrm{C}$. On the left, means of eight sites (group $A$ ) are given, the primitive being the horizontal plane. On the right, all the specimen directions of group $B$ are given, the primitive being the east-west meridian plane. These differing plotting conventions are adopted to avoid interference between directions on the upper and lower hemispheres. The means and error circles are indicated by stars. The squares labelled TR, J, K, and F are the expected Triassic, Jurassic, Cretaceous and present field directions.
direction with respect to present horizontal $\left(337,+77\right.$; error $\left.(P=0.05)=17^{\circ}\right)$ does not differ significantly from the expected Jurassic and Cretaceous fields; and is only marginally different from the present field. The stability of group $A$ is generally very low. The a.f. demagnetization curves fall rapidly and directional stability is poor (Specimen L of Figure 5). The mean coercivity (the a.f. required to reduce the n.r.m. intensity by one half) is 60 oersted, which is very low. The blocking temperatures are also low, the decay under thermal demagnetization being rapid and sometimes erratic (Specimens LA and D2 of Figure 6).

The second group of directions (group $B$ ) have negative (upward) inclination. The agreement among samples from the same site is good, the mean withinsite Fisher precision being 64. The magnetizations are stable, and the mean coercivity is 190 oersted. Under a.f.
demagnetization the directions are generally little changed up to 400 oersted (Specimen D3 of Figure 5). The blocking temperatures are high (mostly above $500^{\circ} \mathrm{C}$ ), and the thermal decay curves are square-shouldered and typical of finegrained magnetite (Specimens L6 and D3 of Figure 6). A further characteristic which distinguishes these two sets is that whereas in $B$ the demagnetization curves of anhysteretic remanent magnetization (a.r.m.) and n.r.m. are similar, as is found in recent stably magnetized pillow basalts, in group $A$ the two are grossly different (Figure 6) indicating that any original magnetization has been lost (Park and Irving, 1970).

Polished sections of all samples have been studied. The high coercivity, high blocking temperature rocks of group $B$ contains iron mineral grains (skeletal in lava L6) commonly ranging in size up to
$60 \mu \mathrm{~m}$. They contain well-developed very fine intergrowths of magnetite and ilmenite whose thicknesses range down from $5 \mu \mathrm{~m}$ to below the limit of resolution $(1 \mu \mathrm{~m})$. The low coercivity, low blocking temperature lavas of group $A$ contain grains (commonly skeletal) ranging up to $60 \mu \mathrm{~m}$ in which there are no visible intergrowths. These grains contain irregular widely-spaced ( $10 \mu \mathrm{~m}$ spacing is characteristic) cracks, and have granular surfaces and corroded margins. The dolerite of group $A$ (D2) contains very large (100 to $1000 \mu \mathrm{~m})$ grains, with intergrowths of ilmenite and magnetite whose thicknesses usually exceed $10 \mu \mathrm{~m}$. Thus, the effective grain size of the magnetic minerals of group $A$ rocks is generally in excess of $10 \mu \mathrm{~m}$, whereas that of group $B$ rocks is less, commonly very much less, than $5 \mu \mathrm{~m}$. The stability of magnetization of iron minerals depends on grain size, and it seems clear that the unstable


Figure 5. Stability (a.f.) of the Karmutsen groups $A$ and $B$. Above, the variation in directions, and below, the decay of intensity, versus strength of alternating field (in oersted peak values). Circles (D3) denote negative (upward) inclinations, and dots (LI) positive inclinations. The numbers in the top diagram denote the field strengths in hundreds of oersted. The contrast between the very rapid decay and wide scatter of the unstable $A$ group specimen, and the slow decay and small scatter of the stable $B$ group specimen are clearly shown.


Figure 6. Above is shown the thermal stability of the Karmutsen groups $A$ and $B$. L6 and D3 belonging to group (B) and D2 and L4 to group A. Open circles denote the point at which all the original magnetization has been destroyed and the directions become random. Below, the different rates of decay versus alternating magnetic fields for two of these specimens are shown, together with the comparison of the decay of a.r.m.
magnetization of group $A$ is due to the large effective grain size. Although the group A magnetizations are generally scattered, they are, on average, directed along a late Mesozoic field (Figure 4), and it seems reasonable to suppose that they were acquired at the time of granite intrusion in the Jurassic when there may have been mild regional heating. The high stability of the Group $B$ magnetizations is presumably due to the presence of very fine-grained intergrowths of magnetite. The intergrowth textures are original cooling textures, and hence the group $B$ magnetization was probably acquired at the time of formation and is indicative of the field in the Upper Triassic. The mean direction of group $B$ with respect to bedding is $354,-35$ (error ( $\boldsymbol{P}=0.05$ ) $=$ $19^{\circ}$ ) and the corresponding pole is at $061 \mathrm{E}, 21 \mathrm{~N}$. The error is large because the number of sites (three) is small, but the mean is significantly different from the expected Triassic field (Figure 4, Table I). Dips average about $20^{\circ}$ to the north over the sampling area.

## Discussion of results relevant to the Cordillera

The results from the Pacific seamounts indicate that the latitude of the Pacific plate has increased by about $30^{\circ}$ since the Cretaceous whereas the results from the main body of North America indicate, if anything, a decrease in latitude since that time; that is, the Pacific plate has moved northwards with respect to the North America plate by about $3,000 \mathrm{~km}$. Their relative longitudinal movement cannot yet be calculated.

Of the results from the Pacific rim of North America, only those from the Siletz volcanics are straightforward, presumably because they are the youngest rocks and have been the least subject to secondary changes. The discrepancy between the results from Oregon and those of Torreson et al. (1949) from Eocene sediments in Colorado, can be accounted for by assuming a clockwise rotation of the Siletz region by $70^{\circ}$ relative to the main body of North America (Irving, 1959), a rotation which is similar to that suggested by Carey (Carey, 1958; Ivring, 1964, fig. 10.4) on geological grounds.

In order to explain the discordance between their results from Franciscan mafic rocks and those of comparable age from other parts of the continent, Grommé and Gluskotter listed three possible causes: (1) a clockwise rotation of the entire rock unit by about $70^{\circ}$, (2) the occurrence at that time (late Jurassic or early Cretaceous) of a predominantly non-dipole field, and (3) a temporary excursion of the pole of the dipole field, from its customary late Mesozoic position near the Bering Strait, into the central Atlantic. When discussing his own more complicated results Saad (1969) favoured the latter explanation. He argued that his discordant group 3 directions were acquired at about the time of emplacement during a polar excursion, that his group 2 directions were acquired later when the pole was in its usual position, and that his intermediate group 1 directions were acquired while the pole was in the process of moving. However, Saad's observations are also consistent with the first hypothesis of Grommé and Gluskotter; that the Franciscan region has been rotated clockwise by about $70^{\circ}$. On this view his group 3 directions (since they were acquired at about the time of emplacement) are the only reliable data, and the group 1 and 2 directions, which Saad acknowledges to be secondary and due to a high degree of serpentinization, were acquired during or after rotation.

Similar arguments apply to the Karmutsen results. Those directions that are stable and paleomagnetically reliable are strongly discordant with Triassic data from the rest of North America, whereas those directions that are generally unstable are concordant with later fields. Again it can be argued, either that the stable magnetizations represent a true tectonic discordance, or that they reflect an aberrant field. Although the latter possibility cannot be disproved, it seems to us that the tectonic hypothesis is the more reasonable.

In the four instances from the Pacific rim of North America, representing at least three independent points in time, in which there is evidence that the magnetization was acquired at the time of formation, large significant discordances
in direction are found, whereas in the two instances (Saad's group 1 and Karmutsen group $A$ ) in which the magnetization is of unstable type, the directions have a configuration appropriate to a younger field and are probably secondary. Furthermore, all four localities show major discordances, whereas none of the 18 Mesozoic and Lower Tertiary units from elsewhere in North America show them; for example, the Cretaceous poles observed at localities spaced from the Sierra Nevada to the eastern and northern coasts of the continent are in excellent agreement (Larochelle, 1968).

The paleomagnetic evidence therefore suggests that the Pacific plate was displaced southward with respect to the North America plate, so that the zone of mafic and ultramafic rocks in the Cordillera (Figure 1) could be parts of oceanic crust trapped in the subduction zone between them. The details of the displacements will not become clear until very much more data are available. However, it is notable that the discrepancies are of two types. The Siletz and Franciscan discrepancies are largely (but not entirely) in declination, so that they can be explained, to a first approximation, by a clockwise twist (rotation about a pivot point near their present location). The discrepancy in Pacific seamounts and in the Karmutsen rocks, however, is largely in inclination, implying a large displacement of several thousand kilometres relative to North America without any gross twist.

The Triassic latitude expected for Vancouver Island from the paleomagnetic data from the main body of North America is 27 N , whereas that calculated from the Karmutsen result is 19S, estimates which could be in error by $15^{\circ}$. The implied northward movement of Vancouver Island is consistent with the occurrence, between the Western and Eastern Cordiflera, of large post-Triassic faults (the Tintina Trench for example) on which right-lateral transcurrent movements have occurred (Roddick, 1967). Also Tozer (1970) has suggested on faunal grounds "that the warm-water Triassic deposits of the Western Cordillera were originally deposited south of the
latitude of the contemporaneous rocks in the Eastern Cordillera". Presumably it was this motion, which in Vancouver Island was terminated by the Nassian orogeny (and therefore occurred within the Jurassic), which realtes to the emplacement of ultrabasic rocks in the Canadian Cordillera. The general northward movement of the Pacific plate relative to the main body of North America continued (Vancouver Island now being part of the North American plate) through the Cretaceous and Tertiary to the present, as the paleomagnetic poles from the Pacific seamounts and as the dextral strike slip motion on the San Andreas and Queen Charlotte Island faults show. Assuming the Jurassic to be of $40 \mathrm{~m} . \mathrm{y}$. duration, the relative velocity (northsouth component) prior to the Nassian orogeny is of the order 10 $\mathrm{cm} / \mathrm{yr}$, which is comparable to that occurring beneath modern ocean trenches.

## Appalachian occurrences

If plate tectonic models for the emplacement of Appalachian ophiolites (sites 20 to 26 of the Frontispiece) are correct, then there should be large paleomagnetic discrepancies among the bordering cratons. The opening of the Atlantic during the Mesozoic did not occur exactly along the line of the Caledonian geosyncline so that the comparisons of late Proterozoic results can be made in three ways: (1) within Canada, by comparing results from the Avalon peninsula and the Canadian Shield, (2) within Europe, by comparing results from the Lewisian platform and the Baltic Shield, and (3) by comparing results from the Canadian and Baltic Shields after restoration to their late Paleozoic positions. Should all comparisons show agreement (disagreement) between their late Proterozoic polar paths, then the Caledonian geosyncline was not (was) the site of a wide ocean. Of all the tests applicable (in part) to Canadian terrain this one regarding the emplacement of the Appalachian ophiolites is experimentally the most accessible, because suitable late Proterozoic rocks occur on all six crustal elements, and because the paleomagnetic directions that
have been observed from them are roughly perpendicular to the trend of the orogen, which is geometrically the optimum configuration for measuring crustal movements. The first two comparisons are particularly powerful, since they involve no assumptions about postCaledonian movements.

## Franklinian occurrences

There are ultrabasics in northern Ellesmere Island (see Irvine and Findlay this volume) associated with Ordovician rocks folded during the Devonian. If these are remnants of Lower Paleozoic oceanic crust then a literal interpretation in terms of plate tectonics would imply that the Franklinian geosyncline was once a wide ocean. The problem may be stated in another way: do the Precambrian rocks which outcrop in northwestern Ellesmere Island represent the re-emergence (from beneath the Franklinian geosyncline) of a northern prolongation of the Canadian Shield, or are they an exotic remnant of continental crust which was formerly displaced by many thousands of kilometres from the Canadian Shield? The problem could be studied by obtaining paleomagnetic observations from northwestern Ellesmere Island and comparing them with results from the Canadian Shield. The task will be a difficult one technically, because the rocks are altered and stable secondary magnetizations will have to be sought.

## Precambrian occurrences

A useful starting point for the discussion of the kinematic history of the Canadian Shield is to consider the question of the origin of the Churchill Province. The Churchill Province consists of a series of Aphebian (earliest Proterozoic) geosynclines containing Archean fragments (McGlynn, 1970, fig. 14). These could have been the sites of a successive series of subduction zones (Gibb and Walcott, 1970) which during Aphebian time consumed oceanic lithosphere, so narrowing the wide ocean that formerly separated the Archean Superior and Slave Provinces and the Superior and eastern Nain Provinces. As the oceans contracted, and as the Slave and Nain continental
cratons neared the subduction zone peripheral to the Superior craton, buoyancy would prevent their descent, and the resulting continental collision closed the ocean, caused the Hudsonian orogeny ( $1800 \mathrm{~m} . \mathrm{y}$ ), sealed the intervening rocks into what is now the Churchill Province, and terminated the Aphebian Era. Those parts of the Chruchill Province peripheral to the Superior Province (Manitoba Nickel Belt, Fox River Region, Belcher Islands, Cape Smith Belt, Labrador Trough, see Frontispiece), contain mafic and ultramafic rocks with abundant pillow basalt, and it is these that suggest that former existence of a wide ocean between the Archean cratons. These rocks could once have been oceanic lithosphere, which sank beneath a deep ocean trench peripheral to the Superior craton and which became trapped during the Hudsonian orogeny, and sealed into the Canadian Shield.

Such reconstructions are interesting as speculations but have no firm foundation until quantitative estimates of the displacements have first been made. The problem therefore is to measure, paleomagnetically, the pre-Hudsonian relative positions of the Slave and Superior Provinces, of the eastern Nain and Superior Provinces, and of the Archean fragments within the Churchill Province. It may eventually be possible to obtain abundant data on pre-Hudsonian primary magnetization (particularly from late Archean intrusive rocks) but this will undoubtedly be a very difficult task because of the generally altered nature of such old rocks. Another experiment which may be performed on the geographical scale appropriate to the problem, is to study the general phenomenon in metamorphic terrain of secondary magnetization (of Kenoran age in particular) with a time scale provided by the apparent (reset) K-Ar ages. Before this idea can be exploited, basic research into the magnetic properties of metamorphic rocks is needed.

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# alpine-type peridotite with particular reference to the bay of islands igneous complex 

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#### Abstract

The characteristics of alpine-type peridotite are reviewed, and some comparisons are made with other kinds of olivine-rich ultramafic rocks. Information is summarized which indicates that such peridotite is rare, if present at all, in the Canadian Shield and only infrequently has associated Ni-sulphide deposits, In some occurrences the mineralogical and chemical relationships suggest that the rock at stage just prior to its final consolidation consisted of olivine, subordinate orthopyroxene, and minor chromite, in association with variable amounts of interstitial picritic liquid.

In the Bay of Islands Igneous Complex in western Newfoundland, alpine-type peridotite forms the floor of a rudely stratiform intrusion in which cumulate feldspathic ultramafic rocks and gabbro have precipitated from a K-poor, Ti-poor, tholeiite magma of low silica activity emplaced into basaltic roof rocks. However, the peridotite itself appears to have been through a partial melting process and to have solidified at considerably greater depths than the feldspathic rocks. It may therefore be residual mantle material. These features are consistent with current opinion that complexes of this type represent sections of oceanic crust and upper mantle.


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This paper reviews a large number of analytical data on various kinds of ultramafic rocks obtained in studies sponsored by the Geological Survey of Canada in the past 10 years (Tables 1-8). Appreciation is expressed to the Survey Laboratories that provided the data, with particular thanks going to J.A. Maxwell, S. Abbey, S. Courville, W.H. Champ, K.A. Church, D.A. Brown, and R.N. Delabio. Sources of infomation are indicated throughout the text, but special acknowledgment is given for data used from a thesis dissertation by W.J. Wolfe (1966). Chemical analyses illustrated for Mount Albert rocks are from samples collected by C.H. Smith and I.D. MacGregor. The Bay of Islands data were obtained by the second author; the review section of the paper was prepared by the first author. The manuscript was critically read by W.R.A. Baragar, O.R. Ekstrand, T.M. Gordon, H. Helmstaedt, G.B. Skippen and D.R.E. Whitmore, whose comments and suggestions have contributed substantially to its improvement. E. Froese also gave helpful consultation.

## Introduction

Although it is widely believed that the alpine-type peridotite of Phanerozoic orogenic belts was largely solid when emplaced in its exposed positions (Smith, 1958; Moores, 1969; Wyllie, 1970), opinions differ greatly as to its origin. Two interpretations have received most attention. One, advocated especially by Thayer (1964, 1967, 1969), is that the peridotite, together with associated chromitite, pyroxenite, and gabbro, formed by magmatic differentiation, at least in part by crystal settling in intrusions in the deep crust or upper mantle (see also Challis, 1965). The other, which has become increasingly popular along with the concept of plate tectonics, is that the peridotite is the depleted residue of more primitive mantle material from which basaltic and other materials have been removed by partial fusion (e.g. Hess, 1964; Green and Ringwood, 1967; Dickey, 1970; Dewey and Bird, 1970; Bonnatti, Honnorez and Ferrara, 1970). Despite their great difference, these possibilities are not easily distinguishable petrologically because they involve the
same kinds of crystal-liquid equilibria. In this paper, we first summarize several criteria that appear useful in making the distinction. This section serves also to introduce the terminology and certain of the concepts involved. The characteristics of alpine-type peridotite are then reviewed.

Finally we present and discuss data from the Bay of Islands Igneous Complex in western Newfoundland that appear relevant to the problem.

## Criteria for distinguishing products of fractional crystallization from residues of partial melting

The postulate that an ultramafic rock is an accumulation of mafic minerals settled from magma does not necessarily require that the minerals be formed by progressive fractional crystallization (they might, for example, have settled from a suspension), although this is likely if there has been appreciable differentiation. The evidence that some ultramafic rocks are products of fractional crystallization comes mainly from stratiform layered intrusions, like the Stillwater and Muskox intrusions, in which the rocks are precipitates from basaltic magmas. The evidence is principally of three types:
(1) Layering structures and textural features that show that the rocks consist of settled (cumulus) crystals cemented together by a later (post-cumulus) generation of materials crystallized from pore (intercumulus) magma (Hess, 1960; Wager, Brown and Wadsworth, 1960; Jackson, 1961; Irvine, 1965a).
(2) Layer sequences, such as peridotite-pyroxenite-gabbro, in which the succes-

TABLE 1. MAJOR CHEMICAL CONSTITUENTS IN ROCKS FROM
THE MOUNT ALBERT ULTRAMAFIC CUMPLEX.

| SAMPLE | FOOTAGE ROCK | SIO2 | AL203 | FE203 | WEIGHT PERCENT |  |  | NA2O | K20 | TI02 | P205 | MNO | NIO | CR203 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | FEO | MGO | CAO |  |  |  |  |  |  |  |
| 57- 8 | ALP PD | 38.7 | 3.2 | 0 | 8.6 | 37.0 | 1.7 | . 1 | 0 | .01 | 0 | . 15 | . 25 | . 28 |
| 57-17 | ALP PD | 35.6 | 2.5 | 0 | 7.7 | 37.8 | . 7 | . 1 | 0 | 0 | 0 | . 12 | - 32 | .23 |
| 57-25 | ALP PD | 36.6 | . 8 | 0 | 6.5 | 41.4 | . 2 | . 1 | 0 | 0 | 0 | .11 | . 29 | . 29 |
| 57-41 | ALP PD | 36.6 | 2.8 | 0 | 6.4 | 40.8 | - 4 | . 1 | 0 | 0 | 0 | . 11 | . 28 | . 42 |
| 57-44 | ALP PD | 35.4 | 3.8 | 0 | 6.8 | 41.1 | - 2 | -1 | 0 | 0 | 0 | .12 | . 29 | . 85 |
| 57-45 | ALP PD | 35.2 | 2.6 | 0 | 7.4 | 38.8 | - 3 | -1 | 0 | 0 | 0 | .15 | . 22 | . 58 |
| 57- 52 | ALP PD | 37.0 | 2.7 | 0 | 6.8 | 39.7 | - 3 | . 1 | 0 | 0 | 0 | .14 | . 32 | . 29 |
| 57-56 | ALP PU | 38.7 | 2.6 | 0 | 6.7 | 38.2 | . 4 | . 1 | 0 | 0 | 0 | .12 | . 24 | - 32 |
| 57- 57 | ALP PD | '39.5 | 3.3 | 0 | 7.7 | 35.2 | -8 | . 1 | 0 | 0 | 0 | .17 | . 29 | . 29 |
| 57-60 | ALP PD | 36.0 | 2.4 | 0 | 7.1 | 40.3 | . 4 | . 1 | 0 | 0 | 0 | . 14 | . 39 | . 23 |
| 57-91 | ALP PD | 40.0 | 2.6 | 0 | 7.4 | 38.9 | . 5 | . 1 | 0 | 0 | 0 | . 15 | . 33 | . 29 |
| 57-95 | OL. OPXN | 48.1 | 7.4 | 0 | 6.0 | 29.9 | 2.4 | . 1 | 0 | .42 | 0 | .16 | . 28 | . 84 |
| 57-105 | ALP PD | 39.7 | 4.0 | 0 | 7.6 | 36.1 | 1.5 | . 1 | 0 | . 01 | 0 | .15 | . 38 | . 32 |
| 57-117 | ALP PD | 39.4 | 4.0 | 0 | 7.9 | 38.4 | 1.6 | . 1 | 0 | . 01 | 0 | .15 | . 29 | - 36 |
| 57-118 | ALP PD | 41.0 | 3.5 | 0 | 7.5 | 36.3 | 1.8 | . 1 | 0 | . 01 | 0 | . 15 | . 31 | . 34 |
| 57-124 | ALP PU | 40.9 | 4.7 | 0 | 7.4 | 34.3 | 2.2 | . 1 | 0 | .01 | 0 | . 14 | . 34 | . 41 |
| 57-126 | ALP PD | 37.5 | 2.1 | 0 | 6.7 | 37.7 | .5 | . 1 | 0 | 0 | 0 | .11 | . 46 | . 23 |
| 57-131 | ALP PD | 40.1 | 3.5 | 0 | 7.6 | 34.8 | 1.7 | -1 | 0 | . 01 | 0 | .14 | . 28 | . 32 |
| 57-144 | ALP PD | 38.7 | 3.2 | 0 | 6.8 | 34.9 | . 7 | . 1 | 0 | 0 | 0 | . 13 | .46 | . 04 |
| 57-150 | ALP PD | 40.7 | 3.2 | 0 | 6.8 | 36.6 | 1.9 | . 1 | 0 | .01 | 0 | .12 | . 18 | . 04 |
| 57-165 | ALP PD | 39.5 | 3.1 | 0 | 7.6 | 37.0 | 1.0 | . 1 | 0 | 0 | 0 | .14 | . 23 | - 35 |
| 57-186 | ALP PD | 38.1 | 2.3 | 0 | 7.6 | 37.8 | . 7 | . 1 | 0 | 0 | 0 | .13 | . 32 | . 31 |
| 57-246 | ALP PD | 39.4 | 2.9 | 0 | 6.7 | 35.2 | . 9 | . 1 | 0 | 0 | 0 | . 12 | . 33 | . 50 |
| 57-26? | ALP PD | 38.6 | 2.1 | 0 | 5.1 | 36.2 | - 4 | -1 | 0 | 0 | 0 | . 08 | . 38 | - 29 |
| 57-268 | ALP PD | 33.7 | 2.3 | 0 | 6.4 | 39.9 | . 4 | . 1 | 0 | 0 | 0 | .10 | . 31 | - 35 |
| 57-269 | ALP PD | 34.8 | 2.8 | 0 | 7.4 | 38.7 | . 4 | . 1 | 0 | 0 | 0 | .12 | . 36 | .41 |
| 57-270 | ALP PD | 35.3 | 2.0 | 0 | 6.4 | 36.3 | . 4 | .1 | 0 | 0 | 0 | .11 | . 37 | . 28 |
| 57-504 | $A L P P D$ | 37.5 | 1.8 | 0 | 6.8 | 41.5 | - 8 | . 1 | 0 | .01 | 0 | .11 | . 33 | - 39 |
| 57-528 | ALP PD | 39.3 | 2.1 | 0 | 7.3 | 42.8 | . 8 | -1 | 0 | . 01 | 0 | -12 | . 34 | - 25 |
| 57-570 | ALP PO | 35.9 | 1.7 | 0 | 7.4 | 39.9 | . 5 | . 1 | 0 | .01 | 0 | .13 | - 36 | - 32 |
| 57-612 | ALP PD | 39.1 | 2.5 | 0 | 7.5 | 37.9 | 1.0 | . 1 | 0 | . 03 | 0 | .13 | . 36 | . 47 |
| 57-621 | ALP PD | 38.8 | 3.1 | 0 | 7.0 | 37.7 | 1.9 | . 1 | 0 | .01 | 0 | .13 | - 32 | . 53 |
| 57-628 | ALP PD | 36.2 | 1.8 | 0 | 6.7 | 39.9 | . 5 | - 1 | 0 | 0 | 0 | .13 | . 23 | -31 |

NOTES.

1. all sample numbers have a som-prefix.
2. SYMBOLS. ALP PD = ALPINE-TYPE PERIDOTITE, OL OPXN = OLIVINE ORTHOPYROXENITE.
3. FEO REPRESENTS TOTAL IRON. FEZO3 NOT DETERMINED.
4. NAZO NOT DETERMINED. ASSUMED TO BE O.1 PERCENT FOR CALCULATION PURPOSES.
5. K2O AND P2O5 NOT DETERMINED.
6. TIO2, NIO AND CRRO3 BY EMISSION SPECTROGRAPHIC METHOOS.
7. OTHER CONSTITUENTS BY X-RAY FLUORESCENCE.
8. ANALYSES BY THE ANALYTICAL CHEMISTRY SECTION, GEOLOGICAL SURVEY OF CANADA.


| SAMPLE | FOOTAG |  | ROCK | SIO2 | AL203 | FE203 | FEO | MGO | CAO | NAZO | K20 | T102 | P205 | MNO | NIO | CR203 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 64－44 | 1895 | ALP | PD | 37.3 | 2.3 | 2． 8 | 3.9 | 37.2 | ． 8 | ． 1 | 0 | 0 | 0 | .10 | ． 30 | ． 28 |
| 64－43 | 1839 | ALP | PD | 38.4 | 2.2 | 2.4 | 4.4 | 37.5 | ． 9 | ． 1 | 0 | 0 | 0 | .10 | ． 34 | ． 57 |
| 64－42 | 1695 | ALP | PD | 36.4 | 1.9 | 3.3 | 3．8 | 37.5 | 1.0 | －1 | 0 | 0 | 0 | .11 | ． 23 | ． 35 |
| 64－41 | 1618 | ALP | PD | 34.9 | 1.6 | 2.9 | 3.0 | 38.1 | .7 | ． 1 | 0 | 0 | 0 | ． 08 | ． 23 | ． 34 |
| 64－40 | 1472 | ALP | PD | 34.4 | 1.9 | 4.5 | 2.7 | 32.7 | ． 9 | －1 | 0 | 0 | 0 | .10 | ． 25 | ． 41 |
| 64－34 | 1228 | ALP | PD | 35.4 | 2.0 | 3.7 | 3.4 | 37.7 | － 4 | ． 1 | 0 | 0 | ． 01 | .10 | ． 27 | ． 31 |
| 64－31A | 1148 | ALP | PD | 37.2 | 2.4 | 4.5 | 3.3 | 39.1 | － 6 | ． 1 | 0 | 0 | 0 | .10 | ． 28 | ． 37 |
| 64－29 | 963 | ALP | PO） | 39.7 | 1.9 | 4.8 | 2.7 | 41.5 | － 8 | －1 | 0 | 0 | 0 | .10 | ． 23 | ． 44 |
| 64－28 | 875 | ALP | $P D$ | 39.5 | 2.8 | 3.7 | 3.4 | 40.3 | ． 5 | ． 1 | 0 | 0 | ． 01 | .11 | ． 20 | ． 37 |
| 64－27 | 786 | ALP | PD | 39.3 | 2.2 | 3.3 | 3.3 | 44.9 | ． 5 | ． 1 | 0 | 0 | 0 | ． 08 | ． 28 | .26 |
| 64－26A | 745 | ALP | PD | 37.3 | 2.0 | 4.7 | 2.5 | 41.9 | ． 4 | ． 1 | 0 | 0 | 0 | .10 | .23 | ． 31 |
| 64－25 | 532 | ALP | PD | 38.7 | 2.4 | 4.2 | 3.0 | 40.6 | ． 8 | －1 | 0 | 0 | 0 | ． 09 | ． 23 | ． 44 |
| 64－24A | 415 | ALP | PD | 36.9 | 1.8 | 3.8 | 3.4 | 41.9 | ． 6 | －1 | 0 | 0 | 0 | .09 | ． 28 | － 23 |
| 64－16A | 370 | ALP | $P D$ | 37.4 | 2.5 | 4.1 | 3.3 | 37.6 | ． 8 | ． 1 | 0 | 0 | 0 | ． 10 | ． 38 | － 32 |
| 64－18 | 350 | ALP | PD | 38.2 | 2.3 | 3.3 | 3.6 | 42.4 | ． 7 | －1 | 0 | 0 | 0 | ． 08 | ． 38 | .37 |
| 64－15 | 105 | ALP | PD | 36.6 | 1.4 | 4.2 | 3.2 | 41.1 | ． 5 | ． 1 | 0 | 0 | 0 | .10 | .17 | .13 |
| 64－12A | 80 | ALP | PD | 41.3 | 2.4 | 2.7 | $4 \cdot 4$ | 40.0 | ． 7 | 0 | 0 | 0 | 0 | .10 | .23 | ． 29 |

1．all sample numbers have a fjbt－prefix．
2．THE $\neq$ FOOTAGE $\neq$ VALUES ARE IN ARBITRARY UNITS PROGRESSING FRUM SOUTHEAST TO NORTHWEST ACROSS THE PLUTON．THEY SERVE GENERALLY TO PUT THE SAMPLES IN approximate stratigraphic sequence，but the top of the pluton is reached AT 2367 AND THE REMAINING SAMPLES CONSTITUTE A SEQUENCE BACK DOWN INTO THE CRITICAL ZONE．
3．ROCK SYMBOLS．ALP PD＝ALPINE－TYPE PERIDOTITE，FELD ON＝FELDSPATHIC DUNITE， OL CPXN＝OLIVINE CLINOPYROXENITE，TROCT＝TROCTOLITIC GABBRO，OL GABB＝ OLIVINE GABBRO，GABBRO＝OLIVINE－FREE GABBRO，HB GABB＝HORNBLENDE GABBRO， CONT RK＝CONTACT OR COUNTRY ROCK，AB GRAN＝ALBITE GRANITE．SOME OF THE gabbroic rocks are altered to the extent that it is uncertain whether they CONTAINED OLIVINE，HOWEVER，OLIVINE GABBRO IS PREDOMINANT AMONG THE LESS altered samples，therefore in cases of doubt it is assumed to have been the ORIGINAL ROCK．
4．FEO DETERMINED CHEMICALLY．
5．NAZO BY FLAME PHOTOMETRY．
6．TIO2，NIO AND CR2O3 BY EMISSION SPECTROGRAPHIC METHODS．
7．TOTAL IRON AND OTHER CONSTITUENTS BY X－RAY FLUORESCENCE METHODS．
8．ANALYSES BY THE ANALYTICAL CHEMISTRY SECTION，GEOLOGICAL SURVEY OF CANADA．

TABLE 3. MAJOR CHEMICAL CONSTITUENTS IN ROCKS FROM BAY OF ISLANDS IGNEOUS COMPLEX, NORTH ARM MOUNTAIN, WEST

| WEIGHT PERCENT |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| SAMPLE | FOOTAG | RUCK | SIO2 | AL203 | FE203 | FEO | MGO | CAO | NA20 | K20 | T102 | P205 | MNO | NIO | CR203 |
| 64-651C | 3595 | OL GABB | 47.7 | 15.5 | 2.5 | 6.7 | 7.5 | 13.6 | 3.6 | 0 | 1.67 | . 09 | .13 | . 01 | . 04 |
| 64-651A | 3562 | OL GABB | 47.3 | 17.4 | . 7 | 4.4 | 5.0 | 15.4 | 3.7 | .17 | 1.37 | . 07 | . 06 | 0 | .03 |
| 64-640 | 3463 | OL GABB | 46.7 | 18.8 | 1.5 | 4.6 | 8.6 | 12.4 | 2.8 | -11 | .47 | 0 | . 08 | 0 | . 03 |
| 64-614 | 3432 | AB GRAN | 75.5 | 13.2 | 1.5 | $1 \cdot 3$ | 1.2 | 1.1 | 6.0 | .11 | .17 | . 02 | . 05 | 0 | 0 |
| 64-639 | 3398 | OL GABA | 44.5 | 25.9 | 1.5 | 2.4 | $5 \cdot 1$ | 13.0 | 2.1 | 0 | .16 | 0 | .02 | . 02 | . 02 |
| 64-638 | 3305 | GABHRO | 49.1 | 21.6 | 1.5 | 4.4 | 4.9 | 12.0 | 2.9 | - 22 | - 18 | 0 | . 16 | .01 | . 05 |
| 64-636 | 3070 | OL GABB | 43.2 | 21.6 | . 7 | $4 \cdot 3$ | 9.5 | 12.4 | 1.7 | 0 | . 27 | . 01 | .07 | .01 | . 04 |
| 64-634 | 2822 | OL GABB | 46.2 | 20.1 | . 4 | 4.3 | $7 \cdot 7$ | 11.7 | 3.1 | - 10 | - 28 | .01 | .07 | .01 | . 05 |
| 64-632 | 2632 | OL GABB | 48.4 | 18.3 | 1.5 | 5.0 | 9.4 | 13.1 | 2.5 | 0 | . 27 | .01 | .12 | .01 | . 05 |
| 64-737 | 2448 | OL GABB | 45.9 | 22.7 | . 7 | 4.6 | 8.2 | 13.1 | 2.3 | 0 | . 20 | .01 | .09 | . 02 | . 05 |
| 64-546A | 2230 | OL GABB | 46.3 | 20.7 | . 6 | 4.0 | 11.8 | 13.5 | 1.9 | 0 | .17 | . 01 | . 06 | .03 | . 06 |
| 64-537 | 2090 | GABBRO | 50.6 | 21.5 | . 9 | 2.8 | 4.7 | 15.6 | 2.6 | 0 | . 15 | 0 | . 09 | . 01 | .01 |
| 64-540 | 1930 | OL GABB | 45.3 | 24.5 | . 7 | 2.3 | 6.1 | 16.1 | 1.8 | 0 | . 09 | 0 | . 05 | .01 | .02 |
| 64-745 | 1762 | GABFRO | 48.2 | 22.9 | . 5 | 4.8 | 7.1 | 14.7 | . 9 | 0 | . 14 | 0 | .11 | .01 | . 04 |
| 64-746 | 1692 | GABERO | 47.4 | 20.2 | - 3 | 5.6 | 8.6 | 12.9 | 1.4 | - 31 | . 08 | . 01 | .12 | 0 | . 01 |
| 64-747 | 1537 | ALP PD | 37.6 | 2.0 | 4.3 | 3.4 | 39.9 | 1.1 | -1 | 0 | 0 | 0 | . 12 | . 23 | . 04 |
| 64-710 | 1338 | ALP PD | 34.7 | 1.5 | 3.6 | 3.7 | 40.3 | . 8 | -1 | 0 | 0 | 0 | .10 | . 29 | . 31 |
| 64-721 | 126 ? | ALP PD | 37.3 | 2.6 | 3.5 | 3.4 | 41.8 | . 8 | . 1 | 0 | 0 | 0 | .11 | . 29 | . 35 |
| 64-723 | 1082 | ALP PD | 36.8 | 2.4 | 3.9 | 3.4 | 40.8 | . 6 | -1 | 0 | 0 | 0 | .12 | . 42 | . 32 |
| 64-715 | 798 | ALP PU | 35.3 | 1.8 | 4.0 | 3.6 | 41.1 | . 5 | . 1 | 0 | 0 | 0 | . 12 | . 28 | .37 |
| 64-716 | 670 | ALP PD | 35.2 | 2.1 | 4.5 | 3.4 | 41.0 | . 7 | . 1 | 0 | 0 | . 01 | . 12 | . 31 | . 32 |
| 64-717 | 614 | ALP PD | 35.4 | 1.9 | 4.7 | 3.4 | 38.4 | 1.4 | . 1 | 0 | 0 | 0 | . 12 | - 32 | - 32 |
| 64-797 | 445 | ALP PU | 39.1 | 2.8 | 3.0 | 3.8 | 44.4 | . 7 | . 1 | 0 | 0 | 0 | .12 | . 19 | . 31 |
| 64-796 | 285 | ALP PD | 39.2 | 2.7 | 3.0 | 4.5 | 41.2 | 1.4 | . 1 | 0 | 0 | . 01 | .13 | - 18 | . 34 |
| 64-779 | 262 | ALP PD | 39.1 | 2.3 | 2.2 | 4.1 | 41.1 | 1.9 | -1 | 0 | 0 | 0 | .10 | . 32 | . 34 |
| 64-777 | 213 | ALP PD | 39.7 | 2.8 | 3.2 | 4.9 | 38.4 | 1.6 | .1 | 0 | 0 | . 01 | .15 | .33 | . 35 |
| 64-775 | 188 | ALP PD | 37.0 | 2.3 | 4.1 | 4.2 | 41.8 | . 9 | . 1 | 0 | 0 | 0 | . 13 | - 35 | . 02 |
| 64-895 | 177 | AL.P PD | 37.2 | 2.4 | 3.3 | 3.8 | 38.1 | 1.8 | . 5 | 0 | 0 | .01 | . 11 | -31 | . 31 |
| 64-896 | 162 | CONT RK | 47.9 | 14.7 | - 5 | 11.2 | 11.0 | 8.3 | 3.5 | - 84 | 1.50 | . 11 | . 27 | . 01 | . 02 |
| 64-894 | 154 | CONT RK | 48.2 | 17.4 | 1.9 | 7.6 | 7.7 | $10 \cdot 3$ | 3.8 | 1.21 | 1.17 | . 14 | . 18 | . 01 | . 03 |
| 64-893A | 142 | CONT RK | 47.2 | 21.0 | 3.1 | 5.6 | 4.7 | 9.8 | 4.4 | $1 \cdot 23$ | . 85 | . 13 | . 14 | . 01 | . 03 |
| 64-878 | 92 | CONT RK | 70.8 | 16.2 | . 6 | 4.2 | 2.2 | . 6 | 2.5 | 2.50 | - 70 | . 08 | . 14 | 0 | .01 |
| 64-874 | 53 | CONT RK | 78.7 | 12.4 | 1.0 | 2.2 | 2.9 | . 4 | 1.7 | 2.62 | . 50 | . 04 | . 05 | 0 | 0 |

1. ALL SAMPLE NUMBERS HAVE A FJBN-PREFIX.
2. THE $\neq F$ UOTAGE $\ddagger$ VALUES ARE IN ARAITRARY UNITS PROGRESSING FROM SOUTHEAST TO northwest acruss the pluton. they serve generally to put the samples in approximate stratigraphic sequence.
3. for other relevant notes see table 2.

TABLE 4. MAJOR CHEMICAL CONSTITUENTS IN ROCKS FROM BAY UF ISLANDS IGNEOUS COMPLEX, NORTH ARM MOUNTAIN, EAST.


1. ALL SAMPLE NUMBERS HAVE A FJBN-PREFIX.
2. FOR OTHER RELEVANT NOTES SEE TABLE 3 .
table 5. mineralogical data and trace element abundances for rocks from the mount albert ultramafic complex.

|  |  |  | MOL. | PCT | \% |  |  |  |  | P | MIL |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| SAMPLE | FOOTAGE | ROCK | F? | IN | CHROMITE | BA | CO | CR | CU | NI | SC | SR | V | ZN |


| $\begin{array}{lr} 57- & 8 \\ 57- & 17 \end{array}$ |
| :---: |
| 57- 25 |
| 57-41 |
| 57-44 |
| 57-45 |
| 57- 52 |
| 57- 56 |
| 57- |
| 57-60 |
| 57-91 |
| 57- 95 |
| 57-105 |
| 57-117 |
| 57-118 |
| 57-124 |
| 57-126 |
| 57-131 |
| 57-144 |
| 57-150 |
| 57-165 |
| 57-186 |
| 57-246 |
| 57-262 |
| 57-268 |
| 57-269 |
| 57-270 |
| 57-504 |
| 57-528 |
| 57-570 |
| 57-612 |
| 57-621 |
| 57-628 |


| ALP PD | 91.2 | 8.150 | 13 |
| :--- | :--- | :--- | ---: |
| ALP PD | 90.2 | 8.170 | 12 |
| ALP PD | 90.6 | 8.320 | 0 |
| ALP PD | 91.6 | 8.275 | 0 |
| ALP PD | 90.5 | 8.315 | 12 |
| ALP PD | 90.6 | 8.310 | 0 |
| ALP PD | 91.2 | 8.315 | 0 |
| ALP PD | 90.9 | 8.270 | 0 |
| ALP PD |  | 8.225 | 0 |
| ALP PD | 90.5 | 8.240 | 0 |
| ALP PD | 91.0 | 8.290 | 0 |
| OL OPXN |  | 8.145 | 0 |
| ALP PD |  | 8.170 | 0 |
| ALP PD | 89.6 | 8.150 | 0 |
| ALP PD |  | 8.155 | 8 |
| ALP PD | 89.7 | 8.155 | 0 |
| ALP PD | 91.2 | 8.280 | 0 |
| ALP PD | 90.0 | 8.145 | 0 |
| ALP PD | 89.7 | 8.215 | 0 |
| ALP PD | 90.0 | 8.160 | 0 |
| ALP PD |  | 8.220 | 10 |
| ALP PD |  | 8.280 | 10 |
| ALP PD | 90.0 | 8.225 | 12 |
| ALP PD | 90.6 | 8.295 | 0 |
| ALP PD | 91.2 | 8.315 | 0 |
| ALP PD | 90.1 | 8.265 | 8 |
| ALP PD |  | 8.300 | 0 |
| ALP PD | 90.6 | 8.150 | 8 |
| ALP PD | 89.4 | 8.200 | 16 |
| ALP PD | 90.6 | 8.260 | 0 |
| ALP PD | 89.0 | 8.150 | 18 |
| ALP PD | 89.5 | 8.160 | 13 |
| ALP PD | 91.2 | 8.280 | 0 |
| EMMBERS HAVE A SDM-PREFIX |  |  |  |

TABLE 6. MINERALOGICAL DATA AND TRACE ELEMENT ABUNDANCES FOR ROCKS FROM bay of islands igneous complex. table mountain pluton


TABLE 6．CONTINUED．


TABLE 7. MINERALOGICAL DATA AND TRACE ELEMENT ABUNDANCES FOR ROCKS FROM BAY OF ISLANDS IGNEOUS COMPLEX, NORTH ARM MOUNTAIN, WEST


## NOTES.

1. ALL SAMPLE NUMBERS HAVE A FJBN-PREFIX.
2. FOR EXPLANATION OF THE FOOTAGE VALUES, SEE TABLE 3.
3. FOR OTHER RELEVANT NOTES SEE TABLE 6.

TABLE 8．MINERALOGICAL DATA AND TRACE ELEMENT ABUNDANCES FOR ROCKS FROM BAY OF ISLANDS IGNEOUS COMPLEX，NORTH ARM MOUNTAIN，EAST．

|  |  |  |  | PCT | \＆ |  |  |  |  | S P | MIL |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| SAMPLE | FOOTAGE | ROCK | FO | INN | CHROMITE CELL EDGE | BA | co | CR | CU | NI | SC | SR | $v$ | 2N | 2R |
| 64－505 | 2195 | HB GABB |  |  |  | 24 | 0 | 180 | 8 | 180 | 100 | 190 | 390 | 65 | 0 |
| 64－511 | 1902 | HB GABE |  |  |  | 20 | 0 | 220 | 8 | 39 | 0 | 230 | 200 | 40 | 0 |
| 64－513 | 1680 | OL GABB |  |  |  | 78 | 0 | 350 | 46 | 120 | 0 | 0 | 71 | 0 | 0 |
| 64－525 | 1445 | OL GABB | B | 69.6 |  | 19 | 0 | 700 | 54 | 120 | 0 | 100 | 170 | 40 | 0 |
| NOTES． |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1. | L SAMPLE | NUMBER | RS | HAVE | A FJBN－PR | FFIX |  |  |  |  |  |  |  |  |  |
| 2. | OR OTHER | RELEVAN | NT N | NOTES | SEE TABL |  |  |  |  |  |  |  |  |  |  |

sion and modal proportions of the main minerals correlate closely with experimentally based fractional crystallization models for the type of magma represented in the chilled margins of the intrusions (Irvine and Smith, 1967; Irvine, 1970). In such stratiform intrusions these sequences are commonly repeated (due to the periodic influx of fresh magma; Irvine and Smith, 1967) and are called cyclic units (Jackson, 1961).
(3) Chemical grading or cryptic layering (i.e. chemical trends in the cumulus minerals, and in the rocks themselves) corresponding to the order in which the pertinent constituents are known to be extracted from basic magma during fractional crystallization. Relevant examples are trends of (a) iron enrichment as expressed by a decrease of the ratio $\mathrm{Mg} /\left(\mathrm{Mg}+\mathrm{Fe}^{+2}\right)$, of (b) Ni depletion as reflected in its abundance in solid solution in olivine and pyroxene, and of (c) Cr depletion as reflected in either the amount of chromite in the rock or the abundance of the element in pyroxene (Irvine and Smith, 1969).

Criteria for identifying the residue of a partial fusion process are more tenuous, as they generally involve some assumption regarding the nature of the original rock, or the nature of the process; they tend to be negative criteria. In general, the rock should be fairly refractory with a "reduced" content of highly "fusible" constituents such as the alkalies and sulphide minerals. Fractional or partial fusion of an ultramafic rock will ordinarily increase its $\mathrm{Mg} /(\mathrm{Mg}+\mathrm{Fe}$ ) ratio (e.g. Carter, 1970), and, in a case of broadscale melting under relatively gentle thermal gradients (as one might anticipate for alpine-type peridotite), this ratio should probably also be fairly uniform. The constraints imposed on the modal composition of a rock during fractional fusion can lead to appreciably different products than those developed by fractional crystallization (Presnall, 1969), and one might expect this to be reflected in certain trace-element relations. Also, partial melting is probably less apt to produce spatially systematic rock sequen-
ces and chemical or mineralogical trends, than fractional crystallization. However, it is emphasized that all these criteria are provisional and it is not difficult to visualize circumstances in which they would not be valid: for example, systematic chemical trends might persist from an earlier stage of differentiation.

## Characteristics of alpine-type peridotite

In this paper the term "alpine-type peridotite" is applied only to a very particular kind of ultramafic rock. This rock spans certain of the boundaries ordinarily drawn in petrographic classifications of ultramafic rocks, but, as a unit, it is characterized by a combination of features by which it can generally be identified (quite independently of genetic considerations) provided it is not too altered. It is commonly associated with other kinds of ultramafic rocks and may even be found with other types of peridotite. On the continents it typically occurs in Phanerozoic mountain belts in the bodies here referred to as "alpine ultramafic complexes". These are variously described in the literature as discrete intrusions, as parts of more varied plutonic bodies containing gabbroic and other intrusive rocks, and as members of ophiolite complexes in which they bear a definite relation to volcanic and sedimentary rocks. The peridotite as described below is the characteristic rock of these bodies, the principal features of which are as follows:

1. Occurrence: They are found in large numbers along certain orogenic belts, such as the Appalachians and the Coast ranges of California. In Canada, they are the principal kind of ultramafic body in the Cordillera, and they occur in a discontinuous belt from the Eastern Townships to the north coast of western Newfoundland (Figure 1). Interestingly, however, the exact kind of peridotite discussed here is rare, if present at all, among the large numbers of ultramafic bodies in the Canadian Shield (see below).
2. Size: In terms of area of exposure at least, alpine ultramafic complexes comprise many of the largest bodies of
olivine-rich ultramafic rocks in the world; in fact, it appears that the only occurrence of greater extent is the Great Dyke of Rhodesia, a stratiform intrusion. The largest example in Canada is the Nahlin complex in northern British Columbia, which is more than 50 miles long and has an area of about 140 square miles (Smith, 1962). Several of the other bodies in the Cordillera are 50-80 square miles in size. In the Appalachians, the ultramafic rocks of the Bay of Islands Igneous Complex, consisting, in large part of alpine-type peridotite, have a composite area of about 130 square miles (Smith, 1958). The great majority of the bodies are intermediate or small in size, but the large ones are distinctive, and, as Smith (1962) pointed out, are much larger than anything found in the Canadian Shield.

A related point is that none of the large stratiform intrusions contain coherent masses of olivine-rich rocks to compare with those found in the alpine complexes. The layers of dunite and peridotite in stratiform intrusions, although extensive laterally, are rarely more than a few hundred feet thick, being closely interstratified with major layers of pyroxenite and gabbro, By contrast, in alpine-type bodies, the peridotite and associated dunite may be virtually the sole rock types throughout mountain masses having thousands of feet of relief and extending over many square miles.

On the other hand, geophysical studies, particularly gravity surveys, have (so far as we are aware) failed to show that any Canadian alpine ultramafic complex extends to depths of more than a few miles, and there seems no evidence that any of them are directly "rooted" in the mantle.
3. Conditions of emplacement: As already noted, it is generally accepted that alpine-type peridotites were largely solid when emplaced in their present country rocks. Some complexes have well developed contact metamorphic aureoles (Green, 1964a; Challis, 1965), and it is evident that the peridotite was very hot when emplaced. Some Canadian examples with aureoles are the Bay of Islands


Figure 1. Map showing a partial, very generalized classification of ultramafic and related rocks in Canada and adjoining U.S.A., with some data on the composition of olivine in the peridotitic rocks.

Complex (Smith, 1958), the Mount Albert intrusion in the Gaspe (MacGregor,1962, 1964a), and the Blue River intrusion in northern British Columbia (Wolfe, 1966). More commonly, however, contact metamorphism is absent or inconspicuous, and the peridotite bodies have serpentinized and talcose margins, and are bounded by, or associated with, major faults, so that they appear to have been emplaced "cold" through the action of faulting (Hess, 1955). It is notable, however, that while the Mount Albert body has a beautifully developed metamorphic aureole around one side, it is bounded by a major fault on the other (MacGregor, 1962). Also, in a general petrographic comparison, the peridotite in the "hot" intrusions is not conspicuously different from that in the "cold" ones, unless perhaps that it shows more penetrative deformation.
4. Petrography of alpine-type peridotite: Alpine-type peridotite is generally a spinel peridotite in the harzburgite-dunite range, grading in places to lherzolite. Typically it is a partly to completely serpentinized assemblage of 60-90 per cent olivine, 5-35 per cent orthopyroxene and 1-7 per cent clinopyroxene (Figure 2), plus $1 / 2-2$ per cent chromiumbearing spinel (chromite). Uncommon minor phases are amphibole (Green, 1964a) and, very rare in North America at least, pyrope garnet (Church, this volume). Plagioclase may occur in associated peridotite, but is not generally found in the alpine-type. (An exceptional occurrence of plagioclase-bearing alpinetype peridotite is described by Walcott, 1969.) The olivine occurs as coarse spheroidal to polygonal grains if it is undeformed, but commonly it is strained and granulated and shows two distinct sizes of anhedral grains all in a foliated fabric. (e.g. Ragan, 1967; Moores, 1969). Compositionally, its range is small, generally between $\mathrm{FO}_{87}$ and $\mathrm{FO}_{94}$, and its variation in particular occurrences may be even smaller - for example, most of the olivine in the Mount Albert and Bay of Islands peridotites is between Fo89
and Fog2 (Tables 5-8). The pyroxenes show similarly high $\mathrm{Mg} /(\mathrm{Mg}+\mathrm{Fe})$ ratios. In some complexes the pyroxenes contain 5.7 per cent $\mathrm{Al}_{2} \mathrm{O}_{3}$ (Green, 1963, 1964) but such large amounts are not universal (e.g. Challis, 1965, Table 6). The orthopyroxene generally appears as blocky prisms that are prominent on weathered surfaces and persist in the deformed rocks as augen with conspicuously bent cleavages. It may be partly grown around the olivine grains but shows little evidence of having formed by reaction from olivine, and rarely is it poikilitic like the pyroxene oikocrysts common to olivine cumulates in stratiform intrusions. (Challis (1965) compared peridotite containing poikilitic orthopyroxene in the Red Hill alpine complex, New Zealand with Stillwater cumulates, but Walcott (1969) considered the same rock to be formed by replacement and recrystallization.) Some of the clinopyroxene forms exsolution lamallae in the orthopyroxene, but much of it occurs as small grains "interstitial" to the olivine and orthopyroxene. The chromite shows a large compositional range, particularly in $\mathrm{Cr} / \mathrm{Al}$ ratio (MacGregor and Smith, 1963; Irvine, 1967) and, if undeformed, differs in habit accordingly. At one extreme is an opaque to deep red, Cr-rich, subhedraleuhedral type, that looks much like the cumulus chromite in stratiform intrusions. At the other, apparently gradational in all respects with the Cr-rich type, are olive to green Al-rich spinels that generally appear interstitial or micropoikilitic (Figure 3; see also Smith, 1958, P1. X).

Serpentinization of the peridotite variously produces a host of serpentine minerals, talc, brucite, carbonates, secondary magnetite, native Ni and Fe alloys, and other minerals. There has been much controversy as to whether the alteration occurred as a "constant composition" process, except for the addition of volatiles, that caused expansion of the rock, or as a "constant volume" process marked by major chemical changes (e.g. Hostetler et al, 1966; Thayer, 1966). However, there appear to be valid argu-
ments on both sides, and probably both interpretations have some application.*

The peridotite commonly shows a rude layering on the scale of inches owing to thin bands altemately enriched in olivine and orthopyroxene. The layering is generally steeply dipping, and, while it may have broadly regular strike over large areas, commonly shows local irregularity and folding (e.g. Leech, 1953; Smith, 1958). In the Mount Albert intrusion it defines a broad fold pattern that appears to be indicative of diapiric emplacement (MacGregor, 1962). The layering has frequently been interpreted as flow banding (Smith, 1958; Dickey, 1970), but it occasionally shows grading and other features suggestive of crystalsettling and current-sorting. In some of the examples that we have seen, the pyroxenes appear to be oriented normal to the layering, a feature that is difficult to explain by flow. Dickey (1970) distinguished between "fectonic-type" layers, described as occurring in several cross-cutting generations, and "magmatictype" layers considered to have formed from a basic magma produced by partial fusion of the peridotite.
5. Associated dunites: Although the peridotite commonly grades to dunite, there is also associated coarse-grained dunite, in sharply defined bodies ranging from "veins" less than an inch wide, to irregular masses measurable in hundreds of feet (e.g. Leech, 1953; Smith, 1958; Burch, 1969). These occasionally contain

[^13]

Figure 2. Ternary plots of $O I, C p x$ and $O p x$ in three alpine ultramafic complexes, based on a spinel peridotite norm. Provisional fields for conventional petrographic classification of feldspar-free ultramafic rocks are indicated.



Figure 3. A. Plot comparing the compositional fields of chromite in alpine ultramafic complexes, stratiform intrusions, spinel peridotite xenoliths from basaltic lavas, and kimberlite (one sample only), after Irvine (1967). The indicated cell edge values will not generally apply to chromites in stratiform intrusions because they tend to be fairly rich in $\mathrm{Fo}_{2} \mathrm{O}_{3}$, which acts strongly to increase cell size. B. Textural variants of chromite in the Mount Albert complex. Cell edge data from MacGregor and Smith (1963).
small chromite deposits varying from thin median zones in the veins (Smith, 1958) to irregular pods and vein-like accumulations in the larger bodies (Thayer, 1963a). The veins are frequently interpreted as having formed due to the removal of silica by an aqueous fluid phase. However, this implies a volume reduction, whereas in the Shulaps Complex in British Columbia, for example, fairly large dunite bodies of this type can be seen to transgress layering in peridotite in a way that suggests that they have formed by volume-for-volume replacement.

Still other dunite occurs in major, roughly "conformable" zones, which in some complexes occur between the peridotite and adjoining gabbro (Thayer, $1960,1964,1967$ ). This type of dunite commonly contains layered deposits of chromite, and it is from these deposits that Thayer (1969) has gathered much of his most convincing textural and structural evidence of crystal settling. Two of the principal occurrences cited by Thayer are in the Camaquey Complex in Cuba and the Zambales Complex in the Phillipines. Canadian examples are to be found in the Bay of Islands Complex (Smith, 1958), and in the vicinity of the abandoned chromite mines on Colline Provincial near Thetford Mines, Quebec.
6. Other rock associations: Other rocks associated with alpine-type peridotite are pyroxenite, gabbro, quartz-diorite, and albite granite (Thayer, 1963, 1967; Moores, 1969). Some of the pyroxenite occurs in "dykes" or "veins" and pegmatitic pods; but the main masses, which are usually websterite or olivine clinopyroxenite, range from irregular "blocks" a few feet in size, to rude layers up to a few hundred feet in thickness or even several miles in length, to still more extensive bodies or areas of no distinctive shape. The larger bodies tend to occur around the apparent top of the peridotite (e.g. Thayer, 1963; Moores, 1969). Among the gabbroic rocks are olivine gabbro, clinopyroxene gabbro, and norite, but perhaps of more frequent occurrence are the highly-altered types in which hornblende, actinolite, epidote, albite, and other secondary minerals predominate. Diorite
and granite occur in minor quantities as small late plutons and dykes.

The idealized ophiolite sequence is as follows: peridotite at the base, overlain by pyroxenite and gabbro, followed by pillowed lavas and associated diabase dykes, the whole overlain by chert-rich sediments (e.g. Maxwell, 1969). This succession is now considered by many to represent a section of the oceanic crust and part of the upper mantle (e.g. Gass, 1968; Dewey and Bird, 1970; Church, this volume). Thayer (1967) stressed that the same lithological association is common to many alpine complexes, and his descriptions, and those of Moores (1969), emphasize the structural and petrological complexities that can be involved (see also Walcott, 1969). Many authors now apply the term ophiolite in a broader sense to any ensemble of alpinetype peridotite and these other rocks.
7. Chemical characteristics: Alpine-type peridotite ordinarily shows only a very limited range of chemical composition (e.g. Tables $1-8$; Hess, 1964). The major constituents $\left(\mathrm{SiO}_{2}, \mathrm{MgO}, \mathrm{FeO}\right.$ and $\left.\mathrm{Fe}_{2} \mathrm{O}_{3}\right)$ essentially reflect the modal abundance and composition of the olivine and orthopyroxene, and the nature and extent of their serpentinization. As a rule, $\mathrm{Al}_{2} \mathrm{O}_{3}$ is between 0.5 and 4 per cent, CaO is between 0.5 and 2.5 per cent, and $\mathrm{TiO}_{2}$ is less than 0.03 per cent. $\mathrm{Na}_{2} \mathrm{O}$ and $\mathrm{K}_{2} \mathrm{O}$ are generally less than 0.3 and 0.02 per cent, respectively, and both may be extremely low (Hamilton and Mountjoy, 1965; Stueber and Goles, 1965). BaO, $\mathrm{P}_{2} \mathrm{O}_{5}, \mathrm{Cu}, \mathrm{Zr}$, and S are also very low, and Frey (1970) has interpreted rareearth element abundances as indicating that the peridotite is a depleted residue after basalt magma formation. Our data show that NiO is slightly higher than in the peridotitic cumulates of the Muskox Intrusion, whereas $\mathrm{Cr}_{2} \mathrm{O}_{3}$ is generally only half to two-thirds as abundant (Figure 4).
8. Sr-isotope characteristics: Several occurrences of alpine-type peridotite have exceptionally high $\mathrm{Sr}^{87} / \mathrm{Sr}^{86}$ ratios compared to oceanic basalts and other magmatic materials believed to come directly from the mantle, and regression lines
based on the ratio $\mathrm{Rb} / \mathrm{Sr}$, tracing the isotope ratios back in time, suggest that the analyzed rocks were isolated from the present magma-producing parts of the mantle long before their times of emplacement. However, a between-laboratory discrepancy in the abundance of Sr has left a large uncertainty as to when the separation occurred (Hurley, 1967). Stueber and Murthy (1966) suggested from their data that the peridotite is a residue of melting that occurred in early Archean times at a stage when most of the continental crust was being formed, whereas Roe, Pinson and Hurley (1965) placed the time of separation in the latter half of earth history (at about $730 \mathrm{~m}, \mathrm{y}$. for their particular samples). Bonnatti, Honnorez and Ferrara (1970) recently reported data for peridotite of alpinetype character from the Mid-Atlantic Ridge in agreement with Stueber and Murthy's results, and they interpret their findings as indicating the presence of a very ancient zone of depleted mantle beneath the Atlantic.

## 9. Absence from the Canadian Shield:

 Alpine-type peridotite does not occur in any abundance, if at all, in the Canadian Shield. The absence there of bodies of comparable size to the large alpine-type complexes has already been noted: the largest Shield peridotite bodies are a series of sills in the Labrador Trough and Cape Smith-Wakeham Bay fold belts (Smith, 1962), but structural, textural, mineralogical and chemical data from those bodies that have been studied in detail (Fahrig, 1962; Baragar, 1967; Wilson et al., 1969) all show clearly that the peridotite is not alpine-type. The next largest Shield bodies occur as layers and sills associated with stratiform complexes, particularly in the Muskox Intrusion (Smith, 1962), in the Abitibi region (Naldrett and Mason, 1968; MacRae, 1969), and in several areas in Manitoba (Scoates, 1969). But again, in those occurrences familiar to us, or for which reasonably detailed information is available, no alpine-type peridotite can be recognized. It appears that in most Shield peridotites: plagioclase (now generally much altered) or hornblende are
$\Delta_{x}^{\circ}$ - Alpine - type peridotite

- Feldspathic peridotite Troctolite

Figure 4, Plots showing the relative abundances of NiO and $\mathrm{Cr}_{2} \mathrm{O}_{3}$ in (A) four alpine complexes, and (B) the lower half of the Muskox layered series. The dashed line effectively separates the alpine-type peridotite from the rocks of the Critical and Gabbro Zones at Bay of islands and from most of the cumulate rocks in the Muskox Intrusion. Mayaguez (Puerto Rico) data from Hess (1964); Blue River data from Wolfe (1966).
important constituents; cumulate-type textures featuring poikilitic pyroxenes and reaction replacement of olivine by pyroxene are common; the associated chromite is more generally opaque than in alpine-type peridotite; and much of the olivine either has a lower Fo-content or ranges to lower Fo-values (Figure 1). The data on which the last point is based are still scanty, but the same pattern is shown by $\mathrm{Mg} /(\mathrm{Mg}+\mathrm{Fe})$ ratios calculated from more than a thousand unpublished chemical analyses obtained by Cameron, Siddley and Durham (1971) in an extensive geochemical survey of Canadian Precambrian ultramafic rocks.

One area in the Shield where alpinetype peridotite might be present is along the Manitoba Nickel Belt. Coats (1966) described rocks from this belt consisting of magnesian olivine and orthopyroxene, and transparent chromite, having the same general chemical composition as alpine-type peridotite; and the tectonic setting close to the boundary of the Superior and Churchill Provinces might suggest a similar association with faulting. However, the rock does not appear to show the same kind of deformation found in alpine peridotite, and Coats' data and illustrations demonstrate clearly that other kinds of peridotite are present; consequently there is some uncertainty.
10. Paucity of associated Ni-sulphide deposits: In connection with the last point it is recalled that Smith (1962) noted an important difference between Shield ultramafic rocks and those in the Cordillera and Appalachians that Nisulphide deposits are much more numerous in the former than in the latter. It is now evident that this difference, which is essentially confirmed by Chamberlain and Johnson's (1970) recent compilation map of Ni-deposits in Canada, represents in large degree a contrast between undoubted alpine-type peridotite and other kinds of uiltramafic rocks. There are exceptions (for example, the Eastern Metals deposit in the Eastern Townships is associated with alpine-type peridotite), but it is particularly notable, that among the relatively few Ni -sulphide deposits found with Cordilleran ultra-
mafic bodies, at least three of the main ones (the Giant Mascot orebody in southern British Columbia, and two deposits in the Kluane ranges in the western Yukon) accompany peridotites that are definitely not alpine in type (Figure 1). The difference would appear to reflect a generally lower level of sulphur in the alpine-type rock, although different processes of origin may also be a factor.

## Some general genetic considerations

 1. Temperatures of formation or equilibration: Information on the temperatures at which alpine-type peridotite has formed comes mainly from an experimental study of a natural peridotite by Ito and Kennedy (Figure 5), and from data on a few "high-temperature" intrusions. Metamorphic grades in the contact aureoles of the Lizard and Mount Albert Intrusions indicate that they were emplaced at close to solidus temperatures (Green, 1964b; MacGregor, 1964). Challis (1965) considered that the New Zealand hightemperature intrusions formed from basaltic magma at liquidus temperatures. Green (1964a) showed that the relative distribution of Mg and $\mathrm{Fe}^{+2}$ between coexisting pyroxenes in the Lizard Intrusion was the same as found in pyroxenes formed from basaltic magmas, and O'Hara (1967) estimated near solidus temperatures for the peridotites of several complexes on the basis of the distribution of Ca amongst coexisting pyroxenes.
## 2. Pressures of formation or equilibration:

 Experimental data relevant to defining the pressures at which alpine-type peridotite may have formed are summarized in Figure 5 together with a semi-quantitative illustration of the interrelation of $\mathrm{Cr} / \mathrm{Al}$ ratio, mineral assemblage, and chromite composition.Some alpine-type peridotite has clearly formed at moderately high pressures (Green, 1964a; O'Hara, 1967) although exact values are still rather uncertain. The essential evidence is that the $\mathrm{Al}_{2} \mathrm{O}_{3}$ in the rock is contained in pyroxenes and spinel rather than in plagioclase, with minimum pressures
being determined essentially by the reaction

Anorthite + Forsterite $\rightleftharpoons$ Aluminous enstatite + Aluminous diopside + Spinel $\left(\mathrm{MgAl}_{2} \mathrm{O}_{3}\right)$

For the pure system, the right side of the reaction is favoured above $7^{1 / 2}-8^{1} / 2 \mathrm{~kb}$ at $1000-1300^{\circ} \mathrm{C}$ (Kushiro and Yoder, 1966). However, the reaction boundary is strongly affected by $\mathrm{Cr}_{2} \mathrm{O}_{3}$ and $\mathrm{Fe}_{2} \mathrm{O}_{3}$, which act to stabilize the spinel phase, and in fact, at high $\mathrm{Cr} / \mathrm{Al}$ ratios, plagioclase-free "spinel" peridotite may be stable at pressures right down to one atmosphere (Figure 5; see also Ito and Kennedy, 1967). Therefore, in the absence of detailed mineralogical data, a high-pressure origin can be inferred for alpine-type peridotite only if the rock contains olive to green Al-rich chromite in association with olivine and two pyroxenes (Figure 5). This assemblage probably indicates a minimum pressure somewhere in the range 5.7 kb .
$\mathrm{Na}_{2} \mathrm{O}$ also has a considerable effect on the above reaction, as it tends to stabilize plagioclase. Green and Hibberson (1970) found that, starting with Cr-free mixtures of olivine and a sodium-bearing plagioclase $\left(\mathrm{An}_{59}\right)$ at $1200^{\circ} \mathrm{C}$, spinel did not appear until 9 kb , and all five phases involved in the reaction persisted together to $10-14 \mathrm{~kb}$, depending on starting composition. This effect is not critical to the immediate discussion, as alpine-type peridotite is generally very low in $\mathrm{Na}_{2} \mathrm{O}$, but it is pertinent to the Bay of Islands data presented below.

An upper pressure limit for the crystallization of most alpine-type peridotite is set by the appearance of garnet, essentially by the reaction (MacGregor, 1964).

Aluminous enstatite + Spinel $\rightleftharpoons$ Pyrope garnet + Olivine

Important additional constituents in this case are CaO , which stabilizes the garnet and causes the appearance of clinopyroxene as an extra phase (Kushiro and Yoder, 1966), and $\mathrm{Cr}_{2} \mathrm{O}_{3}$, which continues to stabilize the spinel (MacGregor, 1970). In the natural peridotite studied


Figure 5. Diagram summarizing experimental data relating to pressures and temperature of formation of peridotitic rocks. Abbreviations: OI - olivine; Fo - forsterite; Cpx - clinopyroxene; Opx - orthopyroxene; Chr - chromite; Sp - spinel; Gar - garnet; An - anorthite; SS - solid solution; N.S.P. - natural spinel peridotite; N.G.P. - natural garnet peridotite. The lines labelled 4, 14, 32, 42 mark the appearance of garnet as a function of the $\mathrm{R}_{2} \mathrm{O}_{3}$ composition of the rock. The dashed line " $\mathrm{An}_{5} 9$ " illustrates the effect of $\mathrm{Na}_{2} \mathrm{O}$ on the appearance of spinel in a Cr -free system. The inset diagrams are projections showing the possible mineral assemblages that may coexist with olivine ( $\mathrm{FO}_{9}{ }_{0}$ ) and clinopyroxene in a $\mathrm{Na}_{2} \mathrm{O}$-free system. Assuming idealized compositions for the olivine and clinopyroxene, the vertical coordinate of the projections is the molecular ratio:

$$
\frac{\mathrm{SiO}_{2}-1 / 2(\mathrm{MgO}+\mathrm{FeO})-1^{1 / 2} \mathrm{CaO}}{\mathrm{SiO}_{2}-1 / 2(\mathrm{MgO}+\mathrm{FeO})-1^{1 / 2} \mathrm{CaO}+\mathrm{Al}_{2} \mathrm{O}_{3}+\mathrm{Cr}_{2} \mathrm{O}_{3}+\mathrm{Fe}_{2} \mathrm{O}_{3}}
$$

The horizontal coordinate is strictly applicable only to the plotted mineral compositions: to project rock compositions, the amount of Al and Cr contained in clinopyroxene must first be subtracted. The solid solution ranges shown for the minerals are roughly consistent with data on natural assemblages; and the slopes of the tie lines are consistent with observed distribution coefficients for Cr and Al . Note how the possible compositional range, abb, of chromite in association with olivine and two pyroxenes first expands with increased pressure and then contracts. This compares with the data summarized in Figure 3A, and at very high pressures would be expected to give extremely Cr-rich chromites and garnets like the inclusions found in diamonds by Meyer and Boyd (1970). Similar projections showing the phase relations of clinopyroxene, chromite, plagioclase and garnet coesixting with olivine and orthopyroxene can be constructed by plotting $\mathrm{Ca} /(\mathrm{Ca}+\mathrm{Al})$ against $\mathrm{Al} /(\mathrm{Cr}+\mathrm{Al})$.
by Ito and Kennedy (1967) - which had a representative content of $\mathrm{CaO}(1.76$ per cent), $\mathrm{Al}_{2} \mathrm{O}_{3}$ (2.05 per cent) and $\mathrm{Cr}_{2} \mathrm{O}_{3}$ ( 0.48 per cent) for alpine-type peridotite (cf. Figure 6 and Hess, 1964) - the first appearance of garnet was established at the solidus $\left(1350^{\circ} \mathrm{C}\right)$ at 23 kb . However, the reaction zone is expected to have large positive slope (see Figure 5) in which case garnet could form at appreciably lower pressures, depending on temperature. If the reaction is kinetically significant in nature at temperatures as low as $1100^{\circ} \mathrm{C}$, as seems likely from the experimental studies, then a common upper limit for equilibration pressures in alpine-type peridotite should be around 16.20 kb .

More precise definition of pressures of formation requires quantitative data on mineral chemistry, with the $\mathrm{Al}_{2} \mathrm{O}_{3}$ content of the pyroxenes being especially important (Green, 1964a; Boyd, 1970). O'Hara (1967) set up a provisional scale based on the sum $\left(\mathrm{Al}_{2} \mathrm{O}_{3}+\mathrm{Cr}_{2} \mathrm{O}_{3}+\right.$ $\mathrm{Fe}_{2} \mathrm{O}_{3}$ ) in clinopyroxene as variously contained in plagioclase, spinel, and garnet peridotites. The scale shows that with increasing pressure at constant temperature, this quantity should gradually increase until garnet begins to form, and then gradually decrease. The scale appears fairly reliable (Boyd, 1970) although control data are rather sparse and no systematic testing has been done on the effects of $\mathrm{Cr}_{2} \mathrm{O}_{3}$ and $\mathrm{Fe}_{2} \mathrm{O}_{3}$. $\mathrm{O}^{\prime} \mathrm{Hara}$ estimated equilibration pressures for alpine ultramafic complexes ranging from less than 1 kb for the New Zealand occurrences, to as high as about 17 kb for the Lizard Intrusion and rocks from the Pyrenées. He noted that his results were generally consistent with inferences made previously from detailed petrological studies of the rocks. The indication of low pressures for the New Zealand rocks is qualitatively consistent with Walcott's (1969) more recent observation that much of the Red Hill peridotite contains small amounts of anorthitic plagioclase.
3. Observations relating to the possibility of an origin by cumulus processes: An important question in establishing that alpine-type peridotite is a cumulate is, can its composition be simulated by a
fractional crystallization model based on phase equilibria data? Where the rock is relatively free of penetrative deformation, its modal composition and texture and, in particular, the makeup of the layers in which there is some suggestion of gravitative sorting would seem to require that, if it has formed by crystal settling, it be a cumulate of both olivine and orthopyroxene precipitated in proportions of about $\mathrm{Ol}_{85} \mathrm{Opx}_{15}$. Such a precipitate would not be expected to form at pressures less than about 5 kb because of the well known magmatic reaction relation between olivine and orthopyroxene at low pressures which prevents them from crystallizing simultaneously, and indeed cumulates of this constitution do not occur in large quantity in any of the better known stratiform intrusions. Olivine and orthopyroxene were precipitated together for short periods during formation of some of the cyclic units in the Stillwater, Bushveld, and Great Dyke Intrusions (Jackson, 1970), apparently because they were at pressures just high enough for the two minerals to have a temporary cotectic relation (Irvine, 1970), but the cumulates produced contain a maximum of only about 50 per cent olivine and grade rapidly upwards into pure orthopyroxene cumulates. On the other hand, there appears to be a possibility within the rather loose framework of liquidus relationships presently available for higher pressures (Green and Ringwood, 1967; Ito and Kennedy, 1968; O'Hara, 1968), that olivine and orthopyroxene might coprecipitate in the proportions $\mathrm{Ol}_{85} \mathrm{Opx}_{15}$ from a liquid of tholeiitic picrite composition at pressures somewhere in the range $10-20 \mathrm{~kb}$. However, the data are still far from definitive.

The $\mathrm{NiO}-\mathrm{Cr}_{2} \mathrm{O}_{3}$ relations shown in Figure 4 also seem critical in deciding whether or not alpine-type peridotite is a cumulate. A comparative study indicates that the relation shown by the Muskox peridotite is a characteristic pattern for fractionation of olivine and chromite from basaltic liquids at low pressures. Thus, if the pattern revealed for alpinetype peridotite in Figure 4 is also due to crystal fractionation, then either the liquid was considerably different from
basalt, or the crystallization occurred under very different conditions (the most likely possibility being higher pressures). The low $\mathrm{Cr}_{2} \mathrm{O}_{3}$ values might, for example, reflect fractionation of a relatively aluminous spinel at high pressures rather than Cr-rich chromites of the type common to stratiform intrusions. But another, perhaps more attractive possibility is that the level of $\mathrm{Cr}_{2} \mathrm{O}_{3}$ was basically established by fractionation of chromian pyroxenes and garnet (cf. O'Hara, 1968) and was then somewhat modified (most probably slightly increased) by the extraction of basaltic melt during a subsequent episode of fractional fusion, with the existing chromite being produced at that time as a refractory, residual product. In stratiform intrusions, there is commonly evidence of crystallization reaction relations of the type (Irvine, 1967)

## Chromite + Liquid $\rightarrow$ Chromian pyroxene The melting reaction suggested here would, in effect, be the reverse <br> Chromian pyroxenes + Chromian garnet $\rightarrow$ Chromite + Liquid

4. Relation of spinel composition to bulk rock composition: In attempting to understand further the large compositional range of the chromite in alpinetype peridotite, we have compared its $\mathrm{Al} /(\mathrm{Cr}+\mathrm{Al})$ ratio as indicated by its unit cell size against the bulk composition of its host rock using data from three different intrusions (Figure 6). The results show no significant correlation with $\mathrm{Cr}_{2} \mathrm{O}_{3}$ and only a vague dependency on $\mathrm{Al}_{2} \mathrm{O}_{3}$ (the Blue River Complex excepted). However, there is a rather surprising correlation with CaO (Plot B ), which must be largely contained in clinopyroxene (Plot D). Since the clinopyroxene and aluminous chromite both tend to be "interstitial", a possible interpretation is that the correlation is due to the original presence of differing percentages of a liquid component (such as basalt) containing fairly definite amounts of CaO and $\mathrm{Al}_{2} \mathrm{O}_{3}$ in a crystal aggregate of olivine, orthopyroxene, and minor Cr-rich chromite. When the liquid solidified, it could have precipitated the clinopyroxene and reacted with the


Figure 6. Plots relating the unit cell edge of chromite in alpine ultramafic complexes to the bulk composition of its host rock. In plot D, Opx and Cpx are based on a spinel peridotite norm (see text); the vertical coordinate is an estimate of the amount of Cpx occurring as modal clinopyroxene, assuming the orthopyroxene contains 3 per cent in solid solution. Blue River data from Wolfe (1966). The indicated solubility level for $\mathrm{Cr}_{2} \mathrm{O}_{3}$ in tholeiitic basalt is from Irvine and Smith (1969). The cell edge of the chromite is approximately the inverse of the ratio Al/(Cr+Al) (see Figure 3A).
chromite to produce the more aluminous spinel (Irvine, 1967).* This interpretation is consistent with the slightly higher $\mathrm{TiO}_{2}$ content of these Mount Albert rocks having the more aluminous chromite (Plot E) inasmuch as natural magmas are generally slightly enriched in $\mathrm{TiO}_{2}$ compared to derived olivine, pyroxenes, and chromite. For the rocks examined, the range of CaO is about $1 \frac{1}{2}$ per cent; hence if the inferred liquid was basaltic with a typical line content of $10-12$ per cent, its amount would be indicated to have varied over about 15 per cent. Alternatively, if the liquid were picritic, the variation could have been considerably larger, perhaps to as high as 20 or 25 per cent. The latter possibility is considered important because several studies have shown that the first liquid to be derived by partial fusion of peridotite of alpine-type composition at high pressures under anhydrous conditions is picritic rather than basaltic (O'Hara, 1965; Ito and Kennedy, 1967, 1968; Green and Ringwood, 1967). Therefore, accepting that a liquid phase was involved, two questions are raised: (1) Which of the two kinds of liquid just mentioned is the more probable? and (2) Was the liquid the pore magma of the cumulate, or undrained liquid in a residue of partial fusion? These are examined below on the basis of data from Bay of Islands.

## Bay of Islands Igneous Complex

The structure and igneous geology of the Bay of Islands Igneous Complex

[^14]have been described by Cooper (1936) and Smith (1958), and its tectonic setting by Rodgers and Neale (1963) and Stevens (1970). Only a few of its main features are mentioned here, with the emphasis on our petrologic observations.

As exposed, the complex is a discontinuous north-south belt of layered ultramafic and gabbroic rocks, about 60 miles long and 15 miles wide, contained within an allocthonous plate of a major thrust system (Rodgers and Neale, 1963). It embodies four principal segments or "plutons" in which it appears as a rude "sheet" divisible into a lower Ultramafic Zone, $2^{1 / 2}$ to 4 miles thick, and an upper Gabbro Zone of variable thickness to a maximum possibly of 3 miles. The sheet is emplaced within basic volcanic rocks that show contact metamorphism along both its roof and floor (Smith, 1958). The volcanic rocks in the roof are partly pillowed and are locally cut by numerous basic dykes; small intrusions of quartz diorite are associated; and minor bodies of albite granite are found in the Gabbro Zone (Smith, 1958). The association therefore has the essential earmarks of an ophiolite complex, and several authors have suggested that it represents a section of ancient oceanic lithosphere (Stevens, 1970; Moores, 1970; Church, this volume).

Ultramafic Zone. Through most of its thickness this zone consists of alpine-type peridotite and dunite. Layering on the scale of inches is widely developed in the peridotite. The layers in places show modal grading suggesting mineralogical sorting by magmatic currents. However, the microscopic evidence for cumulate textures is not conclusive, and there are no obvious major layers or cyclic units as in the better known stratiform intrusions. Also, while the layering is broadly conformable with the overall structure of the complex, it locally has undergone "plastic" folding, and Smith (1958) suggested that it was due to solid flow. Penetrative deformation is common in the peridotite, especially near the base of the zone (Smith, 1958).
Gabbro Zone. This zone consists largely of rocks that are readily classified as
cumulates on the basis of small-scale layering, lamination, and detailed textural features. The principal rock is olivine gabbro, which is a plagioclase-clinopyroxene-olivine cumulate. Less common is a one-pyroxene gabbro, generally a plagioclase-clinopyroxene cumulate, while relatively massive (noncumulate? ) hornblende gabbro is found locally in at least one of the main "plutons" (North Arm Mountain).

A peculiarity of the gabbroic rocks is that they only rarely contain orthopyroxene, a feature that is also evident in their chemistry in that they commonly show normative nepheline rather than hypersthene (Figure 7). This is in such contrast to the mineralogy of the alpinetype peridotite of the Ultramafic Zone, where orthopyroxene is a major phase, as to suggest a fundamental difference in genesis - if not in mechanism of formation, then in composition of parent magma or depth of crystallization. Moreover, it indicates that the gabbroic rocks were precipitated from magma of relatively low silica activity, similar perhaps to the "transitional" type of tholeiite (transitional to alkali basalt) found along the Mid-Atlantic Ridge (e.g. Muir and Tilley, 1964). Like the transitional tholeiite, the gabbroic rocks are very poor in $\mathrm{K}_{2} \mathrm{O}$ and $\mathrm{TiO}_{2}$ (Table 2-4).

In the few specimens of gabbro in which we have found orthopyroxene, olivine is absent - an antipathy that could develop during fractional crystallization by virtue of the reaction relation, olivine $\rightarrow$ orthopyroxene. It is of interest to know if this relation was effective as this might place some limit on depth of crystallization. In the "simple basalt systems" studied in the laboratory, the reaction relation obtains under anhydrous conditions only at pressures less than 5 6 kb , giving way at higher pressures to a cotectic relation (Boyd and Davis, 1964). Unfortunately we have not as yet been able to establish whether orthopyroxene ever occurs as reaction rims around the olivine grains, or, alternatively, whether the two minerals have ever precipitated together. However, comparison of the chemical composition of the rocks with the inferred liquidus relations in Figure


Figure 7. Ternary plots of normative $O I, N e$ and $Q$, with $A n$ and $A b$ combined. Cation norm based on CIPW conventions. Note that the alpine-type peridotite contains large amounts of Opx whereas most of the Bay of Islands Critical and Gabbro Zone rocks contain Ne. Plot C shows approximate liquidus boundaries for basaltic melts at 1 atmosphere and $4^{1 / 2} \mathbf{~ k b}$ (after Irvine, 1970).

7C suggests that they may have formed at pressures of about 5 kb .

Critical Zone. The contact of the Ultramafic and Gabbro Zones is marked by a seemingly transitional unit, termed the Critical Zone, consisting of feldspathic "dunite" and olivine gabbro with complexly interbanded layers and lenses of olivine clinopyroxenite, troctolitic, and anorthositic rocks. The "dunite" (which actually ranges in composition to feldspathic peridotite) is a typical olivinechromite cumulate with minor postcumulus clinopyroxene and poikilitic growths of plagioclase (now much altered). According to Smith (1958), it contains the main deposits of chromite at Bay of Islands. The olivine clinopyroxenite forms one major "layer", three miles long and up to several hundred feet thick, and numerous smaller "lenses" and thin layers (Smith, 1958). The troctolite is gradational to both dunite and gabbro, while the anorthosite occurs in thin layers that are almost certainly formed by the sorting and concentration of plagioclase through the action of magmatic currents. The Critical Zone does not have a well defined "stratigraphy" that can be traced for any distance along its length, and according to Smith (1958) some of the layers and lenses are slightly discordant to the general contact trend of the Ultramafic and Gabbro Zones. However, the layering and repetition of contrasting rock types are typical of stratiform intrusions, and in our experience the zone is particularly reminiscent of a complexly interstratified sequence of compositionally and texturally almost identical rocks in the middle of the Muskox Intrusion (Layers 10 and 11; Findlay and Smith, 1965). This latter sequence formed by accumulation of olivine, clinopyroxene and plagioclase precipitated in different proportions by fractional crystallization of basaltic magma at shallow depths during a period when fresh magma was repeatedly introduced into the intrusion (Irvine, 1970). While the Bay of Islands Critical Zone is thicker and structurally more complicated, we feel that it must have much the same origin. Notable in this respect is that
$\mathrm{NiO}-\mathrm{Cr}_{2} \mathrm{O}_{3}$ relations in the Critical Zone are the same as observed in the ultramafic cumulates of the Muskox Intrusion (Figure 4).

Compositionally, the rocks of the Critical Zone appear more closely tied to the Gabbro Zone than to the alpine-type peridotite that underlies them. Besides containing feldspar, they are like the gabbro in that they rarely contain orthopyroxene. The chemical data suggest that the base of the Critical Zone is a discontinuity in that it is the first level in the complex at which $\mathrm{Na}_{2} \mathrm{O}, \mathrm{TiO}_{2}, \mathrm{Ba}$, $\mathrm{Sr}, \mathrm{Sc}$ and Cu were detected with certainty by the analytical methods used (Tables 2-4 and 6-8). Moreover, the chromite in the Critical Zone is different from that in the alpine-type peridotite immediately beneath in that it is opaque rather than red and has a larger unit cell size (Figure 8), possibly indicating a lower Al/(Cr+Al) ratio. This last feature, if correctly inferred, together with the presence of feldspar, suggests that the Critical Zone solidified at appreciably lower pressures than the peridotite (see Figure 5). However, confirmation of this inference must await a quantitative study of the mineral chemistry and an evaluation of the effect of the slightly higher $\mathrm{Na}_{2} \mathrm{O}$ content of the Critical Zone.

The contrast between the Critical and Ultramafic Zones appears to be of major importance in view of Smith's (1958) suggestion, based mainly on structural relations, that the Bay of Islands Complex was emplaced with the ultramafic rocks largely solid and the gabbro in a much more fluid state. From present knowledge and observations, it seems clear that the alpine-type peridotite was the solid part, and that the ultramafic and other rocks of the Critical Zone are early differentiates of the gabbro parent magma precipitated during the general period of instability that accompanied its intrusion. The problem is whether the peridotite is a still earlier differentiate of the same magma, formed at some appreciably greater depth and then remobilized when the complex was emplaced in its present country rocks, or whether it is a block of residual mantle material, perhaps having no direct compositional relation to
the gabbroic magma, that in some way came to serve as the floor on which the overlying cumulates were deposited. Since the peridotite is layered in a fairly regular manner, the first possibility can be tested by looking for effects of fractional crystallization. This matter is now considered.
Mineralogical and chemical variations through the complex: Figure 8 shows olivine and whole rock $\mathrm{Mg} /\left(\mathrm{Mg}+\mathrm{Fe}^{+2}\right)$ ratios for samples collected across two of the plutons in the Bay of Islands Complex, together with data on the NiO and $\mathrm{Cr}_{2} \mathrm{O}_{3}$ contents of the rocks, the unit cell size of the chromite, and the amount of CaO in the Ultramafic Zone. The sample interval is too large to give good definition of possible "stratigraphic" trends (especially within the Critical Zone), but the data indicate certain broad features, and since both the main zones appear relatively uniform in the field we tentatively accept the illustrated features as representative.

The $\mathrm{Mg} /\left(\mathrm{Mg}+\mathrm{Fe}^{+2}\right)$ ratios show distinct (although very irregular) trends of upward decrease through the rocks of the Critical and Gabbro Zones - as they should if the rocks are cumulates formed by fractional crystallization. However, in the alpine-type peridotite of the Ultramafic Zone their total range of variation is only about 3 percentage units, and possible overall trends, even if real, are extremely slight. At Table Mountain, the ratios of both olivine and whole rock show some indication of upward decrease, but the maximum change that could possibly be suggested from the data is only about 2 percentage units through what may be as much as four miles of section. In the North Arm Mountain pluton the $\mathrm{Mg} /(\mathrm{Mg}+\mathrm{Fe})$ ratio of the rock is essentially constant while that of olivine appears to increase upwards, the opposite of a fractional crystallization trend.

NiO and $\mathrm{Cr}_{2} \mathrm{O}_{3}$ decrease sharply from the ultramafic to the gabbroic rocks, as in many intrusions; and a slight increase in their concentrations about a third the way up the North Arm Mountain gabbro may signify an addition of "fresh" magma, as is common in strati-


Figure 8. Mineralogical and chemical variations through the Bay of Islands Complex. A. Table Mountain; B. North Arm Mountain. In each section the Ultramafic Zone is about three miles thick. The light "trend lines" (and the $\Delta$ - values) are intended only to facilitate comparison; they are not fitted statistically, and they may not be significant genetically. Olivine compositions were determined by the x-ray method of Jambor and Smith (1964).
form intrusions. In the Ultramafic Zone, local variations are large, but overall trends of upward increase are suggested for both NiO and $\mathrm{Cr}_{2} \mathrm{O}_{3}$ at Table Mountain - again, the inverse of the trends expected from fractional crystallization, at least of basaltic magmas. As noted previously, the relation of NiO and $\mathrm{Cr}_{2} \mathrm{O}_{3}$ is not typical of established cumulate peridotites (Figure 4).

The data therefore do not support an hypothesis that the alpine-type peridotite was formed by fractional crystallization; in fact, on the basis of the criteria suggested earlier, they favour the alternative, that the peridotite is a residue of a partial fusion process. However, it is not unknown in layered intrusions for stratigraphic trends of $\mathrm{Mg} /\left(\mathrm{Mg}+\mathrm{Fe}^{+2}\right)$ to be weak, non-systematic, or the inverse of the trend expected from fractional crystallization. Thick sections of ultramafic cumulates in the Duke Island Ultramafic Complex, Alaska, show no strong trends of variation (Irvine, 1959); and inverse trends are shown by cumulus olivine in the lower parts of the Muskox Intrusion (Smith and Kapp, 1963) and Stillwater Complex (Jackson, 1970), and by cumulus hypersthene near the lower (outer) edge of the Sudbury Irruptive (Naldrett et al., 1970). The following analysis of the problem is therefore undertaken before drawing conclusions.

Discussion of the $\mathrm{Mg}-\mathrm{Fe}$ variations: Among the factors that might affect the $\mathrm{Mg} /\left(\mathrm{Mg}+\mathrm{Fe}^{+2}\right)$ ratios of mafic minerals in igneous rocks are two principal ones that can be examined on a more or less quantitative basis: (1) crystal fractionation, and (2) reaction with trapped interstitial (e.g. intercumulus) liquid. The first is illustrated in Figure 9A, which shows theoretical fractionation curves for olivine where the first crystals have the compositions given by the abscissa intercepts. The curves are calculated assuming a distribution coefficient

$$
\mathrm{K}_{\mathrm{D}}=\left(\frac{\mathrm{Mg}}{\mathrm{Fe}+2}\right)^{\text {liquid }} /\left(\frac{\mathrm{Mg}}{\mathrm{Fe}^{+2}}\right)^{\text {solid }}=0.3
$$

as was found by Roeder and Emslie (1970) to be characteristic of olivineliquid equilibria over a wide range of liquid compositions and temperatures.

Fractionation curves for the pyroxenes should be very similar, because the coefficients describing the distribution of Mg and $\mathrm{Fe}^{+2}$ between olivine and pyroxene at magmatic temperatures are close to unity (Nafziger and Muan, 1967). The light curves with $\Delta$ labels indicate the differences in composition between crystals precipitated as fractionation progresses and the first crystals. In the simple case of olivine crystallizing from an olivine melt, the ordinate is per cent solidification. However, in natural situations the liquid will generally have a different percentage content of $\left(\mathrm{Mg}+\mathrm{Fe}^{+2}\right)$ than the minerals that crystallize from it, and more than one mineral may precipitate at a time; consequently to obtain per cent crystallization, the ordinate scale must be adjusted by multiplying it by the ratio
$\left(\mathrm{Mg}+\mathrm{Fe}^{+2}\right)$ initial liquid /
$\left(\mathrm{Mg}+\mathrm{Fe}^{+2}\right)$ fractionated solids
where the denominator is a constant. Thus, for olivine precipitating from basaltic liquid, the adjustment factor is about 20/67 (see inset, Figure 9A), and if a second mineral such as plagioclase were subsequently to join the olivine, then it would be necessary to define a new factor based on the bulk $\left(\mathrm{Mg}+\mathrm{Fe}^{+2}\right)$ content of the precipitate and the current composition of the liquid, and to start over again in terms of per cent solidification of the remaining liquid using the fractionation curve appropriate to the current $\mathrm{Mg} /\left(\mathrm{Mg}+\mathrm{Fe}^{+2}\right)$ ratio of the olivine.

Considering the fractionation curves in reference to the present problem, it is notable that, if the percentage ratio $\mathrm{Mg} /\left(\mathrm{Mg}+\mathrm{Fe}^{+2}\right)$ of the first crystals is greater than 90 , then the rate of change in the composition of subsequent crystals with solidification will for a time be appreciably slower than for a value of 87 , the common upper limit for cumulus olivine in some stratiform intrusions formed from basaltic magmas (e.g. the Stillwater and Muscox Intrusions). If we add to this the possibility that the more magnesian olivine might have precipitated from a picritic liquid containing, say, 40 per cent ( $\mathrm{Mg}+\mathrm{Fe}^{+2}$ ) (equivalent to about 40 per cent normative olivine) rather than
from basalt, then we see what might be at least a partial explanation of why there is such relatively little variation in the composition of olivine in alpine-type peridotite. However, the percentage amount of olivine that can be derived even in the more magnesian system without causing appreciable change in the fractionating crystals is still relatively small. For example, if the first crystals were $\mathrm{FO}_{93}$ and the liquid contained 40 per cent $\left(\mathrm{Mg}+\mathrm{Fe}^{+2}\right)$, the Fo-content of later crystals should be lower by 2 percentage units by the time the liquid was only 18 per cent solidified. Thus, applied to the Table Mountain section (Figure 8A) even those rather optimum conditions would require that the Ultramafic Zone represent less than a fifth of its parent magma, whereas the unit forms well over half the volume of the Bay of Islands Complex as presently exposed. It is perhaps possible that a large amount of a residual liquid was lost from the complex - for example while it was being emplaced (reintruded?) with the peridotite solidified - but the whole situation is rather unprecedented, especially from the viewpoint that none of the well know stratiform-type layered intrusions contain such large volumes of peridotitic cumulates without showing conspicuous cyclic units defined by major layers of pyroxenite or gabbro. (The ultramafic cumulates of the Great Dyke provide some parallel, consisting as they do of highly magnesian olivine and orthopyroxene, but they feature a great deal of cyclic repetition, cf. Worst (1960); Jackson (1970).) However, a still more critical point arising directly from our data is that it appears likely that the $2-$ 3 per cent variation in the $\mathrm{Mg} /\left(\mathrm{Mg}+\mathrm{Fe}^{+2}\right)$ ratios of the Bay of Islands peridotite including the apparent "inverse trend" shown by olivine at North Arm Mountain - is largely due to variations in amount of trapped interstitial liquid. This, if true, leaves little basis on which even to attempt to apply the fractionation curves.

The effect of equilibration with trapped interstitial liquid can be evaluated by means of Figure 9B. Examining first the main diagram, where the fractionation curves now serve simply to


Figure 9. Curves showing the theoretical effect of fractional crystallization on $\mathbf{M g} /\left(\mathrm{Mg}+\mathrm{Fe}^{+2}\right)$ in olivine and its parent liquid in a system "closed" or "unbuffered" with respect to oxygen. For explanation, see text.
illustrate the equilibrium compositions of coexisting olivines and liquids, it is seen that for olivine in the range $\mathrm{FO}_{89}$ to $\mathrm{FO}_{92}$, such as found in alpine-type peridotite, the $\mathrm{Mg} /\left(\mathrm{Mg}+\mathrm{Fe}^{2}\right)$ ratio of the liquid should be lower by some 13 percentage units. The phase diagram in the inset shows schematically how an increased porportion of the liquid (represented in the succession of "mixtures" a-b-c) can cause the olivine to become increasingly enriched in iron. In natural situations, the critical factor is not just the proportions of liquid and solid, but the ratio:
Per cent liquid $x$ per cent $\left(\mathrm{Mg}+\mathrm{Fe}^{* 2}\right)$ in
the liquid
Per cent liquid $x$ per cent $\left(\mathrm{Mg}+\mathrm{Fe}^{+2}\right)$ in the solid
Hence, other things being equal, a picritic liquid should have more affect than basaltic liquid, and basaltic liquid should have more affect in gabbroic rocks than in ultramafic rocks.

Quantitative application of Figure 9B to the Bay of Islands Complex shows that to change the Fo-content of the olivine in the peridotite by 2 percentage units would require about 40 per cent of interstitial basaltic liquid. From textural relations and the low $\mathrm{Na}_{2} \mathrm{O}$ content of the peridotite, it is clear that this amount is too large. However, the same change could be effected by only 20-25 per cent picritic liquid (Na-poor), and, although this quantity is perhaps also rather high, it is the same amount as was suggested earlier for picritic liquid from the correlation between CaO and chromite cell edge. Moreover, the data in Figure 8 show that the $\mathrm{Mg} /\left(\mathrm{Mg}+\mathrm{Fe}^{+2}\right)$ ratios of the peridotite and its olivine do bear the appropriate relation to the CaO content of the rock and the cell edge of the chromite. As a rule, if these ratios are low, CaO is high and cell edge is low (implying the presence of a relatively large amount of liquid); if they are high, the opposite obtains. These correlations are not strong, but this is not surprising considering that the variations are so small and that there might be other complicating factors*. The

[^15]evidence therefore seems reasonably good that the inferred effect is significant and has lowered the $\mathrm{Mg} /\left(\mathrm{Mg}+\mathrm{Fe}^{+2}\right)$ ratios of the samples richest in CaO by $1-2$ percentage units.

Differences in amount of trapped interstitial (intercumulus) liquid are probably also partly responsible for the erratic $\mathrm{Mg} /\left(\mathrm{Mg}+\mathrm{Fe}^{+2}\right)$ variations in the Gabbro Zone. In the compositional range of the Gabbro the ratios of the liquid and the cumulus mafic minerals should have differed by $25-30$ percentage units, and accordingly, equilibration of the crystals with 15 per cent of the liquid should have lowered their ratio by about 5 percentage units. If the equilibration was incomplete, still lower ratios could have resulted.

## Conclusions

On the basis of the foregoing discussion the following conclusions appear valid for the Bay of Islands alpine-type peridotite, and probably apply also to the peridotites at Mount Albert and Blue River:
(1) Prior to its final solidification, the peridotite was an aggregate of olivine, subordinate orthopyroxene and minor Cr-rich chromite with a variable content, from 0 to about 20 per cent, of interstitial liquid, probably of picritic composition.
(2) At this stage, the Fo-content of the olivine was virtually constant at a value close to its present upper limit - that is, in the approximate range $\mathrm{FO}_{9} 0.5$ to Fog 2.

These features would suggest that the peridotite is the residue of a fractional melting process in which it was subjected to prolonged heating under very gentle thermal gradients, with the melt being slowly filtered off so that, through reaction, it had a homogenizing effect.

This interpretation does not eliminate the possibility that the alpine-type peridotite was originally a cumulate; in fact, it would even allow that the melt was partly composed of intercumulus liquid. However, it does seem clear that
the peridotite has had a very different sub-liquidus history from the feldspathic dunite and other ultramafic rocks that overlie it, with several features suggesting that it solidified at considerably greater depths. On this basis, therefore, the rock could be regarded as a block of mantle material quite independent in origin from the cumulates of the Critical and Gabbro Zones, except for being the floor on which they accumulated. Moreover, since the roof of the Gabbro Zone is basalt, a possible extension of this postulate is that the gabbro magma was intruded along the interface between the mantle and crust. In an oceanic environment, the situation would be essentially like that pictured by Dewey and Bird (1970, fig. 4C) in their model of oceanic lithosphere.

We have no strong convictions in respect to these last interpretations their evaluation requires detailed know. ledge of the regional structure of the Bay of Islands area. An obvious problem is the presence of contact metamorphosed basalt beneath the Ultramafic Zone, but possibly this is in some way accounted for in the process of transfer of the complex from an oceanic to the continental regime.

Our main point is that the complex comprises two distinct kinds of olivinerich ultramafic rocks of apparently two distinct origins - one, the feldspathic "dunite" of the Critical Zone, undoubtedly a cumulate, and the other, the alpine-type peridotite of the Ultramafic Zone, probably a residue of partial fusion solidified at considerably greater depths. Several authors have suggested that the Bay of Islands Igneous Complex is "intermediate" or "transitional" between stratiform and alpine complexes. It would seem more accurate to say that it is a combination of a rudely stratiform intrusion with alpine-type peridotite.

It is intriguing to speculate that such a combination might be fairly common in alpine ultramafic complexes. This could account for many of the seemingly dichotomous features and relations that have lead to the conflicting interpretations expressed in the literature. For example, could it be that the small irregular bodies of dunite with associated
pods and veins of chromite found within alpine-type peridotite are residual materials, recrystallized and to some extent redistributed during partial fusion and degassing of the mantle, while the larger zones of dunite with layered deposits of chromite are cumulates in adjoining intrusions? If the cumulates formed at fairly great depths, they might show similar mineralogy and be subject to the same deformation as the peridotite. Also, the interface between a peridotitic mantle and basaltic crust would seem a very likely site for emplacement of stratiform intrusions. Being a major structural and density discontinuity, it would be somewhat analogous to the unconformities between crystalline basement rocks and overlying sedimentary deposits that are commonly the locus of major basaltic and diabasic intrusions in the continents.

In reference to the specific problem posed for this symposium - the identification of ancient oceanic lithosphere two observations from this study seem particularly significant:
(1) The Bay of Islands Critical and Gabbro Zones comprise the kinds of cumulates that would be expected to form from a K-poor, Ti-poor "transitional tholeiite" magma of the type common to the mid-ocean ridges. The objection has been made that ophiolite complexes thought to represent oceanic lithosphere do not contain this kind of basalt (Engel and Fisher, 1969) but this does not seem appropriate to Bay of Islands.
(2) There is little if any alpine-type peridotite in the Canadian Shield. An intriguing possibility is that there might be a distinctly different, "Precambrian alpine-type peridotite" representative of a very early, more primitive mantle, but at the moment we cannot point to a specific ultramafic body in the Shield that would seem to fit such a category. An alternative, of course, is that tectonic conditions or processes were sufficiently different in Precambrian times that solid mantle material was not emplaced into the continental crust.

Finally, it is suggested that the
difference between cumulate and alpinetype peridotites revealed by the plots of NiO vs $\mathrm{Cr}_{2} \mathrm{O}_{3}$ in Figure 4 may be a useful additional criterion for distinguishing these rocks among altered materials dredged from the ocean floor. The dis crimination is not unequivocal, but an examination of many data besides those illustrated indicates that it is very good on a percentage basis. The difference may also prove to be one of the more useful clues toward defining the nature and origin of alpine-type peridotite before it underwent partial fusion, if indeed this has been one of the stages in its development.

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No. 9

# some physical and chemical aspects of precambrian volcanic belts of the canadian shields 

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Abstract. This paper reviews some of the physical and chemical characteristics of Precambrian greenstone belts of the Canadian Shield; mainly those of Noranda, Yellowknife, and Uchi Lake (Archean) and of the Grenville Province (Proterozoic). The greenstone belts are thick, mainly conformable successions of volcanic rocks characterized by a cyclic, upward change in lithology and composition from basic to acid. Basic and ultrabasic sills and iron-formation are commonly present, particularly in the basic and acid fractions respectively. The boundary relationships of the greenstone belts are generally obscured by intrusive granites, but the Labrador Trough and possibly the Yellowknife belt, appear to be founded upon continental crust. The composition of the basaltic fraction of the greenstone assemblages is similar to oceanic tholeiite except for slightly higher potash content, iron-magnesium ratio, and lower alumina content. The intermediate to acidic fraction resembles the calo-alkaline succession of the circumpacific belt except for generally lower potash contents and contrasting alumina differentiation trends. In circumpacific successions alumina is characteristically depleted with differentiation from high-alumina basalts to low-alumina felsites, whereas in Precambrian successions, which commence with low-alumina basalts, it may be either enriched, maintained at about the same level, or depleted with differentiation.

The characteristics of Precambrian greenstone belts taken together, contrast markedly with those of oceanio-ridge assemblages. It might be supposed that the basic fraction of the greenstone belts was generated at the ridge and the acid fraction at the subduction zone. If so, the continuous sequential transition from basic to acidic rocks, the repetition of basic to acid cycles, and the compositional distinctions manifest between Precambrian greenstone assemblages and their supposed oceanic and circumoceanic counterparts, would be difficult to explain.

## Introduction

The purpose of this symposium, to survey the continents for possible remnants of ancient ocean crusts, limits the scope of this paper to the greenstone belts, a term that will be used throughout this paper. The plateau basalts of Coppermine River. Lake Superior, and Seal Lake regions are subaerial for the most part and were deposited on the continents. They could not, therefore, have been oceanic crust. Most of the material herein is drawn from the Archean belts near Yellowknife, Uchi Lake, and Noranda, and from the Proterozoic belts near Kaladar in the Grenville Province, and the Labrador Trough. The purpose is to review the principal physical and chemical properties of Precambrian greenstone belts so that they may be compared with those of oceanic deposits.

## Physical aspects of Precambrian greenstone belts

Greenstone belts, a name reflecting the
generally low-grade metamorphic character of the volcanic rocks, are widely scattered in the Canadian Shield. They are generally linear in form with the exception, principally, of the Yellowknife Group which appears to have formed in a broad basin. Volcanic rocks typically form the basal and predominant part of the greenstone belts. Exceptions are the Yellowknife Group where sedimentary rocks predominate, and the Labrador Trough where volcanic rocks are late in the sequence. The volcanic rocks are mostily or entirely of submarine deposition and are commonly interlayered with thin cherty beds. Pillowed lavas are characteristic of the volcanic assemblage. Quartzose greywackes, impure quartzites and slates appear to be the principal associated sediments. According to some authors (Goodwin and Shklanka, 1967; Ridler, 1970; Ayres, 1969) such sediments are mainly volcanogenic. However, Donaldson and Jackson (1965) and McGlynn and Henderson (in press) find that sediments associated with voicanic belts in north-
western Ontario and Mackenzie District respectively contain a higher proportion of coarse quartz than is consistent with a volcanogenic origin. In addition, associated conglomerates contain at least subordinate quantities of granitoid boulders. Thus, they conclude that the sediments are partly derived from preexisting sialic basement.

Volcanic sequences in the greenstone belts are typically thick; $30,000-50,000$ feet being not uncommon (e.g. Goodwin, 1967; Baragar, 1966, 1968; Ridler, 1969). Less is known about the accompanying sediments, which are more readily deformed and accordingly less easily measured.

The volcanic rocks of the greenstone belts are predominantly basaltic. Baragar and Goodwin (1969) estimated the relative proportions of the main volcanic classes in four well-studied Archean belts as: basalts -60 per cent; andesites -28 per cent; and remaining salic rocks -12 per cent.

Metamorphic grades are generally low - mainly greenschist or low amphibolite facies - and structures in the volcanic rocks are commonly little deformed.

The stratigraphy of Precambrian volcanic assemblages in the greenstone belts is exemplified by the four stratigraphic sections given in Figure 1. Three Archean belts - Uchi Lake (Goodwin, 1967); Yellowknife (Henderson and Brown, 1966; Baragar, 1966); and Noranda (Baragar, 1968); - and one Proterozoic belt (Grenville, Sethuraman, 1970) are represented. The Grenville section is a synthesis of two partial sections but it is believed that they can be joined together as shown here with little misfit (Sethuraman, 1970).

The principal features of the stratigraphy are as follows:


Figure 1. Comparison of stratigraphic sections characteristic of four Precambrian greenstone belts. The stratigraphic position of the offset segment of the Duparquet section is uncertain, but it is at least partly younger than the main section.
(1) The lithology changes systematically from basic to salic upward in the succession. The change is not generally abrupt but takes place over a stratigraphic range of varying thickness by interlayering of flows of different composition.
(2) More than one mafic to acid cycle may be present in any one succession. Examples shown here are Yellowknife and Uchi Lake. Ridler (1969) recognizes parts of three cycles in the Kirkland Lake region.
(3) The entire succession of a greenstone belt, regardless of number of cycles, is generally conformable. An exception is in the Yellowknife section where an unconformity occurs high in the upper cycle. However, elsewhere in the Yellowkife Group no unconformity is recognized at this level.
(4). The mafic fractions of the volcanic sequences are dominated by pillowed and massive flows whereas the salic or acid fractions are dominated by fragmental rocks.
(5) The mafic rocks show repeated evidence throughout the sections of submarine deposition but the salic rocks rarely show evidence of either submarine or subaerial deposition.
(6) Mafic sills with compositions similar to their host rocks are generally abundant in the lower parts of the volcanic sequences.
(7) Iron-formation, although present only in the Uchi Lake section of Figure 1, is a characteristic component of Precambrian yolcanic belts. It commonly occurs near the tops of the volcanic cycles or in the immediately overlying sediments. Examples are the Bee Lake and Michipicotin belts described by Goodwin and Shklanka (1967), the Timmins-Kirkland LakeNoranda belt described by Goodwin (1965a) and Ridler (1970a) and the Ennadai-Tavani belt observed recently by Ridler (1970, personal communication).
(8). Ultramafic sills are not shown separately in Figure 1. Although not present in
most of these sections, they are a common associate of the greenstone belts and commonly appear with the mafic fraction (Naldrett and Mason, 1968; MacRae, 1969). Whether or not they occupy a distinctive stratigraphic position in most greenstone belts is not known. In the Labrador Trough they are late components of the volcanic succession.

Most of the Precambrian greenstone belts are bounded by intrusive granites. Accordingly the bases of the successions are rarely preserved and the nature of their floors is generally unknown. An exception is the Aphebian Labrador Trough which is clearly founded on Archean continental crust (Baragar, 1967; Dimroth et al, in press). Among Archean belts some evidence exists that the Yellowknife Group was similarly deposited upon continental crust (Baragar, 1966; Heywood and Davidson, 1969; McGlynn and Henderson, 1970). Because of the importance of this point to the present discus. sions some of the evidence might be briefly reviewed here.

In the Cameron River area about 45 miles east of Yellowknife volcanic rocks of the lower Yellowknife Group (there about 9,000 feet thick) are bounded on the west side by the conformably overlying greywacke and slates and on the east side by granitic gneisses. The contact between the gneisses and flows is generally concordant with the attitude of the flows but no clear evidence is present as to the nature of the contact. A swarm of closely-spaced mafic dykes roughly parallel in attitude to the contact, intrudes both gneisses and flows in great profusion but does not penetrate the overlying sediments. A few miles farther east a younger, generally massive granite invades the gneisses and the dykes that intrude them. The mafic dyke swarm can reasonably be assumed to be the subsurface expression of the Yellowknife volcanic rocks and, if so, the granitic gneisses are clearly basement to the Yellowknife Group. Green (1968), on the basis of $\mathrm{Rb}-\mathrm{Sr}$ ages has disputed this conclusion. Nevertheless, some 80 miles to the east a similar relationship between gneisses intruded by mafic dykes and structurally overlying Yellowknife vol-
canic rocks led Heywood and Davidson (1969) to the same conclusion. McGlynn and Henderson (in press) citing, in addition, Stockwell's (1933) evidence of a basal conglomerate in the Yellowknife Group at Point Lake generally concur in this interpretation.

## Chemical properties of the greenstone belts

Three aspects of the chemistry of Precambrian greenstone belts are presented in this section: the bulk compositions; the variation of composition with time in the eruptive sequence; and the relative variation between chemical components of each succession.

## Bulk compositions

The most characteristic bulk composition of a volcanic sequence is probably that of the basalts erupted early in the sequence. These can be expected to be close to the parent magma in composition.

Table I shows the average compositions of basalts from a number of Precambrian greenstone belts. The Archean and Grenville averages are from systematically sampled sequences and are probably representative of basalts in these sequences. The average basalt of the Labrador Trough comprises analyses from widely scattered localities and a number of sources. Nevertheless because of the general similarity of most of the individual analyses it too is probably close to a representative result. An average of 25 oceanic tholeiites is given for comparison.

The method of classifying analyses as basalts is that followed by Baragar and Goodwin (1969) utilizing normative colour index and plagioclase composition, but including both the basalt and Type A categories of that publication. Thus all analyses that comprise the averages of Table I have been selected by the same criteria.

The average basalts of Table I are remarkably similar although the oceanic tholeiite is slightly more primitive. That is to say, the usual measures of differentiation - potash content, iron-magnesium ratio - are somewhat lower. The most significant differences between the aceanic tholeiite and the Precambrian basalts are

Table I
Comparison of average analyses of Precambrian basalts with an average of some oceanic bealits

|  |  | $\mathrm{SiO}_{2}$ | $\mathrm{Al}_{2} \mathrm{O}_{3}$ | $\mathrm{Fe}_{2} \mathrm{O}_{3}$ | FeO | CaO | MgO | $\mathrm{Na}_{2} \mathrm{O}$ | $\mathrm{K}_{2} \mathrm{O}$ | $\mathrm{TiO}_{2}$ | $\mathrm{P}_{2} \mathrm{O}_{5}$ | MnO | $\mathrm{CO}_{2}$ | $\mathrm{H}_{2} \mathrm{O}$ | $\mathrm{CO}_{2}$ | + $\mathrm{H}_{2} \mathrm{O}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. Bitch-Uchi | 56 | 48.7 | 15.0 | 2.57 | 8.60 | 8.82 | 5.83 | 2.30 | . 36 | . 95 |  | . 20 |  |  | 5.35 ) |  |
| 2. Lake of the Woods Wabigoon | 181 | 50.0 | 14.5 | 2.72 | 9.05 | 8.60 | 5.95 | 2.45 | . 40 | 1.01 | . 26 | . 21 |  |  | 5.10 | Archean |
| 3. Timmins Noranda | 141 | 50.2 | 14.4 | 2.32 | 9.13 | 9.39 | 6.01 | 2.68 | . 26 | 1.24 | . 13 | . 20 | 1.23 | 3.32 | 4.55 |  |
| 4. Yellowknife | 69 | 50.1 | 15.0 | 2.78 | 9.38 | 9.50 | 6.50 | 2.24 | . 34 | 1.11 |  | . 18 | . 30 |  |  |  |
| 5. Labrador Trough | 22 | 48.8 | 14.1 | 2.36 | 9.78 | 10.07 | 7.28 | 2.52 | . 22 | 1.08 | . 10 | . 22 | . 22 | 3.14 | 3.36 | Aphebian |
| 6. Grenville | 29 | 48.0 | 14.7 | 1.89 | 10.30 | 9.83 | 8.12 | 3.27 | . 20 | 1.06 | . 10 | . 19 | 1.64 | 1.63 | 3.27 | Neohelikian |
| 7. Oceanic Tholeïtes | 25 | 49.29 | 16.89 | 2.06 | 6.79 | 11.55 | 7.46 | 2.81 | . 18 | 1.37 | . 12 | . 16 |  | 1.12 |  |  |

 Grenville, Average 5, Dimroth et al (in press). Average 6 produced on the basis of results reported in Sethuraman, 1970 . Average 7 for analytes reported by Nicholls et alo, 1964; Engel and Engel, 1963; Engel, Engel, and Hivens, 1965; Engel, Fisher, and Engel, 1965, Cann and Vine, 1966; Engel and Fisher, 1969.
the lower alumina, and less markedly, lime and titania contents of the latter.

Note that there is no evidence of an evolution in basaltic composition with time in these averages. Fahrig (1970) and Mueller (1970) found a consistent potash enrichment in Precambrian diabase dykes of diminishing age and Mueller, in addition, found parallel enrichment in titania and impoverishment in magnesia.

## Variations of composition with time in the eruptive sequence

The variation of lava composition with time in an eruptive sequence has been examined in a few thick, closely sampled stratigraphic sections in the Yellowknife, Noranda, and Grenville volcanic belts (Baragar, 1966, 1968;Sethuraman, 1970). In Figure 2 results from the three sections are presented. Samples in each section were generally taken at 400 - or 500 -foot stratigraphic intervals but to eliminate local scattering the results have been averaged over intervals of chiefly 3,000 (Grenville) and 5,000 (Yellowknife, Noranda) feet. Salic rocks in the Yellowknife section have been averaged separately. The average analysis of each interval has been plotted at the mid-point of the interval. The two segments of the Grenville section have been joined to give a continuous section as is believed appro-
priate on the basis of field work (Sethuraman, 1970).

Note that the Yellowknife section includes two basic to acidic cycles each of about the same thickness as the Grenville section. The Noranda section, on the other hand, although nearly as thick as the two Yellowknife cycles together does not span a complete cycle in that acidic rocks are virtually absent. Minor amounts of salic fragments are found in the upper parts of the Noranda section and these are thought to be stratigraphically equivalent to major acidic units farther east.

The major features to be noted from Figure 2 are:
(1) The rocks become progressively less mafic with time; that is, upward in the volcanic sequence. This is represented in a gross way by the colour index and in more detail by the marked upward decline in iron, magnesia, and to lesser degree, titania contents.
(2) The rocks become more alkalic and siliceous with time. The proportion of lime generally diminishes while that of alkalis and silica rises. In the case of Noranda, which is an extended mafic part of the cycle, the changes are less marked.
(3) The alumina content of both Noranda and Grenville sequences increases steadily with increasing stratigraphic level. The upper cycle of the Yellowknife section tends towards a similar trend.

The changes in composition with stratigraphic level illustrated by these three sections are probably characteristic of Precambrian greenstone belts in general, as evident in studies by Goodwin in the Birch-Uchi (1967) and Lake of the WoodsWabigoon (1965) areas and by Ridler (1969) in the Kirkland Lake area. The salient feature of the changing composition is the mafic to acidic eruptive cycle.

## Relative variations between chemical components

The chemical characteristics of magmatic provinces are generally distinguished by the manner in which their constituents vary with respect to one another, In Figures 3 to 6 are illustrated some of the variations that may be characteristic of Precambrian greenstone belts.

Figure 3 shows projections onto the base of the Diopside-Olivine-NephelineQuartz tetrahedron of average analyses from the Uchi Lake, Yellowknife, Noranda, and Grenville sections of Figure 1. The last three sections are represented


Figure 2. The variation of volcanic compositions with stratigraphic level in well-sampled sections of three Precambrian greenstone belts. Sample interval is 400 500 feet stratigraphically but the plotted points are average analyses for each 3,000-foot (Grenvile) or 5,000 -foot (Yellowknife and Noranda) stratigraphic interval. Acidic rocks in the Yellowknife section are averaged separately.
by the 5,000 -foot and 3,000 -foot averages of Figure 2, and the Uchi section by average analyses of the basic and acidic segments of each cycle (Goodwin, 1967). In addition are plotted the average basalt, andesite, and salic rock for the Archean of the Canadian Shield as determined by Baragar and Goodwin (1969). In these plots the analyses are totally recast into normative olivine, nepheline, and quartz. The purpose of the diagrams is to show clearly the contrast between trends leading to feldspathoidal, and to quartz enrichment, respectively.

The trends of the Precambrian sequences are all sharply directed towards the quartz apex. Most of them originate well within the tholeiitic field but the Grenville sequence does commence on the alkali basalt side of the plane of critical undersaturation. Clearly the major trend of the Precambrian sequences is towards silica enrichment. This contrasts with what we know of trends along much of the midocean ridges where tholeiitic substructures are commonly topped by feldspathoidal rocks of the islands (Engel et al, 1965).

One exception to the general Precambrian trend of silica enrichment is the Timiskaming feldspathoid-bearing yolcanic rocks at Kirkland Lake (Cooke and Moorehouse, 1969). Ridler (1969) has suggested that these form the upper part of the greenstone succession of that region rather than a discrete volcanic episode unrelated to the greenstones.

Another aspect of the chemistry of Precambrian greenstone belts is shown in the alkali-iron-magnesium diagrams of Figure 4. In each of the three greenstone belts (Yellowknife, Grenville, Noranda) represented in the figure two trends of differentiation are evident. One represents enrichment in iron relative to magnesiathe tholeiitic trend-; the other represents enrichment in alkalis with negligible enrichment in iron - the calc-alkaline trend. The former is the common differentiation trend of mafic intrusions crystallizing at shallow depths. Indeed, the trends of differentiated mafic sills from each of the Yellowknife and Noranda sections shown in the diagram, parallel the tholeiitic trend of the lavas. Thus it seems reasonable to attribute this trend to fructional crystal-
lization of the mafic magma in high-level reservoirs such as the accompanying sills.

The other trend is that which may be traced upward through the stratigraphic successions (Figure 2) and is evidently a more fundamental attribute of the volcanism. It is similar to calc-alkaline trends of the circumpacific belt but differs in some important respects which will be noted in the next two diagrams.

Figure 5 shows plats of normative An-Ab-Or for Yellowknife and Noranda rocks. Because the sections sampled at Noranda contained few acidic volcanic rocks these are not well represented in the diagram. The diagrams illustrate two features of Precambrian greenstone belts: the lack of a coherent trend, and a general impoverishment in orthoclase relative to rocks of the circumpacific* belt. Possibly two trends are distinguishable; a main trend with little enrichment in potash and a subsidiary trend similar to that of the circumpacific belt.

The distinction between Precambrian volcanic belts and the circumpacific belt is more apparent in the alumina-colour-index plots of Figure 6. These show the contrasting behaviour of alumina with differentiation in the two environments. In the upper diagram the density of analyses from several localities along the circumpacific belt is represented by contours. The trends of several Precambrian greenstone belts are shown by lines joining average analyses representing successive segments of each trend. The main features are presented in the simplified lower diagram. Circumpacific volcanic rocks form a smooth trend from high-alumina basalts at the mafic end to low-alumina salic rocks at the acidic end of the sequence. Precambrian volcanic rocks of the greenstone belts originate with low-alumina basalt and proceed along one of three trends: (1) enrichment in alumina (Noranda, Grenville); (2) maintenance of original alumina content (Yellowknife, lower cycle of Uchi section, average Archean basalt, andesite, salic); and (3) impoverishment in alumina (upper cycle of

[^16]Uchi section). The second trend is thought to be the major one.

## Summary of chemical properties

(1) Basalts of Precambrian greenstone belts are generally similar to oceanic basalts except for lower alumina, slightly lower titania, and higher potash contents and higher iron-magnesia ratio.
(2) Precambrian greenstone assemblages characteristically evolve from mafic to acidic compositions with time in the eruptive sequence. More than one such cycle may be present in a continuous, conformable sequence.
(3) The Precambrian greenstone successions lack simple, coherent differentiation trends. Elements of both tholeiitic and calc-alkaline trends are recognized. The tholeiitic trend, attributable to differentiation in high-level reservoirs, is superimposed upon the major calc-alkaline trend.
(4) The calc-alkaline trend of the Precambrian greenstone successions differs from that of the circumpacific belt in the behaviour of alumina and in the generally lower levels of potash present. Alumina is characteristically depleted during differentiation of circumpacific lava sequences from high-alumina basalt to low-alumina salic rocks. In contrast Precambrian succes. sions commence with low-alumina basalts and either gain, maintain or lose alumina during differentiation.

## Precambrian greenstone belts as remnants of oceanic crust?

It will be readily apparent from the previous descriptions that there is little resemblance between the Precambrian greenstone belts of the Canadian Shield as they exist today and volcanic sequences of the oceanic ridges. The Precambrian successions typically evolve from mafic to acidic rocks, alkali basalts are rare, and feldspathoidal lavas are known only at Kirkland Lake. In contrast, acidic rocks are rare on the oceanic ridges and feldspathoidal rocks seem to be the principal end products of the eruptive sequence.


Figure 4. AFM diagram of individual analyses from sampled sections of the Grenville, Yellowknife, and Noranda greenstone belts (cf. Figure 2). Also shown are successive samples from differentiated sills (joined by lines) associated with the Yellowknife and Noranda volcanic assemblages.


Figure 5. Normative An-Ab-Or plots of analyses from the sampled sections at Yellowknife and Noranda. The trend of circumpacific magmas is shown for comparison.


Figure 6. The upper diagram compares the variation trends of alumina with colour index (representing differentiation) of a number of Precambrian greenstone belts and the circumpacific belt. The Precambrian belts are represented by average analyses of successive stratigraphic fractions and the circumpacific belt by summary contours of the density of analyses. Also shown are an average Archean basalt, andesite, and salic fraction. The Noranda analyses have been supplemented by an average analysis of thyolite from the district (Sakrison, 1966). The lower diagram is a generalized version of the trends displayed in the upper diagram. The lower limit of circumpacific lavas shown is the limit of densest concentration of analyses.

An additional possibility that might be considered is that the greenstone belts are a combination of volcanic rocks formed at the oceanic ridge and in the subduction zone. According to this view tholeiites in the lower parts of the sequences would represent the ridge effusions and the overlying calc-alkaline rocks the contributions of the subduction zone.

At first sight there appears to be some support for this view. Tholeiitic basalts in the lower parts of Precambrian sequences are generally similar to oceanic tholeiites. Where ultramafic rocks are present they are commonly in the tholeiitic part of the sequence. The AMF and An-Ab-Or diagrams suggest the presence of two superimposed trends; the tholeiitic and the calc-alkaline trends. Rocks of the calcalkaline part of the sequence are roughly similar to those of the present circumpacific belt.

However there are major obstacles to this point of view. If a tholeiitic sequence is formed at the ridge, rafted to the subduction zone, scraped on to the walls of the trench and covered with calc-alkaline rocks one would certainly expect to find a major break between each part of the sequence. Instead, in the sections examined the rocks are conformable throughout and even interlayered where they pass from tholeiites to andesites. In some sequences certain elements vary so smoothly and consistently throughout the sequence that it is difficult to imagine that different parts of the sequence were derived from different sources. Alumina in the Grenville and Noranda sections is one example.

The superposition of more than one mafic to acidic volcanic cycle is also difficult to explain in this way.

Precambrian greenstone successions have some distinctive chemical features that are unmatched by oceanic tholeiites on the one hand and calc-alkaline rocks of the circumpacific belt on the other. The generally low alumina content of their initial basalts is an example. The rarity of alkaline, subsilicic volcanic rocks in the greenstone belts in contrast to their relative abundance on the ocean ridges remains a major obstacle to the hypothesis.

Finally the possibility that some of the greenstone belts may have been de-
posited upon continental crust invokes a feeling of caution towards the view that they originated at the oceanic ridges. The Precambrian assemblage that most closely resembles the oceanic tholeiites in composition, that of the Labrador Trough, seems to be indisputably underlain by continental crust.

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# archean ultramafic rocks 



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## Introduction

Classification of ultramafic bodies
Bodies of ultramafic and related mafic rocks fall into a number of natural classes based on the composition of their magma, the form (shape) of the bodies and the timing of their emplacement in relation to the tectonic history of the area in which they occur. These factors are related to one another and reflect the conditions under which the magma involved was generated and then crystallized. In devising a classification scheme, (Naldrett and Gasparrini, 1971) it is logical to put particular emphasis on the tectonic environment in which the body was emplaced because this exerts a considerable influence on the other two factors.

With our present very imperfect knowledge of Precambrian tectonic processes, it is convenient to make the major division in the classification between those bodies emplaced in orogenic belts and those in non-orogenic (generally cratonic) areas. Ultramafic bodies in orogenic belts can be subdivided on the basis of the timing of their final emplacement with regard to the development of the orogen; namely into
(1) those that were emplaced and crystallized before major folding affected their enclosing rocks,
(2) those whose final emplacement occurred during folding (so-called "Alpine-type" ultramafic bodies), and
(3) those whose emplacement occurred during the final stages of orogenesis, after the most intense folding but before the main period of batholith intrusion. Examples of this class include the concentrically zoned ultramafic bodies of Alaska, British Columbia and the southern Urals
of the U.S.S.R. (Taylor, 1967; Irvine, 1967).

## Classes of Archean ultramafic bodies

The different classes of ultramafic bodies that are common in Canadian Archean greenstone belts are well represented in that portion of the Superior Province designated as the Abitibi orogenic belt (Figure 1) by Goodwin and Ridler (1970). Three main classes are present: All of these classes are conformable in a broad sense with their enclosing rocks. Where gravity-stratified layers are present, these are parallel to stratification in the surrounding rocks. All classes therefore belong to subdivision (1) of the orogenic division of the scheme outlined above; that is they were emplaced prior to folding.

The classes are:
(1) Large (20 - 50 miles long, $>20,000$ feet thick) igneous complexes such as the Dore Lake complex (1 on Figure 1) described by Allard (1970); the Bell River complex (2 on Figure 1) described briefly by Sharp (1965); and possibly the large body of gabbroic rocks located 15 miles west of Timmins (3 on Figure 1). These complexes consist primarily of anorthositic gabbro and are notably rich in titaniferous magnetite and ilmenite. Although they contain pyroxenitic layers, they are mafic rather than ultramafic in overall composition and are not discussed further in this analysis.
(2) Smaller ( $1-10$ miles long, up to 5,000 feet thick) gravity-stratified sills such as the Dundonald sill (4 on Figure 1) described by Naldrett and Mason (1968) and the Munro Lake, Garrison and Ghost Range ( 5 on Figure 1) sills described by MacRae (1969). These sills are well developed in a narrow belt running eastsoutheast from just south of Cochrane.
(3) Lenses of peridotite and pyroxenite (ranging from $10 \times 200$ feet to $4,000 \times$ 20,000 feet surface dimensions) that show no evidence of gravity stratification. These lenses appear to be developed throughout the Abitibi orogen.

The small sills and lenses (classes 2 and 3 ) are the subject of the remainder of this paper.

## Gravity-stratified sills

## Canadian examples

The Dundonald sill is a typical example of this class. It is composed of a basal zone of serpentinized peridotite ( 1,100 feet thick) that was originally an olivine cumulate, with up to 80 modal per cent olivine enclosed poikilitically by augite; this is successively overlain by 500 feet of an augite cumulate and 1,200 feet of gabbro composed of cumulus augite, plagioclase and titaniferous magnetite; a localized zone of granophyre occurs close to the upper contact. Cryptic variation with enrichment of iron in augite and sodium in plagioclase is well developed. Figure 2 is a reconstruction of a vertical cross-section through the sill as it was before folding.

The other sills of the Abitibi belt resemble the Dundonald sill although some of them show additional complexities. The Munro Lake sill has a lower contact zone of homblende peridotite and is remarkable in being composed of seven cyclical units involving the sequences, peridotite-clinopyroxenite, and peridotite-clinopyroxenite-gabbro. Following Irvine and Smith (1967), MacRae attributes this cyclic development to the intrusion of seven pulses of magma with concomitant expulsion of the residual magma of the previous pulse. Some of the smaller sills of the belt are wholly ultramafic while others are wholly gabbroic.


Figure 1. The Abitibi orogenic belt modified after Goodwin and Ridler (1970).


Figure 2. A vertical section through the Dundonald sill as it was before folding. Points $\mathbf{G}^{\prime}, \mathrm{H}$ and $\mathrm{I}^{\prime}$ relate to a plan of the sill in its unfolded state given by Naldrett and Mason (1968) Figure 8.

Calcium-rich pyroxene (augite) predominates in the sills of the Abitibi belt. No fresh calcium-poor pyroxene has been identified although MacRae interprets serpentine pseudomorphs as indicating that it was present as an intercumulus mineral in most of the sills that he studied. However, predominance of calcium-rich pyroxene is probably not a characteristic of this class of sills throughout Canada generally. Ridler (1965) describes the ultramafic portion of one of a similar group of sills from the Kakagi Lake area, south of Kenora, Ontario, as being composed predominantly of harzburgite.

## Examples from outside Canada

Viljoen and Viljoen (1970) describe a group of layered ultramafic sills from the Kaapmuiden area of the Barberton geosyncline in South Africa that have all of the characteristics of the class under discussion. The sills have been intruded conformably between silicate ironformation and pillowed basalts and have differentiated to give rise to a basal zone of dunite overlain successively by layers of orthopytoxenite, websterite and gabbro. Cyclical units such as these found in the Munro Lake sill are developed in a number of the Kaapmuiden sills.

Similar layered sills are common in the greenstone belts of the Eastern Goldfields area of the Western Australian shield. Two examples form the Norseman area are the Mount Thirsty and Mission Sills (McCall, 1970). These both consist of a basal zone or dunite or harzburgite overlain by a bronzite cumulate and then a gabbro capped by localized zones of granophyre. Both sills occur conformably within a thick sequence of pillowed basalts, banded iron-formation and clastic sediments and have been tightly folded with these rocks.

General remarks and the chemical composition

An estimate of the bulk composition of any of the sills of this class is very difficult because of the periodic influxes and effluxes of magma that have apparently given rise to the numerous cyclic units in some of the more complex sills, and also because of the migration of
residual magma during crystallization of even the simpler sills that has resulted in the "offlap - onlap" relationship such as that illustrated in Figure 2. Naldrett and Mason have attempted a very rough estimate of the overall composition of the Dundonald sill which appears in column 1 of Table I; this composition is distinetly ultramafic. They point out, however, that a large proportion of the olivine in the sill was apparently carried in suspension and their estimate for the liquid portion at the moment of intrusion (Table I, colurmn 2), which is based on the relative proportion of the rock types of the sill apart from the peridotite, is mafic rather than ultramafic.

MacRae, assuming that his vertical section through the Munro Lake sill is representative of the whole, calculates the overall composition of the magma, after deposition of the magma, after deposition of the basal peridotite, to be that shown in column 3 of Table I. This is higher in alumina and soda and lower in calcium than Naldrett and Mason's estimate, reflecting the difference in the weight given to granophyre, gabbro and diopsidic pyroxenite in the different averages. Despite this difference, the estimates are both broadly tholeiitic in their affiliation. It seems clear that the sills of this class are the result of the intrusion of tholeiitic or olivine tholeiitic magma

Table 1

|  | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{SH}_{2}$ | 44.7 | 52.7 | 51.2 | 45.4 | 45.6 | 46.2 |
| $\mathrm{Al}_{2} \mathrm{O}_{3}$ | 2.90 | 8.29 | 11.2 | 10.2 | 8.75 |  |
| $\mathrm{Fe}_{2} \mathrm{O}_{3}$ | 1.74 | 2.33 | 2.78 | 4.68 |  |  |
| FeO | 11.8 | 9.53 | 11.9 | 8.14(12.4)* | 12.2* | 13.0 |
| MgO | 32.9 | 10.4 | 7.99 | 20.6 | 23.0 | 22.4 |
| CaO | 3.61 | 13.1 | 9.94 | 10.1 | 7.73 | 18.4 |
| $\mathrm{Na}_{2} \mathrm{O}$ | 0.49 | 1.96 | 3.08 | 0.78 |  |  |
| $\mathrm{K}_{2} \mathrm{O}$ | 0.05 | 0.20 | 0.25 | 0.13 |  |  |
| $\mathrm{TiO}_{2}$ | 0.42 | 1.09 | 1.30 |  | 0.48 |  |
| MnO | 0.22 | 0.20 | 0.20 |  | 0.22 |  |
| NiO | 0.33 | 0.018 |  |  | 0.11 |  |
| $\mathrm{Cr}_{2} \mathrm{O}_{3}$ | 0.88 | 0.23 |  |  | 0.48 |  |
| CIPW Norm |  |  |  |  |  |  |
| Quartz |  | 1.8 |  |  |  |  |
| Orthoclase | 0.3 | 1.2 | 1.5 | 0.8(0.8)* |  |  |
| Albite | 4.1 | 16.6 | 26.1 | 6.6(6.6)* |  |  |
| Anorthite | 5.6 | 13.2 | 16.0 | 23.9(23.9)** | 24.4 |  |
| Salic | 10.1 | 32.8 | 43.6 | 31.3(31.3)* | 24.4 |  |
| Augite | 9.8 | 41.9 | 27.6 | 20.8(21.2)* | 11.7 |  |
| Hypersthene | 22.3 | 19.5 | 17.4 | 12.8(3.7)* | 31.0 |  |
| Olivine | 53.2 |  | 4.9 | 28.3(43.5)* | 31.3 |  |
| Magnetite | 3.8 | 3.7 | 4.0 | 6.8(0)* | 0.7 |  |
| Ilmenite | 0.8 | 2.1 | 2.5 |  | 0.9 |  |
| Mafic | 89.9 | 67.4 | 56.4 | 68.7(68.7)* | 75.6 |  |

[^17]carrying a considerable, although variable, proportion of olivine phenocrysts in suspension.

## Ultramafic lenses

## Canadian examples

Although these lenses apparently occur widely throughout the Abitibi orogen and in other greenstone belts of the Superior Province (for example the Shebandowan area, 60 miles west of Thunder Bay), the most intensive study has been given to those in the Dundonald area and also those south of Timmins, Ontario. These studies include those of Naldrett and Mason (1968) and Pyke (1970).

In their simplest form the lenses consist of a central core ( $10-1,000$ feet thick) rich in olivine or serpentine pseudomorphous after olivine ( $75-90$ per cent original olivine) with minor pyroxene and accessory chrome spinel. The core is surrounded by a marginal zone, 10 100 feet wide, over which pyroxene increases steadily at the expense of olivine toward the contact with enclosing rocks. The pyroxene consists of calciumpoor and/or calcium-rich pyroxene and occurs interstitial to the equant olivine grains as bladed or acicular crystals, sometimes showing a radiating or sheaf-like development; this contrasts strongly with the poikilitic texture of the ultramafic portion of the gravity-stratified sills just described. Naldrett and Mason have attributed the central concentration of olivine in these simple lenses to flowage differentiation of the type described by Bhattacharji (1967). In some of the lenses the olivine, pyroxene, chrome spinel and occasional plagioclase found in the marginal portions have developed distinctive skeletal forms identical with those shown by rapidly chilled experimental charges. This material, which will be referred to as quench rock, reaches its ultimate development in complex lenses in which a series of lens-like zones rich in normal equant olivine are separated by thin, less olivine-rich bands with the quench textures.

The best exposed complex lens is in southern Langmuir township where a body of ultramafic rock, 4,000 feet wide
by 4 miles long, strikes in conformity with the enclosing volcanic rocks. The lens-like zones with normal olivine vary in thickness from 15 feet to more than 150 feet and are separated by $2-15$-feetthick bands of quench rock. A weathered sample of this material is shown in Figure 3. With the rather limited detailed mapping undertaken so far, it has not been possible to trace individual lenses for more than 500 feet although it is very probable that they have a much greater strikelength than this, possibly several thousand feet. Most of the bands of quench rock appear to be as continuous as the olivine-rich lenses although occasional bands feather out into a series of disjointed blocks of quench material in normal peridotite and others pinch out altogether (Figure 4). The normal peridotite is sometimes foliated, particularly adjacent to bands of quench rock, where it commonly contains elongated blocks similar to the quench rock. Thin (2 -6-inch) veins of quench material have also been observed cutting the normal peridotite.

Two complex lenses are also known to exist in the Dundonald area. Exposure is much more restricted here than in Langmuir township, but this disadvantage is offset by the availability of drill core and the much better state of preservation of the textures; all of the available analyses of quench rock also come from this area. In general, the zones of normal peridotite are richer in olivine in Dundonald than in Langmuir township ( $65-80$ as compared with $45-60$ modal per cent). The bands of quench rock contain between zero and 50 modal per cent skeletal olivine. Figure 5 illus. trates some of this material in drill core. Figure 6(a) illustrates the skeletal olivine of Figure 5(c) in thin section, and 6(b) the interstitial quench pyroxene from the same sample.

Despite close similarity in the forms, the natural skeletal textures are very much coarser grained than those produced experimentally. Very occasionally, books of parallel plates similar to those in Figure 5a are as much as 3 feet long. The coarse grain size has led some investigators to discount quenching as the origin
and to conclude that the textures result from metamorphism. In this regard, it is instructive to note the similar textures that have developed in the slag from the International Nickel Company's slag pile at Copper Cliff, Ontario. Figures 7a, b and $c$ are of this material and show skeletal crystals of fayalite developing from an iron-rich silicate glass. The scale of these textures is very similar to that of those in the majority of the natural quench rocks.

## Examples from outside Canada

Ultramafic lenses associated with zones and patches of quench rock comprise more than 30 per cent of the total stratigraphic thickness in the lower half of the Onverwacht volcanic sequence in the Barberton mountainland of South Africa (Viljoen and Viljoen, 1969). The lenses interfinger with pillowed basalts, and rare pillow structures have been reported in the ultramafic rocks themselves. The writer has examined these reputed pillows and, bearing in mind the tendency of ultramafic rocks to develop a joint pattern that looks remarkably like pillows, is unable to accept them as such without more detailed work, particularly on the pillow selvages.

Simple and complex lenses of ultramafic rock are also common in the Eastern Goldfields area of Western Australia where they are hosts to at least 95 per cent of the recent discoveries of nickel ore. The lenses occur at intervals throughout the large thickness of pillowed basalt that is also host to the stratified sills described previously. An interesting feature of the Australian rocks is that thin bands of fine-grained siliceous or argillaceous sediment, many of them rich in iron sulphides and graphite, occur within the complex lenses. The bands are conformable with the lenses, occur at as many as four different horizons within a given complex, and extend for as much as 2,000 feet along strike.

General remarks including a discussion of the chemical composition

As mentioned previously, the simple lenses are thought to have been emplaced as magma carrying a very high proportion of equant olivine grains in suspension.


Figure 3. Sample of weathered "quench rock" from Langmuir township, Ontario. The sample is 9 inches long.

Figure 4. Sketch of a small outcrop showing interbanding between normal peridotite with equant olivine (unshaded area) and quench rock. The dashed lines indicate zones over which the rock shows marked foliation. The outcrop is in southern Langmuir township, 30 miles southeast of Timmins.


 Figure 5. Samples of quenct rock
samples are 6 inches long.

Figure 6.
a) Thin section showing serpentine after skeletal olivine cut from the sampel shown as Figure 5(b) above. Plane polarized light. 6X.
b) Thin section showing acicular, skeletal crystals of augite in the material interstitial to the olivine illustrated in Figure 6(a). Plane polarized light. 100X.

a

b

a

b


C

Figure 7. a) Skeletal growths of fayalite in smelter slag. 4X.
b) and c) Details of skeletal crystals from sample shown as 7(a).
b) Crossed nicols. 100X.
c) Plane polarized light. 100X.

These olivine phenocrysts presumably crystallized under the conditions of slow cooling common to many peridotites. The contrast between this olivine and the skeletal material developed in the marginal zones suggests that the latter crystallized subsequently in a much cooler environment, and raises the question of whether some of the lenses may be extrusive.

The complex lenses, consisting of thin sheets of quench rock interleaved between thicker, stratiform sheets of normal peridotite are readily interpreted as a series of submarine flows in which the quench material represents the rapidly chilled top or base of a single flow. It is difficult to conceive how a single intrusion, or possibly a series of multiple intrusions, could give rise to such a sequence of parallel lenses with well developed sheets of quenched material between each. The Australian examples, in which the sulphide-rich sediments are also laminated within the complex lenses, lend further support to the extrusion hypothesis. These sediments are very similar to the banded zones of cherty or tuffaceous material that are a common feature between, for example, volcanic flows of the Noranda district and that are interpreted as forming during quiescent periods during the volcanism. If the Australian ultramafic rocks are regarded as intrusive, one has to postulate that a series of intrusions invaded the sedimentary horizon, each splitting off a thin band of sediment between itself and its neighbour without disrupting the sediments in any other way.

Viljoen and Viljoen conclude that much of the ultramafic material in the Onverwacht formation is extrusive. They suggest that this is due to the thin crust prevailing at this early stage in the earth's history ( 3.4 billion years ago) and point out that the Barberton rocks (both mafic and ultramafic) have a unique composition. They characterize this crust as having a high $\mathrm{Fe}: \mathrm{Mg}$ ratio and an unusually high $\mathrm{CaO} / \mathrm{Al}_{2} \mathrm{O}_{3}$ ratio, both factors implying an unusually large proportion of normative diopside. They consider that the rocks are members of a previously unrecognized igneous rock suite to which they give the name "Komartiite".

The $\mathrm{CaO}:\left(\mathrm{CaO}+\mathrm{Al}_{2} \mathrm{O}_{3}\right)$ and $\mathrm{FeO}:(\mathrm{FeO}+\mathrm{MgO}) *$ ratios of both ultramafic and basaltic Komartiites from Barberton are compared with Wilson et al's (1965) average for Canadian Archean basalts, Baragar's (1968) rocks from the Noranda area, and Engel, Engel and Havens' (1965) and Aumento's (1968) oceanic tholeiites in Figure 8. The high $\mathrm{CaO} / \mathrm{Al}_{2} \mathrm{O}_{3}$ ratio of the Barberton rocks is very apparent. Also shown are Naldrett and Mason's (1968) analyses of samples from the ultramafic lenses of the Dundonald area. Although overlapping with some of the Barberton rocks, in general these have a distinctly lower $\mathrm{CaO} / \mathrm{Al}_{2} \mathrm{O}_{3}$ ratio and do not appear to be part of the Komartiite suite. The large cross indicates the average (column 5 , Table I) for the quench rocks of the Dundonald area. This figure, being of rocks carrying no olivine phenocrysts, is representative of the liquid portion of the lenses; it has a distinctly higher $\mathrm{MgO}: \mathrm{FeO}$ ratio than any of the Archean or oceanic basalts shown in the figure. It is interesting to note, however, that the average is remarkably similar to the most mafic of the high lime basic silicate liquids that Drever and Johnston (1966) describe from Skye (Table I, column 4). Furthermore, in Figure 8, other liquids described in Drever and Johnston's paper (solid squares) bridge the gap between the Dundonald average and oceanic basalts. It is quite possible that as the ultramafic lenses are studied in greater detail more rocks similar to those from Skye, and spanning the gap between existing analyses and basalts, will be found.

As can be seen from Table $I$, the average composition of the liquid portion of the Dundonald lenses is distinctly ultramafic. This raises the question of the temperature required for this composition to be liquid. In a brief note, Clark and Fyfe (1961) reported the results of melting experiments under water pressures of $500-1,000 \mathrm{~kb}$ on charges with the composition of serpentine. The first suggestion of melting was obtained at about $1,300^{\circ} \mathrm{C}$ and the samples were nearly entirely molten at $1,400^{\circ} \mathrm{C}$. No

[^18]further data on these experiments have been published and one cannot attach too much weight to them until this is done. Presnall (1966) reports that, under dry conditions at 1 atm . confining pressure, an experimental charge with the composition listed in column 6 of Table I has a liquidus temperature of $1,450^{\circ} \mathrm{C}$. On cooling it first crystallizes olivine, with diopside joining olivine at $1,330^{\circ} \mathrm{C}$. This experimental composition is close to the estimate for the Dundonald liquid, if one counts the alumina in the latter as calcium. It is a reasonable assumption that the effect of $500-1,000 \mathrm{~kb}$ of water pressure, the substitution of some alumina for calcium, and the addition of small amounts of alkali might lower the experimentally determined liquidus temperature by as much as $100^{\circ} \mathrm{C}$, suggesting a possible temperature of about $1,350^{\circ} \mathrm{C}$ for extrusion of the Dundonald lenses.

## Conclusions

In conclusion, most ultramafic rocks of Archean greenstone belts are of two types, gravity-stratified sills and ultramafic lenses, that were emplaced within eugeosynclinal volcanic rocks either during the volcanism or very shortly afterwards. Although more work remains to be done, there is much evidence to suggest that some of the lenses are the result of extrusion of ultramafic lava.

In some areas bodies of both types are particularly rich in normative diopside but, for the most part, the bodies appear to have formed from magmas composed of silicate liquids ranging in composition from tholeiite to distinctly ultramafic, olivine-rich picrite, and carrying varying quantities of olivine phenocrysts in suspension.

Except that they carry olivine phenocrysts, the bodies are essentially autochthonous and were emplaced in a sequence of voicanic and sedimentary rocks that was relatively undisturbed. They differ, therefore, from the alpinetype peridotites and ophiolite complexes of Phanerozoic orogenic belts, whose final emplacement was largely allochthonous and occurred in a tectonically dynamic environment.


Figure 8. Plot of wt per cent $\mathrm{CaO}:\left(\mathrm{CaO}+\mathrm{Al}_{2} \mathrm{O}_{3}\right)$ against wt per cent Fe : $(\mathrm{FeO}+\mathrm{MgO})$ for a number of rocks including those of the Dundonald area.

As claimed by some authors in this publication, it is possible that some Phanerozoic ultramafic bodies are fragments of oceanic crust that have been rafted into the debris collecting in the trench at the top of a subduction zone. The geology of the Archean bodies is not consistent with this interpretation. Archean bodies belong to a distinctive synvolcanic class that may not be present in Phanerozoic orogens. The presence of this class, coupled with the apparent restriction of ultramafic lavas to the

Archean, is support for the view that tectonic processes may have been quite different in the early Precambrian to those in younger eons.

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# oceanic crust and the identification of ancient oceanic crust on the continents: <br> a summary 

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## Introduction

One of the major principles underlying reconstruction of the earth's history is that of uniformitarianism which has proved serviceable in explaining many processes that produced ancient rocks. The emergence in recent years of convincing evidence for sea-floor spreading and plate tectonics in geologically young rocks, however, has raised questions as to whether such processes can be assumed to have operated from the earliest history of the earth. No one doubts that the earth's crust and mantle have evolved through time and this in itself is sufficient reason to question whether sea-floor spreading and plate tectonics may be consequences of the evolutionary process and thus be confined to the latter part of earth history.

Enquiry into the potential significance of plate tectonics and ocean-floor spreading in past geological eras provided the stimulus for this symposium volume. Although it is concerned chiefly with Canadian examples, these span a wide variety of geological ages and settings. The following summary is an attempt to distill briefly some of the features of importance and problems that arise in attempting to trace evidence for plate tectonics and ocean-floor spreading from modern examples back through geological time.

Characteristics of modern oceanic crust and criteria for recognition of ancient oceanic crust-mantie rocks

A review of the characteristics of a modern dynamic ridge system based primarily on studies of the Mid-Atlantic Ridge at $45^{\circ} \mathrm{N}$ latitude is presented by Aumento. A typical oceanic crustal
section is interpreted as comprising about 5 km of mafic extrusive and intrusive rocks whose metamorphism increases with depth from negligible through zeolite facies to amphibolite facies. These rocks are pierced locally by diapiric serpentinites and the whole is overlain by a thin veneer of sediments. The mafic rocks range from quartz tholeiites through alkali basalts with olivine tholeiites being dominant. Large layered intrusive/extrusive mafic lopolithic complexes are believed to be emplaced in the vicinity of the ridge axis. Small bodies of homblende quartz diorite, trondjhemite and albite granite are closely associated with ultramafic rocks. Certain geochemical parameters such as $\mathrm{Fe}_{2} \mathrm{O}_{3} / \mathrm{FeO}$, U and $\mathrm{H}_{2} \mathrm{O}$ content, $\mathrm{O}^{18} / \mathrm{O}^{16}$ and $\mathrm{Sr}^{87} / \mathrm{Sr}^{86}$ are known to vary with distance from the ridge axis. However, some or all of these may be too ephemeral in character to be useful criteria in the search for older oceanic crustal rocks: Kay, Hubbard, and Gast (1970) conclude that olivine tholeiite basalts with low $\mathrm{SiO}_{2}$, low K , and generally high but variable $\mathrm{Al}_{2} \mathrm{O}_{3}$ with characteristic dispersed element patterns (rare earth abundances, $\mathrm{Sr}, \mathrm{Ni}$ ) are distinguishing features of rocks formed in the axial zone of an ocean ridge. It is important to note, however, that oceanic ridges are sites of oceanic plate accretion and not sites of basinal sedimentation or continental growth. Description of the characteristics of oceanic crustal sections in marginal and inter-arc basins (Karig, 1971a, 1971b) will be anticipated with great interest.

Alpine-type peridotite is now widely believed to be an excellent indicator of the presence of oceanic crust-mantle.

Irvine and Findlay provide a detailed review of comparisons and contrasts of alpine-type peridotite with other ultramafic rocks. In Canada, alpine-type peridotites are found in the Cordillera and in the northern Appalachians; they have not been identified among the ultramafic bodies of the Precambrian Shield. Some of the better defined features brought out are:
(1) Typical alpine-type (spinel) peridotites consist of a more or less serpentinized assemblage with 60-90 per cent olivine, 5.35 per cent orthopyroxene, 1-7 per cent clinopyroxene, and 0.5-2 per cent chromium-bearing spinel. Additional minerals that may occur are amphibole, pyrope-rich garnet, and plagioclase.
(2) In general the bodies appear to have been largely solid when emplaced; "cold" contacts seem to be most common but substantial contact metamorphism has been found in places.
(3) Ni-sulphide deposits seem to be rarely associated with alpine-type peridotites.
(4) Temperatures of equilibration of alpine-type peridotite mineral assemblages commonly lie in the range from basalt liquidus temperatures to temperatures of the peridotite solidus. Pressures of equilibration appear to range from 1 atmosphere to about 17 kb .
(5) Plots of NiO vs. $\mathrm{Cr}_{2} \mathrm{O}_{3}$ are believed to be potentially useful for distinguishing alpine-type peridotites from ultramafic cumulates of basaltic magmas.
(6) The ultimate origin of alpine-type peridotite is not satisfactorily resolved but its production as a residue of partial melting processes has gained favour over an origin by fractional crystallization.

The characteristics and significance of ophiolites are discussed by Church who recommends a more restricted usage of the term to those complexes with complete "ophiolite stratigraphy" i.e. a lower alpine-type peridotite member overlain by gabbroic rocks followed by pillow basalts and then cherty sediments. Sheeted diabase intrusions seem commonly to have been injected between the pillow lavas and underlying gabbro. Ophiolites are believed to be emplaced early in an alpine-type tectonic cycle rather than during the main orogenic phase. There is considerable controversy about the nature of ophiolite emplacement and whether it can be explained by: differentiation of large mafic submarine extrusions; upwelling and partial melting of the mantle to form a composite subsea laccolith; tectonically incorporated allochthonous fragments of ocean floor, etc. Regardless of the mechanism of emplacement, the present level of knowledge strongly suggests that ophiolite complexes represent oceanic crustmantle.

## Evidence bearing on the existence of old oceanic crustal rocks in Canada

The subject matter of most of the contributions can be broken down conveniently into three groups which deal with: 1) the Cordillera, 2) the Appalachians, and 3) the Precambrian Shield.

## The Cordilleran belt

Souther states that the existence of oceanic crustal rocks is unknown in Tertiary and Mesozoic sequences of the Canadian Cordillera. In the western Cordillera andesitic volcanic arcs existed and migrated westward during the first half of the Mesozoic. West of these arcs contemporaneous thick piles of tholeiitic pillow basalts and pyroclastics were deposited. Eruptions of large volumes of silicic volcanics including rhyolites, rhyodacites, dacite ash-flows, and ignim-
brites took place in late Cretaceous and early Tertiary. Mid-Tertiary and younger volcanic activity comprised plateau and central vent eruption of mainly alkali basalt. The volcanic history can be related to plate tectonic interpretations of Cordilleran geology.

Monger discusses the tectonic implications of some upper Paleozoic rock sequences in the light of possible oceanic-continental plate interactions. Alpine-type peridotites are spatially associated with upper Paleozoic rocks. The association of peridotite, basalt, and chert has been reported but the existence of classical ophiolites has yet to be verified. Permo-Carboniferous basalts with their associated deep water sediments, alpine-type peridotites and serpentinites in the McDame map-area (Gabrielse, 1963) and adjacent parts of northern British Columbia comprise one assemblage that bears closer examination as a possible representative of oceanic crust-mantle.

## The Appalachian belt

Lamarche reviews the geological setting of the ultramafic rocks of the Eastern Townships of Quebec and discusses their origin. The rocks are contained within a fairly closely defined stratigraphic interval in the Lower Ordovician. The lower contacts lie unconformably on schistose, folded, eugeosynclinal deposits. Contacts of the complexes range from apparently "cold" to ones with pronounced metamorphic effects on the underlying rocks only. In addition to the mafic-ultramafic components of these complexes, Lamarche believes that dioritic, syenitic, and granitic intrusions are genetically related and that the whole suite originated by submarine extrusion on a eugeosynclinal floor.

Irvine and Findlay discuss the geology of the Bay of Islands Complex and its interpretation. The complex consists of a lower Ultramafic Zone $2.5-4$ miles thick, an upper Gabbro Zone up to 3 miles thick and is emplaced into basic volcanics, partly pillowed, with contact metamorphic effects on both roof and floor. It is intruded by basic dykes and small bodies of quartz diorite and albite granite. Consideration of the mineralogy,
spinel compositions, $\mathrm{Mg} / \mathrm{Mg}+\mathrm{Fe}^{2}$ in olivines and rocks, and NiO and $\mathrm{Cr}_{2} \mathrm{O}_{3}$ contents of rocks leads to the tentative conclusions that the alpine-type peridotir te of the Ultramafic Zone is the residue of a fractional melting process and the overlying feldspathic dunite is a cumulate from fractional crystallization of the magma that produced the Gabbro Zone. The rock assemblage has the essential earmarks of an ophiolite complex and probably represents oceanic crust-mantle.

Church considers the general characteristics of ultramafic-mafic associations in the northern Appalachians. He believes that these suites in the Bay of Islands Hare Bay belt, the Baie Verte belt, and the Betts Cove belt all show characteristics of alpine-type ophiolite complexies and as such may represent Early Ordovician or older oceanic crust-mantle. At present, these seem to be the oldest probable ophiolites recognized on the North American continent.

## The Precambrian Shield

Baragar deals with the physical and chemical characteristics of lava sequences at Noranda, Yellowknife, Uchi Lake (Archean) and at Kaladar (Proterozoic). These cover a substantial time interval and are geographically widely dispersed yet they show many similarities. Volcanic successions commonly have thicknesses of 30,000 to 50,000 feet and have associated substantial thicknesses of sediments comprising principally quartzose greywacke, impure quartzite, and slate. Basalt, andesite and silicic volcanics occur in estimated relative proportions of about $6: 3: 1$. A characteristic common to all belts is the conformable succession of one or more mafic to felsic cycles. Evidence concerning the floors on which these sequences were deposited is largely now inaccessible but it is probable that the Yellowknife and Labrador Trough belts were laid down upon pre-existing continental basement. Precambrian basaltic sequences have similarities to modern oceanic tholeiites but tend to have lower $\mathrm{Al}_{2} \mathrm{O}_{3}$ and $\mathrm{TiO}_{2}$ and higher $\mathrm{K}_{2} \mathrm{O}$ and $\mathrm{Fe} / \mathrm{Mg}$. The overall trend shown by the successions is calc-alkaline, although the tendency toward high $\mathrm{Na}_{2} \mathrm{O} / \mathrm{K}_{2} \mathrm{O}$ ratios
suggests a possible relationship to differentiation trends that produce the trondjhemite-keratophyre association in oceanic crustal rocks and ophiolites.

Naldrett classifies the common occurrences of ultramafic rocks in the Canadian Precambrian as:
(1) ultramafic cumulates associated with large layered gabbroic complexes,
(2) smaller layered ultramafic sills intruded into Archean greenstone belts and
(3) still smaller peridotite and pyroxenite lenses that are layered but may be zoned, also associated with greenstone belts. The latter two types are of most frequent occurrence and some type 3 examples have textures resembling quench textures thus implying that they formed from ultramafic liquids some of which may have been extrusive. Naldrett finds no evidence to support interpretations of allochthonous ultramafic material introduced into Archean sequences.

## Paleomagnetism

Measurement and interpretation of paleomagnetic properties of rocks is the single most powerful tool available for investigation of the direction and magnitude of plate motions during Paleozoic and earlier times.

Irving and Yole concern themselves primarily with relative plate motions and only incidentally with the direct identification of fossil oceanic crust. Nevertheless, as these authors point out, the two approaches are intimately connected and provide independent criteria for recognition of continental-oceanic plate interactions.

The principles involved in determination of plate motions by paleomagnetic methods are discussed and several examples dealing with Mesozoic and younger rocks of the Pacific margin of North America are described. Potential applications of paleomagnetism to plate motion studies are outlined for the Appalachians, the Franklinian geosyncline and Precambrian structural provinces. Primary magnetization is probably fairly common in rocks as old as Paleozoic but in still older rocks it is expected that
heavier reliance will have to be placed on measurements of secondary magnetizations. Analysis of possible plate motions back through the Paleozoic should be fairly readily attainable. The major challenge, however, will be in detection and measurement of plate motions in the Precambrian.

## Concluding remarks

There is agreement that the northern Appalachians contain a number of examples of probable ophiolite complexes emplaced entirely or in part allochthonously. These rocks are likely representatives of Ordovician or older oceanic crust-mantle.

Alpine-type ultramafic bodies are emplaced into upper Paleozoic rocks in the Cordillera. None is yet established as being associated with an ophiolite complex and further investigation is required to determine their exact nature.

Evidence of fossil oceanic crustmantle rock within the Canadian Precambrian Shield has not yet been discovered. Alpine-type peridotites, if they exist, must be rare. Tools for accurate identification of ocean floor basalts are not yet available and it is not possible to verify any Precambrian basalts as oceanic. Ultramafic rocks associated with thick basaltic sequences appear to have solidified in place and are not allochthonous.

As Irving and Yole point out, a major challenge exists in evaluating plate motions in the Precambrian. An equally exciting and closely related challenge lies in unravelling the history of tectonic development in the Precambrian. It is widely believed that the major period of evolution of the earth's crust and mantle took place prior to the end of the Archean i.e. before about 2.5 b.y. ago. By that time large plates of continental crust had stabilized and little has affected parts of them since. If this is so, one might expect Proterozoic tectonism to be similar to that of Paleozoic and younger eras. To a degree this seems to be true, e.g. the Labrador Trough - Cape Smith belt has many similarities to younger orogenic belts yet it contains no alpinetype peridotites and no syntectonic or
post-tectonic granites. Possibly both these aspects can be related to its development as an intracontinental basin.

A popular conception of Archean greenstone belts is that they have a characteristic and relatively simple tectonic style comprising essentially synformal keels enclosed within granitoid terranes part of which may, or may not, represent pre-existing basement rocks. This simple tectonic style and apparent lack of alpine-type ultramafic rocks seems impossible to reconcile in any fashion with current concepts of Alpine orogenic processes and modern continental-oceanic plate interactions.

The western Superior Province represents, for the most part, a relatively shallow level of erosion. The Superior Province of northwestern Quebec, on the other hand, shows clear evidence of deeper erosional levels in which greenstone belts give way to relict amphibolites and then disappear altogether in dominantly granulitic terranes. This constitutes a strong argument that the rocks of the granulite terranes formed a basement upon which greenstone successions were deposited. It follows that these belts were deposited in intracontinental basins which accords with evidence cited by Baragar for deposition of at least some greenstone belts on continental crustal rocks. The calc-alkaline volcanic trends, however, suggest that some sort of oceanic crust consumption was involved. It is tempting to consider analogies with marginal basins of the modern western Pacific region. Karig (1971a, 1971b) believes these basins are of extensional origin which formed at continentaloceanic interfaces behind island arc systems and subsequently migrated oceanward. If these basins are indeed extensional and thus floored by oceanic crust then we have an important inconsistency with at least some continentallyfloored Archean basins. An alternative is that Archean greenstone belts may have formed in sites akin to modern intracontinental small ocean basins (Menard, 1967). The modern examples accumulate up to 20 km of sediment in deep water and evidently are not subsequently strongly deformed. Archean basins may
have formed in a similar manner but were filled with larger volcanic contributions.

Some of the major geosutures on the Precambrian Shield, the structural province boundaries, seem to provide natural loci in the search for ancient oceanic crustal rocks which may have been caught up during closing of an ocean. The Churchill-Superior boundary in Manitoba, with its complex structural and lithologic relations and a peridotite belt, seems especially worthy of closer examination.

For good reason, the paradigm of plate tectonics has fired the imaginations of earth scientists of many disciplines working with rocks of all ages. It is clear that careful and detailed studies will be required to evaluate the extent to which these processes contributed to shaping the geological record in ancient rocks.

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## polar magnetic substorms $03-06$, u.t. december 5, 1968

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# polar magnetic substorms $03-06$, u.t. december 5, 1968 

E. I. LOOMER and G. JANSEN VAN BEEK


#### Abstract

Magnetic effects associated with a westward travelling surge are illustrated by analysis of simple bays which occurred during three moderately weak substorms, 03-06 U.T. on December S, 1968.

South of the electrojet centre, at $\Phi=57^{\circ}$, magnetic effects are shown to be attributable solely to the auroral electrojet and its return currents.

The azimuth of the Thule current vector, previously shown to reflece the westward extension of the electrojet in the auroral oval, is used to identify individual substorms, to estimate the rate of westward rotation of the oval, and to distinguish between trigger and main bays, All storms show a rapid decay and eastward swing in the final phase. The westward rotation of the oval, deduced from the azimuth of the Thule vector and the velocity of the D demarcation line, is found to be highly irregular.


Résumé. Les effects magnétiques associés à un sursaut se propageant en direction de l'ouest sont illustrés par l'analyse des baies simples qui se sont produites au cours de trois sous-orages modérément faibles, entre 3 et 6 h . (temps universel) le 5 décembre 1968.

Au sud du centre de l'electrojet, à $\Phi=57^{\circ}$, on constate que les effets magnétiques sont attribuables seulement au jet auroral et à ses courants de retour.

L'azimut du vecteur du courant de Thule, qui indiquait auparavant le prolongement vers l'ouest du jet đe particules électrisées dans l'ovale auroral, est utilisé pour reconnaître les sous-orages individuuels, évaluer la vitesse de rotation vers l'ouest de l'ovale et distinguer le sursaut précurseur des principales baies. Tous les orages présentent un décroissement rapide et un mouvement vers l'est au cours de la phase finale. On constate que la rotation vers l'ouest de l'ovale, déduite de l'azimut du vecteur de Thule et de la vitesse de la ligne de démarcation $D$, est très irrégulière.

## Introduction

There are certain advantages in selecting relatively weak magnetic substorms of simple form for analysis. With a satisfactory distribution of observatories such analyses can be expected to reveal details in the morphology of substorms which would be lost in larger disturbances.

A weak substorm developed in the midnight sector around 03 U.T. on December 5, 1968. The largest $H$ perturbation was 500 gammas, recorded at Baker Lake, and the electrojet was apparently confined in longitude to the sector bounded by Leirvogur and Baker Lake. The greatest width of the electrojet was probably not more than 4 degrees. At this time, the number of observatories located in and near the auroral oval was sufficient to give a reasonably clear picture of several interesting features of the storm: in particular, the development at the northern edge of the oval of a travelling westward surge, and the identi-
fication of the trigger bays postulated by Rostoker (1970).

The intense negative $H(X)$ bays frequently observed in the early evening hours at Baker Lake were explained by Akasofu and Meng (1967) as resulting from the westward extension of the polar electrojet which follows the travelling auroral surge along the auroral oval. Two very distinct negative bays occurred in X at Baker Lake during the weak substorm activity of 03-06 U.T. An analysis of these bays and the associated changes in Y and Z have clearly illustrated the magnetic effects associated with a westward travelling surge at a station in the evening sector inside the auroral zone.

Rostoker (1970) has suggested that a substorm consists of a trigger bay and a main bay, with the amplitude of the trigger bay appreciable only close to the centre of the disturbance. According to his hypothesis, the trigger bay is generated by the short-circuiting of the
quiet-time ring current, and the resulting collapse of the field lines is seen as a signal propagating back into the tail. After about 07-10 min this signal reaches the region of the tail where it may trigger reconnection of field lines. The reconnected field lines will move inward and rejoin the inner dipole configuration. The plasma brought in by the freshly reconnected field lines may overload the ring current again, and its subsequent collapse is associated with the main bay and the development of a westward surge. The average time delay between trigger and main bays is thus 15-20 min. The process may repeat itself, causing substorm regeneration with a periodicity of $15-20 \mathrm{~min}$. If the initial signal does not cause reconnection of field lines in the tail, only the trigger bay and the northward movement of the auroral arcs will be observed; the westward surge will not develop.

The azimuth of the Thule current vector has been found to reflect very closely the development of polar magnetic substorms (Loomer and Jansen van Beek, 1971). In particular, by identifying the periods in a substorm characterized by a westward extension of the electrojet in the auroral oval, the azimuth plot provides one method of distinguishing between trigger and main bays.

## Analysis of data

The 03 U.T. storm has been analyzed using the magnetograms from 19 observatories (Figure 1 and the table). The method of analysis is essentially that described previously by Loomer and Jansen van Beek (1971). Deflections of $X(H), Y(D), Z$ from the baseline were measured at approximately 9 -minute


Figure 1. Map in geomagnetic coordinates showing the stations used for this analysis.
intervals from 02 to 06 U.T. Perturbations from the midnight level of the quiet day (December 14) were then expressed in the geomagnetic coordinate
system $\mathbf{X}^{\prime}, \mathrm{Y}^{\prime}, \mathrm{Z}$. Plots of equivalent line currents, calculated from the three perturbation vectors $\Delta \mathrm{X}^{\prime}, \Delta \mathrm{Y}^{\prime}, \Delta \mathrm{Z}$ for a height of 112 km (equivalent to 1 degree
of latitude) were drawn for several instants of time during the storm (Figure 2). H perturbation vectors for the four observatories - Narssarssuaq, Great Whale River, Fort Churchill, Baker Lake - for selected intervals of the storm, are shown in Figure 3. The orientation of the Thule current vector for the period 0225 to 0600 is given in Figure 4. Magnetogram traces for selected observatories are reproduced in Figure 5.

The Kp indices for the 8 three-hour U.T. intervals of this day were 3-305+50403-3+3-. Dst had a small positive maximum of 3 gammas at 08 U.T. and a minimum of -48 gammas at 01 U.T. on December 6. The AE indices showed 4 distinct maxima: 235 gammas at 05 U.T., 356 gammas at 10 U.T., 511 gammas at 13 U.T. and 155 gammas at 18 U.T.

Auroral data available for this storm from the National Research Council, Ottawa, were limited. All sky camera (ASCA) records for Churchill were not usable owing to cloud cover, and a full moon limited the usefulness of the ASCA records at Great Whale River. No ASCA records were available for this period from Narssarssuaq, Sondrestrom, and Godhavn. Auroral radar plots were available for Thompson, Ottawa, Great Whale River and Churchill, but unfortunately azimuth indicators were missing on the Churchill records.

|  |  | Geomag. Lat.N. | Coords. Long.E | $\Psi_{\mathbf{E}}$ | U.T. of local midnight (hrs) |  |  | Geomag. <br> Lat. $\mathbf{N}$ | Coords. <br> Long. $E$ | $\Psi_{E}$ | U.T. of local midnight (hrs) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Th | Thule | 89.2 | 357.4 | 2.4 | 04.61 | Ab | Abisko | 65.9 | 115.3 | 330.2 | 22.75 |
| Al | Alert | 85.7 | 168.7 | 197.7 | 04.17 | Co | College | 64.6 | 256.1 | 27.6 | 09.86 |
| RB | Resolute Bay | 83.1 | 287.7 | 47.1 | 06.33 | DI | Dixon Is. | 62.8 | 161.7 | 347.0 | 18.63 |
| Go | Godhavn | 80.0 | 33.1 | 341.8 | 03.56 | Le | Lerwick | 62.5 | 89.0 | 336.0 | 00.07 |
| MLB | Mould Bay | 79.1 | 255.4 | 55.3 | 07.96 | Me | Meanook | 61.9 | 300.7 | 17.5 | 07.55 |
| BL | Baker Lake | 73.9 | 314.8 | 19.4 | 06.40 | We | Welen | 61.6 | 236.8 | 24.8 | 11.32 |
| Na | Narssarssuaq | 71.4 | 37.3 | 345.2 | 03.02 | Ti | Tixie Bay | 60.3 | 192.6 | 351.9 | 15.40 |
| HI | Heiss Is. | 71.1 | 156.3 | 330.0 | 20.13 | Si | Sitka | 60.0 | 275.0 | 21.8 | 09.02 |
| Leir | Leirvogur | 70.3 | 71.6 | 333.8 | 01.45 | Nu | Nurmijarvi | 59.6 | 114.4 | 336.4 | 22.36 |
| Ch | Fort Churchill | 68.8 | 322.5 | 13.8 | 06.27 | St.J | St. John's | 58.7 | 21.4 | 353.7 | 03.51 |
| PB | Point Barrow | 68.4 | 240.7 | 33.5 | 10.45 | Ot | Ottawa | 57.0 | 351.5 | 2.4 | 05.04 |
| GWR | Great Whale River | 66.8 | 347.2 | 4.5 | 05.18 | Vi | Victoria | 54.3 | 292.7 | 16.4 | 08.23 |
| CC | Chelyuskin Is | 66.1 | 176.5 | 356.6 | 17.05 | Ya | Yakutsk | 50.8 | 193.8 | 5.9 | 15.35 |

[^19]

Figure 2. Current vector plots for 0227 U.T. (Figure 2b), 0358 U.T. (Figure 2c), 0430 U.T. (Figure 2d). Key to location of stations is shown in Figure 2a.

## Sequence of magnetic events

The magnetograms (Figure 5) indicate that a disturbance was developing in the Na area shortly after 02 U.T., with sharp impulses in all elements at 0225,0238 and 0258. At 0327 magnetic effects were evident at all observatories in and near the auroral oval. The main negative H bay at Na and Leir and a gradual bay at BL in H (negative) and Z (positive) began at this time. However, the largest magnetic effects were recorded at GWR where large perturbations occurred in all elements, and at Ch where the gradual negative movement in H was abruptly indented with a large positive bay. The storm activity was most intense at BL, where the sharply increased negative movement
in $X$, beginning 0339, reached its maximum value of 500 gammas at 04 U.T. The effects of this disturbance had disappeared by 0447, and another storm, beginning 0500, was recorded on the BL magnetogram.

At St. J and Ot, south of the oval in the late evening sector, magnetic effects were very small with maxima less than 25 gammas in $-\Delta X^{\prime}, \Delta Y^{\prime}$, and less than 50 gammas in $\Delta Z$. At Me , geomagnetically south of $\mathrm{BL}, \Delta \mathrm{X}^{\prime}$ was slightly negative (less than 20 gammas) from 0330 to 0500 , and $\Delta Y^{+}$was maximum east (70 gammas) at 04 U.T. $\Delta Z$ at Me was positive but did not exceed 30 gammas.

In the daytime sector magnetic perturbations were less than 100 gammas.

Small positive H bays and negative Z bays were recorded at PB and CC from 0300 to 0600 . During this interval negative H bays were observed at $\mathrm{Co}, \mathrm{Si}, \mathrm{Ya}, \mathrm{Ti}$ and We, and $\Delta \mathrm{Z}$ was generally positive. $\Delta \mathrm{H}$ was slightly negative at HI and positive at DI until 0500. Following this the sign of the $H$ perturbation at these stations was reversed. No effect was evident in Z at HI until 0430 , after which $\Delta Z$ became slightly negative.

The outstanding magnetic events are thus the sharp impulses at Na at 0225 and 0238, followed by the larger impulse $(-270 \gamma$ in $\Delta H,-69 \gamma$ in $\Delta Z)$ at 0258 ; the extensive magnetic effects observed at 0327; the abrupt movement in all elements at BL at 0339, and the new disturbance beginning there at 0500 .


Figure 3. H perturbation vectors and the sign of $\Delta Z$ for selected intervals at $\mathrm{Na}, \mathrm{GWR}, \mathrm{Ch}, \mathrm{BL}$.

## Development of the westward surge

In his discussion of transitional bays at middle latitudes, Rostoker (1966) defined a demarcation line which divided the region of the return current south of the oval into two parts: a western part, where $\Delta \mathrm{D}$ is always east, and an eastern part, with $\Delta \mathrm{D}$ always west (Figure 6). The Y transitional bays at Baker Lake and Churchill and the less regular changes in D at GWR and Na similarly define a demarcation line in the return current flow immediately south of the electrojet, although not necessarily the same as that observed at middle latitudes. The information given by the changes in D (or $Y^{\prime}$ ) is conveniently summarized in the
$\Delta H$ vector plots, based on $\Delta X^{\prime}, \Delta Y^{\prime}$, (Figure 3).

The effects at Na associated with the large impulse at 0258 indicate a rapid movement of the current system to the north of the station, placing Na in the return flow south of the main electrojet. However, it is not possible to determine if a western travelling surge developed at this time. $\Delta \mathbf{Y}^{\prime}$ is west, suggesting that the demarcation line was to the west of the station at 0258. Following the impulse, the equivalent current vector, much enhanced, is again south of Na (Figure 2).

At CH , from 0321 to 0440 , the $\Delta H$ vector swings 330 degrees in an anticlockwise direction. At 0358 the demarcation line passes over Churchill as
the station moves from $\Delta \mathrm{Y}^{\prime}$ east to $\Delta \mathrm{Y}^{\prime}$ west in the return current south of the oval (Figure 2). A gradual negative bay in X , typical of a station just south of the oval in the evening sector (Akasofu, 1968), begins at 0215 (Figure 5). This is indented suddenly at 0327 with a large positive bay which peaks at 0405 and lasts until 0442. A negative Z bay begins at 0327. These effects imply a rapid movement of the electrojet northward at 0327 .

The changes in the H perturbation vector at GWR from 0227 to 0327 are similar to those at $\mathrm{Ch} . \Delta \mathrm{Y}^{\prime}$ changes from east to west at 0312 as the demarcation line passes over the station. From 0327 to 0330 the $\Delta H$ vector swings sharply to the north through 90 degrees. This would
result from the rapid northward movement of the electrojet noted at CH at 0327, causing both CH and GWR to be located farther south in the return current system (Figure 6) and indicates the passage of a westward travelling surge north of GWR and Ch at this time.

BL remains in the polar cap return current until 0345 (Figure 2), when the positive Z bay is abruptly indented with an intense negative bay, which peaks at 0406 and ends abruptly at 0447 (Figure 5). The station comes under the influence of the main electrojet as early as 0327, when the negative $X$ bay begins. At 0339 a rapid negative movement begins in $X$, and $Y$ suddenly increases to the east. $\Delta Z$ still moves in the positive direction, but at an increased rate until 0345 . These effects can be understood as resulting from the close approach of the electrojet to the station from the east at 0339, and simultaneously its rapid movement to the north of the station, effectively moving the station out of the polar cap into the anti-clockwise circulation of the leakage current south of the oval. $\Delta Y^{\prime}$ is maximum east at 0348 , changing to west at 0424 , and reaching its westerly maximum at 0432. The electrojet remains north of the station until 0432, after which the auroral bulge has passed to the west of the station and BL is again located in the polar cap flow.

These effects are clearly illustrated in Figure 7, which is a synthesis of equivalent current vector plots for several instants during the storm. The effect of the surge is represented schematically by a westward travelling bulge of the electrojet, which leads the westward advance of the primary current flow in the dark sector of the auroral oval (Akasofu and Meng, 1967; Rostoker et al., 1970). This is a development of the model proposed by Rostoker (1966). The equivalent current system is regarded as fixed in space with relation to the earth. The movement of BL $\left(\Phi \sim 74^{\circ}\right)$ relative to the current system for the interval 0321 to 0442 is shown by the dashed line. Values of the BL perturbation vectors for several instants during the storm are given with the figure.

The magnetic effects are closely
repeated in miniature at BL during the smaller storm 0500-0545. However, for this period, since the demarcation line is now to the west of the station, Baker Lake passes south of the electrojet into the east half of the return current cell associated with $\Delta \mathrm{D}$ west (or $-\Delta \mathrm{Y}^{\prime}$ ). The effects of this storm can be explained by a surge causing an explosive poleward shift of the electrojet west of BL with the bulge approaching close to the station from the west shortly after 0500, causing $\Delta D$ to swing farther west and $\Delta Z$ to increase in the positive direction (Figure 7). At 0510, as the station comes under the eastward edge of the expanding bulge, the negative movement begins abruptly in Z. $D$ is maximum west at 0512 and $-\Delta H$ is maximum at 0520 . Following 0527 the station is south of the electrojet. The negative bay ends abruptly in $Z$ at 0545. The abrupt ending of the $\mathbf{Z}$ bay in this and the preceding storm is explained by the passage of the electrojet over the station, as the main current returns to the south. The effects of the second surge are over at 0546 after which the station is again in the polar cap return.

## Velocity of the westward surge and rotation of the oval

The approximate speed of the surge which developed north of GWR and Ch at 0327 and was detected at BL at 0339 may be estimated as follows. The current vector plot (Figure 2) suggests that the electrojet is at dipole latitude $\Phi=70^{\circ}$ at this time. The difference in geomagnetic longitude between BL and the point midway between Ch and GWR is 20 degrees. The distance along the $70^{\circ}$ geomagnetic parallel is $38.185 \mathrm{~km} /$ degree of geomagnetic longitude $\Lambda$. This distance must be reduced by approximately $\Delta t / 4 \mathrm{x}$ 38.185 to correct for the rotation of the earth, where $\Delta t$ is the time difference in minutes between the surge effects at the two locations. Then, if $y$ is the speed of the surge in $\mathrm{km} / \mathrm{sec}$
$y(\Delta t \min \times 60) \sec =(\Delta \Lambda-\Delta t / 4) 38.185$ and $y=0.9 \mathrm{~km} / \mathrm{sec}$

This calculation can only be approximate owing to the uncertainty in locating the point of origin of the surge and in reading the time of events on normal magnetograms. The commonly

Figure 4. Graph of change with time of geomagnetic azimuth of Th current vector.



Figure 5. $H(X), D(Y), Z$ magnetogram traces drawn from 75 sec digitized data for Na , GWR, Ch, BL.
accepted value for the velocity of the westward surge is $1 \mathrm{~km} / \mathrm{sec}$ (Akasofu, 1968).

The demarcation line defined by high latitude D transitional bays associated with surge activity, does not move westward at a consistent rate. This is in contrast to the movement of the demarcation line calculated by Rostoker et al (1970) for transitional D bays at mid-latitudes, in which the demarcation line was found to move west with respect to the sun-earth line at about $0.9 \mathrm{~km} / \mathrm{sec}$ at the latitude of the polar electrojet in the case of two geomagnetic arrays located at $45^{\circ} \mathrm{N}$ and $53^{\circ} \mathrm{N}$. The velocity
of the demarcation line calculated from its passage over GWR (0312UT) and CH (0358), and Ch and BL, (0424) is, in each case, that to be expected from the rotation of the oval as inferred from the change in orientation of the Th current vector (Figure 4) which is discussed in the following section. Figure 4 suggests that the oval rotated to the west at a rate just slightly greater than $15^{\circ} / \mathrm{hr}$ (equivalent to $0.16 \mathrm{~km} / \mathrm{sec}$ at $\Phi=70^{\circ}$ ) between 0312 and 0358. The corresponding velocity of the demarcation line was $0.18 \mathrm{~km} / \mathrm{sec}$. The velocity of the demarcation line from Ch to BL is $0.03 \mathrm{~km} / \mathrm{sec}$; the change in azimuth of the Th current vector between

0358 and 0424 implies that the oval has moved to the west in this interval at a rate of $3^{\circ} / \mathrm{hr}$ or $0.03 \mathrm{~km} / \mathrm{sec}$. These comparisons underline the significance of the orientation on the Th current vector in determining the westward rotation of the oval.

## Identification of trigger bays

As shown in an earlier paper (Loomer and Jansen van Beek, 1971), the changing orientation of the current vector at Thule, near the geomagnetic pole, reflects very closely the extension of the polar electrojet which follows the westward surge along the oval. However, the Thule current vector would be quite insensitive to a purely poleward movement of the electrojet, and could be expected to distinguish between trigger bays and the main bay, if a westward surge develops only with the main bay.

A plot of the azimuth of the Thule current vector is shown in Figure 4. Since the azimuth is derived from arc tan $\Delta \mathbf{Y}^{\prime} / \Delta \mathbf{X}^{\prime}$, values become quite uncertain for small $\Delta \mathbf{X}^{\prime}, \Delta \mathbf{Y}^{\prime}$. In practice this precludes use of the azimuth information prior to 0220 U.T. when $\Delta X^{\prime}, \Delta Y^{\prime}$ were generally small and oscillated about the adopted quiet level. For the period shown in Figure 4 the uncertainty of the azimuth values does not exceed 3 degrees.

The impulsive negative H bays at Na at 0225 and 0238 could be interpreted as trigger bays. These bays are also observed at Leir, and the 0238 bay may be identified on the Ch record as a small negative X bay.

It can be argued that the westward surge which was identified on the Churchill and BL magnetograms developed north of GWR and Ch at 0327, and is thus connected with the main negative H bay beginning at that time. If a surge, travelling westward along the oval at 1 $\mathrm{km} / \mathrm{sec}$, developed north of Na at 0258 , it could be expected to appear north of GWR at about 0327. The effect would be felt to the east at Leir at about the same time. However, it is reasonably certain that the surge observed north of GWR and Ch developed in that area at 0327, and did not originate earlier in Na . The occurrence of negative H bays at stations
along the active part of the oval at 0327 indicates that a significant new disturbance began at that time. This is confirmed by the change in azimuth of the Th current vector around 0330 .

The graph of the Th current vector in Figure 4 suggests that three distinct sub. storms occurred in the interval 03-06 U.T. The first was very short-lived, and decayed soon after its onset around 0258. The second and third lasted much longer, and reached maximum intensity (as inferred from the maximum geomagnetic east azimuth of the Th current vector) at $0348-0354$ and 0536 respectively. The storms show the rapid decay and pronounced eastward swing of the storm centre noted previously by Loomer and Jansen van Beek (1971) for the storms of 08 U.T. and 11 U.T.

There is no evidence from Figure 4 of a westward extension of the electrojet following the impulse at 0225 . There is a suggestion that a short-lived substorm developed after the 0238 impulse, although the anomalously large increase in azimuth between 0240 and 0250 does not resemble the usual substorm signature. It is possible that the abrupt increase in azimuth at this time, which is also observed at Resolute Bay, results from a local disturbance in the polar cap and does not reflect a westward extension of the jet in the auroral oval.

It is concluded that the bay at 0225 is a trigger bay. Lacking evidence of a westward surge in the Na area at 0238 , it is not possible to establish whether the bay which began at that time is a second trigger bay or the beginning of a small substorm. If the latter interpretation is correct, then the bays at 0258 and 0327 result from the periodic regeneration of substorms discussed by Rostoker (1970), although the delay of 29 minutes is significantly longer than the $15-20$ minutes which he postulated.

The extent of the auroral electrojet
The auroral electrojet did not attain a large east-west extent during these disturbances, and was probably confined at its most intense to a sector between Leir and a point slightly west of BL (about $120^{\circ}$ in geomagnetic longitude) in which
the flow was estimated to lie between $71.5^{\circ} \mathrm{N}$ and $75.5^{\circ} \mathrm{N}$ at 0358 (Figure 2). In the daytime sector at 0227 a weak eastward current flowed at HI and PB , with a westward current south of CC and DI. At 0358 and 0430 HI is in the polar cap return flow. By 0518 an eastward current flowed south of $\mathrm{HI}, \mathrm{CC}$ and PB , and north of DI. Only very small effects were observed at stations south of the active part of the oval at $\mathrm{Ot}, \mathrm{St}$. J and Me.

Fukushima (1969) has shown that the geomagnetic effect of the auroral electrojet return current is confined practically to a rather small area in high latitudes, and does not extend down to low latitudes, if the electrojet flows in a narrow latitude range within several degrees. For a station at the latitude of Ot on the meridian passing through the auroral electrojet centre, the calculated effect for an auroral electrojet of 4 degrees width would be 63 gammas for an electrojet of 120 degrees longitudinal extent. The
calculation applies to the case where the maximum field change under the jet is 1000 gammas. At 0358 the total maximum effect at BL was about 500 gammas. The effect measured at Ot, slightly east of the central meridian, was 36 gammas. This agrees closely with the value predicted from Fukushima's model and implies that in this case the geomagnetic effect observed at Ot can be attributed solely to the westward auroral electrojet and its return currents. The calculation is relatively insensitive to the longitudinal extent of the electrojet.

## Auroral information

As already noted, the auroral information for this period was very limited. From 0200 to 0500 quiet homogeneous arcs directed approximately east-west were visible to the north of GWR. These were located typically at 32 degrees from the zenith. Double arcs were observed occasionally. In addition to the

Figure 6. Rostoker's equivalent current system for a polar magnetic substorm.



Figure 7. Schematic representation of westward surge effect at Baker Lake ( $\Phi \sim 74^{\circ}$ ) for storms 0327-0447 and 0500-0545.

Storm (0327-0447)

| Storm |  | $\begin{gathered} \text { 0327-0447) } \\ \Delta x^{\prime} \end{gathered}$ |  |  | Storm |  | 545) | $\Delta Y^{\prime}$ | $\Delta z$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\Delta r^{\prime}$ | $\Delta z$ | $\Delta x^{\prime}$ |  |  |  |  |
| A | 0321 |  | U.T. -52 | -31 $\gamma$ | $20 \gamma$ | E | 0500U.T | -159\% | -141 $\gamma$ | $196 \gamma$ |
| B | 0339 | -113 | -16 | 118 | D | 0527 | -205 | -97 | -39 |
| C | 0354 | -320 | 197 | -301 | E | 0554 | -17 | -8 | 52 |
| C' | 0358 | -451 | 215 | -85 |  |  |  |  |  |
| D | 0424 | -268 | -159 | -275 |  |  |  |  |  |
| E | 0442 | -168 | -166 | 92 |  |  |  |  |  |

weak homogeneous arcs, additional auroral activity in the form of patches was observed northeast of the station at 0221 and 0223, at 0238-0240, at 0301, and at 0331. At $0405-0407$ patches were visible to the north-northwest and moved west at 0407, disappearing at 0413. The patches were generally preceded by brightening of the arcs. Unfortunately GWR was too far south of the oval to see the effects of the surge which developed to the north around 0327. The weak homogeneous arc less than 15 degrees above the northern
horizon was observed to brighten in the northeast at 0330 , followed by a patch about 35 degrees from the zenith at 0331. This activity was doubtless associated with the magnetic effects of 0327.

Since ionized patches do not always give rise to radar echoes, it is difficult to correlate the auroral radar records with magnetic effects. At GWR and Thompson ( $\Phi 65 \mathrm{~N}, ~ \Lambda 317.5 \mathrm{E}$ ) these echoes were always observed to move in a counterclockwise direction from the south to a position east or north of the station, returning again to the south. Echoes were
observed due east, or north of east, of GWR within 400 km of the station at $0238,0300,0330$ and 0445 . The echoes were structured in all cases except tr first, and were especially bright at 03 . Although this information adds little to the understanding of the magnetic storms in this period, it does not conflict with the interpretation which has been presented.

## Conclusions

The magnetic effects associated with a westward travelling surge at a high latitude ( $\Phi=74^{\circ}$ ) station in the evening hours have been clearly illustrated by the analysis of the simple bays which occurred at BL during the weak substorms of December 5, 1968. In particular, the smoothly varying transitional bays in D (or $\mathrm{Y}^{\prime}$ ) and the sharply defined negative indentations of Z , lasting about an hour, have been interpreted by means of a simple model to show the rapid movement of the electrojet to the north, west and east.

The storm developed east of the midnight sector in the vicinity of Na . In the interval 03-06 U.T. three distinct substorms were identified, each initiated by the rapid poleward shift and the westward extension of the electrojet characteristic of the auroral surge. The longitudinal extension of the electrojet was limited to approximately $120^{\circ}$ for the largest of the three substorms (0327-0447), and current flow, as given by the equivalent current vectors, was confined between geomagnetic latitudes $71.5^{\circ}$ and $75.5^{\circ} \mathrm{N}$ approximately. Magnetic effects south of the oval at Ot and St. J were very small and apparently can be attributed solely to the auroral electrojet and its return currents. The largest effects in the daytime sector were about $1 / 5$ of the maximum observed for the storm.

The velocity of the 0327 surge inferred from magnetic effects was 0.9 $\mathrm{km} / \mathrm{sec}$, in good agreement with values found in the literature (Loomer and Jansen van Beek, 1971). The westward rotation of the oval, deduced from the change in azimuth of the Th current vector and confirmed by the calculated
velocity of the $D\left(Y^{\prime}\right)$ demarcation line, was found to be highly irregular. The usefulness of the azimuth plot of the Th current vector for identifying individual substorms and for estimating the rate of rotation of the oval was again illustrated. The rapid swing of the oval to the east during the decay phase of substorms, first noted for the intense substorm of 08 U.T., was again evident in the orientation plot of the $T h$ vector for the weak substorms of 03-06 U.T.

The negative H bay which occurred at Na at 0225 and was visible also with reduced intensity on the Leir record, was identified by means of the Th azimuth plot as a trigger bay. However, it was not possible to clearly establish whether the impulse at Na at 0238 was associated
with a second trigger bay, or marked the beginning of the main bay of a weak substorm. Although the sensitivity of the orientation of the Thule current vector to the westward extension of the electrojet is useful in distinguishing between trigger and main bays, the unambiguous identification of the trigger bay is clearly very difficult.

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# an astatic magnetometer with negative feedback 

J. L. ROY, J. REYNOLDS and E. SANDERS


#### Abstract

This paper describes an astatic magnetometer designed for the measurement of weakly magnetized rock specimens with special reference to a magnetic control method as a means of improving both the performance and efficiency of the instrument.

In the first section, it is shown that for high sensitivity and rapid response, the two magnets should be long and thin, magnetized perpendicular to the long axis, and that the moment of inertia of each magnet should be $1 / 4$ the moment of inertia of the whole suspended system. In general, magnetic materials of high coercive force give the best design.


The second section describes in detail the construction of an astatic magnetometer according to the above principles, including a method of astatizing without the use of trimmer magnets. Following a discussion on the size, shape and positioning of the rock specimen, a cylindrical specimen (height/diameter $=\pi^{1} / 2 / 2$ ) placed directly beneath the lower magnet is chosen. A specimen table and a method for accurate determination of the distance between specimen and magnetometer are described.

The third section describes the procedure for measuring three orthogonal components of magnetization of a specimen. When the instrument is operated in the conventional manner, that is with the restoring torque provided by the suspension fibre, with a period of 14 seconds the sensitivity is $1 \times 10^{-8} \mathrm{oe} / \mathrm{mm}$ deflection on a scale 5 m distant. This sensitivity permits the measurement of specimens magnetized to an intensity of $1 \times 10^{-6}$ e.m.u.

The fourth section describes the use of negative feedback to improve the performance and efficiency of the instrument. Here, in addition to the torque of the suspension, a magnetic restoring torque is provided by a small solenoid connected to a pair of photo resistors centred on the light beam. Measurements can be made in terms of current or voitage with a variety of electrical instruments. High sensitivity ( $0.56 \times 10^{-9} \mathrm{oe} / \mathrm{mv}$ ) can be obtained while maintaining a short period ( 5.1 sec ). The sensitivity and the period can be lowered instantly through 11 steps down to $1.2 \times 10^{-7} \mathrm{oe} / \mathrm{mv}$ and 1.2 sec . The quick response permits the direct measurement of the direction and total intensity of magnetization of the specimen, rather than computing them from three components. This eliminates much calculation and increases the accuracy, especially with weakly magnetized rocks. The range of the instrument provides for accurate measurement of specimens magnetized to an intensity of $1 \times 10^{-7}$ to $5 \times 10^{-3}$ e.m.u.; the time required for a measurement of direction and intensity is eight and three minutes, respectively. The period and damping of the system can be altered in many ways to suit particular conditions and requirements. Disturbances affecting the instrument and means of avoiding of reducing them are discussed.

Résumé. Les auteurs décrivent un magnétomètre astatique servant à mesurer l'intensité d'aimantation, généralement très faible, d'échantillons de roches; ils insistent tout particulièrement sur une méthode de contrôle par champ magnétique permettant d'améliorer la sensibilité et le rendement de l'appareil.

Dans la première partie, ils démontrent que, dans un système astatique à deux aimants, il est préférable d'utiliser des aimants longs et étroits aimantés perpendiculairement à leur axe longitudinal; en outre, le moment d'inertie de chaque aimant devrait être égal au $1 / 4$ de celui de l'ensemble de l'équipage mobile. En général, ce sont les matériaux magnétiques à haute coercitivité qui répondent le mieux à ces conditions.

Dans la deuxième partie, les auteurs décrivent en détail la construction d'un magnétomètre astatique conçu suivant les principes énoncés précédemment, et la méthode employée pour le rendre astatique sans utiliser des aimants compensateurs.Après avoir discuté des dimensions, de la forme et du positionnement de l'échantillon, ils fixent leur choix sur un échantillon cylindrique (hauteur/diamètre $=$ $\pi^{1} / 2 / 2$ ) placé directement sous l'aimant inférieur. Ils décrivent ensuite le porte-échantillon ainsi que la méthode permettant de déterminer avec précision la distance optimale entre échantillon et magnétomètre.

Dans la troisième partie, les auteurs énoncent la procédure à suivre pour mesurer trois composantes orthogonales de l'intensité d'aimantation d'un échantillon. Quand l'appareil fonctionne suivant le mode habituel, c'est-à-dire quand le couple de rappel du fil de torsion correspond à une période d'oscillation de 14 secondes, la sensibilité est de $1 \times 10^{-8}$ oersted pour une déflection de 1 mm sur une mire graduée distante de 5 m . Cette sensibilité permet de mesurer l'intensité d'aimantation d'échantillons présentant des intensités aussi faibles que $1 \times 10^{-6}$ gaus.

Dans la quatrième partie, les auteurs décrivent le procédé par lequel ils améliorent la sensibilité et le rendement de l'appareil à l'aide d'un système de rétroaction négative. On ajoute au couple de torsion du fil de suspension un couple de rappel électromagnétique fourni par un petit solénoïde connecté à deux photorésistances encadrant le faisceau lumineux. Les mesures se font en termes d'intensité ou de tension, à l'aide d'appareils électriques variés. Grâce à la méthode indiquée ci-dessus, on peut obtenir une haute sensibilité ( $0.56 \times 10^{-9}$ oersted/millivolt), tout en conservant une courte période d'oscillation ( 5.1 sec .). On peut réduire instantanément la sensibilité et la période, en 11 étapes successives jusqu'à $1.2 \times 10^{-7}$ oersted/millivolt et 1.2 seconde. Le temps de réponse très court ainsi obtenu permet la mesure directe de la direction et de l'intensité de l'aimantation de l'échantillon sans avoir à les calculer à partir de trois composantes. Ceci ćlimine une grande partie des calculs et améliore la précision, en particulier dans le cas des roches faiblement aimantées. L'appareil permet une mesure précise sur des échantillons dont l'intensité est comprise entre $1 \times 10^{-7}$ et $5 \times 10^{-3}$ gauss; il faut 8 et 3 minutes respectivement, pour mesurer la direction et l'intensité de l'aimantation. Il est possible de modifier à volonté la période et l'amortissement de l'équipage mobile pour répondre aux conditions et aux exigences particulières qui pourraient se présenter. Les auteurs examinent enfin les perturbations pouvant affecter l'appareil et indiquent la façon de les éviter ou d'en atténuer les conséquences.

## Introduction

Astatic magnetometers have been used extensively for the measurements of the remanent magnetization of rock specimens since Blackett (1953) showed them to be well suited for measuring weak fields. Blackett's magnetometers were designed to measure the weakest field possible without regard to the time taken, and instrument periods were as long as 60 to 70 seconds. In paleomagnetic work, a large number of measurements are required and shorter period instruments are desirable. Various designs for maximum sensitivity at a limited period have been described (e.g. Collinson et als, 1957; As, 1960; Collinson and Creer, 1960; Roy, 1963). Owing primarily to new manufacturing processes of magnetic materials, it has been possible over the last two decades to improve the design and consequently the performance of astatic magnetometers. The performance of a magnetometer constructed according to the design theory given by Roy (1963) and using Platinax II magnets shows that the instrument can accurately measure the components of magnetization of a rock specimen magnetized to an intensity of 1 $\times 10^{-6}$ e,m.u. with an acceptable response time of 14 seconds. With a change of the suspension fibre, the response time can be shortened to, say, 4 to 5 seconds; the corresponding reduced sensitivity ( $\approx$ a tenfold reduction) is still adequate to measure intensities of $1 \times 10^{-5}$ e.m.u. These performances are obtained when using the conventional torsion control method of measuring (by means of lamp mirror and scale) the deflection produced by a magnetized specimen placed near the instrument. When using the instrument in this mode, the deflection of the magnet system should be entirely controlled by the torsion of the fibre. For this reason, by changing the suspension, the instrument can be made into a high sensitivity magnetometer or a quick-response magnetometer; however, the two characteristics (high sensitivity and quick response) cannot be combined because an increase of one is accompanied by a reduction of the other.

The range of intensities found in rock specimens is large ( $\approx 1 \times 1 \sigma^{-7}$ to $1 \times 1 \sigma^{2}$ e.m.u.) and an instrument with multiple sensitivities is desirable for reasons of efficiency. Changing suspension fibres to attain this objective is most impractical. Because of the high risk of breaking the fibre, such changes are usually avoided. Furthermore, the time required for realignment of the system would defeat the purpose. An alternative would be to have several magnetometers of different sensitivities. However, because it is preferable to operate these instruments in field-free spaces, an array of such spaces far apart one from the other (to avoid interference) would be required. Such a proposition would be costly and not the most practical for obvious reasons, such as the time spent travelling from one instrument to the other.

Part IV describes a method by which the same instrument can be converted into a multiple sensitivities magnetometer. By using a feedback system, the sensitivity can be changed electrically to different preset values. In this way, the measuring range of the instrument can be expanded and, with the proper choice of sensitivities, the magnetometer can be operated at maximum efficiency whatever the intensity of the specimen. The performance (both sensitivity and speed of operation) can also be greatly improved. The sensitivity attainable with the present magnetometer is 10 times greater in the magnetic control mode than in the torsion control mode; at the same time the response is markedly quickened and kept below 6 seconds for all sensitivities. This rapid response permits the use of a direct-read method of determining the direction and total intensity of the magnetization of a rock specimen. Because two measuring procedures (three-component and directread) can be used with this instrument, both are described.

## Part I - Theory of design

## 1. The magnet system

An astatic magnetometer consists essentially of two magnets fixed to a vertical rod which is suspended by a fibre or ribbon. The magnets of nearly equal
moments are set with their directions of magnetization horizontal and antiparallel, and with one a distance $L$ above the other. A mirror fixed to the rod permits one to measure the angular deflections of the suspended system about a vertical axis. To avoid susceptibility effects and to increase the sensitivity of the instrument, the magnetometer is usually placed in a quasi-zero field. The earth's field can be reduced by means of a magneticshielded room such as described by Patton (1967) or compensated for by means of a system of Helmholtz (or a similar type) coils. The choice of shielding or compensating coils does not alter the basic design but could possibly affect performance.

When a magnetized specimen is placed under the bottom magnet and oriented so that its direction of magnetization is not parallel to the axis of magnetization of the magnet, the deflection of the suspended system in a zero field is given by

$$
\begin{equation*}
\theta=\Delta H P / \sigma \tag{1}
\end{equation*}
$$

where $\Delta H$ is the vector subtraction of the fields produced at the bottom and upper magnets, $P$ is the horizontal moment of a magnet and $\sigma$ is the torsion constant of the fibre. The period is given by

$$
\begin{equation*}
T^{2}=\frac{4 \pi^{2} I}{\sigma}=\frac{4 \pi^{2}\left(2 I_{1}+I_{2}\right)}{\sigma} \tag{2}
\end{equation*}
$$

where $I, I_{1}$ and $I_{2}$ are the moments of inertia of the system, of one magnet and of the system without the magnets, respectively.

From (1) and (2), we find the sensitivity is

$$
\begin{equation*}
\frac{\theta}{\Delta H}=\frac{T^{2}}{4 \pi^{2}} \cdot \frac{P}{1}=\frac{T^{2}}{4 \pi^{2}} \cdot \frac{P}{2 I_{1}+I_{2}} \ldots \tag{3}
\end{equation*}
$$

showing that the sensitivity can be increased by increasing the period and the ratio $P / I$.

## 2. Period limitations

Three considerations limit the increase of $T$. The first is the efficiency of the instrument. With critical damping, as is usually the case, the time taken for an observation may be taken as equal to the
period. For routine measurements, because of the number of observations required ( 6 or 12 for each specimen), 30 seconds is normally regarded as the maximum period allowed.

The second limitation is due to the fact that a system cannot be made and remain truly astatic. The astaticism $A$ is defined as the ratio of $P / P^{\prime}$ where $P^{\prime}$ is the residual moment of the system and can be written

$$
\begin{equation*}
A=P / P^{\prime}=P /\left(P_{A}^{\prime} 2+P_{S}^{\prime}\right)^{1 / 2} \ldots \tag{4}
\end{equation*}
$$

where $\quad P_{S}^{\prime}=P_{B}-P_{M}$

$$
P_{A}^{\prime}=\alpha P_{B}=\alpha P_{U}
$$

$P_{\mathrm{B}}$ and $P_{\mathrm{U}}$ being the dipole moments of the lower and upper magnets and $\alpha$ the angular departure from antiparallelism. Although an astaticism of 5,000 or even 10,000 can be obtained, it is unlikely to remain for any length of time owing to changes with time and temperature; changes which affect the whole system and particularly the magnetic properties of the magnets. For periods of months or years, it is more realistic to consider an astaticism of about 1,000 . This is normally sufficient for accurate measurements on a magnetically quiet day. However, the error introduced in the readings owing to variations on disturbed days may be large and, for this reason, it is usually preferable to keep the period short. This source of error can be practically eliminated by using a negative feedback fluxgate system (Roy, 1963) which automatically detects and compensates for the diurnal variation.

The third limitation arises from the effect of changes in the dimensions and shape of any part of the apparatus, mainly of the compensating coils. These changes, which become more serious as the sensitivity is increased, may originate from different sources such as vibration and ambient temperature changes. Distortion or relative displacements of the compensating coils produce different field changes at the upper and lower magnets. Since the astaticism cannot reduce the effect of this type of disturbance, the drifts that occur might be
considerable. This is exemplified in Part IV. These disturbances can be reduced by rigid construction of the coil system and good temperature control and their effect minimized with short periods.

## 3. Ratio $P / I$

This ratio which should be made as large as possible is given by

$$
P / I=m J(\beta) /\left(2 I_{1}+I_{2}\right) \ldots(5)
$$

where $m$ is the mass of one magnet. $J(\beta)$ is the specific intensity of magnetization of a rectangular magnet of square cross section where $\beta=w / h=$ width $/$ height.

Although the $J(\beta)$ of many materials increases asymptotically to a maximum value as $\beta$ increases, it is found (Roy, 1963) that, because $I_{2}$ cannot be neglected (5), the maximum $P / I$ is usually obtained for $\beta<1$, that is, when the magnet is magnetized transversely or parallel to the short side. $J(\beta)$ is then $(0<$ $\beta<1$ ) almost independent of shape (or $\beta$ ) and as a first approximation $J(\beta)$ can be treated as a constant. Under this condition, it can be shown that $P / I$ is maximum for

$$
\begin{equation*}
I_{1}=I_{2} / 2 \tag{6}
\end{equation*}
$$

and from (5), we get

$$
\begin{equation*}
P / I=m J(\beta) / 2 I_{2} \tag{7}
\end{equation*}
$$

$I_{2}$ should therefore be made as small as possible keeping in mind the necessity of a mirror large enough to provide a good light beam and a structure rigid enough to maintain high astaticism.

The dimensions of the magnet can be obtained from

$$
\begin{equation*}
I_{2}=p h w^{4} / 3 \tag{8}
\end{equation*}
$$

where $\rho$ is the density of the magnetic material or from

$$
\begin{equation*}
I_{2}=\pi \rho h d^{4} / 16 \tag{8a}
\end{equation*}
$$

for an upright cylindrical magnet of diameter $d$.

From (7) and (8), one finds that $P / I$ is inversely proportional to $w^{2}$ for rectangular magnets and to $d^{2}$ for cylindrical magnets indicating that the magnets be made high and thin. However, depending on the positioning of the specimen with respect to the magnet system, a practical limit of $h$ usually has to be set. For example, when the specimen is placed under the bottom magnet, $h$ should be small compared to the distance $z$ between magnet and specimen; otherwise only part of the magnet would be reacting to a field produced by a nearby specimen. In general, $h$ should be kept $<1 \mathrm{~cm}$.

## 4. Magnetic materials

New manufacturing processes have made available magnetic materials well suited for astatic magnetometers; products of ceramic barium ferrite ( $\mathrm{BaFe} \mathrm{Fe}_{12}$ $\mathrm{O}_{19}$ ) such as Magnadur II, Magnadur III, Indox V and Arnox Va , and cobaltplatinum alloys such as Platinax II have very high coercive forces and their specific intensity of magnetization is almost independent of shape. The $P / I$ curves of these materials are comparable and the performance of a magnet system built with any of these materials would be approximately the same (Deutsch et al., 1967). Platinax II, however, is a very hard material that can be easily machined and is not as friable as the ceramic material. The Platinax II $P / I$ curve is given in Figure 1 for different practical values of $I_{2}$. The $I_{2}$ of the system described next is $0.0019 \leqslant I_{2} \leqslant 0.0025 \mathrm{gm}_{\mathrm{gm}}{ }^{2}$. The uncertainty arises from the limits of error in calculating the moment of inertia of each component of the system. For this $I_{2}$, the maximum $P / I$ requires 0.18 cm diameter magnets while ours are 0.2 cm . The reason for the discrepancy is that the exact value of $I_{2}$ cannot be determined in advance.

## Part II - Experimental design

## 1. The magnet system (Figure 2)

The separation $L$ (centre to centre) between the magnets (height $=0.8 \mathrm{~cm}$ ) is 7.68 cm . The glass connecting rod $(0.90$ cm dia.) is inserted and cemented into the aluminum holder (wall thickness $=0.03$


Figure 1. Values of $P / /$ plotted against the diameter of transversely magnetized cylindrical magnets (height $=0.8 \mathrm{~cm}$ ) for fixed $/ 2$ and calculated from (7). $\rho=15.5$. The calculated $J_{2}$ of the astatic system described in Part II is indicated.


Figure 2. Astatic system of Platinax 11 magnets as described in Part II.
cm ). The upper magnet is inserted and cemented into its holder (wall thickness $=$ 0.025 cm ). The mirror (side $=0.5 \mathrm{~cm}$, thickness $=0.001 \mathrm{~cm}$ ) is cemented into a depression of the top holder in order to maintain the dynamic balance of the system. The cross section of the bottom of the hook is of the knife edge type to avoid relative angular displacement between the magnet system and the suspension. The bottom magnet is pressure fitted into the slotted bottom holder so that with the aid of the rig described here it is possible to obtain high astaticism without the use of trimmer magnets that would add substantially to the moment of inertia. The magnets were first chosen out of a lot of 20 by comparing their magnetic moments using a commercial oerstedmeter. With repeat measurements at different distances from the probe, two magnets could be matched to better than 0.002 for an astaticism $A_{5}\left(=P / P_{5}^{\prime} ;\right.$ eq. 4$)>$ 500. The final $A_{S}(1000)$ was obtained by rubbing down the bottom magnet with an emery cloth. An azimuthal astaticism $A_{A}\left(=P / P_{A}^{\prime}\right.$; eq. 4) of 2200 was obtained with the following method. The bottom holder (with its magnet) is loosely clamped into an expansible hole (by means of a set screw) made at the end of a long pointer $(25 \mathrm{~cm})$. The pointer and the magnet system are placed onto a plate where an expansible hole receives the protruding bottorn magnet which is then securely clamped. The pointer is moved in the required direction on a graduated scale drawn on the plate; in this way, the upper part of the system (carrying the upper magnet) can be accurately rotated while the bottom magnet is held in place. With such controlled rotations, a high astaticism can be obtained in a few $(\approx 4)$ trials. $A_{A}$ and $A_{S}$ were determined by producing uniform fields parallel to (for $A_{A}$ ) and perpendicular to (for $A_{S}$ ) the direction of magnetization of the magnets. It is preferable to do both astaticisms at the same time as they become large. Unless the applied field is exactly parallel (or perpendicular) to the axis of magnetization of the upper magnet, and this usually is not the case when astatizing (because the system is
taken in and out so often), the field will not be applied solely to $P_{A}^{\prime}$ or $P_{S}^{\prime}$ but to a component of each. If $P_{S}^{\prime}$ is much larger than $P_{A}^{\prime}$, for example, part of it can easily be mistaken for a $P_{A}^{\prime}$ with the result that the magnet will be rotated the wrong way.

## 2. Magnet system housing (Figure 3)

The system is suspended by a $30-\mathrm{cm}$ long phosphor bronze strip attached to a threaded rod passing through a circular plate which closes the upper end of an aluminum tube (length 23.5 cm ; diameter 2.5 cm ). The threaded rod and circular plate permit height adjustment of the magnet system. The tube is fixed to a 3-point aluminum plate resting on a wooden tripod. Levelling screws permit plumb adjustment of the tube. Under the plate, a rectangular box (height 18.7 cm ; sides 7.6 and 3.2 cm ) is attached. The short sides are made of aluminum and hold a nylon bottom plate. On the centre of this plate, a threaded holder carrying an aluminum disc (diameter 2.5 cm ; thickness 0.15 cm ) can be height adjusted for critical damping. The long sides are closed by detachable Perspex windows. The width of the box facilitates the installation and removal of the magnet system from the suspension hook. Two sides and the bottom are of nonmetallic materials to avoid eddy currents. Lenses of different focal lengths can be easily installed on the window facing west. The mirror has been set facing west so that the light beam is not in the direction of the operator.

## 3. Field compensation

The magnetometer is installed in the centre of a set of three orthogonal pairs of square (side $=244 \mathrm{~cm}$ ) coils, which is part of an array of five identical sets (Roy et al., 1969). The set (Figure 3) is located at the south end of a $3 \times 12$ meters building oriented along the magnetic meridian. Each component (vertical $Z$, horizontal along $H_{H}$ and perpendicular to $H_{D}$ the meridian) of the earth's field are compensated for by two circuits. Constant fields produced by constant currents compensate the mean field and a negative feedback fluxgate system compensates the diurnal variations. An addi-
tional winding on the coils is used to produce nearly uniform fields when astatizing the magnet system.

The system is oriented with the north pole of the bottom magnet pointing north. The effective compensation of the
diurnal variations are $0.998 \pm 0.0002$ for $H_{H}$ and $1.000 \pm 0.0002$ for $H_{D}$. Since the astaticisms are $A_{A}=2200$ and $A_{S}=$ 1000 , the ratio of apparent uniform disturbing field is $10^{-6}$ for north-south and $2 \times 10^{7}$ for east-west disturbances.


Figure 3. Astatic magnetometer with styrofoam head and specimen presentation table. Descriptions are given in Part II.

This means that for a change of say $100 \gamma$ in the north-south component, the deflection of the magnet system would correspond to a field of $10^{-9}$ Oe applied to the bottom magnet. At the location, the diumal variations on a normal day are in the $60-70 \gamma$ range and on a disturbed day, they average about $200 \gamma$. The instrument drift due to diurnal variations is therefore negligible.

## 4. Response of an astatic magnetometer

The amplitude of the angular deflection of the magnet system to the magnetization of a rock sample depends (1) on the positioning of the sample with respect to the system, (2) on the distance $L$ between the two magnets and (3) on the shape and size of the sample.
(1) The sample can be positioned many ways (see Collinson and Creer, 1960). For a given distance ( $z$ ) between the sample and one of the magnets, maximum response is obtained when the sample is placed in the horizontal plane and in a direction perpendicular to the axis of magnetization of the magnet (position A). Another position (B) is the placing of the sample on the axis of rotation of the system and below the lower magnet. The response of the instrument is about twice as large for position $A$ as for position $B$. However, for practical considerations, position B is usually favoured. Technically, with a more sophisticated magnet system housing design, it is possible to make $z$ as small for position $A$ as for position B. However, because the presentation of the sample must be done by remote control (to avoid magnetic and other disturbances caused by the operator) safety devices to protect against accidentally hitting the instrument must be added. For position B, such devices (aluminum clamp on Figure 3) can be installed without increasing $z$ since the sample and holder slide under the instrument. For position A, the sample has to be pushed toward or alongside the instrument. Since it is useful to be able to vary the distance (for measuring different intensities) the latter case should have a transverse motion. Therefore, in both cases, the sample has to be pushed toward the instrument and a protective screen
must be installed, and $z$ increased Because the field reduces as the third power of the distance, a small increase of $z$ will considerably reduce the instrument response. So, in practice, it is found that there is little to choose between the two positions. Position B was chosen because only one component (horizontal) of magnetization is measured in a single reading. In position $A$, the vertical component produced a field at the upper magnet; the deflection produced by this component is nulled by inverting the sample and averaging.
(2) The sensitivity of the instrument depends on $L$ since the field produced at the oppositely magnetized upper magnet reduces the deflection. $L$ should then be made large. On the other hand, the larger $L$ is, the larger are the deflections produced by magnetic disturbances other than diurnal variations; disturbances such as those caused by a nearby magnetic object and distortion of the field compensating coils.
(3) The standard size specimen used in our laboratory is an upright cylinder of 2.5 cm diameter and $2,2 \mathrm{~cm}$ height for a ratio height/diameter $=\pi^{1 / 2} / 2$. A larger ratio would increase the response of the magnetometer (Roy, 1967). However, since the specimen is of finite size and not a dipole point, corrections as calculated by Papapetrou (see Blackett, 1953) must be applied. When the specimen is cut according to the above ratio, the corrections are quite small ( $2 \%$ for $z=3.6$ cm ) and the same whether the specimen is upright or on its side (Roy, 1966); thereby, the errors due to shape are small and the computation of results simplified.

A larger deflection would be obtained by using a larger specimen even if, for small 2 , the increase in deflection is not equal to the increase in volume. To make room for the larger specimen, 2 must be increased by $\Delta z=\left(V_{x}^{1 / 3}-V_{s}^{1 / 3}\right) / 2$ where $V_{s}$ and $V_{x}$ are the volumes of the standard and larger specimens respectively. The increase of the ratio deflection/volume varies with the increase in volume; for a typical $z=3$ to 4 cms , the ratio increase would amount to $0.6-0.8$ of a two- to four-fold increase in volume or about a 3-times larger deflection for a

4-times larger volume. There are many hindrances to using too large a specimen; for example, as the size is increased, the effects of inhomogeneity increase, larger coring equipment is required, etc. The main consideration is that, in rock magne. tism, a specimen is often fitted into different apparatuses. Because other pieces of equipment such as alternating field demagnetizer favour small specimens, a medium-size specimen must be adopted as a standard.

## 5. Calibration

The system is calibrated by means of a coil suspended from the ceiling. The distances from the centre of the coil to the centres of the magnets are 122.27 and 129.95 cm . The 91 turns are tapped on the fifth turn to provide two fieldproducing sources for calibration of high ( 5 turns) and low ( 91 turns) sensitivities. The difference of field $\Delta H$ at the magnets is $1.010 \times 10^{8} 0 \mathrm{e} / \mathrm{ma}$ for the 5 turns (diameter $=16.76 \mathrm{~cm}$ ) and $0.6794 \times 10^{-7}$ $\mathrm{Oe} / \mathrm{ma}$ for the 91 turns (diameter $=15.98$ cm).

## 6. Specimen table (Figure 3 and 4)

The specimen is placed in a graduated ( $10^{\circ}$ spacing) Perspex cylinder which has been bored so that the specimen fits snugly. The cylinder fits into a rectangular piece of laminated wood veneer (permali). The dimensions of the cylinder and the wood holder are such that the distance between the centre of the specimen and all faces of the holder is constant so that 2 remains constant for all attitudes of the specimen. Holes in the bottom and two sides of the holder fit onto a pin in the centre of a small table for accurate centring of the specimen. Ridges on each side of the table maintain the orientation of the holder. The table is attached to a female tapered post which fits onto a male tapered post in the centre of a disc (diameter $=14 \mathrm{~cm}$ ) whose perimeter is graduated in degrees. The assembly is installed on a three-wheeled carriage which is rolled under the magnetometer by means of string and pulleys. When the assembly is against its stop, gear coupling (ratio 4 to $1 ; 1$ turn $=90^{\circ}$ ) permits rotating the assembly from a distance of two meters. The orientation


Figure 4. General view of astatic magnetometer and accessories.
of the specimen given by the graduated circle is read through a lens.

Centring and levelling of the holder table was accomplished by means of a small coil producing vertical fields. The carriage table is moved and tilted on the stationary table until the magnet system remains undeflected when a large field is applied in different azimuthal directions. A levelling to within $0.5^{\circ}$ and a centring to within 0.3 mm could be obtained. Five different $z$ 's are provided by inserting tapered spacers (shown on the desk) under the holder table. The alignment of all parts is maintained by a slot and a pin at the bottom and top of the spacers. The distance $z$ between each position and the bottom magnet is measured by means of magnetic fields; this is more accurate than direct readings of the distance. For each position a small two-turns coil (diameter $=.503 \mathrm{~cm}$ ) is placed with its axis perpendicular to the axis of magnetization of the magnet. A field is produced by passing a calibrated current through the coil. The difference of field $\Delta H$ at the bottom and upper magnets (for large A)
is given by

$$
\begin{gather*}
\Delta H=\pi N i C_{c} r^{2} 10^{-4} \mathrm{X} \\
{\left[\frac{C_{B}}{\left(r^{2}+z^{2}\right)^{3 / 2}}-\frac{C_{U}}{\left\{r^{2}(z+L)^{2}\right\}^{3 / 2}}\right] \cdots} \tag{9}
\end{gather*}
$$

where $i$ is the current in milliampere, $N$ is the number of turns and $r$ the radius of the coil. $C_{c}, C_{B}$ and $C_{U}$ are the corrections for the shape of the coil, bottom and upper magnets respectively. These corrections are to compensate for the differences between the physical and effective centres of coil and magnets; differences that are not negligible when $z$ is comparable to the dimensions of these components.

The angular deflection $\theta$ of the system produced by $\Delta H$ is measured by the deflection (defl.) of the light spot reflected from the mirror. Using a scale at a distance $D^{\prime}$,

$$
\Delta H=\frac{H_{s} \times \operatorname{defL}(\mathrm{mm})}{2 D^{\prime} \theta}=S \times \operatorname{deff} .(\mathrm{mm}) \ldots(10)
$$

where $S$ is the sensitivity expressed in $\mathrm{Oe} / \mathrm{mm}$ defl. and is defined as the difference of field $H_{s}$ required to deflect the light spot by 1 mm at a distance $D^{\prime}$. From (9) and (10) we find that

$$
\begin{gathered}
\frac{C_{c} i}{\text { defl. (mm) }} \times \\
{\left[\frac{C_{B}}{\left[r^{2}+z^{2}\right]^{3 / 2}}-\frac{C_{U}}{\left\{r^{2}+(z+L)^{2}\right\}^{3 / 2}}\right]=C}
\end{gathered}
$$

where

$$
\begin{equation*}
C=\frac{10^{4} S}{\pi N r^{2}} \tag{12}
\end{equation*}
$$

Taking measurements at the different positions different $i, z$ must be determined so that $C$ in (11) is a constant. It is found that with precise measurements of $i$ and defl. (the two large variables), $z$ can be determined to within 0.3 mm . The method also provides an excellent check on the sensitivity (12) obtained from the
calibration coil. The agreement between the two methods of calibrating is within 1 per cent.

The ratio of $P / I$ can be checked experimentally. From (3) and (10), we get

$$
\begin{equation*}
P / I=2 \pi^{2} / D^{\prime} S T^{2} \tag{13}
\end{equation*}
$$

The $P / I$ obtained by measuring $T$ is 1975 and in agreement with the theoretical value (Figure 1).

## Part III - Torsion method

## 1. Performance

The system was first tested by placing a graduated scale at $D^{\prime}=1.7$ meters. Using suspensions of different torsional constants, the following sensitivities and periods were determined
$S=13.5 \times 1 \sigma^{8} 0 \mathrm{e} / \mathrm{mm}$ defl. $\quad T=6.6 \mathrm{sec}$. $S=3.37 \times 10^{8} \mathrm{Oe} / \mathrm{mm}$ defl. $T=13.2 \mathrm{sec}$.
$S=1.94 \times 10^{8} 0 \mathrm{e} / \mathrm{mm}$ defl. $T=17.4 \mathrm{sec}$.
On a scale at $D^{\prime}=5$ meters, the deflection would be about three times larger. The system could then be used as a moderately high sensitivity magnetometer ( 4.6 $\times 1 \sigma^{8} \mathrm{Oe} / \mathrm{mm}$ defl.) with a low period ( 6.6 sec ) or as a high sensitivity ( 6.6 x $10^{-9} \mathrm{Oe} / \mathrm{mm}$ defl.) with a period of 17.4 sec.

## 2. Measurements

The magnetic moment of a specimen is often determined by measuring its three orthogonal components; $p_{x} p_{y}$ and $p_{z}$. Since this measuring method can be used with the torsion and the magnetic control methods, a brief account of the procedure is given.

The specimen is placed upright with its orientation mark on $0^{\circ}$ azimuth of the table to obtain $p_{x} ; p_{y}$ is obtained by rotating the table by $90^{\circ} ; p_{z}$ is obtained by placing the specimen on its side and with its axis perpendicular to the axis of magnetization of the bottom magnet. The components of magnetization are obtained ( $A$ being large) from
$p_{x}=B_{x} s\left[\frac{E_{B x} C_{B}}{z^{3}}-\frac{E_{U x} C_{U}}{(z+L)^{3}}\right]^{-1}$
$p_{y}=B_{y} S\left[\frac{E_{B x} C_{B}}{z^{3}}-\frac{E_{U x} C_{U}}{(z+L)^{3}}\right]^{-1} \ldots(15)$
$p_{z}=B_{z} S\left[\frac{E_{B z} C_{B}}{z^{3}}-\frac{E_{U z} C_{U}}{(z+L)^{3}}\right]^{-1} \ldots .(16)$
where $E$ is a specimen shape correction which depends on the distances ( $z$ and $z+L)$ to the bottom $\left(E_{B}\right)$ and upper $\left(E_{U}\right)$ magnets and on the presentation of the specimen: upright $\left(E_{x}\right)$ or on its side $\left(E_{z}\right)$. $B_{x}, B_{y}$ and $B_{z}$ are the scale deflections. For large $L, E_{U}$ and $C_{U}$ can be neglected and we have
$p_{x}=B_{x} z^{3}\left[E_{B x} C_{B}-\left(\frac{z}{z+4}\right)^{3}\right]^{-1}$
$p_{z}=B_{y} s_{z^{3}}\left[E_{B x} C_{B}-\left(\frac{z}{z+L}\right)^{3}\right]^{-1}$
$p_{z}=B_{z} S_{z} z^{3}\left[E_{B z} C_{B}-\left(\frac{z}{z+L}\right)^{3}\right]^{-1}$

Since $z$ is constant, it is more convenient to determine the corrections in terms of the different positions used so that

$$
\begin{align*}
& p_{x}=B_{x} s C_{x}  \tag{20}\\
& p_{y}=B_{y} s C_{x} \\
& p_{z}=B_{z} s C_{z} \tag{22}
\end{align*}
$$

where all the corrections are included in $C_{x}$ and $C_{z}$ which can be readily obtained from tables. In a rock collection, most specimens are long enough to be cut to standard length ( 2.2 cm ); $z$ and the volume are then constant and $C_{x}=C_{z}$. The intensities (Int.) of each component are then given by

$$
\begin{align*}
& \text { Int }_{x}=B_{x} E  \tag{23}\\
& \text { Int } t_{y}=B_{y} E \tag{24}
\end{align*}
$$

$$
\begin{equation*}
\ln t_{g}=B_{z} E \tag{25}
\end{equation*}
$$

where $E$ is the constant correcting factor multiplied by the sensitivity and divided by the volume. The directions ( $D$ and $n$ ) and the total intensity of magnetization are determined from these components. The effects of inhomogeneity of magnetization are reduced by averaging readings $180^{\circ}$ apart and also by averaging readings of upright and inverted positions of the specimen. In the side position (lnt.z), the holder is rotated $180^{\circ}$ about its axis.

## Part IV - Magnetic control method

The performance and efficiency of a torsion-controlled astatic system can be improved by using magnetic fields to control and measure the deflection. This is illustrated by using as an example the previously described system, two photo resistors and an electrical circuit which provides an automatic negative feedback. The circuit (Figure 5) has been designed to suit specific conditions that will be discussed. However, it can be easily modified for different conditions and requirements, and great freedom is left to the designer.

By comparing the two methods, the magnetic control is preferred. For example, it permits, while maintaining short periods, sensitivities not possible with the torsion method since the period would then be too long to meet the requirements. As opposed to the torsion method where the sensitivity and period are set by the suspension fibre, the magnetic control method allows quick switching among several different sensitivities and associated periods. This increases the working range and efficiency of the magnetometer since the more strongly magnetized specimens can be measured at much lower period and therefore in less time. Because of the quick response, the system can be used as a null detector and the direction of magnetization can be determined directly. The direct-read method in turn allows taking full advantage of the flexibility of the instrument, thereby increasing the accuracy of results achieved with the three-component method. Problems
arising as the sensitivity is increased and precautions to be taken will be discussed.

## 1. Principle of operation

When the horizontal field is equal at the upper and lower magnets ( $\Delta H=0$ ), the light spot (diameter 2.1 cm ) illuminates equally two photo resistors (diameter 2.5 cm ) placed side by side at a distance of 90 cm from the magnet system. The current through each photo resistor is 6 ma , the lower branch of the circuit (Figure 5) is in balance, and no current flows in the upper branch. When a magnetized specimen is brought under the magnet system $(\triangle H \neq O)$, the spot is deflected, the resistance of one photo resistor decreases, the resistance of the other increases, and a current flows through the upper part of the circuit and one of the seven solenoids, depending on the switch position. The solenoid is located near the upper magnet and in the same horizontal plane (Figures 3 and 4) with its axis perpendicular to the axis of magnetization of the magnet. It is wired so that the torque it produces on the upper magnet tends to reduce the deflection. If, in a particular switch position, the circuit gives a current through the solenoid of $K_{1} \mathrm{ma} /$ radian deflection, and the solenoid produces a field of $K_{2}$ De/ma at the upper magnet, the feedback torque for a small deflection $\theta$ is $P K_{1} K_{2} \theta$. When the system has come to rest

$$
\begin{equation*}
P \Delta H=P K_{1} K_{2} \theta+\sigma \theta \tag{26}
\end{equation*}
$$

writing

$$
\begin{equation*}
P K_{1} K_{2} / \sigma=G \tag{27}
\end{equation*}
$$

where $G$ is the (magnetic/torsion) control ratio

$$
\begin{equation*}
\Delta H=K_{1} K_{2}\left(1+\frac{1}{G}\right) \theta \tag{28}
\end{equation*}
$$

The deflection $\theta$ is determined by taking the reading $n$ in millivolts as measured across a precision resistor $R$ inserted in the feedback circuit and is given by

$$
\begin{equation*}
n(\mathrm{mv})=K_{1} R \theta \tag{29}
\end{equation*}
$$



* NEG. FEEDBACK ACTING ON UPPER MAGNET

Figure 5. Circuit used to provide negative feedback from signal picked up by the photo resistors.
and from (28)

$$
\begin{equation*}
n(\mathrm{mv})=\frac{R \Delta H}{K_{2}\left(1+\frac{1}{G}\right)} \tag{30}
\end{equation*}
$$

The sensitivity $S$ in oersted per millivolt is then given by

$$
\begin{equation*}
S(\mathrm{Oe} / \mathrm{mv})=\frac{\Delta H}{n}=\frac{K_{2}\left(1+\frac{1}{G}\right)}{{ }_{\mathrm{G}}} \ldots \tag{31}
\end{equation*}
$$

The factor $K_{2}$ can be calculated from the geometry:

$$
\begin{equation*}
K_{2}=\frac{\pi N 10^{-4}}{l} \times \tag{32}
\end{equation*}
$$

$$
\left[\frac{x+l}{\left\{(x+l)^{2}+r^{2}\right\}^{1 / 2}}-\frac{x-l}{\left\{(x-l)^{2}+r^{2}\right\}^{1 / 2}}\right]
$$

where $l$ is the half-length of the solenoid, $r$ its radius, $x$ its distance from the magnet, and $N$ the number of turns.

The control ratio $G$ can be determined by comparing the deflection produced by a given $\Delta H$ with and without
feedback. However, it is difficult to obtain an accurate estimate in this way, and it is preferable to measure the sensitivity first by means of the calibration coil (III, 5), and then derive $G$ from (31):

$$
\begin{equation*}
G=\left[\frac{R S}{K_{2}}-1\right]^{-1} \tag{33}
\end{equation*}
$$

The sensitivity can be accurately determined by measuring in mv the deflection caused when a $\Delta H$ is applied. The application of progressively higher $\Delta H$ permits one to determine the operating range of the photo resistors and the accuracy of the readings (i.e. the near linearity of the curve $\Delta H / n$ ) within that range.

The period of the undamped system is

$$
\begin{align*}
T_{c} & =2 \pi\left[\frac{I}{\sigma+K_{1} K_{2} P}\right]^{1 / 2}  \tag{34}\\
& =2 \pi\left[\frac{I}{\sigma(G+1)}\right]^{1 / 2}
\end{align*}
$$

by analogy to (2). Both the aluminum damping disc (II, 2) and the capacitors shown in Figure 5 are used for damping the system. The damping disc is adjusted for critical damping at a period $T_{c}$ of 5 sec. The additional damping provided by the capacitors reduces both the time required to take a reading and the oscillations of the magnet system caused by vibrations of the ground. The frequency of these oscillations varies (about a 4 cycles/sec frequency) depending on the disturbing conditions. Without electrical damping, oscillations would occasionally build up (especially when operating the instrument at lower sensitivities where the magnetic control is large and $T_{c}$ short $\cong 2$ to 3 sec ) until the light spot was driven out of the range of the photo
resistors. The values of the capacitors were determined empirically, and a variety of time constants provided to meet different conditions.

## 2. Characteristics of the system

The light source is a Pye (W.G. Pye Co. Ltd.) lamp outfit (\#8122). The light bulb ( $4 \mathrm{~V}-1 \mathrm{~A}$ ) and the optical system is placed at 1.1 m from the magnetometer. The transformer ( $117 / 4 \mathrm{~V}$ ) is magnetic and placed 10 meters away. A lens ( 1 m focal length) is placed at 1.6 cm from the mirror. The light beam is received on two cadmium sulphide photo resistors (NSL 4972; Dwg 5472; National Semiconductors Ltd.) mounted on a brass carriage (at $D^{\prime}=90 \mathrm{~cm}$ ) that can be remotely displaced ( $\pm 3 \mathrm{~cm}$ ) in a hori-
zontal direction perpendicular to the direction of the light beam. The photo resistors are housed in a tapered rectangular box which projects to within 25 cm of the magnet system; the inside of the box has been painted black and the instrument can be operated in a lighted room. The photo resistors (shown on the table; Figure 6) were specially manufactured without a metal case and the magnetization of the pins produces a negligible field at the magnet system. Their rated characteristics are max power $=1$ watt, max voltage $=420 \mathrm{~V}$, resistance at 100 foot-candles $=140$ ohms and in darkness $=2.3$ meg ohms. In the system described, when the light spot is directed on one photo resistor, the resistance is 2.1 K on the lighted photo resistor and


Figure 6. Control panel as described in Part IV. The deflection shown has been obtained by passing a current through the calibration coil. The dial indicating the alignment of the magnet system is shown on the left. The aluminum spacers used to obtain different distances are also shown. On the table are photo resistors of the type used.

200 K on the other giving a max/min ratio of about 100 . Among several types of photo resistors tested, this type gave the highest ratio. Since the deflection ratio $\mathrm{mv} / \mathrm{mm}$ increases with this ratio, the photo resistors should be chosen accordingly. When the spot is equally split onto the two photo resistors, the resistance of each is about 17 K .

A 185 -volts power source is trimmed so that on zero deflection of the magnetic system a current of 6 ma (base current) flows through the photo resistors. Owing to long term changes in the circuit and light intensity changes due to voltage variations and dirt on the lenses, the input voltage might have to be changed slightly to obtain the right base current. This is done by trimming down a constant voltage source set slightly higher than required, and which is placed at the other end of the room because of its magnetic properties. The voltage across and the power through the photo resistors are about 100 yolts and 0.6 watt. With a rated power of 1 watt, the current (and sensitivity) could be increased by 25 per cent if necessary. However, as a precaution and for longer life of the photo resistors, all calibrations have been performed on the 6 ma base current and therefore hereafter parameters such as $D$, $G$ and working range, which depend on the base current, are given on this basis.

The negative feedback can be switched to one of the seven solenoids (radius = 0.4 cm ). Their number of turns with the mean distance (given in cm in brackets) from the upper magnet are in descending order of sensitivity 1(7.6), 2(7.6), 5(7.5), $10(7.2), 4(3.7), 60(6.1)$ and $100(4.6)$. The deflections are measured in mv across a $1-K$ resistor by means of a DC null voltmeter (Hewlett Packard; 419A) and/or an integrating digital voltmeter (H.P. 2401.C).

Different spacings between the photo resistors were tried. As the spacing is increased (from 0.2 to 1 cm from side to side) the sensitivity increases slightly ( $5-10 \%$ ) and the overall working range remains about the same; the portion of the range, where $\Delta H / n$ is almost linear, decreases. In practice, the feedback current increases with the angular deflec-
tion until the spot is fully (or centred) on one of the photo resistors. However, for the feedback current to be practically linear with respect to the deflection, i.e. ratio (current/deflection) constant, the spot must be on both photo resistors. Once the spot has left one photo resistor but keeps moving onto the other the ratio (current/deflection) becomes smaller and smaller (from $100 \%$ to $90 \%$ ) resulting in a decrease in sensitivity. Therefore, in order to minimize the sensitivity variations within a given range, the photo resistors have been placed as close as possible to each other, that is 0.2 cm for these caseless photo resistors.

## 3. Sensitivities

Without magnetic control, and with a suspension giving $\sigma=5.5 \times 10^{-3}$ dyne $\mathrm{cm} /$ radian, the period of the system is 6.6 sec and the sensitivity is $2.55 \times 1 \sigma^{7}$ $0 \mathrm{e} / \mathrm{mm}$ at $D^{\prime}-90 \mathrm{~cm}$. Table I gives the eleven sensitivities ( S 1 to S 11 ) available with the magnetic control. They were measured with the aid of the calibration coil over a range of $\Delta H$ values (IV, 1), and the table shows the range of output readings for each switch position within which the sensitivity is constant to 3 per cent and 1 per cent respectively.

Table I also gives the factor $G$, calculated from (33), the ratio

$$
\begin{equation*}
f_{c}=1 /\left(1+\frac{1}{G}\right. \tag{35}
\end{equation*}
$$

which is the fraction of $\Delta H$ measured by magnetic control, and the period of the system $T_{c}$, calculated from (34).

S 1, S 2, S 6, S 8, S 9, S 10 and S 11 are regarded as the primary sensitivities, and are generally used, because of their larger $G$ and $f_{c}$ values, and smaller $T_{c}$. The instrument can measure (on S 11) fields as large as $3 \times 10^{-5} \mathrm{Oe}$ and it can detect (on S 1) fields as low as the disturbing conditions at the location permit. The disturbances affecting the instrument are discussed in (IV, 6); under the best conditions at the site, magnetizations producing fields as small as 2 x $10^{9} \mathrm{Oe}$ at the lower magnet can be detected. One advantage of the photoelectric system can be seen from the following comparison. To obtain a sensitivity of $0.56 \times 10^{-9} 0 \mathrm{Oe} / \mathrm{mm}$ deflection on a scale at a distance $D^{\prime}$ of 5 meters, the system without feedback would have a period of 60 seconds, which would be impractical because of disturbance problems.

The control panel is shown in Figure 6. The meters on the right-hand side indicate at all times the voltages across and the currents through the photo resistors. On zero deflection a large change in voltage from 100 volts would be indicative of a lighting or photo resistor problem. The input current trimmer is located between the two milliammeters and is the only adjustment required for

Table I. Particulars of the system for each of the 11 circuits shown in Figure 5.

|  | Sensitivity |  |  |  | RANGE | IT (mv.) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\times 10^{-9} \mathrm{Oe} / \mathrm{mv}$ | $G$ | $f_{c}$ | $\underset{(\mathrm{sec})}{T_{c}}$ | 3 per cent accuracy | 3 per cent accuracy |
| S 1 | 0.56 | 0.64 | 0.40 | 5.1 | 3000 | 2500 |
| S 2 | 0.68 | 1.50 | 0.60 | 4.2 | 2400 | 2000 |
| S 3 | 0.88 | 0.35 | 0.26 | 5.7 | 1500 | 1200 |
| S 4 | 1.17 | 0.58 | 0.36 | 5.2 | 1200 | 900 |
| S 5 | 1.48 | 0.42 | 0.30 | 5.5 | 1000 | 700 |
| S 6 | 1.77 | 2.00 | 0.67 | 3.9 | 1500 | 1250 |
| S 7 | 3.15 | 0.58 | 0.37 | 5.2 | 550 | 450 |
| S 8 | 5.30 | 1.03 | 0.51 | 4.6 | 450 | 350 |
| S 9 | 13.30 | 2.78 | 0.69 | 3.4 | 400 | 325 |
| S 10 | 29.40 | 9.10 | 0.90 | 2.1 | 300 | 275 |
| S 11 | 120.00 | 28.50 | 0.97 | 1.2 | 275 | 250 |

$G$ is the control ratio (magnetic/torsion) given by (33).
$f_{c}$ is the fraction of $\Delta H$ measured (35).
Without magnetic control, the period of the magnetometer is 6.6 seconds.
intensity measurements (no adjustments are required for direction determinations). The milliammeter in the upper left-hand corner is used for calibration. In this photograph, a current is applied to the calibration coil to deflect the system off zero. A digital ammeter of high resolution can be used by switching to the terminals below the meter. The high or low sensitivity calibration coil can be selected by a switch. The milliammeter (centre left) indicates the deflection of the magnet system during measurement and is useful because its response is quicker (no damping) than that of the nullmeter shown on the left of the panel. For direction finding, the milliammeter is used to find an approximate zero and fine zeroing is accomplished using the nullmeter which has a large scale and is easier to read. The other meter (bottom left) is an indicator for the zeroing procedure (when $\Delta H=0$ ) that will be explained later.

## 4. Design variations

Under this heading, we consider the possibility of extending the measuring range of a magnetically controlled astatic magnetometer beyond the limits imposed by the present requirements and the disturbing conditions (described in IV, 6) existing at this particular site.

The upper limit has been set so that, with the present specimen table and specimen size, most weakly magnetized (intensity $\leqslant 4 \times 10^{-3}$ e.m.u.) rock specimens can be measured; the direction and intensity of specimens of larger intensity are quickly measured by means of a fluxgate magnetometer especially adapted for this purpose. Thus, in this instance, the largest field ( $3 \times 10^{5} \mathrm{Oe}$ ) the instrument can measure is adequate; however, for other applications or with a different setting, it might be desirable to design an instrument which could measure higher fields. The upper limit can easily be raised and it is not necessary to open the housing (III, 2) of the magnetometer.

When the instrument is operated at lower sensitivities, $G$ is large (Table I), and (31) shows that $S$ is then almost independent of $G$ and proportional to
$K_{2}$. Therefore, the sensitivity can be reduced (more Oe per mv) by simply adding turns to the solenoid or reducing the distance between the solenoid and the upper magnet. From (27), (31) and (34), it is found that the reduction of $T_{c}^{2}$ is then almost proportional to the reduction of $S$. Thus, without changing the suspension, the measuring range can be extended upwards so that the instrument can also be used as a low sensitivity and short period magnetometer.

Under the present disturbing conditions discussed in IV, 6, the measuring range of this particular instrument cannot be extended downwards. Higher sensitivities would not increase the performance unless the disturbances or their source (mainly temperature changes) can be better controlled or damped. However, under the assumption that this can be done and as a matter of interest to people designing a magnetometer for operation under more favourable conditions, the extension of the measuring range downwards is now considered.

Equations (27) and (31) show that higher sensitivities (less oersted per mv) can be obtained by reducing either $K_{2}$ or $\sigma$. However, because, at high sensitivity, $G$ is usually small, the change of $S$ obtained by changing $K_{2}$ or $a$ is not readily visualized from the equations and may be illustrated by an example. Using S 1 of Table I as a base for comparison, the calculated sensitivities $\left(S_{x}\right)$ and periods $\left(T_{x}\right)$ obtained by
changing $K_{2}$ and $\sigma$ to arbitrary $K_{X}$ and $\sigma_{X}$ are given in Table II. In the calcutations, $f_{c}$ has been kept equal or larger than 0.20 so that a reasonable fraction of $\Delta H$ is measured. The table shows that a small improvement in sensitivity can be optionally obtained by reducing $K_{2}$ or $\sigma$; changes of suspension can therefore be avoided by using a different solenoid to change the sensitivity. Table II also shows that to obtain a large increase of $S_{3}$, both $K_{2}$ and $\sigma$ must then be reduced. In Nos. 6,7 and 8 where $G_{x}$ is kept constant, the increase of both $S_{x}$ and $T_{x}$ is proportional to the reduction of $\boldsymbol{K}_{x^{*}}$

The sensitivity could also be increased by increasing $K_{1}$. An increase of $\boldsymbol{K}_{1}$ would increase the control ratio $K_{1}$ (27) which in turn would increase $S$ (31). $K_{1}$ could be increased in a number of ways, e.g. light beam of stronger intensity and photo resistors with a higher power rating. The use of a stronger magnet cannot increase the sensitivity and, as in the torsion method, the magnet system must be designed according to the theory given in Part I. From (27), (31) and (34), we find

$$
S=\frac{1}{R K_{1}}\left(\frac{2 \pi}{T_{c}}\right)^{2} \cdot \frac{I}{P}
$$

showing that the sensitivity increases as $P / I$ increases.

## 5. Measuring method (direct read)

Because of the quick response, the instrument is used to read directly the

Table II. Calculated periods $\left(T_{x}\right)$ and sensitivities $\left(S_{x}\right)$ obtained by changing $G, K_{2}, 0$ and $f_{c}$ of S 1 (Table I) to arbitrary $G_{x}, K_{x}, \sigma_{x}$ and $f_{x}$. See Part IV - 4. Design variations.

| NO | $G_{x} / G$ | $K_{x} / K_{2}$ | $\sigma_{x} / \sigma$ | $G_{x}$ | $f_{x}$ | $T_{x}$ <br> sec | $\times 10^{9} 0_{\mathrm{e} / \mathrm{minv}}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{S 1}$ | $\underline{1}$ | $\underline{1}$ | $\underline{1}$ | $\underline{0.64}$ | $\underline{0.39}$ | $\underline{5.1}$ | $\underline{0.56}$ |
| 1 | 3.00 | 3.00 | 1.00 | 1.92 | 0.65 | 3.8 | 1.02 |
| 2 | 3.00 | 1.00 | 0.33 | 1.92 | 0.65 | 6.6 | 0.34 |
| 3 | 2.00 | 1.00 | 0.50 | 1.28 | 0.56 | 6.1 | 0.40 |
| 4 | 0.39 | 0.39 | 1.00 | 0.25 | 0.20 | 5.8 | 0.43 |
| 5 | 0.39 | 1.00 | 2.56 | 0.25 | 0.20 | 3.6 | 1.09 |
| 6 | 1.00 | 0.67 | 0.67 | 0.64 | 0.39 | 6.3 | 0.37 |
| 7 | 1.00 | 0.50 | 0.50 | 0.64 | 0.39 | 7.3 | 0.28 |
| 8 | 1.00 | 0.33 | 0.33 | 0.64 | 0.39 | 8.8 | 0.19 |

direction of magnetization. The specimen is placed in the holder so that its orientation mark is towards the $0^{\circ}$ azimuth on the graduated circle and the assembly is rolled under the instrument (as in Figure 4). It is then rotated until a zero deflection is obtained on the nullmeter. This occurs when the mean direction of the horizontal component of magnetization is parallel to the axis of magnetization of the bottom magnet. The angle $D_{1}$ between this direction and the mark is read directly on the graduated circle. The assembly is then rotated until a second zero giving $D_{2}$ is encountered at approximately $\left(D_{1}+180^{\circ}\right)$. Averaging of the two readings reduces the effect of inhomogeneity. With weakly magnetized specimens, the first reading is usually repeated (and used for averaging) for eventual drift. The sense of the direction is obtained from the positive or negative reading on $0^{\circ}$ azimuth. The same procedure is followed with the specimen in an inverted position. The declination $D$ is obtained by averaging the four readings. The graduated Perspex cylinder containing the specimen is rotated in its wooden holder so that, when the specimen is placed on its side, the horizontal component of magnetization lies in the horizontal plane. The assembly is then rotated until a zero reading is obtained on the nullmeter; this occurs when the mean direction of (the total) magnetization is parallel to the axis of magnetization of the bottom magnet. The angular reading on the graduated circle is that of the direction of magnetization with respect to the axis of the specimen, i.e. the inclination $l^{\prime \prime}$. $l^{\prime \prime}$ is obtained at about $180^{\circ}$ from $I^{\prime}$ and the average of the two readings gives $I_{1}$. The assembly is rotated to $I_{1}-90^{\circ}$ and then $I_{1}+90^{\circ}$ so that the direction of total magnetization is at right angle to the axis of magnetization of the bottom magnet and two intensity readings are measured on the integrating DVM (not shown). The holder is then rotated $180^{\circ}$ about its horizontal axis and the procedure is repeated; $I_{2}$ is obtained and $I_{2}-90^{\circ}$ and $I_{2}+90^{\circ}$ are measured. $I_{1}$ and $I_{2}$ are averaged to obtain $I$ and the four intensity readings averaged to get the total intensity (Int.). Whether $I$ is
positive or negative is determined from the direction of the deflection on $0^{\circ}$ azimuth.

Using the spacers (Figure 5), the specimen can be placed at five different distances $(z=3.58 ; 4.08 ; 5.08 ; 6.08$; 11.08 cms ) from the bottom magnet. These five positions (Pos. 5 to Pos. 1) and the 11 sensitivities permit to measure specimens of different intensities. From (19) the intensity is given by

$$
\begin{align*}
& \text { Int. }=S \text { defl. (mv) } z^{3} l \\
& {\left[E_{B z} C_{B}-\frac{z}{z+L}^{3}\right] V} \tag{37}
\end{align*}
$$

where $V$ is the volume of the specimen. Writing

$$
K=S z^{3} /\left[E_{B z} C_{B}-\left(\frac{z}{z+L}\right)^{3}\right] V \ldots .(38)
$$

where the constant $K$ is determined for each Pos. and $S$ we get

$$
\begin{equation*}
\text { Int. }=K \times \text { defl. (mv) } \tag{39}
\end{equation*}
$$

For convenience, the 55 different $K$ are tabled on the measuring sheet (Pos. vs $S$ ).

When a specimen is not of standard height ( $\neq 2.2 \mathrm{~cm}$ ), a correction must be added to the intensity measurements. This correction depends on the volume of the specimen and on the inclination $I$ and, for a given Pos., is given by

$$
\begin{equation*}
C_{Z}^{\prime}=\frac{\left[E_{B z} C_{B}-\left(\frac{z}{z+L}\right)^{3}\right] V}{\left[C_{I} C_{B}-\left(\frac{z}{z+L}\right)^{3}\right] V^{\prime}} \tag{40}
\end{equation*}
$$

where $C$ is the correction owing to the shape and orientation of the specimen and $V^{\prime \prime}$ is the volume of the (non-. standard) specimen. For $z>3$ and $L$ much larger than $z$, the effect of $(z / z+$ $L)^{3}$ is negligibly small and we can write

$$
\begin{equation*}
c_{Z}^{\prime}=\frac{c_{s} v}{c_{I} V^{\prime}} \tag{41}
\end{equation*}
$$

where $C_{s}$ is written for $E_{B z}$, the correction applicable to a standard specimen. $C_{I}$ is obtained from

$$
C_{I}=\left\{C_{V}^{2} \sin ^{2} I+c_{W}^{2} \cos ^{2} I\right\}^{1 / 2} \ldots \text { (42) }
$$

where $C_{V}$ is the correction to be applied when $I=90^{\circ}$; the axis of the specimen is then horizontal and perpendicular to the axis of magnetization of the bottom magnet. $C_{W}$ is the correction when $I=0^{\circ}$; the small dimension (height) is then parallel to the axis of magnetization of the magnet and no additional correction is required so that $C_{W}=C_{s}$. Since the volume ratio $V / V^{\prime \prime}=2.2 \mathrm{~cm} /$ height, the correction is then given by
$C_{Z}^{\prime}=2.2 /$ height $\left\{\left(C_{V} \sin I / C_{S}\right)^{2}+\cos ^{2} I\right\}^{1 / 2}$

The intensity of a non-standard specimen is obtained from

$$
\begin{equation*}
\operatorname{Int.}\left(\mathrm{n} . \mathrm{s}_{\mathrm{s}}\right)=K C_{Z}^{\prime} \mathrm{X} \text { defL (mv) } \ldots \tag{44}
\end{equation*}
$$

$C_{Z}^{\prime}$ has been tabled ( $h$ vs $I$ ) for the 5 Pos.
The largest value on the $K$ table is $1975 \times 10^{8} \mathrm{Oe} / \mathrm{mv}$. Since the range at S 11 is $\pm 250 \mathrm{mv}$ ( $1 \%$ accuracy; Table I), intensities up to $4.9 \times 1 \sigma^{3}$ e.m.u. can be measured. The smallest $K$ is $0.261 \times 1 \sigma^{8}$ $\mathrm{Oe} / \mathrm{mv}$ which means that an intensity of magnetization (of a standard specimen) $=$ $1 \times 1 \sigma^{7}$ e.m.u. will produce a deflection (at S 1) of 38 mv . The accuracy of the reading is discussed in IV, 6 .

## 6. Disturbances

Certain precautions must be taken when working at high sensitivities (S 1 to S 5 to measure intensities of 1 to $10 \times$ $1 \sigma^{7}$ e.m.u.). Otherwise, vibrations and temperature changes may cause noise and drift large enough to render the instrument useless for measuring intensities $<1 \sigma^{6}$ e.m.u. Seismic vibrations of 4 cycles/sec cause the magnet system to oscillate about its axis at the same frequency. The instrument is set on an anti-vibration pier which was built at the same time as the building. It consists of a concrete slab ( $1.05 \times 1.05 \times 0.15$ meter) resting on crushed stone and sand to a depth of 1.5 meters. It is detached from the floor of the building. Measurements (by F. Lombardo of the Seismology Division) taken on the floor and on the pier show that the amplitudes are 3 times smaller on the pier. The transmission of
these low frequency oscillations to the electrical circuit can be controlled to a certain extent by the filters but cannot be cancelled. It is then difficult to measure directly the current passing through the negative feedback solenoids and much easier to measure the voltage across a precision resistor. The zero deflections (for $D$ and $I$ ) are measured by means of the DC nullvoltmeter which is normally left on the 100 mv range. The input resistance is high ( $100 \mathrm{M} \Omega$ ) and the response time is less than 1 sec . The remaining small oscillations are not a serious problem. Indeed, since the deflection must be zero, it is relatively easy to rotate the specimen until the oscillations are equally divided on both sides of the scale centre. The intensities are measured on the integrating DVM which is normally set on a 2 -sec integrating time.

The room temperature must be carefully controlled, especially when working at high sensitivity. The magnetometer head is quite sensitive to any temperature change. Such changes will cause expansion of the aluminum plate and vertical tube supporting the suspension; large drifts will then occur. To prevent this, a styrofoam cover (Figure 3) was made and at least 5 cm of insulation protects any part of the head. The shape of the compensating coils system is temperature dependent. As the room temperature changes, the coil system is either distorted or tilted. Although the distortion (or tilt) may be small, the changes in fields at the upper and bottom magnets are different and a drift will occur; a drift that may be large since the astaticism is of little help against this type of disturbance. The amplitude of the drift depends on the source of heat and on the location of this source with respect to the coil system.

The room is heated by 5 electric radiant heaters ( 2000 watts) controlled by 3 thermostats: (1) 2 heaters ( 1 thermostat) at the south end of the building; (2) 1 heater in the middle of the west wall and 1 at the north end of the building (1 thermostat); (3) 1 heater (1 thermostat) in a vestibule. About 20 minutes after switching on any of these groups, an irregular but oscillating drift
starts. Recordings show the zero drifting one way for about 6 sec , then regressing by 70 per cent in 5 seconds before drifting again in the original direction by the same amount; this fairly regular pattern repeats until about 20 minutes after switching off this group of heaters. The amplitude of the drift (in one peak-to-peak oscillation) depends on the source or group that is switched on: (1) $2 \times 1 \sigma^{7} \mathrm{Oe}$; (2) $6 \times$ $10^{8} \mathrm{Oe}$; (3) $4 \times 1 \sigma^{9} \mathrm{Oe}$. These values correspond to the field required at the bottom magnet to reproduce the drift recorded.

When the building is allowed to cool with the heaters off, the oscillating drift disappears and a regular drift of about 2 x $10^{7} \mathrm{Oe} /{ }^{\circ} \mathrm{C}$ takes place. Therefore, it seems reasonable to assume that the oscillating drift is caused by heat convection currents around the compensating coil system thereby producing shape changes. It is intended to install additional bracing in an attempt to reduce the oscillating drift. The drifts would probably be smaller for a smaller $L$ and they would not occur if a magnetic-shielded room was used.

However, by taking certain precautions the instrument can still be used at full sensitivity. Since the amplitude of the drift is dependent on the location of the source, and 3 heaters are sufficient to maintain the room temperature constant, source (1) is never used. When measuring on S 1 to $S 8$, source (2) is switched off and when measuring on $S 1$ to $S 5$, source (3) is also switched off. The maximum decrease of temperature in winter without heat is $4^{\circ} \mathrm{C} /$ hour (in general it is 1 to $2^{\circ} \mathrm{C} /$ hour). The drift is then $8 \times 10^{7}$ $\mathrm{Oe} / \mathrm{hr}$ or $1.3 \times 10^{8} / \mathrm{min}$. Since a set of three readings ( $D_{1}, D_{2}, D_{1}$ ) can be taken in 30 seconds, it is estimated that the error introduced in the mean by drift and noise is probably not much greater than 3 x $1 \sigma^{9}$ Oe. This amounts to $5-6 \mathrm{mv}$ on S 1. The estimate agrees with experimental results such as C84A (Table III) where the individual directions (of a $0.37 \times 10^{6}$ e.m.u. intensity) are all within $3^{\circ}$ of the mean.

The magnetization of the specimen holder should be thoroughly checked. It should not produce fields larger than 1 to
$2 \times 10^{-9}$ Oe at the bottom magnet. The permali holder used can easily be contaminated and it must often be washed with soap or alcohol and magnetically cleaned in alternating fields of 3000 Oe. Another prevention against drift is to insulate the damping disc; otherwise, specimen and holder which are not at room temperature because of previous warm up (by handholding for example) will produce a temperature change at the bottom magnet resulting in a drift. To prevent this, a Perspex cup (Figure 3) has been glued to the damping disc (the rest of the case bottom is of nylon).

## 7. Zeroing

The instrument can be zeroed in two ways: mechanical and electrical. The photo resistor carriage can be displaced by remote control and its position is indicated on a dial (Figure 6; on the left). The alignment of the magnet system with respect to the $0^{\circ}$ azimuth of the specimen holder is indicated by this dial. When the dial reads 000.0 , the two are aligned to within $0.002^{\circ}$ of arc; a reading of 001.0 corresponds to a misalignment of $0.2^{\prime}$ of arc. The dial is normally kept between 950.0 and 050.0 so that the misalignment of the magnet system is $\leqslant 10^{\prime}$ of arc.

The electrical zeroing is accomplished by passing a calibrated current in a 2-turns coil on the feedback solenoid holder. No misalignment of the magnet system occurs when this method of zeroing is used. A meter (Figure 6; bottom left) graduated ( $1^{\circ}-0^{\circ}-1^{\circ}$ ) indicates the angular displacement if no electrical compensation was used.

## 8. Performance

Table III gives the results of routine measurements taken from different rock collections. It is divided into two parts. The first part shows the results of progressive thermal or chemical demagnetization. To check the accuracy of the direction determination, specimens with stable magnetizations are chosen to avoid large direction changes inherent to the specimen. Small direction changes between different demagnetization steps may be owing to real changes of directions or to measurement errors. However, the regularity of the changes

Table III. (a) Measurements taken on the same specimen after each thermal (at $x^{\circ} \mathrm{C}$ ) or chemical (during $x$ hours immersion in $\mathrm{Hcl})$ demagnetization.

| ${ }^{\circ} \mathrm{C}$ | H 134B |  | H 2A |  | H2B |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | D,I | $\begin{gathered} \text { INT. } \\ \times 10^{-6} \text { e.mul } \end{gathered}$ | D,I | $\begin{gathered} \text { INT. } \\ \times 10^{-6} \mathrm{e}_{0} \mathrm{~m}_{0} \mathrm{u}_{0} \end{gathered}$ | D, I | $\begin{gathered} \text { INT. } \\ \times 10^{-6} \mathrm{emu} . \end{gathered}$ |
| 20 | 168,-34 | 4.5 | 184, +05 | 9.6 | 191, +08 | 9.3 |
| 100 | 168,-35 | 4.5 | 185, +01 | 9.0 | 186, +02 | 9.6 |
| 300 | 168,-35 | 3.8 | 185, +00 | 8.7 | 187,+01 | 9.0 |
| 400 | 169,-34 | 3.4 | 185, +00 | 6.3 | 187, +01 | 7.1 |
| 500 | 169,-32 | 2.7 | 188, +00 | 4.9 | 190,-01 | 5.4 |
| 550 | 169,-33 | 2.5 | 189,-05 | 2.2 | 196, +01 | 3.9 |
| 600 | 168,-33 | 1.9 | I.M. |  | 198,-01 | 2.4 |
| 650 | 168,-33 | 1.2 |  |  | L.M. |  |

LM. = Large instantaneous magnetizations, acquired when the specimen is subjected to the field $(0.20 \mathrm{e})$ of the magnetometer, render the readings meaningless,

| Hours | C 23 B |  | C 34 B |  | C 54 B |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | D,I | $\begin{gathered} \text { INT. } \\ \times 10^{-6} \mathrm{e} . \mathrm{m} . \mathrm{u} \end{gathered}$ | D,I | $\begin{gathered} \text { INT. } \\ \times 10^{-6} \text { e.m. u. } \end{gathered}$ | D,I | $\begin{gathered} \text { INT. } \\ \times 10^{-6} \mathrm{em} . \mathrm{m} \end{gathered}$ |
| 00 | 037,+67 | 13.0 | 075, +57 | 4.9 | 045, +43 | 19.1 |
| 29 | 037, +66 | 9.5 | 080,+55 | 1.8 | 045, +40 | 15.1 |
| 100 | 040, +70 | 6.3 | 073, +60 | 1.2 | 046, +45 | 10.9 |
| 241 | 046,+69 | 2.7 | 076,+63 | 0.8 | 050,+48 | 4.8 |
| 423 | 042,+73 | 1.5 | 070, +72 | 0.9 | 045, +54 | 3.3 |
| 790 | 054, +79 | 1.3 | 073,+73 | 0.9 | 048, +55 | 3.2 |

(b) Repeat measurements taken on inhomogeneously magnetized specimens. The measurements are often taken at different distances as indicated by Pos.

| Specimen | D,I | $\stackrel{\text { INT. }}{\times 10^{-6} \mathrm{e}, \mathrm{~m} . \mathrm{u}}$ | POS. | Specimen | D,I | $\begin{aligned} & \text { INT. } \\ & \times 10^{-6} e_{\text {_m.u. }} . \end{aligned}$ | POS. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| C84A | 143,+00 | 0.35 | 4 | H152A | 147, +00 | 1.6 | 4 |
|  | 145, +05 | 0.37 | 4 |  | 145, +00 | 1.5 | 3 |
|  | 147, +03 | 0.38 | 4 | H166 | 261,+36 | 5.2 | 2 |
|  | 145, +04 | 0.36 | 4 |  | 260, +36 | 5.0 | 3 |
|  | 142, +02 | 0.37 | 4 | 690371 | 162, +34 | 11.7 | 2 |
| H8A | 115,+33 | 5.8 | 3 |  | 160, +35 | 12.8 | 3 |
|  | 118, +33 | 5.9 | 2 |  | 162, +34 | 13.3 | 3 |
| H9A | 318, +13 | 4.7 | 4 | 690372 | 184, +23 | 20.2 | 2 |
|  | $320,+13$ | 4.7 | 3 |  | 185, +23 | 20.2 | 3 |
| H108* | 074, +68 | 1.7 | 4 | 690373 | 181, +16 | 54.6 | 2 |
|  | 074, +69 | 1.9 | 4 |  | 181,+16 | 54.4 | 3 |
| H151 | 128,-26 | 2.2 | 4 | 690082 | 050,+37 | 46.3 | 3 |
|  | 128,-26 | 2.2 | 4 |  | 049,+37 | 44.9 | 2 |
|  |  |  |  |  | 048, +35 | 46.8 | 1 |

*Non standard specimens - height $=1.2 \mathrm{~cm}$
between $100^{\circ} \mathrm{C}$ and $600^{\circ} \mathrm{C}$ for H2B for example, suggests that most of the changes can be attributed to direction changes.

The second part consists of repeat measurements taken on the same specimen because the magnetization was very inhomogeneous and the two directions ( $D_{1}$ and $D_{2}$ ) of a set of readings were far
from $180^{\circ}$ apart. In such cases, intensity permitting, the repeat measurements are taken at different distances and the position is indicated. Only specimens of low intensities are listed. Repeat measurements on specimens of intensities $>10^{4}$ e.m.u. normally agree to $1^{\circ}$; readings are taken to the closest degree. Results indicate that the direction of intensity $=1 \mathrm{x}$
$1 \sigma^{7}$ e.m.u. can be determined to within $9^{\circ}$ on S 1 as estimated from the ratio noise/deflection $=6 \mathrm{mv} / 38 \mathrm{mv}$, and the direction of intensity of $3 \times 1 \sigma^{7}$ e.m.u. (such as C 84 A ) to within $3^{\circ}$. The direction of $1 \times 1 \sigma^{6}$ e.m.u. intensities can be determined on S 6 to within $2^{\circ}$. These values can, of course, be improved upon by taking repeat measurements.

For intensities $<10^{6}$ e.m.u., about 8 specimens can be measured in an hour; this includes repeat measurements that may be required because of intermittent increases in the disturbance level. About 12 specimens of intensities in the $10^{-6}$ e.m.u. range can be measured per hour. When the intensities are $>1 \sigma^{4}$ e.m.u. the measurements can be done on S 10 and S 11 and because of the quick response, 15 to 20 specimens are normally measured in an hour. It is found that about $2 / 3$ of the time is spent in handling the specimens, changing spacers and working out the averages of $D, I$ and Int. so that for weakly magnetized specimens repeat measurements can be taken without unduly increasing the total time.

The system could be used to measure three orthogonal components of magnetization. However, for many reasons, it is preferable to measure $D, I$ and Int. as described. Time is saved by eliminating the necessity of computing the results as required in the three-component method. Accuracy obtained with the direct method is greater; in the three-component method, each determination is performed on a fraction of the total intensity while in the direct method $I$ and Int. are determined from the total intensity. The determination of $D$ is obtained from the total horizontal intensity and its accuracy can be further mproved by reducing the distance used for $I$ and Int, or by using a higher sensitivity. Indeed, since only Int. depends on $K$, both Pos. and $S$ can be changed at any time for the determination of $D$ and $I$. A change of distance (or Pos.) is usually avoided in the threecomponent method because of complications in computation; different $z$ and shape correcting factors must then be used for $p_{x}$ and $p_{y}$ and $p_{z}$.

The direct method also provides an instant estimate of the inhomogeneity of magnetization. The direction readings ( $D_{1}, D_{2}$ ) of an inhomogeneously magnetized specimen will not be $180^{\circ}$ apart.

However, measurements taken at different distances show that the mean reading (upright and inverted) is representative of the mean direction of magnetization.

It should be noted that the mean direction of magnetization is not necessarily parallel to the direction of the magnetizing field. For example, if a change of direction or polarity of the field occurs while a sedimentary formation is gradually deposited and consolidated, the direction of magnetization of the upper part of a specimen ( 2.2 cm thickness formed during that change) is different from that of the lower part. Such an occurrence is readily determined by the inequality of $D_{1}$ and $D_{2}$ since $D_{1}$ (upright position) is then biased towards the direction of the latter field and $\mathrm{D}_{2}$ (inverted position) towards the direction of the former. In paleomagnetic work, it is normally assumed that the field at the time of magnetization was a dipole field and that the direction of magnetization obtained after adequate cleaning is representative of the direction of the earth's field at that time. However, if a specimen is highly inhomogeneously magnetized, the mean direction and intensity of magnetization measured may be the resultant vector of two magnetizations acquired in two different fields and therefore that vector is non-representative of a particular field. By comparing $D_{1}$ and $D_{2}$, and $I_{1}$ and $I_{2}$, the direct read method of measuring provides means of assessing if during magnetization the direction of the field remained in the same direction with respect to the orientation and attitude of the specimen. The method has been used successfully to detect the presence of a composite magnetization of the Seal Lake and Croteau Groups sediments (Roy and Fahrig; in preparation).

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the ottawa PZT observations-1956-70, their comparison with BIH values by graphical, spectral and fourier analyses

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Information Canada Ottawa, 1972

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# the ottawa PZT observations-1956-70, their comparison with BIH values by graphical, spectral and fourier analyses 

E. G. WOOLSEY


#### Abstract

Results of measurements of latitude and time made with the Ottawa Photographic Zenith Tube (PZT) from 1956 to 1970 are given. The observations, on magnetic tape, are available to recognized scientific organizations at nominal cost.

The observations are shown to produce values of the variation in latitude and longitude with a probable error of ". 01 . They were compared to the published results of the Bureau International de l'Heure. The residuals so formed were subjected to a spectral analysis and it is demonstrated that the PZT was not capable of detecting secular motions of 10 cm or less. No motion was found for Ottawa.

The star catalogue is published to contribute to the knowledge of stellar positions.


Résumé. La présente publication donne les résultats de mesures de la latitude et du temps effectuées à l'aide de la lunette photographique zénithale d'Ottawa (PZT) de 1956 à 1970. Les observations, enregistrées sur bande magnétique, sont disponibles et seront communiquées aux organismes scientifiques reconnus, pour un coût nominal.

Les observations sont données de manière à indiquer les valeurs de la variation de latitude et de longitude avec une erreur possible de ".01. Elles ont été comparées aux résultats publiés par le Bureau International de l'Heure. Les données résiduelles ainsi obtenues ont été soumises à une analyse spectrale et il a été démontré que la lunette (PZT) ne peut détecter des mouvements séculaires de 10 cm ou moins. Aucun mouvement $\mathrm{n}^{\prime}$ a été décelé pour Ottawa,

Le catalogue des étoiles est publié comme contribution à la connaissance de la position des étoiles.

## Introduction

The PZT (Photographic Zenith Tube) is basically a fixed telescope that observes stars within 15 minutes of arc of the zenith. The light from a star passes through the lens, is reflected by a dish of mercury which establishes the vertical and is brought to focus on a photographic plate placed at just a sufficient distance below the lens to allow room for the plate holder. Each star is photographed four times during transit; the plate is driven to produce point images and is rotated $180^{\circ}$ between each exposure. Each exposure is accurately timed.

The photographic plates are measured in two coordinates. Since we know the positions of the stars, in one coordinate we are able to record the latitude in relation to our star catalogue and, in the other coordinate, record the difference between observed and calculated times of transit of the star over our meridian. Clock comparisons are made daily (in our case with WWV and CHU).

These measures are used to determine the position of the pole and the rate of rotation of the earth. In order to do this we must adopt a coordinate system $(x, y)$ for the position of the pole. By international agreement $x$ is measured as the displacement of the pole toward Greenwich, and $y$ the displacement of the pole toward $90^{\circ}$ west of Greenwich. The origin adopted is the Conventional International Origin (CIO). Both $x$ and $y$ are measured in seconds of arc.

Our measures become:

$$
\begin{aligned}
& \phi=\phi_{0}+x \cos \lambda_{0}+y \sin \lambda_{0} \\
& \Delta T=\left(-x \sin \lambda_{0}+y \cos \lambda_{0}\right) \tan \phi+t
\end{aligned}
$$

where $\phi$ is our observed latitude and $\Delta T$ our observed difference in time, in seconds of mean solar time; $\phi_{0}$ and $\lambda_{0}$ are our adopted latitude and west longitude. The values to be determined are $x$ and $y$ for the position of the pole and $t$ the time correction measured in seconds of mean
time in respect to our reference clock. Thus at any instant we have two equations and three unknowns. It is only by introducing results from other stations that a solution can be found.

Such a solution is regularly carried out by the BIH (Bureau International de l'Heure) using observations from many stations around the world. When the observations from any individual station are compared to the values published by the BIH (Guinot, 1967-70), the major part of the observed variations in latitude and time correspond to the variations in $x, y$ and $t$ of the BIH and therefore must be features of the earth as a whole. There are, however, small residuals at each station that appear to be periodic and a phenomenon of that station. The study of both these types of variation reveals properties of the earth.

## History

This article deals with results only. No effort will be made to describe the instrument in technical detail, which has already been done by Thomson (1955).

The Ottawa PZT was brought into operation in 1952. During the early years it was mounted in the transit annex of the Dominion Observatory, which was a stone, brick and concrete addition on the west side of the main building. In 1960 it was moved about 100 metres southeast to its own light, insulated building. At the end of January 1968 the 10 -inch ( $25-\mathrm{cm}$ ) PZT was replaced with a new 8 -inch $(20-\mathrm{cm})$ instrument. The former was moved to Calgary to be on the same latitude as the Herstmonceux PZT of the Royal Greenwich Observatory. Finally, in January 1970 the Ottawa PZT was moved to a new site 16 kilometres due west. This is the terminal point of this report.

The Ottawa PZT plates from the years 1956 to 1960 inclusive were previously remeasured. The observations in latitude were published in Time \& Latitude Bulletin, A45, of the Dominion Observatory, (Tanner, 1967), from which the following notes have been extracted.
"The principal changes within the period which still may effect the results are:
(1) From 1956 to 1959 inclusive, observations consisted of two, two-hour groups from a 160 -star catalogue, centred near 2200 hours local time; from 1960 onwards observations were made from dusk to dawn.
(2) The instrument was moved in the period May 7 to May 25, 1960, to the new observing hut $1^{\prime \prime} .252$ south and $0 \$ 275$ east of its earlier location. The 0.275 was allowed for in the calculation of time so there is no apparent discontinuity in this coordinate.
(3) From 1962 onwards the catalogue consists of 80 stars in eight, threehour groups.
"It has not been considered profitable to rework the 1952 -1955 results for three reasons; the larger scatter, the smaller number of stars in common with the current catalogue, and the lack of an atomic standard of time com parison."

## Star catalogue

The star catalogues are essentially on the FK4 basis with an epoch of observation about 1962. The positions were amended in 1966 by R.W. Tanner of this Branch, and incorporate the PZT observations to that date. They are relatively free from error and any adjustments made in the future will have litte effect on the results being considered.

In order to have a permanent record, and to assist astronomers forming star catalogues, the catalogues employed for the two periods are published in Appendix A. The 160 -star catalogue was used from 1956 to 1961 and the 80 -star catalogue from 1962 to 1970.

The star catalogues require little explanation since they follow current
practice. The star number is made up of two parts, the hundreds define the group, the tens and units the number of the star within the group. The photographic magnitude and spectral class have been copied from the other publications, principally the Henry Draper Catalogue. The right ascension and declination are presented for the year 1950 and the proper motions are centennial. The BD number is given to provide identification of the star and cross-reference to other star catalogues.

## Preparation of data

Since observations were available on punched cards, it was only necessary to bring them to a uniform basis and decide how to collect and present them in the most usable form for future investigations. The latitude is given directly and presents no problem.

In the time coordinate the readings are the difference between observed and calculated time of transit of a star recorded as differences with the time broadcast by WWV. In the past, time was related to the mean rotation of the earth; with the advent of atomic clocks time was maintained by adopting a constant annual rate and applying step corrections to keep radio transmitted time within 0.1 sec. of mean solar time. The annual rate was changed several times in the period considered. An obvious uniform time is atomic time and the most easily available atomic time was Al (the U.S. Naval Observatory atomic standard) for which they had already published comparisons with WWV. Our observations are published as $\Delta T=$ UTO $-A 1$, the difference between our observed time of transit and the time of the atomic standard A1.

The other adjustment required to bring the observations to a uniform basis was to correct the earlier years for the change in aberration adopted in 1968.

The observations were collected by star groups and comparisons with the original summaries were made to insure that the values were free from errors. Our raw results are available on magnetic tape to recognized scientific organizations at a nominal cost. The tape gives:

Ottawa date of observation - year, month, day.
Julian day to two decimals.
Star group number.
Observed time minus atomic time 'A1'.
Observed latitude - seconds of latitude, omitting the $45^{\circ} 23^{\prime}$.
Number of stars observed.
Our night or reference number.

## Preparation of summary values

Rather than publish our raw data, which would be of use to few investigators, summary values have been derived at intervals of one-twentieth of a year and ten-day intervals. The use of summary values reduces the night-to-night dispersion and provides values that can be compared directly with those published by the BIH.

The information on the raw data tape is similar to that sent to the BIH; the observations are arranged as average of star groups. These star groups originated in the star catalogue and contained about ten stars balanced north and south of the zenith. Unfortunately, it is the exception rather than the rule that complete groups are observed. Also, each night's work is on one plate, and the plate constants are derived from the mean of all stars observed. It therefore seemed preferable to use the average of all stars observed on one night as an observation.

In order to reduce night-to-night dispersion, the nights were grouped to form summary values. The grouping of nights was done in such a manner as to produce values at one-twentieth of a year and at ten-day intervals to facilitate comparisons with the published BIH (1968) values. Two different numerical methods were used, one for the one-twentieth of a year and the second for the ten-day intervals. Both schemes appear to represent our observations equally well.

The summary values are listed in Appendix B, giving time of observation in Besselian years from 1900 for the .05 year values and in Julian days for the ten-day smoothed values. The latitude, $(\phi)$, is in seconds only; the $45^{\circ} 23^{\prime}$ has
been omitted. The time coordinate is observed minus atomic time A1 and is called 'UTO-Al'.

## Values at one-twentieth of a year

The method of combining observations as suggested by Jeffreys (1960, 1961) was used to calculate the values for each twentieth of a year. The night values were weighted one for all nights with ten or more observations, one-half for all nights with five to nine stars, and zero for all nights with less than five stars observed. The various nights were divided into ten groups per year to yield values near $.05, .10$, etc., parts of a Besselian year. Care was taken to ensure that each group had a weight of at least ten, thus each group included a minimum of 10 nights on which observations were successfully carried out. To form values for the exact periods, the three term Lagrange interpolation formula for unequal intervals was used.

A second solution was made by grouping half the nights from each set to form a new series of ten groups per year. The average of the solutions has been adopted as the value at one-twentieth of a year.

This solution lent itself to the calculation of standard deviations. The standard deviations for each star were obtained on each night (as part of the routine calculations) from differences between the observed values and the mean value for the night. The standard deviations for each night and each summary value were obtained using the least-square solution of Jeffreys' formula. The averages of these errors are the values quoted in Table I.

In order to ensure that these standard deviations were indeed correct, a standard deviation for each night was determined from the differences between the observed value and a value for the night determined by straight line interpolation between the two adjacent summary values. This gave standard deviations in latitude and time respectively of ". 090 and 050165 for 1956 to 1959 and ".050 and $\$ 0045$ for 1962 to 1967 . These standard deviations are not significantly different from those of the first solution.

Table I. Standard deviations

| Epoch | Each <br> Lat. | star <br> Time | Each Lat. | night <br> Time | Each summary values |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | Lat. | Time |
| 1956-59 | ".15 | \$021 | ".088 | ${ }^{\text {s }} 0162$ | ".027 | S0062 |
| 1962-67 | ".11 | \$013 | ".051 | S.0045 | ".015 | S.0013 |

The standard deviation for a summary value was checked by comparing the two solutions. The root mean sum of the differences was the same as before.

There is a considerable improvement of the results with the change of location in 1960. In order to indicate the reliability of the results the standard deviations using a representative period for each site are as shown in Table I.

These are considered internal standard deviations since they are formed by comparing results among themselves.

The method of weighting and combining observations is somewhat arbitrary but the considerations leading to the method adopted may be of interest. From our experience, it should never be assumed (without investigation) that precision increases with the square root of the number of observations; there appears to be a limiting accuracy which cannot be improved significantly merely by increasing the number of observations.

Markowitz (1960) has pointed out that "On account of systematic effects no great increase in precision is gained by observing a large number of stars in any one night ... the weight of an observation with 16 stars is about 1.5 times as great as one with 6 stars."

We concur with his reasoning but have solved the problem by graphic means. We graphed the root mean square of residuals formed by subtracting our night values from the curve of best fit through the night values against the number of observations as ordinate. We found that after a certain number of observations the curve becomes a horizontal line.

Examining our night corrections in this manner we found that when ten stars were observed, we were approaching the values ". 05 and ${ }^{5} .005$, which was about 90 per cent of the limit. There was no justification for a more elaborate weight-
ing scheme than a simple one, two ratio (1. and .5).

The summary values became asymptotic at about ".015 and 5.0015 , but the value was not approached until 18 or 20 nights were combined. The minimum number of ten nights was set rather by the number of nights available.

## Ten-day smoothed values

The ten-day smoothed values were calculated by a less sophisticated method. The earlier years were adjusted for the move in 1960 by subtracting 1 ". 252 from the latitude, Running means for ten successive plates were formed. Values for the ten-day Julian dates were interpolated linearly from two adjacent values. The final listing was formed from these tenday values by parabolic smoothing in groups of five.

Both methods produce comparable values and are in good agreement except at the beginning of 1968 where there is a period of thirty days with no observations, then four days observing followed by a gap of nine days. Neither method can be expected to bridge gaps so large.

## Description of observations

Very little can be said about the observations until they are compared to the BIH. However, they have been graphed to give a visual representation to the reader. Figure 1 shows our readings in latitude and time.

As already stated the main part of each variation is common to all stations and these graphs resemble those in other publications.

In the lower or latitude curve the beat period of about six years between the Chandler and annual terms is obvious and during this period the amplitude of the Chandler term appears to be decreasing.

It is not practical to graph the time coordinate in the same manner. The large rate difference between observed and


Figure 1.


Figure 2.


Figure 3.


Figure 4.


Figure 5.


Figure 6.
atomic time would require the scale to be greatly reduced and thus obscure variations. By subtracting an average rate for the period, of $\$ 00168$ per day, the changes in rate are more easily seen and the graph draws attention to the fact that the rate of rotation of the earth is far from constant. This graph is similar to that shown by Markowitz (1969). Even with this method of showing the time, scale has been reduced by a factor of 10 , that is, each division of the time graph is approximately equal to ten in latitude. The graph draws attention to the significant change in the rate of rotation of the earth (more than 100 parts in $10^{10}$ i.e. more than a millisecond per day) that occurred in the short period 1964-1966.

A spectral analysis may show better what is actually happening. Figure 2 shows the amplitude in latitude plotted against frequency.

Table II.

| Frequency <br> cycles per year | Period <br> in days | Power <br> $(.01)^{2}$ |
| :---: | :---: | :---: |
| .73 | 511 | 5 |
| .75 | 465 | 5 |
| .87 | 426 | 49 |
| 1.00 | 365 | 11 |
| 2.00 | 183 | .3 |

The principal features are:

1. A few long terms that may be related to the short period examined (i.e. frequences .73 and .75 ).
2. A large Chandler term. The values given in Table II confirm other findings, that the power of the Chandler term is about four times the annual term.
3. An annual term, and a semi-annual term barely distinguishable from the noise.
4. Amplitude of the noise level is taken as a little over ".003 or 10 cm .
5. The value of $Q$, the figure of merit (cf. electronic circuits), was calculated for the Chandler term as greater than 5. A much longer period would have to be studied to improve this value.

The spectral analysis of the time coordinate is given in Figure 3.

The principal features are:

1. Long-term variations had amplitudes too large to be included in the graph.
2. They are due to the major changes in the rate of rotation of the earth (the cause of which is still unknown). This can be more effectively studied by employing the BIH values, and has been adequately done by Markowitz (1969).
3. The period is too short to show any two- or four-year variations as suggested by some writers.
4. The annual and semi-annual terms of amplitude s.0070 and ${ }^{3} .0065$ dominate the rest of the spectrum.
5. The noise level is about four times as large as that found in latitude.
6. The scale used in the time graph is $1 / 4$ that used to show variations in latitude.

## Comparison with BIH

As stated in the introduction the BIH has solved equations similar to

$$
\begin{aligned}
& \Delta \phi=\phi-\phi_{0}=x \cos \lambda_{0}+y \sin \lambda_{0} \\
& \Delta T=\left(-x \sin \lambda_{0}+y \cos \lambda_{0}\right) \tan \phi+t
\end{aligned}
$$

by assigning latitude, longitudes, and weights to the various stations around the world. In their solution differences in time are expressed with respect to another uniform time, UTC, rather than atomic time. UTC is the coordinated universal time approximating the rotation of the earth and is essentially the same as WWV. It is maintained at a constant rate for the short periods required by their calculations but is not uniform over the longer period used in this report. Their method of calculation is described in detail in their annual reports (Guinot, 1967-70) and it suffices to say it provides the best reference to which we may compare our results (The International Latitude Service (ILS) and International Polar Motion Service (IPMS) only publish values of $x$ and $y$.). The BIH report provides values of $x, y$ and UT1 and UT2-UTC, and comparisons of UTC with various atomic times. From their tables we are able to calculate our value for $t$, the correction to atomic A1 at any instant.

Comparison of our observations with the BIH are given in Appendix C under the headings of D-PHI and D-LAMBDA, the values being given in the sense observed minus computed. The latitude differences (D-PHI) were formed by adopting a latitude of $45^{\circ} 23^{\prime} 37^{\prime \prime}$ (as a convenience to give decimals of a second only), so that the D-PHI values are observed corrections to this adopted latitude. The interpretation of the D. LAMBDA term is not as obvious. Our observed time values were based on an adopted west longitude of $5^{\mathrm{h}} 2^{\mathrm{m}} 51^{\mathrm{s}} 94$, which entered directly into the calculation. If we had chosen a slightly smaller longitude, our recorded observed time would be increased by exactly the same amount. Thus the differences (DLAMBDA) are observed corrections to our adopted longitude. The values used in the comparisons are the values for each twentieth of a year compared to the BIH unsmoothed values on the 1968 system which are only available back to 1962.

As expressed in the introduction "When the observations from any individual station are compared to the BIH . . . there are small residuals at each station that appear to be periodic and a phenomenon of that station." These residuals will now be examined by graph, spectral analysis and analytical solution.

Figure 4 provides a picture of these observations. The upper two graphs show the similarity of our latitude observations to those calculated for Ottawa using the BIH published values of $x$ and $y$. The upper graph is $\Delta \phi=\left(\phi-\phi_{0}\right)$ Ottawa and the lower one $\Delta \phi=x \cos \lambda_{0}+y \sin \lambda_{0}$. The time coordinate has been omitted because the scale required would mask all differences. The two lower graphs show D-PHI and D-LAMBDA, the variations in latitude and longitude of Ottawa compared to the BIH. At a latitude near $45^{\circ}$, ". 01 is nearly equal to ${ }^{\text {s }} .001$ so that the variations are essentially on the same scale. There is no significance to the spacing of the graphs which have been designed to show variations with time. We will now proceed to examine these latter two curves.

The spectral analysis of D.PHI and

D-LAMBDA are given in Figure 5 and Figure 6. They have been graphed to essentially the same scale so that variations in latitude and longitude may be compared in amplitude and frequency. In order to have enough observations the ten-day smoothed values were used.

The noticeable features are:

1. In latitude there is an annual term of amplitude ". 012 and a semi-annual term of amplitude ". 007 and the noise level has remained unchanged at ".003 or 10 cm .
2. In longitude there is an annual term of amplitude ${ }^{5} 0016$ and no semi-annual term. The amplitude of the noise level is about $: 0004$, i.e. near 10 cm .
3. The large reduction in the noise when our results are compared to the BIH shows that this was a feature of the earth as a whole. It was very encouraging to find our error in determining longitude is again the same order as that for latitude.

The small annual and semi-annual terms as shown by the spectral analysis suggest that we submit our results to a Fourier analysis. This is precisely the practice followed by the BIH. Although the semi-annual term is not present in the D-LAMBDA, there appears no harm in
following the BIH and treating both coordinates in the same manner.

The analytical solutions for each year are given in Table III. There is a year-toyear variation but on the average in latitude the amplitude of the annual term is double the semi-annual, and in longitude the annual term is predominant.

The constant terms from the analytical solutions provide corrections to our adopted latitude and longitude. Therefore, we can say the observed mean values (1962-70) for the latitude and longitude of Ottawa in the BIH (1968) system are:
Latitude
$45^{\circ} 23^{\prime}$ $37^{\prime \prime} .132$ Longitude $\quad 5^{\mathrm{h}} 02^{\mathrm{m}} \quad 51^{8} .9525$

The BIH adopted values: $45^{\circ} 23^{\prime}$ 37.121 and $5^{\text {h }} 2^{\mathrm{m}} 51.950$ were based on our observations made in 1967. Our calculated values for the same period are: $45^{\circ} 23^{\prime} 37.122$ and $5^{\mathrm{h}} 2^{\mathrm{m}} 51.9506$. The difference is considered negligible and is probably due to the method of grouping.

An analysis of the variation of the constant terms $a$ and $a^{\prime}$ (Table III) with time should yield the secular motion or continental drift of Ottawa (or an error in the proper motions of our star catalogue). Our solutions give:
Secular variation of
latitude -". $11 \quad \pm .46$ per century
longitude $-5.042 \quad \pm .060$ per century

As would be expected for so short a period, the motion can hardly be called significant.

According to Munk and MacDonald (1960), the local variation described by the variations in D-PHI and D-LAMBDA after the removal of the corrections to the adopted latitude and longitude is "related to wind, pressure, and other meteorological variables." The verification of this is beyond the scope of this report.

The standard deviations obtained by comparing ( $\phi-\phi_{0}$ ) Ottawa $-\Delta \phi$ BIH without adjustment for the annual terms yields values of ".036 and 8.0038 for latitude and longitude respectively. However, when these annual variations are applied, the standard deviations reduce to ". 022 and 5.0019 which are one and half times the calculated internal values of ". 015 and ${ }^{8} .0013$. It is hoped that these differences can be reduced when local effects are studied.

Although the published values for the variation in latitude by the IPMS (Yumi, 1962-68) have not been adjusted for the new aberrational constant, it is interesting to compare our results. In order to avoid our values at the beginning of 1968 , only six years, 1962 to 1967 , were used. The Ottawa values are not adjusted for any annual term.

Table III. Comparison with BIH revised Fourier analysis

| D-PHI |  |  |  |  |  | D-LAMBDA |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\Delta=a+b \sin 2 \pi \theta+c \cos 2 \pi \theta+d \sin 4 \pi \theta+e \cos 4 \pi \theta$ |  |  |  |  |  | $\Delta=a^{\prime} \pm b^{\prime} \sin 2 \pi \theta \pm e^{\prime} \cos 2 \pi \theta \pm d^{\prime} \sin 4 \pi \theta \pm e^{\prime} \cos 4 \pi \theta$ |  |  |  |  |
| $\theta$ is in decimals of a Besselian year |  |  |  |  |  | $\theta$ is in decimals of a Besselian year |  |  |  |  |
|  |  |  | Units "00 |  |  |  |  | Units ${ }^{\text {s }}$ |  |  |
| Year | $a$ | $b$ | $c$ | $d$ | e | $a^{\prime}$ | $b^{\prime}$ | $c^{\prime}$ | $d^{\prime}$ | $e^{\prime}$ |
| 1962 | 148 | 7 | 35 | - 1 | -8 | 137 | 7 | 5 | 4 | 9 |
| 1963 | 117 | - 6 | 41 | 24 | 1 | 159 | 39 | -16 | 28 | 14 |
| 1964 | 133 | 25 | 20 | 15 | -17 | 129 | 36 | -25 | 17 | 0 |
| 1965 | 138 | -9 | 28 | 10 | -11 | 117 | 36 | -23 | 0 | -11 |
| 1966 | 142 | -12 | 20 | 5 | -19 | 118 | 29 | -25 | - 1 | - 1 |
| 1967 | 122 | -34 | 13 | 18 | -21 | 106 | 25 | -34 | - 9 | 5 |
| 1968 | 119 | -7 | 19 | - 6 | -8 | 104 | 4 | -32 | -44 | 7 |
| 1969 | 137 | -30 | 21 | - 1 | -22 | 132 | 40 | -17 | 3 | -10 |
| 8 years | 132 | - 8 | 25 | 8 | -13 | 125 | 27 | -20 | $-3$ | 1 |
| Mean errors $a \pm 5$ |  |  |  |  |  | Mean errors $a^{\prime} \pm 5$ |  |  |  |  |
| $b, c, d, e \pm 7$ |  |  |  |  |  | $b^{\prime}, c^{\prime}, d^{\prime}, e^{\prime} \pm 7$ |  |  |  |  |

The CIO origin was chosen to make the pole of the BIH and IPMS coincide on the average for the years 1964-1966. The Ottawa observations appear to favour the BIH position of the pole. No case is made for the standard deviations since all differences are known to contain systematic terms.

Table IV.

|  | Average | Standard deviation |
| :---: | :---: | :---: |
| $\Delta \phi(B I H)-\Delta \phi(\mathbb{P M S})$ | ",004 | " 028 |
| $\phi-\phi_{0}$ (OTTAWA) - $\Delta \phi($ BIH $)$ | ".001 | ".034 |
| $\phi-\phi_{\phi}($ OTTAWA) - $\Delta \phi$ (IPMS) | ) 0.05 | ".028 |

## Apparent secular change in latitude

The secular change of latitude was investigated by averaging the latitudes at one-twentieth of a year over a period of six years. This should remove most of the annual and Chandler terms. The values for the earlier years were adjusted by
subtracting $1^{\prime \prime} .252$. In Table V the decimals of a second only are listed along with their differences from the mean.

The solution gives the secular drift in latitude as $0.08 \pm 0.13$ per century. This table was formed on the assumption that the Chandler term has a period of exactly 1.2 years, which is not exactly true; the small uncertainty was obtained by assuming each six-year period as independent, which is also not exactly true. The value is about equal and opposite in sign to that obtained by comparing Ottawa with the BIH for the years 1962 to 1970. The only conclusion is that there is no evidence of secular drift.

## Conclusion

The Ottawa PZT has produced results of high order, by determining the variation in latitude and longitude with a probable error of ". 01 . This instrument has now been moved to Calgary and is

Table V.

|  | Period | Average latitude |
| :--- | :---: | :---: |
| 1956 to 1961 inclusive | .357 | Difference from mean |
| 1957 | 1962 | .364 |
| 1958 | 1963 | .361 |
| 1959 | 1964 | .366 |
| 1960 | 1965 | .368 |
| 1961 | 1966 | .369 |
| 1962 | 1967 | .364 |
| 1963 | 1968 | .361 |
| 1964 | 1969 | .369 |

observing the same list of stars as Herstmonceux. We expect the Calgary results to duplicate the accuracy of Ottawa 1962-1967.

The results were examined and no secular motion of Ottawa was determined. The analysis shows that the Ottawa PZT cannot detect variations or motions of 10 cm or less. Although observations can be investigated for weather, tidal effects or corrections to the star catalogue, the noise level inherent in the observations makes it unlikely that any improvement will be made in the final results.

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UTTAWA HZT CATALUGUE 80 STARS IN $\quad$ g groups

| NO | MAG SP |  | RA | 1450 | PM |  | UEC | 1950 | PM | (31) | NO |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 101 | 8.3 KO | 22 | 59 | 17.438 | $+0.26$ | 45 | 14 | 27.72 | +02.1 | 44 | 4307 |
| 102 | 7.7 ko | 23 | 0.3 | 31.4h? | -0.75 | 45 | 14 | 40.47 | -27.5 | 44 | 4347 |
| 103 | $6.3 \mathrm{B9} \mathrm{\%}$ | 23 | 15 | 34.8107 | +0.24 | 45 | 12. | 56.46 | -00.9 | 44 | 4373 |
| 104 | ¢.7 K0 | 23 | 2h | 03.189 | +0.02 | 45 | 23 | 03.86 | -00.4 | 44 | 4424 |
| 105 | 8.1 A2 | 23 | 36 | 53.550 | -0.0.06 | 45 | 26 | 34.76 | -00.9 | 44 | 4464 |
| 106 | 8.4 F0 | 00 | 13 | 00.814 | +0.15 | 45 | 15 | 58.75 | -01.1 | 44 | 50 |
| 107 | 7.515 | 00 | 17 | 53.264 | +0.59 | 45 | 13 | ל4.48 | -00.6 | 44 | 62 |
| 108 | 7.4 F5 | 00 | 50 | 27.340 | +0.96 | 45 | 11 | 00.60 | -01.5 | 44 | 215 |
| 109 | 8.4 K 2 | 01 | 16 | 06.745 | -0.02 | 45 | 2.6 | 35.63 | +01.8 | 44 | 279 |
| 110 | 8.5 K 0 | 01 | 25 | 43.133 | +0.58 | 45 | 22 | 31.21 | +00.3 | 44 | 312 |
| 201 | 8.1 A5 | 01 | 54 | 49.045 | -0.14 | 45 | 2.1 | 22.59 | +00.7 | 44 | 392 |
| 202 | 8.4 A0 | 02 | 14 | 32.511 | -0.07 | 45 | 16 | 56.77 | +00.4 | 44 | 473 |
| 203 | 7.865 | 02 | 21 | 50.216 | -0.23 | 45 | 2.5 | 22.39 | -07.8 | 44 | 483 |
| 204 | 8.3 F8 | 02 | 3 s | 28.557 | +0.46 | 45 | 16 | 54.33 | -03.0 | 44 | 558 |
| 205 | $8 \cdot 6$ F8 | 02 | 41 | 28.822 | -0.18 | 45 | 23 | 21.23 | -04.4 | 44 | 569 |
| 206 | $7.5 \mathrm{H8}$ | 03 | 19 | 04.4008 | -0.06 | 45 | 12 | 28.61 | +01.0 | 44 | 677 |
| 207 | 7.288 | 03 | 22 | 11.257 | -0.01 | 45 | 20 | 25.39 | +00.2 | 44 | 695 |
| 208 | $8.4 \mathrm{K0}$ | 03 | 50 | 24.604 | +0.03 | 45 | 21 | 53.46 | -02.9 | 45 | 836 |
| 209 | $8.3 \mathrm{u5}$ | 04 | 07 | 34.442 | $+0.16$ | 45 | 16 | 24.54 | -04.0 | 45 | 887 |
| 210 | 7.6 A0 | 04 | 17 | 17.945 | +0.22 | 45 | 20 | 46.01 | -02.8 | 45 | 92.1 |
| 301 | 7.0 A0 | 04 | 44 | 15.199 | +0.07 | 45 | 24 | 05.58 | -03.3 | 45 | 987 |
| 302 | 7.589 | 04 | 57 | 34.232 | -0.09 | 45 | 22 | 25.23 | -00.8 | 45 | 1023 |
| 303 | $8 \cdot 5$ A0 | 05 | 21 | 38.176 | +0.04 | 45 | 11 | 04.07 | +00.2 | 45 | 1115 |
| 304 | 8.3195 | 05 | 24 | 03.048 | +0.11 | 45 | 27 | 22.43 | -01.9 | 45 | 1132 |
| 305 | 8.0 F3 | 05 | 45 | 02.924 | -0.02 | 45 | 1.3 | 17.65 | -02.2 | 45 | 1178 |
| 306 | 7.4 A0 | 05 | 57 | 36.672 | -0.02 | 45 | 09 | 35.81 | -01.1 | 45 | 1225 |
| 307 | 7.4 Mz | 06 | 00 | 51.730 | +0.04 | 45 | 35 | 24.79 | -05.5 | 45 | 1235 |
| 308 | 7.8 AO | 06 | 04 | 37.163 | -0.07 | 45 | 33 | 44.46 | -02.0 | 45 | 1248 |
| 309 | 8.7 no | 07 | 07 | 13.727 | -0.12 | 45 | 19 | 48.00 | -00.8 | 45 | 1394 |
| 310 | 7.5 KO | 07 | 11 | 59.681 | -0.08 | 45 | 29 | 52.45 | -02.9 | 45 | 1408 |
| 401 | - . $^{\text {K K }} 0$ | 07 | 40 | 45.666 | 0.00 | 45 | 29 | 20.85 | -02.9 | 45 | 1476 |
| 402 | 8.3 kO | 08 | OH | 24.269 | +0.31 | 45 | 21 | 32.48 | -00.4 | 45 | 1550 |
| 403 | 7.8 F0 | $0 \cdot 3$ | 30 | 49.208 | -0.28 | 45 | 22 | 07.77 | -02.3 | 45 | 1601 |
| 404 | 8.215 | OR | 40 | 29.393 | -0.23 | 45 | 38 | 07.02 | -05.2 | 45 | 1624 |
| 405 | 7.1 KO | 08 | 4* | 48.223 | -0.11 | 45 | 30 | 06.29 | -03.4 | 45 | 1649 |
| 406 | 7.4 kO | 04 | 1 H | 06.177 | -0.07 | 45 | 35 | 00.26 | -03.0 | 45 | 1708 |
| 401 | 7.7 KO | 09 | 43 | 31.098 | $+0.48$ | 45 | 20 | 51.76 | -13.0 | 45 | 1762 |
| 408 | 8.1.12. | 09 | 47 | 14.9885 | $-0.78$ | 45 |  | 08.45 | -09.1 | 45 | 1769 |
| 409 | $7.2 \mathrm{K0}$ | 09 | 54 | 48.110 | $+0.05$ | 45 | 39 | 12.71 | -03.4 | 46 | 1566 |
| 410 | 7-\% K0 | 10 | ל | 36.216 | -0.19 | 45 |  | 05.74 | -02.3 | 45 | 1832 |

UTPAMA PLT CATALOGUE BO STARS IN 8 gROUPS

| NO） | $\mathrm{A} A \mathrm{Al}$ | SP |  | RA | 450 | HN |  | DE | 1950 | PM | HO | NO |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 501 | 4.2 | Ko | 10 |  | 35．791 | －0．71 | 45 | 33 | 11.54 | －03．6 | 46 | 1671 |
| $50 ?$ | 7.8 | KO | 10 |  | 08.877 | －0．48 | 45 | 27 | 58.78 | －03．7 | 45 | 1879 |
| 503 | 8.4 | 60 | 11 |  | 20．111 | －0．48 | 45 | 20 | 05．54 | －06．1 | 45 | 1903 |
| 564 | 8.2 | 42 | 11 |  | i） 5.622 | －0． 0.56 | 45 | 36 | 23.76 | －01．5 | 46 | 1717 |
| 505 | 8.1 | MR | 11 |  | 06.823 | －0．07 | 45 | 27 | 38.85 | －02．3 | 45 | 1924 |
| 506 | $7 \cdot 5$ | F2 | 11 | 37 | 04.720 | ＋0．15 | 45 | 2.6 | 01．66 | －01．4 | 45 | 1952 |
| 507 | 7．b | A3 | 12 | 24 | 13.744 | －0．26 | 45 | 30 | 05．68 | －01．4 | 46 | 1791 |
| 508 | 7.5 | F2 | 12 | 36 | 10.645 | －1．35 | 45 | 29 | 31.93 | －03．8 | 46 | 1805 |
| 509 | 6.7 | K0 | 13 |  | 37.467 | －0．18 | 45 | 32 | 07.59 | ＋02．5 | 46 | 1847 |
| 510 | 9.0 | FS | 13 |  | 05.553 | －1．38 | 45 | 21 | 45.35 | －03．4 | 45 | 2104 |
| 601 | 8． 4 | F 5 | 13 | 3.3 | 51.762 | －0．44 | 45 | 16 | 12.86 | －01．8 | 45 | 2120 |
| $60 \%$ ？ | 8.8 | 15 | 13 | 40 | 33.442 | －0．35 | 45 | 25 | 06.48 | ＋01．0 | 45 | 2131 |
| 603 | 8.4 | 65 | 14 | 39 | 16.406 | －1．10 | 45 | 37 | 44.50 | －19．2 | 46 | 1981 |
| 604 | 7.1 | ドロ | 14 | 4？ | 38．338 | $+0.52$ | 45 | 23 | 47.74 | －02．0 | 45 | 2214 |
| 605 | 8.0 | F5 | 14 | 52 | 31．540 | －0．62 | 45 | 30 | 00.78 | ＋05．4 | 45 | 2233 |
| 606 | 7.4 | K2 | 15 | 22 | 23.836 | －0．16 | 45 | 26 | 48．66 | －00．3 | 45 | 2284 |
| 607 | 8.2 | FO | 15 | 37 | 32.744 | $+0.27$ | 45 | 16 | 42.39 | ＋01．4 | 45 | 2317 |
| 608 | 9.11 | 65 | 15 | $4 \%$ | 27.953 | －0．41 | 45 | 28 | 18.99 | ＋03．1 | 45 | 2325 |
| 604 | 8.2 | K0 | 16 | 06 | 23.425 | －0．03 | 45 | 30 | 41．78 | ＋00．9 | 45 | 2374 |
| 610 | B． 4 | （i5 | 16 | 23 | 47.715 | －0．64 | 45 | 23 | 27.16 | ＋01．7 | 45 | 2404 |
| 701 | 7.9 | K2 | 17 | 10 | 12.145 | －0．01 | 45 | 23 | 01.21 | －01．2 | 45 | 2504 |
| 702 | 7.3 | B3 | 17 | $1 \%$ | 00.269 | －0．12 | 45 | 25 | 45.49 | －01．1 | 45 | 2509 |
| 70.3 | 6.9 | F0 | 17 | 1 H | 23.795 | －0．36 | 45 | 21 | 24.36 | ＋08．6 | 45 | 2521 |
| 704 | 7.9 | G0 | 17 | $3 n$ | 37．7．33 | $+0.02$ | 45 | 35 | 02.75 | $+04.7$ | 45 | 2573 |
| 705 | 8.6 | G5 | 17 | b3 | 14.164 | $+0.41$ | 45 | 33 | 39．90 | ＋02．2 | 45 | 2620 |
| 706 | $8 \cdot 2$ | A0 | 17 | 53 | 17．771 | －0．07 | 45 | 13 | 27.28 | ＋00．4 | 45 | 2621 |
| 707 | 6.2 | B9 | 17 | 57 | 26.447 | －0．07 | 45 | 28 | 40.95 | $+02.5$ | 45 | 2635 |
| 708 | 7.7 | 89 | 17 | 54 | 41.018 | $-0.11$ | 45 | $2]$ | 00.40 | ＋01．4 | 45 | 2643 |
| 709 | 6.4 | 60 | 18 | 14 | 00.194 | －0．81 | 45 | 11 | 34.49 | －11．2 | 45 | 2684 |
| 710 | $7 \cdot 3$ | FO | 18 | 47 | O8．243 | $+0.26$ | 45 | 12 | 10.34 | 08.5 | 45 | 2777 |
| 801 | 8.4 | KO | 19 | 52 | 12．069 | －0．09 | 45 | 20 | 19.21 | ＋00．1 | 45 | 3001 |
| 802 | 7.7 | A2 | 20 | 00 | 11.300 | $+0.28$ | 45 | 20 | 10.19 | ＋02．3 | 45 | 3038 |
| 80.3 | $8 \cdot 1$ | K2 | 20 | 14 | 53.124 | ＋0．03 | 45 | 11 | 00.79 | ＋01．6 | 44 | 3414 |
| 804 | 7.2 | F5 | 20 | 13 | 11．258 | ＋0．1H | 45 | 12 | 19.84 | －02．0 | 44 | 3429 |
| 805 | 6.3 | 13 | 20 | 37 | 41.827 | －0．03 | 45 | 29 | $21 \cdot 48$ | $+00.2$ | 45 | 3233 |
| 806 | 7.7 | K5 | 20 | 45 | 37.171 | －0．02 | 45 | 23 | 43．18 | －01．8 | 45 | 3275 |
| 807 | 7.7 | G0 | 21 | $0 う$ | 05.640 | －0．08 | 45 | 2 H | 25.57 | －01．0 | 45 | 3410 |
| 808 | 6.7 | A0 | 21 | 04 | 27.750 | －0．08 | 45 | 28 | 07.49 | －00．6 | 45 | 3438 |
| 809 | 6.8 | B5 | 21 | 2 3 | 08.531 | －0．02 | 45 | 16 | 26.73 | －00．5 | 44 | 3840 |
| 810 | $7 \cdot 0$ | MC | 21 | 34 | 08.259 | ＋0．59 | 45 | 09 | 00.09 | $+00.9$ | 44 | 3877 |

UTTAWA PLY CATALUGUF 1GO STARS IN 1? GHOUPS

| NO | MAG | SP |  | RA | 1950 | PN |  | UEC | 1950 | PM | B | NO |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 101 | 8.0 | FO | 00 | 13 | 00.819 | $+0.15$ | 45 | 15 | 58.75 | -01.1 | 44 | 50 |
| 102 | 7.0 | F5 | 10 | 17 | 53.264 | +0.59 | 45 | 13 | 54.48 | -00.6 | 44 | 62 |
| 103 | 8.5 | MA | 00 | 34 | 53.232 | +0.12 | 45 | 14 | 45.53 | +01.5 | 45 | 128 |
| 104 | 7.8 | A3 | $(10$ | 43 | 40.231 | -0.21 | 45 | $n 9$ | 12.94 | +00.5 | 44 | 162 |
| 105 | 8.8 | A5 | 00 | 49 | 56.700 | -0.35 | 45 | 10 | 13.18 | -01.7 | 44 | 186 |
| 106 | 6.2 | K0 | 00 | 54 | 4\%.201 | $+0.07$ | 45 | 34 | 10.05 | -00.5 | 45 | 2.37 |
| 107 | 7.0 | $+5$ | 00 | SH | 27.340 | +0.96 | 45 | 11 | 00.60 | -01.5 | 44 | 215 |
| 108 | 8.7 | F8 | 01 | 07 | 03.176 | +0.54 | 45 | 28 | 53.63 | -01.5 | 44 | 252 |
| 109 | 7.5 | $k 2$ | 01 | 16 | 06.745 | -0.02 | 45 | 26 | 35.63 | +01.8 | 44 | 279 |
| 110 | 8.1 | K0 | 01 | 2.5 | 43.133 | +10.58 | 45 | 22 | 31.21 | $+00.3$ | 44 | 312 |
| 111 | 6.3 | AO | 01 | 35 | 30.437 | -0.16 | 45 | 08 | 45.40 | +00.8 | 44 | 341 |
| 112 | $8 \cdot 1$ | A | 01 | 54 | $4 サ .045$ | -0.14 | 45 | 21 | 22.59 | +00.7 | 44 | 392. |
| 113 | 8.1 | A3 | 02 | 00 | 00.257 | +0.04 | 45 | 32 | 14.69 | -00.5 | 45 | 523 |
| 201 | H. 8 | AO | 02. | 14 | 32.511 | -0.07 | 45 | 16 | 56.77 | +00.4 | 44 | 473 |
| 202 | 7.6 | ${ }^{6} 5$ | 02. | 21 | 50.218 | -0.23 | 45 | 25 | 22.39 | -07.8 | 44 | 4133 |
| 203 | 7.3 | G5 | 02 | 21 | 10.353 | +0.05 | 45 | $1{ }^{2}$ | 36.31 | -00.8 | 44 | 512 |
| 204 | 8.4 | F\& | 02 | 3 H | 20.567 | $+0.86$ | 45 | 16 | 54.33 | -03.0 | 44 | 558 |
| 205 | 8.1 | F8 | 02 | 41 | 28.82.2 | -0.18 | 45 | 23 | 21.23 | -04.4 | 44 | 569 |
| 206 | 8.6 | K2 | 03 | 0 13 | 17.783 | -0.19 | 45 | 33 | 01.83 | -01.7 | 45 | 121 |
| 207 | 6.4 | MA | 03 | 12 | 44.017 | $+0.28$ | 4.5 | 09 | 45.02 | -03.0 | 44 | 648 |
| 208 | 7.5 | B8 | 03 | la | 04.408 | -0.06 | 45 | $1 ?$ | 28.61 | +01.0 | 44 | 677 |
| 209 | 7.6 | H8 | 03 | 22 | 11.257 | -0.01 | 45 | 20 | 25.39 | $+00.2$ | 44 | 695 |
| 210 | 8.1 | $k 2$ | 03 | 31 | 35.567 | -0.13 | 45 | 15 | 59.78 | -00.1 | 44 | 744 |
| 211 | 8.1 | $k 0$ | 03 | 4d | 07.130 | -0.10 | 45 | 14 | 15.14 | +00.3 | 45 | 828 |
| 212 | 7. ${ }^{\text {P }}$ | K0 | 03 | 50 | 29.504 | $+0.03$ | 45 | 21 | 53.86 | -02.9 | 45 | 836 |
| 213 | 8.0 | AO | 03 | 50 | 23.122 | +0.14 | 45 | 33 | 25.26 | -01.2 | 45 | 858 |
| 301 | 7.8 | G5 | 04 | 07 | 34.442 | +0.16 | 45 | 16 | 24.54 | -04.0 | 45 | 887 |
| 302 | 7.6 | AO | 04 | 17 | 17.945 | +0.22 | 45 | 20 | 46.01 | -02.8 | 45 | 921 |
| 303 | 7.7 | B9 | 04 | 30 | 27.468 | 0.00 | 45 | 31 | 54.87 | -01.0 | 45 | 955 |
| 304 | 7.7 | AO | 04 | 44 | 15.199 | +0.07 | 45 | '24 | 05.58 | -03.3 | 45 | 987 |
| 305 | $7 \cdot 8$ | 139 | 04 | bl | 39.232 | -0.09 | 45 | 22 | 25.23 | -00.8 | 45 | 1023 |
| 306 | 8.5 | AO | 05 | 21 | 38.178 | +0.04 | 45 | 11 | 04.07 | +00.2 | 45 | 1115 |
| 307 | $7 \cdot \square$ | F8 | 05 | 24 | 57.611 | -0.06 | 45 | 30 | 07.03 | -03.5 | 45 | 1131 |
| 308 | 7. 4 | 65 | 05 | 24 | 03.04 | +0.11 | 45 | 21 | 22.43 | -01.9 | 45 | 1132 |
| 309 | 8.1 | 135 | 05 | 3b | 20.203 | +0.70 | 45 | 2.5 | 18.24 | -10.8 | 45 | 1150 |
| 310 | 8.0 | F3 | 05 | 4 5 | 02.924 | -0.02 | 45 | 13 | 17.65 | -02.2 | 45 | 1178 |
| 311 | 6.6 | AO | 05 | 55 | 42.894 | -0.01 | 45 | 37 | 00.50 | -01.6 | 45 | 1216 |
| 312 | 7.6 | A0 | 05 | bl | 36.672 | -0.02 | 45 | 09 | 35.81 | -01.1 | 45 | 1225 |
| 313 | 7.2 | A2 | 06 | 00 | 51.730 | +0.04 | 45 | 35 | 24.79 | -05.5 | 45 | 1235 |

UTVAWA HZI CATALUGUE 160 STAKS IN 12 GROUPS

| NO | MAij | SP |  | <A | 50 | WM |  | FC | 1950 | PM | BD | NO |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 401 | 7.3 | 40 | 06 | 04 | 37.163 | $-0.07$ | 45 | 33 | 44.46 | -02.0 | 45 | 1248 |
| 402 | 7.4 | KO | 06 | 10 | 03.542 | $+11.05$ | 45 | 38 | 07.59 | -01.5 | 45 | 1289 |
| 403 | H.ll | K5 | 06 | 2! | 52.448 | $+0.13$ | 45 | 11 | 41.50 | $+00.3$ | 45 | 1296 |
| 404 | \&.1 | ${ }^{3} 5$ | 06 | 41 | 22.174 | $+1) .04$ | 45 | 2.4 | 50.05 | $-03.2$ | 45 | 1346 |
| 405 | 4.0 | A2 | 06 | 50 | 50.710 | -0.12 | 45 | 14 | $51 \cdot 16$ | -04.1 | 45 | 1363 |
| 406 | $8 \cdot 9$ | A0 | 06 | 5 ${ }^{\text {c }}$ | 55.120 | -0.02 | 45 | 30 | 01.47 | $-00.7$ | 45 | 1380 |
| 407 | 7.8 | KO | 07 | 07 | 13.727 | $-0.12$ | 45 | 19 | 48.00 | -00.8 | 45 | 1394 |
| 408 | 6.7 | KO | 07 | 11 | 54.641 | $-0.08$ | 45 | 29 | 52.45 | -02.9 | 45 | 1408 |
| 409 | 7.6 | $F 2$ | 07 | 14 | 24.115 | -0.08 | 45 | 13 | 13.09 | -06.9 | 45 | 1415 |
| 410 | 8.1 | G5 | 07 | 27 | 57.558 | $-0.08$ | 45 | 13 | 06.75 | -02.3 | 45 | 1441 |
| 411 | 7.6 | KO | 07 | 40 | 45.666 | 0.00 | 45 | 29 | 20.85 | -02.9 | 45 | 1476 |
| 412 | 8.0 | K2 | 07 | 46 | 59.001 | $+0.09$ | 45 | 28 | 04.63 | -01.0 | 45 | 1496 |
| 413 | 8.1 | A3 | 07 | 5.3 | 21.591 | -0.19 | 45 | 35 | 03.40 | -01.1 | 45 | 1509 |
| 501 | 7.8 | Ko | 08 | 08 | 24.269 | +0.31 | 45 | 21 | 32.48 | -00.4 | 45 | 1550 |
| 502 | 8.1 | K0 | 08 | 14 | 05.887 | -0.37 | 45 | 30 | 45.09 | -07.3 | 45 | 1568 |
| 503 | 7.8 | +0 | 08 | 30 | 49.208 | -0.28 | 45 | 22 | 07.77 | -02.3 | 45 | 1601 |
| 504 | 8.1 | 65 | 08 | 37 | 33.122 | 0.00 | 45 | 19 | 40.22 | +01.5 | 45 | 1613 |
| 505 | 8.1 | F5 | 08 | $4 n$ | 29.395 | -0.23 | 45 | 38 | 07.02 | -05.2 | 45 | 1624 |
| 506 | 6.1 | $k 0$ | 08 | $4 \%$ | 48.223 | $-0.11$ | 45 | 30 | 06.29 | -0.3.4 | 45 | 1649 |
| 507 | 6.4 | G5 | 09 | 03 | 54.561 | -0.58 | 45 | 22 | 41.90 | -04.9 | 45 | 1680 |
| 508 | 6.6 | KO | 09 | $1 H$ | 06.177 | -0.07 | 45 | 35 | 00.26 | -03.0 | 45 | 1708 |
| 509 | 6.6 | KO | 09 | 43 | 31.098 | $+0.48$ | 45 | 20 | 51.76 | -13.0 | 45 | 1762 |
| 510 | 8.0 | F2 | 09 | 47 | 19.985 | -0.78 | 45 | 19 | 08.45 | -09.1 | 45 | 1769 |
| 511 | 8.7 | 05 | 09 | 52 | 36.834 | $+0.16$ | 45 | 25 | 08.06 | -00.9 | 45 | 1778 |
| 512 | $6 \cdot 5$ | K0 | 09 | 54 | 48.110 | +0.05 | 45 | 34 | 12.71 | -03.4 | 45 | 1566 |
| 513 | 7.5 | $F 2$ | 10 | 04 | 02.073 | -0.07 | 45 | 18 | 15.91 | -00.6 | 45 | 1798 |
| 601 | 7.8 | $K \ddot{2}$ | 10 | 11 | 08.518 | -0.04 | 45 | 20 | 07.72 | +00.4 | 45 | 1811 |
| 602 | 7.4 | F 5 | 10 | 13 | 27.840 | -0.13 | 45 | 17 | 34.24 | $+02.3$ | 45 | 1814 |
| 603 | 7.8 | 65 | 10 | 14 | 27.401 | -0.63 | 45 | 16 | 09.23 | -02.0 | 45 | 1819 |
| 604 | 6.5 | K0 | 10 | 25 | 36.216 | -0.19 | 45 | 28 | 05.74 | -02.3 | 45 | 1832 |
| 605 | 8.4 | K5 | 10 | 32 | 46.110 | -0.2? | 45 | 30 | 56.13 | +01.6 | 46 | 1643 |
| 606 | 8.0 | KO | 10 | 44 | 38.791 | -0.71 | 45 | 33 | 11.54 | -03.6 | 46 | 1671 |
| 607 | 7.0 | KO | 10 | 56 | 08.877 | -0.48 | 45 | 27 | 58.78 | -03.7 | 45 | 1879 |
| 608 | 9.0 | G5 | 11 | 01 | 40.650 | $+0.09$ | 45 | 25 | 37.76 | -02.6 | 45 | 1890 |
| 609 | 7.5 | 60 | 11 | 12 | 20.111 | -0.48 | 45 | 20 | 05.54 | -06.1 | 45 | 1903 |
| 610 | 7.9 | 42 | 11 | 14 | 05.622 | -0.56 | 45 | 36 | 23.76 | -01.5 | 46 | 1717 |
| 611 | \% | M H | 11 | 25 | 00.823 | -0.07 | 45 | 27 | 38.85 | -02.3 | 45 | 1924 |
| 612 | 8.4 | 60 | 11 | 36 | 07.336 | $-5.62$ | 45 | 23 | 06.63 | +01.4 | 45 | 1447 |
| 613 | 7.9 | $F 2$ | 11 | 37 | 04.720 | +0.15 | 45 | 2.6 | 01.66 | -01.4 | 45 | 1952 |

* 11. MAG 6.5 107.3

APPENIIIXA

UTIANA HIT CATAIUGIE 160 STARS IN 12 GROUPS

| No | MAG | Sp |  | QA | 1950 | PM |  | DEC | 1950 | PM | 80 | NO |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 701 | 8.8 | F8 | 12 |  | 12.935 | $+0.30$ | 45 | 27 | 13.91 | -06.5 | 45 | 2001 |
| 702 | 7.7 | 43 | 12 | 24 | 13.744 | -0.20 | 43 | 30 | 05.68 | -01.4 | 46 | 1791 |
| 703 | \&s. 01 | +0 | 12 | $3{ }^{3}$ | 10.360 | $+0.15$ | 45 | 31 | 41.96 | +01.2 | 46 | 1802 |
| 704 | 7.1 | F2 | 12 | 3 t , | 10.645 | -1.35 | 45 | 24 | 31.93 | -03.8 | 46 | 1805 |
| 705 | 6.1 | K0 | 13 | 03 | 37.467 | -0.18 | 45 | 32 | 07.59 | +1)2.5 | 46 | 1847 |
| 706 | 8.6 | +5 | 13 | 12 | 12.560 | -0.02 | 45 | 26 | 41.46 | -01.0 | 45 | 2096 |
| 707 | H. 1 | F5 | 13 | 17 | 05.553 | -1.3* | 45 | 21 | 45.35 | -0.3.4 | 45 | 2104 |
| TUH | 8.3 | F5 | 13 | 33 | 51.762 | -0.44 | 45 | 16 | 12.86 | -01.8 | 45 | 2120 |
| 709 | 8.0 | $k$ K | 13 |  | 14.810 | $+0.03$ | 45 | 14 | 24.05 | -01.1 | 45 | 2124 |
| 710 | 8.9 | +5 | 13 |  | 17.137 | $+0.00$ | 45 | 35 | 46.83 | -01.8 | 46 | 1894 |
| 711 | $8 \cdot 6$ | F5 | 13 |  | 33.442 | -0.35 | 45 | 25 | 06.48 | +01.0 | 45 | 2131 |
| 712 | B.b | F8 | 13 | 55 | 33.197 | -0.08 | 45 | 23 | 55.73 | +00.1 | 45 | 2140 |
| 713 | 8.1 | K0 | 13 | 59 | 10.465 | +0.17 | 45 | 31 | 36.54 | -00.8 | 45 | 2148 |
| 801 | 9.1 | 45 | 14 |  | 45.835 | -1.45 | 45 | 22 | 22.42 | +03.4 | 45 | 2178 |
| $8 \cup 2$ | 8.4 | 18 | 14 |  | 54.203 | -0.07 | 45 | 32 | 45.40 | -01.7 | 45 | 2203 |
| 803 | 7.7 | 65 | 14 |  | 16.606 | -1.10 | 45 | 37 | 44.50 | -19.2 | 46 | 1981 |
| 804 | R. ${ }^{\text {ch }}$ | +0 | 14 |  | 38.338 | $+0.52$ | 45 | 23 | 47.74 | -02.0 | 45 | 2214 |
| 805 | 8.5 | F8 | 14 |  | 57.387 | -0.68 | 45 | 22 | 33.50 | +06.8 | 45 | 2230 |
| 806 | 7.9 | F5 | 14 |  | 37.590 | -0.62 | 45 | 30 | 00.78 | +05.4 | 45 | 2233 |
| $8 \cup 7$ | 8.7 | G5 | 15 |  | 23.094 | -0.86 | 45 | 20 | 56.51 | +15.4 | 45 | 2266 |
| 808 | 7.9 | ko | 15 |  | 56.988 | -0.39 | 45 | $1]$ | 52.82 | $+00.9$ | 45 | 2277 |
| 809 | 6.2 | $k 2$ | 15 | 22 | 23.436 | -0.16 | 45 | 26 | 48.66 | -00.3 | 45 | 2284 |
| 810 | 8. H | K2 | 15 | 34 | 00.414 | $+0.15$ | 45 | 36 | 45.90 | -02.1 | 45 | 2307 |
| 811 | 7.4 | +0 | 15 |  | 32.744 | $+0.27$ | 45 | 16 | 42.39 | +01.4 | 45 | 2317 |
| 812 | 8.0 | 65 | 15 |  | 27.453 | -0.41 | 45 | 28 | 18.99 | +03.1 | 45 | 2325 |
| 813 | 8.7 | F2 | 15 |  | 01.352 | -0.27 | 45 | 35 | 35.49 | -00.5 | 45 | 2355 |
| 901 | 7.4 | Ko | 16 |  | 25.425 | -0.03 | 45 | 30 | 41.78 | +00.9 | 45 | 2374 |
| 902 | 7.4 | G5 | 16 |  | 47.715 | -0.64 | 45 | 29 | 27.16 | +01.7 | 45 | 2404 |
| 903 | 8.4 | 65 | 16 |  | 41.730 | -0.28 | 45 | 11 | 37.83 | -00.5 | 45 | 2446 |
| 904 | 8.4 | 60 | 16 |  | 27.468 | -0.33 | 45 | 17 | 12.85 | -00.7 | 45 | 2453 |
| 905 | 6.9 | K2 | 17 |  | 12.145 | -0.01 | 45 | 23 | 01.21 | -01.2 | 45 | 2504 |
| 906 | 7.4 | H3 | 17 | 12 | 00.269 | -0.12 | 45 | 25 | 45.49 | -01.1 | 45 | 2509 |
| 907 | 6.0 | F0 | 17 |  | 23.145 | -0.36 | 45 | 21 | 24.36 | +08.6 | 45 | 2521 |
| 908 | 8.3 | K0 | 17 |  | 11.751 | -0.06 | 45 | 23 | 44.14 | +01.3 | 45 | 2531 |
| 909 | 7.3 | 60 | 17 |  | 37.733 | $+0.02$ | 45 | 35 | 02.75 | +04.7 | 45 | 2573 |
| 910 | 8.2 | 65 | 17 |  | 14.164 | +0.41 | 45 | 33 | 39.90 | $+02.2$ | 45 | 2620 |
| 911 | 8.0 | AO | 17 |  | 17.771 | -0.07 | 45 | 13 | 27.28 | +00.4 | 45 | 2621 |
| 912 | 6.2 | 89 | 17 |  | 20.447 | -0.07 | 45 | 28 | 40.95 | $+02.5$ | 45 | 2635 |
| 913 | 5.4 | $k 2$ | 17 |  | 30.393 | -0.05 | 45 | 30 | 09.87 | -03.0 | 45 | 2638 |
| 914 | 7.4 | 189 | 11 | 54 | 41.018 | -0.11 | 45 | 21 | 00.40 | +01.4 | 45 | 2643 |

OTTAWA PLI CATALOGIJE 160 STARS IN 12 GROUPS

| NO | MAG | Sp |  | Ha | 1950 | ${ }^{\prime} \times M$ |  | UEC | 1950 | PM | Bi) | NO |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1001 | 8.5 | $\mathrm{F}^{\circ}$ | 18 | U8 | 22.094 | $+0.02$ | 45 | 36 | 21.48 | -01.8 | 45 | 2667 |
| 1042 | 6.3 | 170 | 18 | 14 | 06.184 | -0.81 | 45 | 11 | 34.49 | -11.2 | 45 | 2684 |
| 1003 | 7.4 | AO | 18 | 1 i, | 45.251 | -0.01 | 45 | OH | 07.24 | +00.8 | 45 | 2690 |
| 1004 | 8.1 | AO | 18 | 21 | 37.354 | 0.00 | 45 | 11 | 34.56 | $+03.0$ | 45 | 2704 |
| 1005 | 8.5 | KO | 18 | 24 | 41.225 | +0.33 | 45 | 25 | 10.42 | $+00.2$ | 45 | 2731 |
| 1006 | 8.0 | F0 | 18 | 35 | 47.805 | $-0.10$ | 45 | 37 | 38.61 | $+01.1$ | 45 | 2747 |
| 1007 | 6.8 | F0 | 18 | 47 | 08.243 | $+0.26$ | 45 | 12 | 10.34 | $+08.5$ | 45 | 2777 |
| 1008 | 8.4 | F5 | 19 | $\cup 2$ | 16.826 | $+0.18$ | 45 | 31 | 58.28 | -00.9 | 45 | 2824 |
| 1009 | $7 \cdot 3$ | A0 | 19 | 13 | $50.28 \%$ | $+0.10$ | 45 | 14 | 48.09 | -01.0 | 45 | 2865 |
| 1010 | 8.6 | K | 19 | 14 | 55.970 | -0.07 | 45 | 29 | 58.90 | +00.6 | 45 | 2877 |
| 1011 | 7.5 | k0 | 19 | 44 | 44.962 | -0.04 | 45 | 36 | 45.24 | -00.8 | 45 | 2971 |
| 1012 | 7.8 | KO | 19 | 52 | 12.064 | -0.09 | 45 | 20 | 19.21 | $+00.1$ | 45 | 3001 |
| 1013 | 7.5 | A2 | 20 | 00 | 11.300 | $+0.28$ | 45 | 20 | 10.19 | +02.3 | 45 | 3038 |
| 1014 | H. 1 | 65 | 20 | 06 | 32.243 | $-0.12$ | 45 | 23 | 48.25 | $-03.3$ | 45 | 3066 |
| 1101 | 7.5 | K2 | 20 | 14 | 58.124 | $+0.03$ | 45 | 11 | 00.79 | +01.6 | 44 | 3414 |
| 1102 | 7.0 | FS | 20 | 1 ¢ | 11.258 | $+0.18$ | 45 | 12 | 19.84 | -02.0 | 44 | 3429 |
| 1103 | 7.3 | 89 | 20 | 27 | 09.446 | 0.00 | 45 | 33 | 04.86 | -00.5 | 45 | 3191 |
| 1104 | 6.5 | b3 | 20 | 37 | 41.827 | -0.03 | 45 | 24 | 21.48 | $+00.2$ | 45 | 3233 |
| 1105 | 6.7 | $k 5$ | 20 | 45 | 37.171 | -0.02 | 45 | 23 | 43.18 | -01.8 | 45 | 3275 |
| 1106 | 7.5 | A0 | 20 | 46 | 42.8Fil | $+0.04$ | 45 | 15 | 58.32 | $+00.1$ | 44 | 3590 |
| 1107 | 8.2 | 67 | 20 | 51 | 47.534 | $+0.14$ | 45 | 11 | 36.86 | $+00.1$ | 44 | 3622 |
| 1108 | 7.3 | 90 | 21 | 05 | 05.640 | -0.08 | 45 | 28 | 25.57 | -01.0 | 45 | 3410 |
| 1109 | 6.1 | A0 | 21 | 09 | 27.750 | -0.08 | 45 | 28 | 07.49 | $-00.6$ | 45 | 3438 |
| 1110 | 7.6 | 149 | 21 | 14 | 09.125 | -0.0.3 | 45 | 31 | 20.27 | -00.7 | 45 | 3476 |
| 1111 | 8.5 | 60 | 21 | 26 | 15.499 | -0.01 | 45 | 21 | 34.44 | -03.7 | 44 | 3625 |
| 111 ? | 7.0 | H5 | 21 | 28 | 08.531 | -0.02 | 45 | 16 | 26.73 | -00.5 | 44 | 3840 |
| 1113 | \# | MC | 21 | 34 | 08.259 | 0.59 | 45 | 09 | 00.09 | 00.9 | 44 | 3871 |
| 1114 | 6.5 | M 8 | 21 | 4i) | 13.434 | $-0.07$ | 45 | 32 | 13.60 | -01.7 | 45 | 3637 |
| 1201 | 6.5 | 65 | 22 | $0 \rightarrow$ | 34.422 | $-0.56$ | 45 | 29 | 45.59 | 05.1 | 45 | 3813 |
| 1202 | 7.3 | A2 | 22 | '24 | 54.375 | -0.25 | 45 | 32 | 103.82 | -01.5 | 45 | 3941 |
| 1203 | 4.2 | K2 | 22 | 27 | 45.213 | $-0.05$ | 45 | 29 | 17.24 | 00.5 | 45 | 3958 |
| 1204 | 7.4 | K0 | $2{ }^{2}$ | 35 | 36.741 | -0.19 | 45 | 08 | 52.98 | 00.5 | 44 | 4183 |
| 1205 | 7.1 | F8 | 22 | 30 | 02.557 | -1.05 | 45 | 34 | 11.50 | -16.9 | 45 | 4002 |
| 1206 | 8.3 | K 2 | 22 | 41 | 01.671 | 0.06 | 45 | 15 | 57.76 | 1.7 | 44 | 4209 |
| 1207 | 8.1 | Kı0 | 22 | 51 | 58.151 | -0.0\% | 45 | 25 | 37.18 | 0.1 | 44 | 4263 |
| 1208 | 8.4 | +8 | 22 | 53 | 55.36n | $-0.16$ | 45 | 31 | 29.35 | -03.7 | 45 | 4094 |
| 1209 | 7.4 | KO | 22 | 54 | 17.438 | 0.26 | 45 | 14 | 27.72 | 2.1 | 44 | 4307 |
| 1210 | K. 3 | F5 | 23 | 01 | 58.620 | 0.17 | 45 | 12 | 42.42 | 0.8 | 44 | 4320 |
| 1211 | 7.1 | ko | 23 | OH | 31.452 | -0.75 | 45 | 14 | 40.47 | -27.5 | 44 | 4347 |
| 1212 | 0.3 | H9 | 23 | 15 | 34.807 | 0.24 | 45 | 12 | 56.46 | -00.9 | 44 | 4373 |
| 1213 | 1.9 | ko | 23 | 26 | 03.144 | 0.02 | 45 | 25 | 03.86 | -00.4 | 44 | 4424 |
| 1214 | 7.8 | A2 | 23 | 30 | 53.550 | -0.06 | 45 | 26 | 34.76 | -00.9 | 44 | 4464 |

[^20]| APPENUIX E |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| UTTAwA |  | fZt ufsehvations 1956 VALUES AI $1 / 20$ YEAR |  | 101970 |  |
|  |  |  |  |  |  |
| EPOCH | Latitule | Uro-Al | EHOCH | LATITUNE | UTO-A 1 |
| 54.05 | 38.768 | .7458 | 58.55 | 38.777 | -0.3096 |
| 56.10 | 38.820 | .7910 | 58.60 | $38.79 \%$ | -0.3044 |
| 56.15 | 38.831 | . 7634 | 58.65 | $38.74{ }^{\prime}$ | -0.3283 |
| b6. 20 | 38.821 | . 7330 | 54.70 | 38.718 | -0.3440 |
| 56.25 | 38.722 | . 7U3? | 58.75 | 38.645 | -0.3684 |
| 56.30 | 34.692 | - 67896 | 58.80 | 38.473 | -0.4031 |
| 56.35 | 38.630 | -6700 | 58.85 | 38.429 | -0.4511 |
| 36.40 | 36.503 | . 6497 | 58.90 | 38.450 | -0.4696 |
| 56.45 | 3H.536 | . 6367 | 58.95 | 38.459 | -0.4922 |
| 56.50 | 38.500 | . 6307 | 59.00 | 38.320 | -0.5329 |
| 56.55 | 3H.464 | . 6394 | 59.05 | 38.361 | -0.5498 |
| 56.60 | 38.425 | . 6451 | 59.10 | 38.444 | -0.5624 |
| 36.05 | 38.433 | -6,378 | 59.15 | 38.478 | -0.6023 |
| 56.70 | 38.309 | . 6352 | 59.20 | 38.465 | -0.6376 |
| 56.15 | 38.401 | . 5993 | 59.25 | 38.469 | -0.6573 |
| 26.030 | 38.42 .8 | . 5882 | 59.30 | 38.551 | -0.6791 |
| 56.85 | 38.447 | . 5590 | 59.35 | 38.625 | -0.6951 |
| 56.90 | 38.488 | . 5610 | 59.40 | 38.680 | -0.7140 |
| 56.95 | 38.516 | . 5145 | 59.45 | 38.741 | -0.7393 |
| 57.00 | 38.541 | . 5001 | 59.50 | 38.790 | -0.7478 |
| 57.105 | 38.646 | . 4757 | 59.55 | 38.792 | -0.7638 |
| 57.10 | 38.737 | . 4665 | 54.60 | 38.812 | -0.7686 |
| 57.15 | 38.820 | . 4336 | 59.65 | 38.81 ? | -0.8168 |
| 57.20 | 38.851 | . 3950 | 59.70 | 38.836 | -0.8208 |
| 57.25 | 38.838 | . 3614 | 59.75 | 38.838 | -0.8426 |
| 57.30 | 3н. 827 | -3298 | 59.80 | 38.732 | -0.8914 |
| 57.35 | 38.869 | -2467 | 59.85 | 38.687 | -0.919? |
| 57.40 | 38.808 | -2ん71 | 59.90 | 38.6883 | -0.9533 |
| 57.45 | 38.763 | . 2479 | 59.95 | 38.540 | -0.9825 |
| 57.50 | 38.704 | - 2228 | 60.00 | 38.528 | -1.0108 |
| 57.55 | 38.67 .3 | . 2190 | 60.05 | 38.529 | -1.0373 |
| 51.60 | 38.638 | - 2.386 | 60.10 | 38.386 | -1.0559 |
| 57.65 | 38.582 | . 1764 | 60.15 | 38.554 | -1.0791 |
| 57.70 | 38.467 | . 1 150 | 60.20 | 38.482 | -1.1014 |
| 57.75 | 34.405 | .1371 | 60.25 | 38.464 | -1.1347 |
| 57.80 | 38.355 | . 1179 | 60.30 | 38.468 | $-1.1647$ |
| 57.85 | 38.301 | - $0 \rightarrow 09$ | 60.35 | 37.232 | -1.1862 |
| 57.40 | 34.284 | . 0565 | 60.40 | 37.326 | -1.2140 |
| 51.45 | 38.298 | . 0390 | 60.45 | 37.325 | -1.2402 |
| 58.00 | 38.341 | . 0277 | 60.50 | 37.345 | -1.2583 |

## APPENIIX BS <br> OTTA'AA RLT UBSERVATIUNS 1956 TO 1970 VALUES AT $1 / 20$ YEAR

| EPOCH | LATITUJF | UTU-Al | EPOCH | LATITUUE | UTO-A. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 58.05 | 38.3888 | -0.0244 | 60.55 | 37.394 | -1.2645 |
| 53.10 | 38.474 | -0.0457 | 60.50 | 37.451 | -1.2677 |
| 58.15 | 39.551 | -0.078? | 60.65 | 37.427 | -1.285? |
| 58.20 | 34.612 | -0.1151 | 60.70 | 37.484 | -1.2986 |
| 58.25 | 38.649 | -0.1513 | 60.75 | 37.462 | -1.3235 |
| 58.30 | 38.690 | -0.1929 | 60.80 | 37.471 | -1.3488 |
| 58.35 | 38.776 | -0.2219 | 60.85 | 37.465 | -1.3760 |
| 58.40 | 38.836 | -0.7499 | 60.90 | 37.481 | -1.4074 |
| 58.45 | 38.845 | -0.2719 | 60.95 | 37.497 | -1.4356 |
| 58.50 | 38.882 | -0.2.875 | 61.00 | 37.427 | -1.4571 |
| 61.05 | 37.409 | -1.4667 | 63.55 | 37.367 | -2.6277 |
| 01.10 | 37.387 | -1.4938 | 63.60 | 37.318 | -2.6402 |
| 61.15 | 37.348 | -1.5127 | 63.65 | 37.279 | -2.6552 |
| 61.20 | 37.336 | -1.5423 | 63.70 | 37.240 | -2.6781 |
| 61.25 | 37.348 | -1.5727 | 63.75 | 37.187 | -2.7044 |
| 61.30 | 37.337 | -1.5977 | 63.80 | 37.129 | -2.7370 |
| 61.35 | 37.342 | -1.6187 | 63.85 | 37.103 | -2.7721 |
| 61.40 | 37.301 | -1.6469 | 63.90 | 37.130 | -2.8063 |
| 61.45 | 37.314 | -1.6611 | 63.95 | 37.183 | -2.8388 |
| H1. 50 | 37.330 | -1.6712 | 64.00 | 37.192 | -2.8751 |
| 01.55 | 37.330 | -1.6766 | 64.05 | 37.293 | -2.9115 |
| 61.60 | 37.349 | -1.6894 | 64.10 | 37.332 | -2.9466 |
| 61.65 | 37.304 | -1.7072 | 64.15 | 37.403 | -2.9866 |
| 61.70 | 37.330 | -1.7181 | 64.20 | 37.459 | -3.0287 |
| 61.75 | 37.323 | -1.7341 | 64.25 | 37.519 | -3.0731 |
| 61.80 | 37.341 | -1.7539 | 64.30 | 37.556 | -3.1157 |
| 0.1 .85 | 37.364 | -1.7736 | 64.35 | 37.593 | -3.1586 |
| 61.90 | 37.386 | -1.81015 | 64.40 | 37.603 | -3.2048 |
| 01.95 | 37.394 | -1.8257 | 64.45 | 37.576 | -3.2408 |
| 02.00 | 37.449 | -1.8521 | 64.50 | 37.533 | -3.2658 |
| 62.05 | 37.417 | -1.4790 | 64.55 | 37.544 | -3.2913 |
| 62.10 | 37.385 | -1.8984 | 64.60 | 37.486 | -3.3171 |
| 62.15 | 37.44 d | -1.9263 | 64.65 | 37.463 | -3.3396 |
| 12.20 | 37.486 | -1.9544 | 64.70 | 37.410 | -3.3636 |
| 02.25 | 37.465 | -1.9854 | 64.75 | 37.343 | -3.4025 |
| 62.30 | 37.428 | -2.0167 | 64.80 | 37.2.80 | -3.4435 |
| 62.35 | 37.435 | -2.04839 | 64.85 | 37.226 | -3.4836 |
| 02.40 | 37.400 | -2.0791 | 64.90 | 37.176 | -3.5220 |
| 62.45 | 37.34') | -2.0998 | 64.95 | 37.159 | -3.560.5 |
| 02.50 | 37.317 | -2.1073 | 65.00 | 37.164 | -3.5930 |


| APPENUIX B |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | OTTAmA | PZT OBSER | ERVATIUNS 1956 | 101970 |  |
|  |  | VAl_UES | AT 1/20 YEAR |  |  |
| EPOCH | LATITUUR. | UTO-Al | EPOCH | LATITUUE | UTU-Al |
| 62.b5 | 37.31\% | -2.1179 | 65.05 | 37.185 | -3.6270 |
| 52.60 | 37.264 | -2.1314 | 65.10 | 37.2.38 | -3.6647 |
| 02.65 | 37.250 | -2.1440 | 65.15 | 37.221 | -3.7029 |
| 02.70 | 37.234 | -2.1574 | 65.20 | 37.284 | -3.744? |
| 62.75 | 37.273 | -2.1799 | 65.25 | 37.354 | -3.7932 |
| 62.80 | 37.267 | -2.2025 | 65.30 | 37.394 | -3.8422 |
| 62.85 | 37.254 | -2.2340 | 65.35 | 37.421 | -3.8864 |
| 62.40 | 37.271 | -2.2630 | 65.40 | 37.450 | -3.9263 |
| 62.45 | 37.333 | -2.2939 | 65.45 | 37.519 | -3.9662 |
| 63.00 | 37.397 | -2.3237 | 65.50 | 37.543 | -4.0019 |
| 03.05 | 37.432 | -2.3390 | 65.55 | 37.565 | -4.0395 |
| 63.10 | 37.434 | -2.3618 | 65.50 | 37.592 | -4.0731 |
| 63.15 | 37.481 | -2.3853 | 65.65 | 37.533 | -4.0999 |
| 63.20 | 37.512 | -2.4156 | 65.70 | 37.535 | -4.1408 |
| 63.25 | 37.496 | -2.4492 | 65.75 | 37.486 | -4.1884 |
| 63.30 | 37.513 | -2.4853 | 65.80 | 37.402 | -4.2346 |
| 63.35 | 37.486 | -2.5228 | 65.85 | 37.388 | -4.2800 |
| 63.40 | 37.482 | -2.5b72 | 65.90 | 37.363 | -4.3248 |
| 63.45 | 37.454 | -2. 5865 | 65.95 | 37.292 | -4.3700 |
| 03.50 | 37.385 | -2.0108 | 66.00 | 37.242 | -4.4120 |
| 66.05 | 37.235 | -4.4503 | 64. 05 | 37.330 | -6.1874 |
| 66.10 | 37.202 | -4.4977 | 68.10 | 37.356 | -6.2368 |
| 66.15 | 37.205 | -4.5399 | 68.15 | 37.383 | -6.2919 |
| 66.20 | 37.194 | -4.5800 | 68.20 | 37.348 | -6.3391 |
| 66.25 | 37.226 | -4.6291 | 68.25 | 37.397 | -6.3835 |
| n6. 30 | 37.254 | -4.6785 | 68.30 | 37.400 | -6.4460 |
| 66.35 | 37.283 | -4.7304 | 68.35 | 37.391 | -6.4979 |
| 66.40 | 37.323 | -4.7779 | 68.40 | 37.353 | -6.5468 |
| 66.45 | 37.354 | -4.8179 | 68.45 | 37.361 | -6.5895 |
| 66.50 | 37.387 | -4.8343 | 6R.50 | 37.289 | -6.6279 |
| 66.55 | 37.438 | -4.8839 | 68.55 | 37.296 | -6.6586 |
| 66.60 | 37.459 | -4.9174 | 68.60 | 37.301 | -6.6847 |
| 66.65 | 37.489 | -4.9555 | 68.65 | 37.380 | -6.7312 |
| 06.70 | 31.526 | -4.9999 | 68.70 | 37.276 | -6.7727 |
| 66.75 | 37.543 | -5.0478 | 68.75 | 37.303 | -6.8139 |
| 66.80 | 37.503 | -5.1020 | 68.80 | 37.270 | -6.8619 |
| 66.85 | 37.520 | -5.1554 | 68.85 | 37.295 | -6.9131 |
| 66.90 | 37.422 | -5.2066 | 68.90 | 37.312 | -6.9620 |
| 66.95 | 37.350 | -5.2516 | 68.95 | 37.344 | -7.0077 |
| 67.100 | 37.356 | -5.2926 | 69.00 | 37.334 | -7.0541 |



APPENUIX H
UTTA．H HZ UHSERVATIUNS 1966 TO 1970 10 गAY SMUUTHEU VALUES

JUL．IAN DAY
2435509.5 2435519．5 2435529.5 2435539.5 2435547.5 2435564.5 2435 勺หソ． 5 2435574.5 2435589.5 2435599.5
2435609.5 2435617.5 2435629.5 2435639.5 2435649.5 2435659.5 2435669.5 2435679.5 2435609.5 2435099.5
2435709.5
2435719.5
2435729.5
2435739.5
2435749.5
2435759.5
2435769.5
2435779.5
2435789.5
2435799.5
2435809.5
2435819.5 2435829.5 2435439.5 2435849.5 2435854.5 2435869.5 2435819.5 2435889.5 2435899.5 UTO－Al JUlian oar Latitude UTOMAI LATITJいE

| 38.822 | .7910 | 2436009.5 | 38.742 | .2390 |
| :--- | :--- | :--- | :--- | ---: |
| 38.4 .34 | .7782 | 2436019.5 | 38.712 | .2284 |
| 38.335 | .7547 | 2436029.5 | 38.695 | .2206 |
| 38.432 | .7450 | 2436039.5 | 38.669 | .2181 |
| 38.813 | .7280 | 2436049.5 | 38.645 | .2163 |
| 38.771 | .7109 | 2436059.5 | 38.619 | .2073 |
| 38.741 | .6940 | 2436069.5 | 38.605 | .1894 |
| 38.723 | .6808 | 2436079.5 | 38.563 | .1775 |
| 38.644 | .6743 | 2436089.5 | 38.512 | .1706 |
| 38.641 | .6702 | 2436099.5 | 38.452 | .1628 |
| 38.574 | .6664 | 2436109.5 | 38.412 | .1465 |
| 38.923 | .6547 | 2436119.5 | 38.388 | .1340 |
| $38.5<1$ | .6430 | 2436129.5 | 38.364 | .1217 |
| 38.532 | .6366 | 2436139.5 | 38.321 | .1103 |
| 38.514 | .6342 | 2436149.5 | 38.291 | .0938 |
| 38.443 | .6346 | 2436159.5 | 38.288 | .0804 |
| 38.473 | .6351 | 2436169.5 | 38.295 | .0663 |
| 38.446 | .6402 | 2436179.5 | 38.288 | .0565 |
| 38.432 | .6455 | 2436189.5 | 38.325 | .0428 |
| 38.434 | .6465 | 2436199.5 | 38.371 | .0280 |
| 38.431 | .6426 | 2436209.5 | 38.407 | .0091 |
| 38.375 | .6378 | 2436219.5 | 38.420 | -0.0101 |
| 38.343 | .6314 | 2436229.5 | 38.434 | -0.0283 |
| 38.302 | .6160 | 2436239.5 | 38.448 | -0.0444 |
| 38.349 | .6043 | 2436249.5 | 38.487 | -0.0612 |
| 38.418 | .5894 | 2436259.5 | 38.533 | -0.0792 |
| 38.420 | .5759 | 2436269.5 | 38.566 | -0.0975 |
| 38.440 | .5648 | 2436279.5 | 38.590 | -0.1142 |
| 38.454 | .5625 | 2436289.5 | 38.621 | -0.1333 |
| 38.476 | .5552 | 2430299.5 | 38.654 | -0.1572 |
| 38.490 | .5427 | 2430309.5 | 38.679 | -0.1830 |
| 38.507 | .5272 | 2436319.5 | 38.708 | -0.2019 |
| 38.523 | .5111 | 2436329.5 | 38.752 | -0.2162 |
| 38.551 | .4984 | 2436339.5 | 38.804 | -0.2299 |
| 34.584 | .4864 | 2436349.5 | 38.833 | -0.2450 |
| 38.633 | .4730 | 2436359.5 | 38.846 | -0.2599 |
| 38.644 | .4621 | 2436309.5 | 38.853 | -0.2722 |
| 38.746 | .4560 | 2436379.5 | 38.856 | -0.2802 |
| 38.793 | .4453 | 2430389.5 | 38.823 | -0.2896 |
| 38.828 | .4250 | 2436399.5 | 38.796 | -0.3003 |


|  | ot fawa | PLT OBSER <br> 10 Dar SM | B <br> UNS 1956 TO HED VALIJES | 1970 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| JULIAN UAY | LATI THE． | （1T）－A1 | Jultian uay | Lat itude | UTO－A1 |
| 2435909.5 | 38.843 | ． 4018 | 2436409.5 | 38.782 | －0．3072 |
| 2435919.5 | $38.841)$ | ． 3810 | 2436419.5 | 38.785 | －0．3070 |
| 2435429.5 | 3\％．\％ら1 | ． 3647 | 2436429.5 | 38.784 | －0．3084 |
| 2435939.5 | 38.84 n | ． 3476 | 2436439.5 | 38.758 | －0．3206 |
| 2435949.5 | 38.841 | ． 3296 | 2436449.5 | 33.712 | －0．3384 |
| 2435959.5 | 38．び㕲 | ． 3097 | 24.30459 .5 | 38.670 | －0．3507 |
| 2435969.5 | 38.870 | ． 2930 | 2436469.5 | 34．652 | －0．3554 |
| 2435979.5 | 38.854 | .2767 | 24.36479 .5 | 38.601 | －0．3652 |
| 2435989.5 | 38.817 | ． 2627 | 2436489.5 | 38.534 | －0．3830 |
| 2435499.5 | 38.772 | ． 2493 | 2436499.5 | 38.480 | －0．4097 |
| 2436509.5 | 38.455 | －0．4345 | 2437009.5 | 38.489 | －1．1041 |
| 2436519.5 | 38.450 | －0．4534 | 2437019.5 | 38.469 | －1．1223 |
| 2436529.5 | 38.454 | －0．4598 | 2437029.5 | 38.460 | －1．1413 |
| 2436539.5 | 38.4 hl | －0．4668 | 2437039.5 | 38.463 | －1．1572 |
| 2436549.5 | 38.456 | －0．4824 | 2437049.5 | 38.465 | －1．1695 |
| 2436559.5 | 38．4 $\mathrm{l}^{\mathrm{h}}$ | －0．5082 | 2437059.6 | 38.489 | $-1.1828$ |
| 2430569.5 | 38．3aid | －0．5247 | 2437069.5 | 38.519 | －1．1967 |
| 2436579.5 | 38.365 | －0．5443 | 2437979．5 | 37.305 | －1．2120 |
| 2436589.5 | 38.342 | －0．5506 | 24371089.5 | 37.320 | －1．2262 |
| c436549．5 | 38.415 | －0．5570 | 2437099.5 | 37.332 | －1．2380 |
| 2436609.5 | 38．444 | －0．5673 | 2437109.5 | 37.342 | －1．2466 |
| 2436619.5 | 38．4ヶ7 | －0．5876 | 2437119.5 | 37.366 | －1．2530 |
| 2436629.5 | 38．4nd | －0．6118 | 2437129.5 | 37.388 | －1．2584 |
| 2436639.5 | 38．46\％ | －0．6316 | 2437139.5 | 37.411 | －1． 2623 |
| 2436649.5 | 38.447 | －0．6452 | 2437149.5 | 37.437 | －1．2661 |
| 2436659.5 | 38.410 | －0．6559 | 2437159.5 | 37.449 | －1．2726 |
| 2436669.5 | 38.519 | －0．6676 | 2437169.5 | 37.439 | －1．2825 |
| 2436679.5 | 38.55 | －0．6805 | 2437179.5 | 37.446 | －1．2908 |
| 2436689.5 | 38.5411 | －0．6896 | 2437189.5 | 37.464 | －1．2988 |
| 2436699.5 | 38.618 | －0．6960 | 2437199.6 | 37.478 | －1．3094 |
| 2436709.5 | 38.650 | －0．7049 | 2437209.5 | 37.470 | －1．3238 |
| 2436719.5 | 38.684 | －0．7202 | 2437219.5 | 37.471 | －1．3382 |
| 2436729.5 | 38.71 н | －0．7333 | 2437229.5 | 37.467 | －1．3521 |
| 2436739.5 | 38．750 | －0．7403 | 2437239.5 | 37.465 | －1．3669 |
| 2436749．5 | 38．778 | －0．7462 | 2437249.5 | 37.470 | －1．3829 |
| 2436759.5 | 38.789 | －0．7533 | 2437259.5 | 37.483 | －1．3991 |
| 2436769.5 | 38.807 | －0．7582 | 2437269.5 | 37.491 | －1．4145 |
| 2436779.5 | 38.814 | －0．7617 | 2437279.5 | 37.483 | －1．4307 |
| 2436789.5 | 38．817 | －0．7752 | 2437289.5 | 37.469 | －1．4448 |
| 2436799.5 | 38．79力 | －0．7959 | 2437299.5 | 37.450 | －1．4536 |

APPENOIX $G$
OTTANA PLT OHSFRVATIUNS 1956 TO 1970
10 UAY SMOOTHEU VAI_UES

| JUL 1 AN DAY | LATITUIL | 1)TU-A1 | JULIAN DAY | LATITUUE | UTO-A1 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 24.36809 .5 | 38.741 | -0.8116 | 2437309.5 | 37.432 | -1.4595 |
| 2436819.5 | 38.815 | - 0.81195 | 2.437319 .5 | 37.414 | -1.4698 |
| 2436829.5 | 38.837 | -0.8286 | 2437529.5 | 37.396 | -1.4827 |
| 24.36839 .5 | 38.3\% | -0.8442 | 2437339.5 | 37.374 | - 1.4 .446 |
| 2436849.5 | 38.7/4 | -0.8631 | 2431349.5 | 37.360 | -1.5059 |
| 2430859.5 | 38.724 | -0.8844 | 2437359.5 | 37.348 | -1.5209 |
| 2436864.5 | 38.71 c | -0.9023 | 2437369.5 | 37.340 | $-1.5366$ |
| 2436874.5 | 38.701 | -0.9196 | 2437319.5 | 37.342 | -1.5527 |
| 2430807.5 | 34.47\% | -0.9355 | 2437389.5 | 37.346 | -1.5684 |
| 2430899.5 | $38.63 ?$ | -0.9531 | 2437349.5 | 37.343 | -1.5837 |
| 2436909.5 | 38.54d | $-0.9705$ | 2437409.5 | 37.337 | -1.5959 |
| 2436917.5 | 34.9化5 | -0.9871 | 2437419.5 | 37.338 | -1.6079 |
| 2436929.5 | $38.5 c 0$ | -1.0021 | 2437429.5 | 37.334 | -1.6207 |
| $<436939.5$ | 38.5c\% | -1.0174 | 24.37439 .5 | 37.327 | -1.6346 |
| 2436949.5 | 38.5?1 | $-1.0318$ | 2437449.5 | 31.320 | -1.6458 |
| <436959.5 | $34.40{ }^{3}$ | -1.0435 | 2437459.5 | 37.314 | -1.6553 |
| 2436969.5 | $38.45 \%$ | -1.0536 | 24.37469 .5 | 37.311 | -1.6636 |
| $24.56,474.5$ | 38.411 | -1.0642 | 2437479.5 | 37.324 | -1.6699 |
| 24369839.5 | 36.50: | -1.0768 | 2437434.5 | $37 \cdot 334$ | $-1.6729$ |
| 2436949.5 | 38.517 | -1.0844 | 2437499.5 | $37 \cdot 329$ | -1.6763 |
| 2437509.5 | .31.332 | -1.6819 | 2438009.5 | 37.319 | -2.2.474 |
| 2437519.5 | 37.331 | -1.6894 | 2438019.5 | 37.354 | -2.3050 |
| 2437529.5 | 37.327 | -1.6990 | 2438029.5 | 37.381 | -2.3208 |
| 2437534.5 | 37.308 | -1.7080 | 2438039.5 | 37.405 | -2.3315 |
| 2437549.5 | 37.31s | -1.7149 | 2438049.5 | 37.422 | -2.3403 |
| 2437554.5 | 37.324 | -1.72.02 | 2438059.5 | 37.434 | -2.3514 |
| 2437569.5 | 37.370 | -1.7291 | 2438069.5 | 37.446 | -2.3651 |
| 2437579.5 | $37.3+0$ | -1.7401 | 2438079.5 | 37.467 | -2.3779 |
| 2437589.5 | 37.337 | -1.7509 | 2438089.5 | 37.492 | -2.3917 |
| 2437599.5 | 37.350 | $-1.7616$ | 2436099.5 | 37.505 | -2.4064 |
| 2437609.5 | 37.354 | $-1.7732$ | 2438109.5 | 37.507 | -2.4250 |
| 2437619.5 | 37.371 | -1.7866 | 2438119.5 | 37.509 | -2.4440 |
| 2437629.5 | 37.3n4 | -1.8011 | 2438129.5 | 37.51 .3 | -2.4638 |
| 2437639.5 | 37.390 | -1.8155 | 2438139.5 | 37.509 | -2.4835 |
| 2437649.5 | 37.349 | -1.8290 | 2438149.5 | 37.496 | -2.5040 |
| 2437659.5 | 37.426 | -1.8434 | 2438159.5 | 37.486 | -2.5249 |
| 2437669.5 | 37.443 | -1.8585 | 2438169.5 | 37.485 | -2.5436 |
| 2437679.5 | 37.476 | -1.8723 | 2438179.5 | 37.477 | -2.5609 |
| 2437684.5 | 37.347 | -1.8842 | 2438189.5 | 37.457 | -2.5767 |
| 2437699.5 | 37.3 HH | - 1.3 .3954 | 2438199.5 | 37.4 .35 | -2.5915 |



APPENIIX B
OTTAAA PLT（HSERVATIUNS 1956 TO 1970 10 DAY SMOOTHED VALIJES
jullan uay latituie vio－al julian uay latitude（ITO－AI

| 2438609.5 | 37.501 | －3．3099 | 2439104．5 | 37.299 | －4．3721 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2434019．5 | 37.4 mg | $-3.3225$ | 2439119.5 | 37.276 | －4．3958 |
| 2438629.5 | 37.415 | －3．3347 | 2439129.5 | 37.258 | －4．4181 |
| 2438639.5 | 37．4．39 | －3．3406 | 2439139.5 | 37.245 | －4．4399 |
| 2438649.5 | 37.406 | －3．3007 | 2439149．5 | 37.22 .3 | －4．4621 |
| 2438659.5 | 37．3xy | －3．3791 | 2439159.5 | 37.210 | －4．4873 |
| 2438069.5 | 37．35b | $-3.4002$ | 2439169.5 | 37.209 | －4．5127 |
| 2438619.5 | 37.316 | －3．4222 | 2.439179 .5 | 37.205 | －4．5357 |
| 24386859.5 | 37.274 | －3．4455 | 2439189.5 | 37.198 | －4．5．569 |
| 2438699.5 | 37.252 | －3．4682 | 2439194.5 | 37.191 | －4．5798 |
| 2438709.5 | 37.217 | －3．4897 | 2439209.5 | 37.204 | －4．6054 |
| 2438719.5 | 37.188 | －3．5109 | 2439219.5 | 37.231 | －4．6325 |
| 2438729.5 | 37.168 | －3．5323 | 2439229.5 | 37．243 | －4．6606 |
| 2438739.5 | 37．151 | －3．5526 | 2439739.5 | 37.256 | －4．6884 |
| 2438749.5 | 37.154 | －3．5722 | 2439249.5 | 37.267 | －4．7161 |
| く4387ちy．5 | 57．1ヶ7 | －3．5893 | 2439259.5 | 37．297 | －4．7431 |
| 2438709.5 | 37.113 | －3．6066 | 24.39269 .5 | 37.312 | －4．7692 |
| 2438779.5 | 37.144 | －3．6264 | 2439279.5 | 37.329 | －4．7934 |
| 2438789.5 | 37．2？ | －3．6474 | 2434249.5 | 37.343 | －4．8147 |
| 2438799.5 | 37.236 | －．3．6676 | 2439299.5 | 37.351 | －4．8349 |
| 2438809.5 | 37.227 | $-3.6882$ | 2439309.5 | 37.372 | －4．8．538 |
| 2438819.5 | 37.247 | －3．7189 | 2439319.5 | 37.405 | －4．8713 |
| 2438829.5 | 37.274 | $-3.7312$ | 2439329.5 | ． 37.436 | －4．8877 |
| 2438839.5 | 37.31 .3 | －3．7560 | 2439339.5 | 37.451 | －4．9057 |
| 2438849.5 | 37.342 | －3．7839 | 2439349.5 | 37.474 | －4．92．57 |
| 2438859.5 | 37.312 M | －3．8115 | 2439359.5 | 37.494 | －4．9467 |
| 2438889.5 | 37.349 | －3．8377 | 2439364.5 | 37.503 | －4．9680 |
| 2438819.5 | 37．409 | －3．8620 | 2439379.5 | 37.514 | －4．9917 |
| 2438859.5 | 37.414 | －3．8856 | 24393 H9．5 | 37.542 | －5．0172 |
| 2438849.5 | 37.4 .35 | －3．9086 | 2439399.5 | 37.535 | －5．0458 |
| 2438909.5 | 37．4h．1 | －3．9297 | 2.439409 .5 | 37.511 | －5．0750 |
| 2438919.5 | 37.444 | －3．9514 | 2439419.5 | 37.504 | －5．1047 |
| 2438929.5 | 37．525 | －3．9731 | 2439429.5 | 37.516 | －5．1333 |
| 24.36439 .5 | 37.514 | －3．9932 | 2439439.5 | 37.501 | －5．1629 |
| 2438449．5 | 37.543 | －4．0126 | 2439449.5 | 37.456 | －5．1904 |
| 2438959.5 | 37．5¢ | －4．0344 | 2439459.5 | 37.408 | －5．2161 |
| 2438964.5 | 37.574 | －4．0563 | 24394 ¢9．5 | 37.373 | －5．2．407 |
| 2438979.5 | 37.543 | －4．0713 | 2439479.5 | 37.358 | －5．2650 |
| 2438989.5 | 37.513 | －4．08344 | 2439489.5 | 37.348 | －5．2884 |
| 2438999.5 | 37.547 | －4．101H | 2439499.5 | 37.329 | －5．3109 |


|  | UTTANA | APPEN <br> ZTT OBSER 0 DAY SM | B <br> TIUNS 1956 TO HED VALUES | 1970 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| JULIAN UAY | LATI7UME | UTO-A1 | JULIAN JAY | LATITUUE | UTO-AI |
| 2439509.5 | 37.31 2 | -5. 3333 | 2440009.5 | 37.362 | -6.5615 |
| 2439519.5 | 37.317 | -5.3553 | 2440019.5 | $37.35 \%$ | -6.5851 |
| 2439529.5 | 37.294 | -5.3785 | 2440029.5 | 37.329 | -6.6074 |
| 2439539.5 | 37.271 | -5.4034 | 2440039.5 | 37.295 | -6.6280 |
| 2439549.5 | 37.268 | -5.4297 | 2440049.5 | 37.299 | -6.6457 |
| 2439554.5 | 37.26\% | -5.4565 | 2440059.5 | 37.307 | -6.6600 |
| 24.395 カ9. 5 | 37.271 | -5.4834 | 2440069.5 | 37.309 | -6.6742 |
| 2439519.5 | 37.261 | -5.5108 | 2440079.5 | 37.313 | -6.6931 |
| 2439584.5 | 37.255 | -5.5332 | 2440089.5 | 37.337 | -6.7175 |
| 2439599.5 | 37.262 | -5.5665 | 2440099.5 | 37.335 | -6.7424 |
| 2439609.5 | $37.27 \%$ | -5.5944 | 2440109.5 | 37.305 | -6.7655 |
| 2439619.5 | 37.2411 | -5.6218 | 2440119.5 | 37.298 | -6.1872 |
| 2439629.5 | 37.216 | -5.6486 | 2440129.5 | 37.292 | -6.8103 |
| 2439639.5 | 37.247 | -5.6739 | 2440139.5 | 37.282 | -6.4354 |
| 2439649.5 | 37.235 | -5.6965 | 24401.49 .5 | 37.272 | -6.8627 |
| 2434659.5 | 37.254 | -5.7167 | 2440159.5 | 37.286 | -6.8903 |
| 2439669.5 | 37.243 | -5.7349 | 2440169.5 | 37.290 | -6.9185 |
| 2434679.5 | 37.313 | -5.7521 | 2.440179 .5 | 37.295 | -6.9451 |
| 24396889.5 | 37.331 | -5.7682 | 2440189.5 | 37.311 | -6.9710 |
| 2439699.5 | 37.334 | -5.7829 | 2440199.6 | 37.32 .5 | -6.9962 |
| 2439709.5 | 37.3411 | -5.7977 | 2440209.5 | 37.327 | -7.0217 |
| 2439719.5 | 37.341 | -5.8153 | 2440219.5 | 37.328 | -7.0465 |
| 2439729.5 | 37.34.3 | -5.8345 | 2440229.5 | 37.334 | -7.0709 |
| 2439739.5 | 37.3n! | -5.8531 | 2440239.5 | 37.348 | -7.0952 |
| 2439749.5 | 37. उ\% ${ }^{\text {¢ }}$ | -5.8724 | 2440249.5 | 37.373 | -7.1211 |
| 2439759.5 | 37.401 | -5.8942 | 2440259.5 | 37.393 | -7.1495 |
| 2439764.5 | 37.384 | -5.9190 | 2440269.5 | 37.415 | -7.1788 |
| 2439779.5 | 37.376 | -5.9422 | 2440279.5 | 37.444 | -7.2078 |
| 2439789.5 | 37.378 | -5.9669 | 2440289.5 | 37.477 | -7.2379 |
| 2439799.5 | 37.384 | -5.9937 | 2440299.5 | 37.468 | -7.2705 |
| 2439809.5 | 37.367 | -6.0218 | 2440309.5 | 37.443 | -7.3030 |
| 2439819.5 | 37.338 | -6.0495 | 2.440319 .5 | 37.441 | -7.3.355 |
| 24.39829 .5 | 37.334 | -6.0763 | 2440329.5 | 37.462 | -7.3683 |
| 2439834.5 | 37.364 | -6.1027 | 2.440339 .5 | 37.491 | -7.4006 |
| 2439849.5 | 37.349 | -5.1288 | 2440349.5 | 37.506 | -7.4302 |
| $243985 \% .5$ | 37.344 | -6.1541 | 2440359.5 | 37.498 | -7.4607 |
| 2439869.5 | 37.34. | -6.1798 | 2440.369 .5 | 37.466 | -7.4915 |
| 2.439879 .5 | 37.348 | -6. 2054 | 2440379.5 | 37.460 | -7.5187 |
| 2439889.5 | 37.341 | -6.2308 | 2440389.5 | 37.461 | -7.5409 |
| 2439899.5 | 37.343 | -6.2564 | 2440399.5 | 37.457 | -7.5617 |


| APPENUIX H |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| OTTANA PZT UBSERVATIUNS 1956 to 1970 |  |  |  |  |  |
|  |  |  |  |  |  |
| JULIAN DAY | LATITUIE | UTO-A1 | Jul ian day | Latitude | UTO-AI |
| 2439909.5 | 37.312 | -6.2830 | 2440409.5 | 37.425 | -7.5833 |
| 2439919.5 | 37.350 | -6.3092 | 2440419.5 | 37.401 | -7.6045 |
| 2439929.5 | 37.3ヶカ | -6.3378 | 2440429.5 | 37.393 | -7.6259 |
| 2439939.5 | 37.311 | - ¢. 3625 | 2440439.5 | 37.409 | -7.6459 |
| 2439949.5 | 37.344 | -6.3869 | 2440449.5 | 37.401 | -7.6634 |
| 2439959.5 | 37.34 .3 | -6.4169 | 2440459.5 | 37.381 | -7.6820 |
| 2434969.5 | 37.409 | -6.457.2 | 2440469.5 | 37.353 | -7.7054 |
| 2439979.5 | 37.414 | -6.4831 | 2440479.5 | 37.340 | -7.7334 |
| 2439989.5 | 37.346 | -6.5105 | 2440499.5 | 37.322 | -7.7615 |
| 2439999.5 | 37.311 | -6.5373 | 2440499.5 | 37.308 | -7.7876 |
| 2440509.5 | 37.2 my | -7.8130 | 2440549.5 | 37.298 | -7.9258 |
| 2440519.5 | 37.284 | -7.8403 | 2440559.5 | 37.289 | -7.9536 |
| 2440529.5 | 37.293 | -7.8697 | 2440564.5 | 37.273 | -7.9801 |
| 2440539.5 | 37.248 | -7.8980 | 2440579.5 | 37.278 | -8.0085 |

APPENDIX C
COMPARISON WITH RIH REVISED
VALUES AT $1 / 20$ YEAR $1962-1970$

| EPOCH | D-PHI | U-LAMBOA | EPOCH | D-PHI | D-LAMBDA |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 62.00 | .235 | .0139 | 64.50 | . 064 | . 0128 |
| 62.05 | .173 | . 0164 | 64.55 | . 106 | . 0138 |
| 62.10 | .139 | . 0138 | 64.60 | .103 | . 0154 |
| 62.15 | .178 | .0158 | 64.65 | . 122 | . 0119 |
| 62.20 | .186 | .0129 | 64.70 | .134 | .0068 |
| 62.25 | .163 | .0136 | 64.75 | .131 | . 0087 |
| 62.30 | .140 | . 0129 | 64.80 | . 122 | . 0083 |
| 62.35 | .150 | . 0133 | 64.85 | .117 | .0112 |
| 62.40 | .118 | . 0154 | 64.90 | .111 | .0102 |
| 62.45 | .107 | .0154 | 64.95 | . 102 | .0103 |
| 62.50 | .093 | . 0111 | 65.00 | .123 | . 0074 |
| 62.55 | -123 | .0110 | 65.05 | . 152 | . 0097 |
| 62.60 | .109 | . 0155 | 65.10 | . 196 | . 0142 |
| 62.65 | .121 | .0162 | 65.15 | .138 | . 0144 |
| 62.70 | .117 | . 0118 | 65.20 | . 150 | . 0140 |
| 62.75 | .177 | . 0118 | 65.25 | .149 | .0136 |
| 62.80 | .168 | .0103 | 65.30 | .141 | . 0178 |
| 62.85 | .155 | .0128 | 65.35 | . 093 | .0183 |
| 62.90 | .150 | . 0139 | 65.40 | . 087 | . 0155 |
| 62.95 | .152 | .0161 | $65 \cdot 45$ | . 106 | . 0132 |
| 63.00 | .186 | . 0227 | 65.50 | . 095 | .0112 |
| 63.05 | . 185 | . 0171 | 65.55 | .101 | . 0134 |
| 63.10 | .139 | . 0183 | 65.60 | . 158 | . 0144 |
| 63.15 | .147 | .0194 | 65.65 | .111 | . 0064 |
| 63.20 | .152 | . 0196 | 65.70 | . 174 | . 0085 |
| 63.25 | . 098 | . 0189 | 65.75 | . 158 | . 0114 |
| 63.30 | . 0972 | .0179 | 65.80 | . 122 | . 0099 |
| 63.35 | . 077 | . 0180 | 65.85 | . 162 | .0081 |
| 63.40 | .060 | .0169 | 65.90 | .190 | . 0063 |
| 63.45 | . 073 | .0169 | 65.95 | .156 | . 0067 |
| 63.50 | . 05.3 | . 0173 | 66.00 | .149 | . 0082 |
| 63.55 | . 088 | .0213 | 66.05 | . 168 | .0067 |
| 63.60 | .111 | .0190 | 66.10 | . 159 | .0130 |
| 63.65 | .132 | .0147 | 66.15 | . 162 | . 0145 |
| 63.70 | .135 | . 0130 | 66.20 | .137 | . 0135 |
| 63.75 | .132 | .0097 | 66.25 | . 146 | .0146 |
| 63.80 | . 117 | . 0109 | 66.30 | . 129 | . 0156 |
| 63.85 | .084 | . 0085 | 66.35 | .119 | .0157 |
| 63.90 | .128 | -0093 | 66.40 | . 123 | . 0150 |
| 63.95 | -15.3 | . 0084 | 66.45 | .110 | . 0138 |


| APPENDIX C |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| COMPARISON WITH BIH REVISED |  |  |  |  |  |
|  | VALU | AT $1 / 20$ | YEAR 1962 - | 1970 |  |
| EPOCH | D-PHI | D-LAMEDA | EPOCH | D-PHI | D-LAMBDA |
| 64.00 | .126 | . 0092 | 66.50 | . 103 | . 0160 |
| 64.05 | .187 | . 0108 | 66. 55 | .109 | . 0133 |
| $64 \cdot 10$ | -180 | . 0114 | 66.60 | . 119 | . 0124 |
| 64.15 | .183 | . 0143 | 66.65 | .139 | . 0106 |
| 64.20 | . 169 | .0156 | 66.70 | .177 | .0091 |
| 64.25 | .174 | .0179 | 66.75 | .190 | .0087 |
| 64.30 | . 132 | . 0167 | 66.80 | . 155 | . 0082 |
| 64.35 | .141 | .0162 | 66.85 | . 205 | . 0091 |
| 64.40 | .146 | . 0199 | 66.90 | . 135 | . 0085 |
| 64.45 | . 104 | .0165 | 66.95 | .108 | .0102 |
| 67.00 | . 132 | .0091 | 68.50 | . 053 | . 0164 |
| 67.05 | . 116 | . 0098 | 68.55 | .065 | .0126 |
| 67.10 | .136 | .0051 | 68.60 | . 100 | . 0029 |
| 67.15 | . 111 | . 0092 | 68.65 | .186 | .0106 |
| 67.20 | -120 | .0121 | 68.70 | . 097 | .0106 |
| 67.25 | .091 | . 0139 | 68.75 | .138 | . 0065 |
| 67.30 | -103 | . 0154 | 68.80 | .115 | . 0103 |
| 67.35 | . 101 | . 0134 | 68.85 | .130 | . 0125 |
| 67.40 | .062 | . 0150 | 68.90 | .131 | . 0132 |
| 67.45 | . 042 | .0157 | 68.95 | . 152 | . 0111 |
| 67.50 | .093 | . 0141 | 69.00 | . 118 | . 0112 |
| 67.55 | .139 | .0156 | 69.05 | . 131 | .0098 |
| 67.60 | . 132 | .0113 | 69.10 | .109 | .0147 |
| 67.65 | . 148 | .0074 | 69.15 | .141 | . 0186 |
| 67.70 | .189 | .0075 | 69.20 | .166 | .0168 |
| 67.75 | .192 | . 0088 | 69.25 | .103 | .0176 |
| 67.80 | .140 | . 0081 | 69.30 | .112 | . 0179 |
| 67.85 | . 180 | . 0074 | 69.35 | .127 | .0155 |
| 67.90 | .103 | . 0052 | 69.40 | . 092 | .0171 |
| 67.95 | .109 | .0082 | 69.45 | .078 | .0184 |
| 68.00 | .195 | .0102 | 69.50 | .116 | . 0112 |
| 68.05 | .080 | .0002 | 69.55 | . 069 | . 0125 |
| 68.10 | . 114 | . 0022 | 69.60 | .155 | . 0154 |
| 68.15 | . 129 | . 0084 | 69.65 | .176 | . 0072 |
| 68.20 | .091 | .0097 | 69.70 | .174 | . 0100 |
| 68.25 | .135 | . 0065 | 69.75 | .163 | . 0155 |
| 68.30 | . 123 | .0145 | 69.80 | .175 | . 0064 |
| 68.35 | -127 | . 0154 | 69.85 | .192 | . 0098 |
| 68.40 | .102 | . 0181 | 69.90 | .191 | . 0083 |
| 68.45 | . 114 | . 0169 | 69.95 | .150 | .0092 |


| APPENOIX C |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | COMPARISON WITH BIH REVISEU day Smouthfo values 196¿-1970 |  |  |  |  |
|  |  |  |  |  |  |
| JULIAN UAY | D-PHI | U-LAMBDA | JULIAN DAY | D-PHI | D-LAMBDA |
| 2437669.5 | . 223 | . 0153 | 2438169.5 | . 070 | .0179 |
| 2437679.5 | . 191 | . 0164 | 2438179.5 | . 068 | .0167 |
| 2437689.5 | . 153 | . 0158 | 2438189.5 | . 062 | . 0159 |
| 2437699.5 | . 139 | . 0146 | 2438199.5 | . 062 | . 0158 |
| 2437709.5 | . 151 | . 0148 | 2438209.5 | . 064 | . 0164 |
| 2437719.5 | .177 | . 0151 | 2438219.5 | . 066 | . 0185 |
| 2437729.5 | .198 | . 0150 | 2438229.5 | . 078 | . 0207 |
| 2437739.5 | .190 | . 0133 | 2438239.5 | . 094 | . 0211 |
| 2437749.5 | .172 | . 0128 | 2438249.5 | . 109 | . 0202 |
| 2437759.5 | .155 | . 0134 | 2438259.5 | . 116 | .0170 |
| 2437769.5 | . 140 | . 0135 | 2438269.5 | . 119 | .0145 |
| 2437779.5 | . 148 | . 0125 | 2438279.5 | . 128 | . 0133 |
| 2437789.5 | . 147 | .0123 | 2438289.5 | . 134 | . 0122 |
| 2437799.5 | .135 | . 0125 | 2438299.5 | . 135 | . 0110 |
| 2437809.5 | .124 | .0129 | 2438309.5 | . 128 | .0096 |
| 2437819.5 | . 115 | . 0141 | 2438319.5 | . 117 | .0096 |
| 2437829.5 | .110 | . 0147 | 2438329.5 | . 097 | . 0089 |
| 2437839.5 | .101 | . 0146 | 2438339.5 | . 102 | .0083 |
| 2437849.5 | . 102 | .0127 | 2438349.5 | . 126 | . 0083 |
| 2437859.5 | . 117 | . 0112 | 2438359.5 | . 134 | . 0089 |
| 2437869.5 | . 122 | .0122 | 2438369.5 | . 135 | . 0087 |
| 2437879.5 | . 121 | . 0140 | 2438379.5 | . 140 | .0076 |
| 2437849.5 | .116 | . 0157 | 2438389.5 | . 129 | . 0080 |
| 2437899.5 | . 113 | .0161 | 2438399.5 | . 131 | . 0084 |
| 2437909.5 | . 108 | .0152 | 2438409.5 | . 156 | . 0096 |
| 2437919.5 | .123 | . 0140 | 2438419.5 | . 187 | . 0102 |
| 2437929.5 | . 151 | . 0129 | 2438429.5 | .182 | .0118 |
| 2437939.5 | .171 | . 0115 | 2438439.5 | . 180 | . 0127 |
| 2437949.5 | .177 | .0100 | 2438449.5 | . 177 | . 0135 |
| 2437959.5 | . 164 | . 0107 | 2438459.5 | . 170 | . 0138 |
| 2437969.5 | .156 | . 0119 | 2438469.5 | . 164 | .0155 |
| 2437979.5 | .150 | . 0126 | 2438479.5 | . 162 | . 0170 |
| 2437989.5 | . 148 | . 0136 | 2438489.5 | . 159 | .0174 |
| 2437999.5 | . 148 | . 0141 | 2438499.5 | . 145 | .0166 |
| 2438009.5 | .150 | . 0148 | 2438509.5 | . 139 | . 0158 |
| 2438019.5 | . 163 | .0177 | 2438519.5 | .137 | . 0159 |
| 2438029.5 | . 169 | . 0213 | 2438529.5 | . 142 | . 0168 |
| 2438039.5 | . 174 | . 0205 | 2438539.5 | . 141 | . 0187 |
| 2438049.5 | .171 | . 0184 | 2438549.5 | . 136 | . 0190 |
| 2438059.5 | . 159 | . 0178 | 2438559.5 | . 109 | . 0170 |

COMPARISON WITH RIH REVISEN 10 DAY SMOOTHED VALUES 1962-1970

| JULIAN DAY | D-PHI | D-LAMHDA | JULIAN DAY | D-PHI | D-LAMBDA |
| :--- | :---: | :---: | :---: | :---: | :---: |
| 2438069.5 | .143 | .0193 | 2438569.5 | .081 | .0141 |
| 2438079.5 | .143 | .0202 | 2438579.5 | .071 | .0123 |
| 2438089.5 | .153 | .0203 | 2438589.5 | .096 | .0134 |
| 2438099.5 | .151 | .0187 | 2438599.5 | .106 | .0152 |
| 2438109.5 | .135 | .0189 | 2438609.5 | .109 | .0162 |
| 2438119.5 | .118 | .0190 | 2438519.5 | .114 | .0151 |
| 2438129.5 | .105 | .0189 | 2438629.5 | .125 | .0136 |
| 2438139.5 | .091 | .0180 | 2438639.5 | .118 | .0101 |
| 2438149.5 | .078 | .0180 | 2438549.5 | .120 | .0076 |
| 2438159.5 | .071 | .0187 | 2438659.5 | .140 | .0072 |
| 2438669.5 | .143 | .0069 | 2439169.5 | .167 | .0144 |
| 2438679.5 | .124 | .0068 | 2439179.5 | .161 | .0155 |
| 2438689.5 | .121 | .0079 | 2439189.5 | .149 | .0146 |
| 2438699.5 | .124 | .0103 | 2439199.5 | .133 | .0140 |
| 2438709.5 | .115 | .0110 | 2439209.5 | .133 | .0137 |
| 2438719.5 | .111 | .0106 | 2439219.5 | .145 | .0140 |
| 2438729.5 | .109 | .0103 | 2439229.5 | .137 | .0151 |
| 2438739.5 | .096 | .0101 | 2439239.5 | .126 | .0160 |
| 2438749.5 | .104 | .0096 | 2439249.5 | .114 | .0158 |
| 2438759.5 | .123 | .0077 | 2439259.5 | .124 | .0152 |
| 2438769.5 | .135 | .0070 | 2439269.5 | .117 | .0149 |
| 2438779.5 | .160 | .0091 | 2439279.5 | .112 | .0147 |
| 2438789.5 | .191 | .0125 | 2439289.5 | .102 | .0140 |
| 2438799.5 | .188 | .0139 | 2439299.5 | .087 | .0146 |
| 2438809.5 | .159 | .0148 | 2439309.5 | .087 | .0153 |
| 2438819.5 | .148 | .0140 | 2439319.5 | .097 | .0155 |
| 2438829.5 | .157 | .0133 | 2439329.5 | .108 | .0143 |
| 2438839.5 | .164 | .0134 | 2439339.5 | .113 | .0140 |
| 2438849.5 | .161 | .0143 | 2439349.5 | .131 | .0135 |
| 2438859.5 | .152 | .0147 | 2439359.5 | .146 | .0128 |
| 2438869.5 | .138 | .0162 | 2439369.5 | .153 | .0108 |
| 2438879.5 | .117 | .0168 | 2439379.5 | .163 | .0091 |
| 2438889.5 | .094 | .0171 | 2439389.5 | .191 | .0083 |
| 2438899.5 | .079 | .0165 | 2439399.5 | .184 | .0094 |
| 2438909.5 | .083 | .0135 | 2439409.5 | .161 | .0096 |
| 2438919.5 | .095 | .0122 | 2439419.5 | .158 | .0099 |
| 2438929.5 | .107 | .0120 | 2439429.5 | .182 | .0093 |
| 2438939.5 | .101 | .0115 | 2439439.5 | .185 | .0101 |
| 2438949.5 | .093 | .0116 | 2439449.5 | .160 | .0092 |
| 2438959.5 | .106 | .0148 | 2439459.5 | .131 | .0081 |

APPENDIX C
COMPARISON WITH HIH REVISEU
10 DAY SMOOTHED VALUES 1962-1970
JULIAN DAY
$\mathrm{D}-\mathrm{PH}$
()-LAMBJA JULIAN DAY

| D-PHI | D-LAMBUA | JULIAN DAY | D-PHI | D-LAMBDA |
| :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |
| .125 | .0183 | 2439469.5 | .115 | .0097 |
| .157 | .0145 | 2439479.5 | .117 | .0100 |
| .152 | .0084 | 2439484.5 | .124 | .0104 |
| .143 | .0060 | 2439499.5 | .125 | .0102 |
| .159 | .0080 | 2439509.5 | .132 | .0099 |
| .179 | .0100 | 2439519.5 | .129 | .0092 |
| .171 | .0105 | 2439529.5 | .125 | .0090 |
| .147 | .0105 | 2439539.5 | .109 | .0098 |
| .134 | .0096 | 2439549.5 | .104 | .0109 |
| .130 | .0093 | 2439559.5 | .106 | .0118 |
|  | .0092 | 2439569.5 | .110 | .0124 |
| .145 | .0079 | 2439579.5 | .100 | .0134 |
| .156 | .0057 | 2439589.5 | .092 | .0142 |
| .166 | .0052 | 2439599.5 | .097 | .0151 |
| .174 | .0063 | 2439609.5 | .108 | .0143 |
| .170 | .0089 | 2439619.5 | .108 | .0130 |
| .167 | .0100 | 2439629.5 | .088 | .0134 |
| .169 | .0089 | 2439639.5 | .059 | .0148 |
| .174 | .0083 | 2439649.5 | .043 | .0154 |
| .166 | .0109 | 2439659.5 | .060 | .0153 |
| .163 | .0149 | 2440129.5 | .144 | .0057 |
| .087 | .0150 | 2440139.5 | .139 | .0048 |
| .108 | .0150 |  |  |  |
| .122 | .0150 | 2440149.5 | .141 | .0067 |
| .127 | .0136 | 2440159.5 | .163 | .0094 |
| .133 | .0112 | 2440169.5 | .173 | .0120 |
| .138 | .0101 | 2440179.5 | .177 | .0124 |
| .138 | .0095 | 2440189.5 | .185 | .0127 |
| .158 | .0093 | 2440199.5 | .178 | .0129 |
| .192 | .0088 | 2440209.5 | .155 | .0133 |
| .205 | .0092 | 2440219.5 | .134 | .0135 |
| .191 | .0094 | 2440229.5 | .118 | .0138 |
| .176 | .0082 | 2440239.5 | .109 | .0131 |
| .176 | .0065 | 2440249.5 | .115 | .0129 |
| .177 | .0065 | 2440259.5 | .120 | .0140 |
| .148 | .0072 | 2440269.5 | .128 | .0145 |
| .104 | .0069 | 2440279.5 | .141 | .0129 |
| .093 | .0073 | 2440289.5 | .162 | .0112 |
| .119 | .0083 | 2440299.5 | .137 | .0124 |
| .134 | .0099 | 2440309.5 | .100 | .0140 |
| .133 | .0103 | 2440319.5 | .088 | .0152 |
|  |  |  |  |  |
| 105 |  |  |  |  |

2438969.5
2438979.5
2438989.5
2438999.5
2439009.5
2439019.5
2439029.5
2439039.5
2439049.5
2439059.5
2439069.5
2439079.5
2439089.5
2439099.5
2439109.5
2439119.5
2439129.5
2439139.5
2439149.5
2439159.5
2439669.5 2439679.5 2439689.5 2439699.5 2439709.5 2439719.5 2439729.5 2439739.5 2439749.5 2439759.5
2439769.5 2439779.5 2439789.5 2439799.5 2439809.5 2439819.5 2439829.5 2439839.5 2439849.5 2439859.5

| APPENDIX C |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| JULIAN UAY | 10 | COMPARISON WTTH HIH REVISED day smoothed values 1962-1970 |  |  | D-LAMBDA |
|  |  |  |  |  |  |
|  | D-PHI | U-LAMBDA | JULIAN DAY | D-PHI |  |
| 2439869.5 | . 136 | . 0105 | 2440329.5 | . 102 | . 0155 |
| 2439879.5 | . 134 | . 0102 | 2440339.5 | . 126 | . 0153 |
| 2439889.5 | .125 | . 0095 | 2440349.5 | . 139 | . 0140 |
| 2439899.5 | .119 | .0091 | 2440359.5 | . 133 | . 0154 |
| 2439909.5 | .111 | . 0082 | 2440369.5 | . 105 | .0180 |
| 2439919.5 | .100 | . 0066 | 2440379.5 | . 105 | .0175 |
| 2439929.5 | .101 | . 0090 | 2440389.5 | . 115 | . 0136 |
| 2439939.5 | .119 | .0092 | 2440399.5 | . 121 | . 0104 |
| 2439949.5 | .135 | . 0095 | 2440409.5 | . 101 | . 0105 |
| 2439959.5 | . 143 | . 0080 | 2440419.5 | . 100 | . 0112 |
| 2439969.5 | . 156 | . 0129 | 2440429.5 | . 122 | . 0123 |
| 2439979.5 | .154 | . 0173 | 2440439.5 | . 173 | . 0124 |
| 2439989.5 | . 147 | .0198 | 2440449.5 | . 200 | .0100 |
| 2439999.5 | . 133 | . 0210 | 2440459.5 | . 209 | . 0075 |
| 2440009.5 | . 137 | .0196 | 2440469.5 | . 208 | .0081 |
| 2440019.5 | . 140 | . 0173 | 2440479.5 | . 209 | .0108 |
| 2440029.5 | . 122 | . 0184 | 2440489.5 | . 198 | . 0109 |
| 2440039.5 | . 096 | . 0212 | 2440499.5 | . 191 | . 0090 |
| 2440049.5 | .106 | . 0193 | 2440509.5 | .177 | . 0068 |
| 2440059.5 | .119 | . 0138 | 2440519.5 | .176 | .0061 |
| 2440069.5 | . 126 | . 0080 | 2440529.5 | . 189 | . 0066 |
| 2440079.5 | . 133 | . 0063 | 2440539.5 | . 199 | .0068 |
| 2440089.5 | .162 | . 0092 | 2440549.5 | . 200 | .0076 |
| 2440099.5 | . 165 | . 0114 | 2440559.5 | .189 | . 0083 |
| 2440109.5 | .141 | . 0109 | 2440569.5 | .170 | . 0077 |
| 2440119.5 | .143 | .0081 | 2440579.5 | .173 | . 0084 |



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magnetic anomaly maps of british columbia and the adjacent pacific ocean
G. V. HAINES and W. HANNAFORD

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217 Acknowledgments
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# magnetic anomaly maps of british columbia and the adjacent pacific ocean 

G. V. HAINES and W. HANNAFORD


#### Abstract

A three-component aeromagnetic survey of British Columbia and the northeastern Pacific Ocean was carried out in early 1969. The survey data are in the form of averages over 30 seconds of time, or roughly 3.5 km of flight track. The International Geomagnetic Reference Field (IGRF) was removed from these data, and the resulting residuals plotted as profiles. A 3rd-degree polynomial was fitted to the survey data by least-squares to determine how well the IGRF represents the average regional field over the survey area. The polynomial was also used to obtain vector residuals, which require a residual mean close to zero. Lines of zero gradient in the component parallel to the flight tracks are also given.


Résumé. Un relevé aéromagnétique à trois composantes de la Colombie-Britannique et du nord-est de l'océan Pacifique a été effectué au début de 1969. Les données obtenues se présentent sous forme de moyennes sur 30 secondes de temps, ou approximativement sur 3.5 km de ligne de vol. On a soustrait de ces données la valeur du champ geomagnétique international de réference (International Geomagnetic Reference Field - IGRF), et les données rédisuelles ont été tracées sous forme de profils. Un polynome du $3^{e}$ degré a été appliqué aux données du levé par la méthode des moindres carrés afin de vérifier dans quelle mesure la valeur de IGRF représente bien la valeur du champ régional moyen dans la région étudiée. Le polynome a également servi à obtenir des données résiduelles de vecteurs, ce qui demande une moyenne résiduelle située près de zéro. On donne également les lignes de gradient zéro dans la composante parallèle aux lignes de vol.

## Introduction

In 1969, between January 26 and March 20, the Dominion Observatory (now the Earth Physics Branch), Department of Energy, Mines and Resources, carried out a three-component aeromagnetic survey of British Columbia and the northeastern Pacific Ocean. An index map of the survey area is shown in Figure 1. The aircraft used was a DC 6 , chartered from Pacific Westem Airlines. The fluxgate magnetometer and direction-reference system have been described by Serson, et al. (1957) and Hannaford, et al. (1967).

The total number of line-kilometres flown was approximately 90,000 (of which about 15,000 were ferry and calibration flights) and the area covered was $3.4 \times 10^{6}$ square kilometres. The average flight-line spacing was 37 km ( 20 naut. mi.) over British Columbia and 74 km ( 40 naut. mi.) over the adjacent ocean. Flight altitudes ranged from 4.6 to 6.8 km , the average altitude being 5.5 km .

## The data

A gyro-stabilized fluxgate magnetometer produced values of the declination D , the horizontal intensity H , and the
vertical intensity Z. A Barringer OM-104 proton precession magnetometer measured the total field F. Because of the high accuracy of the proton magnetometer the fluxgate measurements of Z were discarded whenever H and F were available, and a new Z was calculated. This was possible because the error in Z resulting from an error in H is proportional to $\mathrm{H} / \mathrm{Z}$, and for the survey area this ratio was only about 0.3. The analysis of the aircraft fields, altitude corrections to sea level, and a discussion of various other problems will be given by Hannaford and Haines (1972).

## Representation of the anomaly field

An anomaly field was obtained by subtracting from the $1 / 2$-minute average values of the International Geomagnetic Reference Field (IGRF). This spherical harmonic reference field has been described by the International Association of Geomagnetism and Aeronomy Commission 2 Working Group 4 (1969). Means and standard deviations of the differences, or residuals, are given in Table I. They are, however, not too meaningful.

To see how well the IGRF represents the average regional field over the survey
area a 3 rd-degree polynomial was fitted, in three orthogonal components, to 5 -minute averages of the survey data. The coefficients of this polynomial and the appropriate formulas for their use are given in Table II. Means and standard deviations for the differences between the $1 / 2$-minute averages and the 3 rd -degree polynomial are given in Table III. The means of Table III are not exactly zero because not every $1 / 2$-minute average forms part of a 5 -minute average. The sample size used in Table I is larger than that used in Table III because many of the observations lie outside the main survey area to which the polynomial was fitted.

The 3rd-degree polynomial of Table II was subtracted from the IGRF, and the resulting difference field was contoured in Figure 2 for the geographic north component $\mathbf{X}$, the geographic east component $Y$, the vertical downward component Z , the declination D , the horizontal intensity H , and the total force F . It is immediately evident that the IGRF does not accurately represent the average field over the region. This is particularly noticeable in the case of Z and F where there is a feature approximately 2000 km in wavelength and over $300 \gamma$ in amplitude which is not present in the IGRF. (Indeed, the lowest wavelength which can be represented in a spherical harmonic expansion of degree 8 is 5000 km .) The horizontal components of the IGRF seem to fit much better, with differences generally being less than $100 \%$.

Figure 2 shows why the means and standard deviations of Table I are not very meaningful. When the residuals in one quarter of the survey area, for example, differ systematically from the residuals in another quarter, the over-all mean has little significance. It could be made to equal zero by choosing appropriate boundaries for the survey area. The
over-all standard deviation is also misleading, since it is affected by the nonzero regional means and depends on the choice of the survey boundaries. This demonstrates a basic difficulty in specifying the goodness of fit of a smooth reference field, such as the IGRF, to survey data from an area even as large as several million square kilometres.

Although it is felt the 3rd-degree polynominal field of Table II would be a much better reference field than the IGRF, in that much smaller wavelengths (in this case, of appreciable amplitude) can be represented, it was decided to use the IGRF for plotting residual profiles (Figures 3-8). The IGRF was favoured because it is an international standard, and residuals from any other overlapping survey can be compared directly with those of this survey if they too are derived from the IGRF. This of course was one of the main reasons for the adoption of an international reference field. For deriving and plotting residual vectors (Figures 9.10), however, the polynomial reference field was used since zero means in all components are necessary. For the zero-gradients of Figure 11 the IGRF was used.

The $1 / 2$-minute residuals were plotted, in Figures 3-11, on a Lambert conformal conic map with standard parallels $37^{\circ}$ and $65^{\circ} \mathrm{N}$ and convergence 0.785 . The flight lines are parallel to the Greenwich meridian so this direction was chosen as the $x$-axis of the map. The $y$-axis is then parallel to $90^{\circ}$ divided by the convergence, or $114^{\circ} 36^{\prime} \mathrm{W}$ on the map.

In Figures 3-8, the IGRF subtracted residuals were plotted in profile form, parallel to the $y$-axis. A residual was plotted toward the top of the map when positive and toward the bottom when negative. The polynomial-subtracted residuals were represented as two-dimensional vector residuals in the horizontal plane (Figure 9) and in a vertical plane parallel to the $x$-axis (Figure 10). Their directions follow the same convention as those of the profiles: positive components of the residual vector are plotted toward the top of the map, negative components toward the bottom.

Table I. Means and standard deviations of the observed minus IGRF field

|  | D | H | X | Y | Z | F |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
|  |  |  |  |  |  |  |
| Sample size | 20679 | 20679 | 20679 | 20679 | 20690 | 20694 |
| Mean | $-.06^{\circ}$ | $45 \gamma$ | $46 \gamma$ | $1 \gamma$ | $126 \gamma$ | $137 \gamma$ |
| Standard deviation | .52 | 144 | 143 | 142 | 182 | 168 |

Table II. 3rd-degree polynomial reference field from least-squares fit of survey data

$$
\left.\begin{array}{ll}
\theta=\text { colatitude } & \lambda=\text { east longitude } \\
a & =-\tan (\theta / 2) \cos \left(\lambda+117^{\circ}\right)+.3072 \\
b & =\tan (\theta / 2) \sin \left(\lambda+117^{\circ}\right)+.0709
\end{array} \quad \begin{array}{rl}
U & =\sum_{1}^{10} u_{i} x_{i}
\end{array} \quad V=\sum_{1}^{10} v_{i} x_{i} \quad Z=\sum_{1}^{10} z_{i} x_{i}\right)
$$

| $i$ | $x_{i}$ | $u_{i}$ | $v_{i}$ | $z_{i}$ |
| ---: | :--- | ---: | ---: | ---: |
| 1 | 1 | $1.2239+4$ | $1.0364+4$ | $5.5262+4$ |
| 2 | a | $-6.2556+4$ | $-1.0855+4$ | $3.7613+4$ |
| 3 | b | $-6.5451+3$ | $-6.1180+4$ | $5.6891+4$ |
| 4 | $\mathrm{a}^{2}$ | $6.3980+3$ | $-4.9853+4$ | $-1.7066+5$ |
| 5 | 2 b | $-1.4139+5$ | $-4.8740+4$ | $-4.6326+4$ |
| 6 | $\mathrm{~b}^{2}$ | $-2.7125+4$ | $-6.1475+4$ | $-1.2595+5$ |
| 7 | $\mathrm{a}^{3}$ | $4.3951+5$ | $1.4481+5$ | $-2.0118+5$ |
| 8 | $\mathrm{a}^{2} \mathrm{~b}$ | $-1.6407+5$ | $-9.0320+4$ | $-7.1641+5$ |
| 9 | $\mathrm{ab}^{2}$ | $-9.2440+4$ | $6.1401+4$ | $-1.9050+5$ |
| 10 | $\mathrm{~b}^{3}$ | $7.4499+4$ | $1.1052+5$ | $-2.3696+5$ |

Note: Coefficients are in floating-point notation, a decimal fraction followed by a power of ten.
Table III. Means and standard deviations of the observed minus polynomial field

|  | D | H | X | Y | Z | F |
| :--- | :---: | :---: | :---: | :---: | :---: | ---: |
| Sample size | 19751 | 19751 | 19751 | 19751 | 19791 | 19795 |
| Mean | $.00^{\circ}$ | $-2 \gamma$ | $-3 \gamma$ | $0 \gamma$ | $1 \boldsymbol{\gamma}$ | $0 \boldsymbol{\gamma}$ |
| Standard deviation | .48 | 134 | 130 | 135 | 144 | 136 |

Figure 11 shows contour-segments of the residuals of the geomagnetic component in the direction of the $x$-axis. Suppose this component is called $\mathbf{X}^{\prime}$ and the component in the $y$-direction is called $Y^{\prime}$. Their respective residuals will be called $\Delta X^{\prime}$ and $\Delta Y^{\prime}$. Then, since the flight lines lie parallel to the $x$-axis the partial gradients $\partial\left(\Delta X^{\prime}\right) / \partial x$ and $\partial\left(\Delta Y^{\prime}\right) / \partial x$ are both known. If the field is derivable from a potential, $\partial\left(\Delta X^{\prime}\right) / \partial y=\partial\left(\Delta Y^{\prime}\right) / \partial x$, and the gradient of $\Delta X^{\prime}$ is given by

$$
\operatorname{grad}\left(\Delta X^{\prime}\right)=\frac{\partial\left(\Delta X^{\prime}\right)}{\partial x} \mathbf{i}+\frac{\partial\left(\Delta X^{\prime}\right)}{\partial y} \mathbf{j}
$$

$$
=\frac{\partial\left(\Delta X^{\prime}\right)}{\partial x} \mathbf{i}+\frac{\partial\left(\Delta Y^{\prime}\right)}{\partial x} \mathbf{j}
$$

where $\mathbf{i}$ and j are unit vectors in the $x$ and $y$ directions, respectively. Rotating this gradient vector $90^{\circ}$ counterclockwise gives the vector plotted in Figure 11:
contour - segment

$$
=-\frac{\partial\left(\Delta Y^{\prime}\right)}{\partial x} i+\frac{\partial\left(\Delta X^{\prime}\right)}{\partial x} j
$$

These contour-segments give the direction of the contour lines of $\Delta \mathbf{X}^{\prime}$ as they intersect the flight lines.

When the distance between adjacent flight tracks is much larger than the distance between successive measurements on the tracks themselves, the con-tour-segments give additional information about the behaviour of $\Delta \mathrm{X}^{\prime}$ between the flight lines. The method, in fact, is equivalent to an extrapolation (or continuation) of the field beyond the actual point of measurement. The advantage of this representation is that linear and other trends, and changes in trends, are immediately apparent.

A contoured Z-residual map, comparable to Figure 7, has been published by Haines, et al. (1971), with an interpretation in terms of geology and tectonics.

## Acknowledgments

The authors wish to thank student assistants J.A. Dunn, D.G. Smith and L.J. Watts for scaling $1 / 2$-minute averages of $\mathrm{D}, \mathrm{H}$ and F from the strip-chart records and preparing the data for computer analysis; and Dr. P.H. Serson for his help and guidance and also for reviewing the manuscript.

The data were collected by Dominion Observatory personnel F. Andersen, G.L. Carr and the authors.

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Figure 1. Flight lines of the British Columbia-northeastern Pacific Ocean aeromagnetic survey, 1969. Flight numbers are circled and arrowheads indicate direction of travel.


Figure 2. Comparison of International Geomagnetic Reference Field (IGRF) with 3rd-degree polynomial (POL). Declination $D$ is in degrees; all other components are in gammas.


Figure 3. Residual profiles of the geographic north component of the earth's magnetic field, relative to the International Geomagnetic Reference Field (IGRF). A residual is an observed value minus the reference-field value.


Figure 4. Residual profiles of geographic east component, relative to the IGRF.


Figure 5. Residual profiles of vertical downward component, relative to the IGRF.


Figure 6. Residual profiles of declination, relative to the IGRF.


Figure 7. Residual profiles of horizontal intensity, relative to the IGRF.


Figure 8. Residual profiles of total force, relative to the IGRF.


Figure 9. Projection of total residual vector onto horizontal plane. Residual vector is taken relative to 3rd-degree polynomial of Table II.


Figure 10. Projection of total residual vector onto vertical plane parallel to $x$-axis (from left to right, in figure). Residual vector relative to 3 rd-degree polynominal.








$+0,4040$
过
-
4-4, +1
49

Figure 11. Contour line segments of the magnetic component parallel to the $x$-axis (from left to right, in figure). Rotating line segments $90^{\circ}$ clockwise would give gradient vector.

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J.-L. ROY, E. SANDERS et J. REYNOLDS

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Ottawa, 1972 $\mathbf{N}^{0}$ de Cat.: M70-42/8F

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235 Contrôle de température d) et g)
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236 Rendement
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# un four électrique pour l'étude des propriétés magnétiques des roches 

J.-L. ROY, E. SANDERS et J. REYNOLDS

Résumé. Les auteurs décrivent la construction, les caractéristiques et le fonctionnement d'un four électrique (diamètre: 30.5 cm , hauteur: 20.3 cm ), et font état des matériaux «non magnétiques» employés à sa construction. Le four peut recevoir 120 échantillons cylindriques (diamètre: 2.5 cm , hauteur: 2.2 cm ) dans un champ magnétique d'intensité $<6 \gamma$ dont 45 dans un champ d'intensité $<1 \gamma$. Le champ magnétique et la température sont contrôlés automatiquement.

Abstract. The construction, characteristics, and performance of an electric oven (diameter 30.5 cm , height 20.3 cm ) are described. The "non-magnetic" materials used are discussed. The oven can accommodate 120 cylindrical samples (diameter 2.5 cm , height 2.2 cm ) within a magnetic field $<6 \gamma ; 45$ of which are within a field $<1 \gamma$. The magnetic field and the temperature are controlled automatically.

## Introduction

Depuis nombre d'années, les chercheurs sur les propriétés magnétiques des roches ou des terres cuites font amplement usage de traitements thermiques. Entre autres, les travaux pratiques de Thellier (1938) et de Thellier et Thellier (1959) et les travaux théoriques de Néel (1955) ont beaucoup contribué à l'étude de certaines lois d'aimantation des roches. Ainsi, il a été démontré que lorsqu'une roche est laissée à refroidir dans l'intervalle de température $T_{1}$ et $T_{2}\left(T_{1}>T_{2}\right)$, situé entre le point de curie $\left(\mathrm{T}_{\mathrm{c}}\right)$ le plus élevé de ses constituants et $\mathrm{T}_{20}=20^{\circ} \mathrm{C}$, elle acquiert une aimantation thermorémanente partielle (ATRP) d'intensité proportionnelle à celle du champ magné. tique ambiant si celuinci est faible; les directions du champ ambiant et de l'ATRP sont habituellement parallèles. Cette ATRP restera imperméable à tout réchauffement inférieur à $\mathrm{T}_{2}$, mais pourra être remplacée totalement, ou en partie, par une nouvelle ATRP par un réchauffement à température $T \geqslant T_{2}$, où $T_{2}<T$ $<T_{1}$, et un refroidissement subséquent. Il en sera ainsi pour chaque intervalle $\mathrm{T}_{2}$ $-T_{3}-\ldots T_{n}$ compris entre $T_{c}$ et $T_{20}$. La somme vectorielle des aimantations de tous ces intervalles constitue l'aimantation thermorémanente dite totale (ATR).

Une ATR peut donc être simple ou composée suivant que la roche a refroidi dans un champ constant ou non. Ainsi, une roche qui, à la suite d'un refroidis-
sement initial à partir de $T_{c}$, a été soumise à un réchauffement jusqu'à $\mathrm{T}<$ $T_{c}$ et à un refroidissement dans un champ différent du premier possédera deux aimantations bien distinctes. Heureusement, grâce à la propriété de la roche de retenir à quelle température chaque ATRP a été acquise, il reste possible, dans bien des cas, de retracer l'évolution de l'aimantation fossile de telle ou telle roche. Pour y parvenir, il s'agit de soumettre la roche à des réchauffements progressifs et à des refroidissements en champ magnétique connu. De cette façon, on efface une aimantation inconnue pour la remplacer par une ATRP acquise dans des conditions connues. En comparant les vecteurs précédant et suivant le traitement thermique, on peut alors déterminer le vecteur de cette aimantation inconnue. Une telle comparaison de vecteurs est de beaucoup simplifiée si le traitement thermique a lieu en champ nul puisque alors on n'a fait qu'effacer l'aimantation fossile sans la remplacer par quoi que ce soit; une simple soustraction de vecteurs est donc suffisante. Afin de profiter de cette simplification dans l'analyse des résultats, il est donc avantageux d'effectuer les traitements thermiques en champ nul.

Le but principal de l'étude de l'aimantation des roches est d'identifier les aimantations contenues dans la roche et d'isoler une aimantation qui peut donner des renseignements sur la direction et
l'intensité du champ magnétique terrestre ancien.

Cette méthode systématique de traitements thermiques peut aider à atteindre ce but. Ainsi, un réchauffement à basse température permet d'éliminer toute aimantation visqueuse ou de trainage (AVR) que la roche peut avoir acquis récemment. Un réchauffement à $\approx 100^{\circ} \mathrm{C}$ (Thellier et Thellier, 1959) est habituellement suffisant pour éliminer ces aimantations parasites. Des réchauffements à températures plus élevées (de $100^{\circ}$ à $500^{\circ} \mathrm{C}$ ) permettent de déceler d'autres aimantations qui peuvent être à la fois des AVR et des ATRP et qui ont été acquises au cours d'une longue période à température basse ou modérée comme dans le cas de roches qui peuvent avoir été enfouies pendant un certain temps. Par ce procédé d'élimination, on peut arriver à isoler une aimantation qui persiste jusqu'au point de curie. En effectuant d'autres tests (de plissement par exemple), il est souvent possible de déterminer à quelle période de l'évolution de la roche l'aimantation appartient. Il n'est donc point surprenant que la désaimantation thermique soit devenue une technique de base pour les recherches archéo- et paléo-magnétiques.

## Construction d'un four

Un four est d'autant plus empluyé et conforme aux besoins requis qu'il répond aux exigences suivantes:
a) avoir un refroidissement rapide, une longue existence, une grande capacité et être facile d'accès
b) opérer en champ nul
c) atteindre au moins $700^{\circ} \mathrm{C}$
d) être prêcis en température absolue
e) avoir une température uniforme
f) exiger peu de surveillance
g) pouvoir garder la température et le champ constants pendant de longues périodes.


Figure 1. Le four électrique.

En a) le refroidissement rapide est nécessaire afin d'éviter les changements chimiques qui pourraient être causés en gardant longtemps l'échantillon à une température élevée; sa grande capacité est indispensable afin de désaimanter plusieurs échantillons simultanément tout en les espaçant suffisamment pour prévenir des interactions magnétiques. L'exigence g) est afin de pouvoir effectuer des expériences en conditions connues. Si l'on espère pouvoir identifier
certaines aimantations, il peut être nécessaire de reproduire certaines conditions.

Le four a donc été construit afin d'approcher le plus possible ces conditions idéales. La façon avec laquelle chacune des exigences a été traitée est indiquée dans l'étude par la lettre correspondante.

## Description du four a) et b)

Le four (fig. 1 et 2) est du type mobile qu'on peut élever et abaisser
(Irving et coll., 1961). De cette façon, les échantillons refroidissent beaucoup plus rapidement que dans le cas des fours fixes. L'accès aux échantillons est facile et si le four est quelque peu aimanté, le champ magnétique transmis aux échantillons sera d'autant plus petit que la distance est plus grande.

L'intérieur du four est constitué d'un tube d'alumine de 30.5 cm de diamètre intérieur, de 20.3 cm de haut, de 1.8 cm d'épaisseut, et fermé en haut. Le fil de


Figure 2. Dessin schématique du four.


Figure 3. Tablettes et supports d'alumine. La thermo-sonde apparaft au centre.
chauffage a été placé autour du tube et cimenté en 56 rangées, espacées de 1.9 cm et paralleles à l'axe du four selon la méthode de Thellier (1938). Le courant de chauffage qui circule par une rangée revient donc par la rangée adjacente. Ainsi, des champs égaux et opposés tendent à se compenser mutuellement. Un deuxième tube d'alumine, d'un diamètre intérieur de 35.6 cm et de 1.3 cm d'épaisseur, entoure le calorifere afin de maintenir les rangées en place. Les extrémités du double tube sont scellées avec du ciment afin d'eviter tout contact avec l'air environnant et prolonger ainsi l'existence du calorifère. Des briques réfractaires de 115 cm d'épaisseur entourent le double tube; l'isolant du dessus est formé d'une épaisseur de 19 cm de briques. Le double tube et l'isolant reposent sur un anneau formé de briques, aux dimensions de 20 cm de haut et de 15 cm de large. Une feuille d'aluminium supportée par un anneau d'aluminium de 1.3 cm d'épaisseur entoure l'ensemble. Six supports d'aluminium ( $1.9 \times 3.8 \mathrm{~cm}$ ) encastrés et vissés dans l'anneau inférieur et la plaque supérieure ( 1.3 cm d'épaisseur) relient le poids à cette dernierre qui est soulevée à l'aide d'une corde de nylon ( 1.3 cm de diamètre).

Le four est contrebalancé par un poids égal ( 143 kg ) de plomb et l'ascension et la descente peuvent être accomplies sans heurts au moyen d'une manivelle (fig. 1). Le déplacement est guidé par trois piliers ( 3.8 cm de diamètre) et des coussinets de nylon rendent l'opération plus régulière. Quatre tablettes d'alumine (fig. 3) de 28 cm de diamètre et de 1.0 cm d'épaisseur peuvent être superposées; le four peut alors recevoir 120 échantillons ( 2.5 cm de diamètre et 2.2 cm de haut) tout en maintenant une distance minimum de 2.5 cm entre eux.

## Champ nul b)

Pour obtenir un espace où le champ magnétique est «pratiquement» nul, il faut: 1) réduire ou compenser le champ magnétique terrestre; 2) n'employer que des matériaux à très faible teneur magnétique dans la construction du four et de ses accessoires. En employant un
matériau à haute perméabilité, tel que du mumétal, dans la construction d'un bouclier magnétique, il est possible de réduire la majeure partie du champ magnétique terrestre. Ainsi, Patton (1967) rapporte qu'à l'intérieur d'une chambre cubique en mumétal de 244 cm de côté un champ magnétique de $50,000 \gamma$ est réduit à $35 \gamma$. A l'aide d'un champ compensateur, le champ magnétique résiduel peut être maintenu à quelques $\gamma$ près de zéro. Dans le cas présent, cependant, un gros four dans un local clos est peu pratique en raison de la chaleur dégagée.

Une compensation du champ terrestre est obtenue en produisant un champ dans le sens contraire de manière que les deux
champs magnétiques soient égaux et opposés. Une pratique très courante d'effectuer cette compensation est d'employer trois paires de bobines placées orthogonalement de façon à compenser pour chacune des trois composantes du champ magnétique terrestre: vertical ( Z ), horizontal nord-sud magnétique ( $\mathrm{H}_{\mathrm{H}}$ ) et horizontal est-ouest magnétique ( $\mathrm{H}_{\mathrm{D}}$ ). Les bobines peuvent être circulaires (type helmholtz, Chapman et Bartels, 1940) ou à section carrée (Parry, 1967). Ce dernier type de bobines ( 244 cm de côté) est celui que nous employons pour compenser le champ magnétique au four.

Ces bobines (fig. 1) font partie d'un réseau de cinq ensembles identiques au centre desquels le champ magnétique est
compensé automatiquement à $1 \gamma$ près ( $2 \gamma$ lors d'un orage magnétique) (Roy et coll., 1969); la compensation étant effectuée à l'aide d'un système de solénoides à noyau saturable placé au centre de l'un des ensembles.

Un troisième enroulement de fil sur chaque bobine permet de créer et de maintenir des champs magnétiques constants de 0 à 1 oersted dans n'importe quelle direction g ).

## Uniformité du champ

Le champ magnétique résiduel à l'intérieur et autour du four est montré graphiquement à la figure 4. Les courbes ont été calculées d'après les équations données par Parry (1967) et en prenant


Figure 4. Champ magnétique résiduel (vertical et horizontal) à partir du centre des bobines. Les dimensions du four sont indiquées par des lignes verticales.
les valeurs locales 0.56 oe pour $Z$ et 0.15 oe pour $H_{H}\left(H_{D}=0\right)$. Les points expérimentaux ont été mesurés par W.A. Robertson et E. Irving à l'aide d'un appareil millioersted dont la résolution est de $1 \gamma$. Les points experimentaux ont tendance à être un peu plus petits que ceux de la courbe calculée. Ceci est probablement dû au fait que la sonde à double tête (deux solénoides de 3.5 cm espacés de 2 cm ) de l'appareil mesure le champ magnétique dans un volume fini et non pas à un point précis.

La compensation de Z est évidernment moins uniforme que celle de $\mathrm{H}_{\mathrm{H}}$ puisque Z est quatre fois plus grand. En même temps, la compensation est meilleure transversalement qu'axialement. Il s'ensuit que le four a été construit plus large que haut afin de bénéficier du plus petit champ résiduel possible. Lorsque le four est utilisé à pleine capacité, tous les échantillons se trouvent dans un champ $<6 \gamma$. En employant trois tablettes et la moitié de la surface (fig. 4, partie droite),

45 échantillons espacés de 2.5 cm peuvent être placés dans un champ $\leqslant 1 \gamma$.

## Matériaux employés b)

Le champ magnétique maximum transmis à un échantillon par le moment magnétique $A$ d'un constituant du four peut être exprimé ainsi

$$
H=2 A / x^{3}=2\left(A_{R}+A_{S}\right) / x^{3} \ldots 1
$$

où $x$ est la distance entre l'échantillon et le matériau magnétique, $A_{R}$ est l'aimantation rémanente du matériau et $A_{S}$ est l'aimantation causée par le champ magnétique $F$ agissant sur ce matériau; $A_{S}$ est donc égal à $\chi \mathrm{F}$ où $\chi$ est la susceptiblité du matériau. L'emploi de matériaux diamagnétiques ou paramagnétiques suffit à rendre négligeable le deuxième énoncé de l'expression ( $2 \times \mathrm{F} / \mathrm{x}^{3}$ ). En effet, la susceptibilité de ces matériaux est de l'ordre de $1 \sigma^{5}-1 \sigma^{6}$ u.é.rn. Toutes les parties du four se trouvent dans un
champ faible ( $1 \sigma^{5}-1 \sigma^{3} \mathrm{oe}$, fig. 4) et, sauf pour les tablettes, $x$ est de plusieurs centimètres. Le champ magnétique causê par $\mathbf{A}_{\mathbf{S}}$ est donc extrémement faible, soít $\leqslant 1 \sigma^{10} \propto e$. L'x des tablettes où reposent les échantillons est petit étant de 0 à 2.2 cm ; cependant $\chi=1 \times 1 \sigma^{7}$ u.é.m. et $\mathrm{F} \leqslant$ $6 \times 10^{5}$ oe (fig. 4) et, en conséquence, le champ magnétique sur l'ensemble de l'échantillon est faible; par exemple, ad centre de l'échantillon ( $x=1.1 \mathrm{~cm}$ ), le champ magnétique causé par $\mathrm{P}^{\prime} \mathrm{A}_{\mathrm{S}}$ des tablettes est $5 \times 1 \sigma^{12}$ oe et même à une distance de 1 mm , il n'est que $6 \times 10^{9}$ oe.

Dans la construction, on s'est limité à l'emploi des matériaux suivants: aluminium, alumine, briques refractaires, mortier, nylon, platine, laiton et nichrome. L'aimantation rémanente d'échantillons de chacun de ces matériaux a été mesurée à l'aide d'un magnétomètre astatique. Les deux demiers matériaux ont démontré une aimantation plus prononcée que les autres. Leur effet est décrit ci-dessous.

CIRCUIT DE CHAUFFAGE - HEATING CIRCUIT


Figure 5. Circuit de chauffage.

Élément de chauffage et composante magnétique b) et c)

On a utilisé un fil de nichrome ( 80 Ni , 20 Cr , tophet A, de calibre $\mathrm{n}^{0} 14 \mathrm{~B}$ et S , 0.163 cm de diamètre, voir Information). Long de 1.14 m , il a une résistance de 7.3 ohms à $20^{\circ} \mathrm{C}$ et 7.75 à $700^{\circ} \mathrm{C}$. Sur un circuit de 117 V.A.C., le courant, qui au
départ est de 16 A, est réduit sous l'effet du chauffage à 15 A qui donnent alors 1,750 W. Le point de fusion de cet alliage est $\simeq 1,400^{\circ} \mathrm{C}$. Du fait que le fil est encastré dans une masse d'alumine dont la conductivité thermique est bonne, la différence de température entre l'élément et le four demeure en principe petite.

Un alliage de nichrome peut être plus ou moins aimanté. L'aimantation rémanente de plusieurs échantillons de ce tophet A nichrome a donc été mesurée. La valeur moyenne du moment magnétique par cm de longueur est de $1.1 \times 1 \sigma^{8}$ u.ém. (l’aimantation la plus grande étant $2 \times 1 \sigma^{-3}$ u.e.m.). La plus proche distance
(d) qu'un échantillon puisse être d'une rangee verticale de fil est de 3 cm . Le champ magnétique maximum ( h ) que ce fil peut transmettre à l'echantillon est

$$
h=2 m \ell d /\left(d^{2}+l^{2}\right)^{2} \ldots 2
$$

où $\mathrm{m}=$ moment $/ \mathrm{cm}$ de fil $\mathrm{n}^{0} 14, \ell=$ longueur, $h$ est alors égal à $1.4 \times 1 \sigma^{-9}$ oe. Si l'on y additionne les champs magnétiques transmis par les fils des rangées adjacentes et en supposant toutes ces aimantations dirigées dans le méme sens, h maximum est encore $<1 \times 1 \sigma^{8} \mathrm{oe}$. Ce nichrome donne donc une intensité (moment/volume) moyenne de $1.3 \times 1 \sigma^{7}$ u.é.m., ce qui est moindre que l'intensité du laiton commercial qui varie beaucoup, d'après nos mesures, autour de $2 \times 10^{-5}$ u.e.m.

L'emploi du laiton a été limité aux boulons qui servent à fixer les différentes parties du four. Bien que l'intensité de cet alliage soit relativement forte, le champ produit à l'intérieur du four sera négligeable si on prend soin de choisir les boulons les moins aimantés $\left(<2 \times 1 \sigma^{5}\right.$ u.ém.). En effet, les plus gros boulons ont $1.1 \mathrm{~cm}^{3}$ et la distance de n'importe quelle partie du four est $>20 \mathrm{~cm}$. Donc, le champ magnétique transmis par un boulon est au maximum $3 \times 10^{-9}$ oe. Bien qu'une soixantaine de boulons soient employés, le champ en un endroit donné ne peut dépasser $1 \times 1 \sigma^{7}$ oe et est vraisemblablement beaucoup plus petit.

## Contrôle de température d) et $g$ )

La température est contrôlée automatiquement au moyen d'un régulateur de chauffage (voir Information). La thermosonde (fig. 5) est accouplée thermiquement avec le caloriferre. La température désirée est signalée sur un indicateur gradué en degrés C. Au début, dès que l'interrupteur est fermé, le calorifère chauffe à pleine puissance. La résistance en platine de la thermo-sonde est alors continuellement comparée à celle qui a été déterminée d'après l'indicateur. Lorsque les valeurs de ces deux résistances approchent l'une de l'autre, la puissance diminue graduellement jusqu'à ce que les deux résistances soient égales.

Le régulateur laisse alors passer juste le courant nécessaire au maintien de cette température. Une minuterie automatique permet de régler l'interrupteur, ce qui signifie qu'un chauffage peut avoir lieu en l'absence d'un opérateur. La thermosonde a été calibrée à $1^{\circ} \mathrm{C}$ près au moyen d'un thermocouple de platine et de platine à 10 p .100 de rhodium et la correction applicable est donné à la table 1. Du fait de la dimension du four et du fait que le calorifère est encastré dans les tubes d'alumine, il existe un décalage de temps entre la température perçue par la thermo-sonde et la chaleur émise par le calorifère. Ce décalage amène la température, au permier cycle, ì dépasser la température signalée. La correction à faire pour compenser cet effet est donnee à la table 1 .

Table 1. Température et sa variation* d'après le réglage

| Réglage <br> ${ }^{\circ} \mathrm{C}$ | Température | Variation* |  |
| :---: | :---: | :---: | ---: |
|  | $\mathrm{C}^{\mathrm{C}}$ | Max. | Min. |
| 100 | 53 | +10 | 00 |
| 150 | 103 | +10 | 00 |
| 200 | 153 | +10 | -01 |
| 250 | 202 | +09 | -03 |
| 300 | 252 | +08 | -04 |
| 350 | 301 | +07 | -04 |
| 400 | 351 | +06 | -04 |
| 450 | 400 | +05 | -05 |
| 500 | 450 | +05 | -05 |
| 550 | 499 | +04 | -04 |
| 600 | 547 | +04 | -04 |
| 650 | 596 | +03 | -03 |
| 700 | 644 | +03 | -03 |
| 740 | 692 | +03 | -03 |
|  | 732 | +03 | -03 |

*Cette variation s'effectue au cours d'une heure environ à $100^{\circ} \mathrm{C}$ et en 20 minutes à $700^{\circ} \mathrm{C}$. Après ce cycle initial, la température demeure constante à $1^{\circ} \mathrm{C}$ près.

## Uniformité de température e) et f)

Bien que l'encastrement du calorifère contribue au décalage de temps, il est fort possible que cette masse d'alumine réchauffée soit une source de chaleur plus uniforme que le serait un élément exposé. La température est uniforme (fig. 6) à quelques degrés près, excepté pour les 5 cm du haut ( $4^{\circ}$ tablette) où elle est de 5 à $10^{\circ} \mathrm{C}$ plus basse.


Figure 6
Thermo-sonde placée à l'intérieur du four à 7.5 cm de la base. La variation de température est en fonction de la hauteur intérieure du four dans les cinq premières minutes après avoir atteint la température désirée. Par la suite, les variations diminuent d'environ 50 p. 100.

L'élévation de la température à l'intérieur du four débute à $2^{\circ} \mathrm{C} / \mathrm{min}$. et baisse graduellement à $0.75^{\circ} \mathrm{C} / \mathrm{min}$. lorsque la température atteint $700^{\circ} \mathrm{C}$. Ainsi, une température de $600^{\circ} \mathrm{C}$ peut être atteinte en $51 / 2$ heures.

## Rendement

Après plus de deux années d'usage, nombre de courbes ont été obtenues et plusieurs ont déjà parues dans différentes publications (Park, 1970; Brooke et coll., 1970; Park et Irving, 1970). Le décroissement régulier d'intensité jusqu'à zéro, que l'on remarque dans plusieurs de ces courbes, témoigne de l'efficacité de la désaimantation thermique en champ quasi nul. A la figure 7 sont données les courbes de désaimantation d'une aimantation rémanente naturelle (ARN) (A) et d'une ATR (B) obtenue en laissant
l'échantillon refroidir de $700^{\circ} \mathrm{C}$ a $20^{\circ} \mathrm{C}$ dans un champ mangétique vertical de 0.57 oe. Entre l'aimantation et la désaimantation, l'échantillon a été soumis à une désaimantation par champ alternatif de 2,900 oe. La courbe B provient d'une étude de Park (1970) et la courbe A, d'une êtude d'Irving et Park (non publiee) effectuée sur une roche sédimentaire du Grand lac de l'Ours. Étant donné que l'aimantation de $B$ est unique, puisqu'elle est provoquée et qu'elle est plus forte que celle de A (ce fait diminue les erreurs des mesures), la courbe B doit être plus représentative du rendement du four.

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dessin schématique du four (fig. 2) et à E . Gélinas pour les photos (fig. 1 et 3 ).

## Information

Adresses des manufacturiers des divers matériaux et accessoires employés a la construction du four. Plusieurs publient des catalogues sur la construc. tion de fours.
Alumine - Norton Company of Canada Ltd., Box 3008, Station B, Hamilton, Ontario.
Bobines - Permali (Canada) Ltd., 2870 Slough St., Malton, Ontario.
Briques réfractaires-Standard Refractories Ltd., 1185 Walkers Line N., Burlington, Ontario.
Nichrome - Canadian Wilbur B Driver Co. Ltd., 85 King St. E., Toronto 1, Ontario. Régulateur de chauffage - Harrel Incorporated, 16 Fitch St., East Norwalk, Connecticut, U.S.A.


Figure 7. Courbes de désaimantation d'après les résultats d'une étude de Park (1970) et d'une étude d'irving et Park (non publiée).

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# record of observations at meanook magnetic observatory 1969 

A. B. COOK and S. J. SPRYSAK

Geographic Coordinates: $54^{\circ} 37^{\prime} \mathrm{N} ; 113^{\circ} 20^{\prime} \mathrm{W}$<br>Geomagnetic Coordinates: $61.8^{\circ} \mathrm{N} ; 301^{\circ} \mathrm{E}$

Officer-in-Charge: Anne B. Cook
Assistant: Steven J. Sprysak

## Introduction

Meanook magnetic observatory was established in July 1916, 85 miles north of the city of Edmonton, Alberta, 11 miles south of the town of Athabasca, Alberta. The observatory is controlled by the Division of Geomagnetism of the Earth Physics Branch, Ottawa, Canada.

## Equipment

Variometers. Three sets of photographic variometers are operated continuously at Meanook: standard-sensitivity Ruska variometers, and standard-sensitivity la Cour and lowsensitivity la Cour variometers. The Ruska variometers were adopted as standard recorders on October 1, 1963. The paper speed is $20 \mathrm{~mm} / \mathrm{hr}$ for the Ruska and $15 \mathrm{~mm} / \mathrm{hr}$ for the la Cour. The temperature of the variometer rooms is maintained constant to $1^{\circ} \mathrm{C}$ by thermostatic controls.

The scale values are determined monthly in the case of the Ruska recorders, less frequently for the la Cour, by applying known fields to the variometers by means of Helmholtz coils.

On August 5, 1969, a major adjustment of the Ruska variometers was carried out. The bench supporting the variometers was rotated by approximately $90^{\circ}$ in order that the H and D calibration coils could be left in the calibration position at all times. (Previously, it was necessary to move the Helmholtz coils between calibrations to avoid blocking light beams during large magnetic disturbances.) The normal direction of the magnetic meridian was first established in the variometer room, using portable fluxgate magnetometer No. TA.8. With the axes of the $H$ and $D$ calibration coils perpendicular to their normal orientation, the $H$ and $D$ variometer magnets were aligned to give no visible deflection when a direct current of 20 ma was sent through the corresponding coil. The coils were then fixed in the calibration position. The temperature-compensating magnet was not reinstalled on the H variometer, since it had affected the other variometers, and good thermostatic control made it unnecessary. The Z variometer was levelled by visual
inspection of the magnet, and then the desensitizing magnet was installed.

The shift of baseline values and changes in sensitivity of the Ruska variometers resulting from these adjustments are shown in the tables following. The scale values per mm adopted for the la Cour variometers were constant throughout the year, as follows:

|  | H | D | Z |
| :--- | ---: | :--- | :---: |
| la Cour standard | $7.18 \gamma$ | $0.93^{\prime}$ | $10.36 \gamma$ |
| la Cour low-sensitivity | $21.67 \gamma$ | $2.35^{\prime}$ | $37.47 \gamma$ |

In addition to the photographic variometers, a three-component recording fluxgate magnetometer ${ }^{1}$ provides a visible record of $\mathrm{X}, \mathrm{Y}$ and Z at a chart speed of 20 mm per hour. The scale value is normally $8.3 \gamma$ per mm, corresponding to a full-scale range of $1000 \gamma$ in each component. By means of a limit switch and a relay, the sensitivity of the recorder is cut in half whenever any element exceeds full-scale indication, thus automatically converting the instrument into a storm recorder.
Absolute instruments. The absolute instruments used at Meanook during 1969 were: Cooke magnetometer No. 15 (with correction of $-0.3^{\prime}$ ) for declination; quartz horizontal intensity magnetometer No. $259^{2}$ (with correction of $-0.00013 H$ ) for horizontal intensity; Ruska earth inductor No. 6540 (with correction of $0.0^{\prime}$ ) for inclination; and a Dominion Observatory proton precessionn magnetometer ${ }^{3,5}$ (4257.60 cps/oersted) for total intensity. A Dominion Observatory portable fluxgate magnetometer ${ }^{4}$ was used as a standby instrument for determining declination, inclination and total intensity and for Meanook field surveys.

## Absolute observations and baseline values

[^21]
## Notes on the tables

Universal time (U.T.) is used throughout. Tables $1-36$ show the mean values of $\mathrm{D}, \mathrm{H}$ and Z for the intervals of 60 minutes centred on the half hour.

Reductions. The hourly values of $\mathrm{D}, \mathrm{H}$ and Z are manually scaled and punched on cards. The tables were calculated by a CDC 3100 computer. The computer was programmed so that the output was compatible with offset printing techniques.

Table 46 lists three-hour range indices and K -indices for Meanook. Lower limit $K_{9}$ is $1500 \gamma$. Throughout the year,
these indices are sent twice a month to De Bilt, Netheriands, and Göttingen, Germany, for use in preparation of planetary K-indices published by the International Association of Geomagnetism and Aeronomy. The magnetograms were read each month for magnetic phenomena and the results were sent to the I.A.G.A.

Maximum hourly ranges in all components were also scaled. Copies of hourly ranges, three-hour indices and magnetograms were sent upon request to Defence Research Telecommunication Establishment. Copies of magnetograms were supplied to researchers during the year 1969.

D Baselines
D Scale Value $/ \mathrm{mm}$


Shift July 31(0724)

*No Ruska Trace Aug. 4(2315) - Aug. 5(1109)

*No Ruska Trace Aug. 4(2315) - 5(1109)

* $\mathrm{X}, \mathrm{Y}, \mathrm{I}, \mathrm{F}$ are derived from annual means $\mathrm{D}, \mathrm{H}$ and Z .


## References

${ }^{1}$ Serson, Paul H. 1967. An electrical recording magnetometer. Can, J. Phys., Vol. 35, pp. 1387-1394.
${ }^{2}$ la Cour, D., and E. Sucksdorff. 1936. Le quartz-magnetomètre QHM, Commun. No. 15, 22 pp., No. 16, 11 pp. Danish Meteorol. Inst. Copenhagen.
${ }^{3}$ Serson, Paul H. 1962. A simple proton precession magnetometer. Report Dominion Observatory, Ottawa, 13 pp.
${ }^{4}$ Serson, P.H., and W.L.W. Hannaford, 1956. A portable electrical magnetometer. Can. J. Technology, Vol. 1, No. 28, pp. 232-243.
${ }^{5}$ U.G.G.I., Helsinki. 1960 . Résolution $\mathrm{N}^{\mathrm{O}} 66$, Comptes Rendus de la XII Assemblée générale.

| HOUR UT |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 0 | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | T0 | T0 | TO | TO | T0 | T0 | 10 | T0 | TO | T0 | T0 | T0 | T0 | TC | T0 | T0 | T0 | T0 | 10 | 10 | T0 | T0 | TO | T0 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |  |
| 1 |  | 737 | 733 | 724 | 729 | 727 | 724 | 724 | 724 | 714 | 698 | 681 | 737 | 732 | 717 | 702 | 735 | 728 | 718 | 719 | 724 | 722 | 717 | 722 | 727 | 721 |
| 2 |  | 727 | 727 | 731 | 724 | 724 | 733 | 733 | 729 | 729 | 732 | 731 | 728 | 727 | 727 | 724 | 721 | 727 | 721 | 720 | 721 | 722 | 722 | 724 | 727 | 726 |
| 3 | 0 | 733 | 735 | 736 | 736 | 735 | 736 | 736 | 736 | 736 | 738 | 741 | 739 | 738 | 735 | 732 | 732 | 727 | 724 | 722 | 124 | 720 | 717 | 72C | 724 | 731 |
| 4 |  | 725 | 727 | 732 | 733 | 733 | 733 | 733 | 733 | 735 | 730 | 726 | 721 | 731 | 135 | 736 | 735 | 731 | 725 | 717 | 715 | 716 | 716 | 720 | 724 | 128 |
| 5 |  | 726 | 733 | 733 | 729 | 729 | 731 | 730 | 735 | 735 | 735 | 735 | 735 | 735 | 733 | 735 | 735 | 728 | 720 | 714 | 712 | 716 | 722 | 722 | 724 | 728 |
| 6 | 0 | 727 | 732 | 732 | 732 | 728 | 727 | 727 | 726 | 727 | 730 | 730 | 733 | 733 | 733 | 732 | 727 | 122 | 112 | 707 | 707 | 712 | 722 | 726 | 731 | 726 |
| 7 |  | 735 | 735 | 736 | 739 | 738 | 742 | 743 | 737 | 735 | 721 | 717 | 669 | 614 | 715 | 743 | 740 | 728 | 712 | 697 | 691 | 717 | 725 | 722 | 724 | 720 |
| 8 |  | 729 | 730 | 729 | 736 | 733 | 738 | 738 | 702 | 718 | 726 | 733 | 727 | 727 | 725 | 724 | 724 | 725 | 720 | 710 | 7 CO | 701 | 705 | 710 | 707 | 722 |
| 9 |  | 726 | 735 | 735 | 732 | 738 | 735 | 732 | 733 | 727 | 727 | 726 | 726 | 726 | 726 | 724 | 727 | 721 | 709 | 7 Cl | 7 Cl | 702 | 711 | 714 | 722 | 723 |
| 10 | 0 | 727 | 735 | 735 | 735 | 736 | 735 | 735 | 733 | 732 | 727 | 728 | 727 | 712 | 731 | 735 | 735 | 724 | 712 | 709 | 710 | 714 | 722 | 726 | 727 | 727 |
| 11 |  | 731 | 733 | 735 | 736 | 737 | 735 | 731 | 726 | 724 | 735 | 133 | 732 | 733 | 733 | 724 | 737 | 736 | 722 | 708 | 7 C 2 | 709 | 712 | 722 | 728 | 727 |
| 12 |  | 735 | 735 | 738 | 736 | 738 | 733 | 736 | 731 | 726 | 727 | 687 | 716 | 724 | 735 | 708 | 732 | 731 | 712 | 706 | 704 | 7.9 | 714 | 72 C | 725 | 723 |
| 13 | 0 | 727 | 733 | 733 | 733 | 733 | 733 | 733 | 731 | 731 | 727 | 721 | 720 | 733 | 733 | 736 | 735 | 731 | 721 | 711 | 711 | 712 | 719 | 722 | 731 | 727 |
| 14 |  | 725 | 719 | 727 | 732 | 731 | 732 | 735 | 712 | 712 | 735 | 761 | 735 | 743 | 735 | 735 | 735 | 727 | 722 | 715 | 714 | 714 | 711 | 701 | 722 | 724 |
| 15 | D | 730 | 733 | 749 | 757 | 749 | 745 | 743 | 733 | 731 | 737 | 724 | 736 | 727 | 732 | 746 | 739 | 737 | 724 | 680 | 670 | 709 | 716 | 717 | 725 | 729 |
| 16 |  | 131 | 728 | 733 | 740 | 747 | 758 | 747 | 746 | 725 | 716 | $7 \mathrm{C6}$ | 735 | 687 | 586 | 694 | 745 | 142 | 725 | 717 | 720 | 722 | 724 | $72 t$ | 120 | 722 |
| 17 | D | 707 | 735 | 747 | 757 | 770 | 789 | 751 | 736 | 767 | 679 | 662 | 726 | 679 | 711 | 733 | 727 | 725 | 699 | 688 | 688 | 114 | 712 | 7 C 9 | 720 | 720 |
| 18 | D | 716 | 722 | 742 | 735 | 746 | 736 | 712 | 632 | 722 | 675 | 695 | 433 | 705 | 735 | 725 | 722 | 716 | 696 | 701 | 702 | 716 | 709 | 711 | 724 | 701 |
| 19 |  | 725 | 731 | 738 | 738 | 743 | 737 | 736 | 731 | 7 C 5 | 623 | 648 | 720 | 714 | 699 | 728 | 735 | 729 | 720 | 701 | 702 | 7 7 8 | 701 | 7 C 4 | 725 | 714 |
| 20 |  | 735 | 738 | 733 | 721 | 737 | 736 | 737 | 737 | 726 | 722 | 722 | 722 | 710 | 719 | 722 | 720 | 718 | 708 | 706 | 707 | 712 | 716 | 712 | 717 | 722 |
| 21 |  | 735 | 740 | 725 | 738 | 745 | 738 | 726 | 732 | 736 | 724 | 711 | 737 | 738 | 737 | 737 | 735 | 728 | 719 | 710 | 714 | 721 | 724 | 725 | 725 | 729 |
| 22 |  | 730 | 732 | 735 | 737 | 740 | 737 | 735 | 735 | 719 | 710 | 736 | 735 | 735 | 735 | 735 | 733 | 728 | 721 | 716 | 712 | 716 | 714 | 718 | 724 | 728 |
| 23 |  | 732 | 735 | 736 | 738 | 736 | 735 | 733 | 733 | 735 | 735 | 735 | 732 | 728 | 742 | 742 | 739 | 735 | 729 | 724 | 722 | $72 t$ | 728 | 726 | 733 | 733 |
| 24 |  | 739 | 738 | 741 | 741 | 741 | 741 | 741 | 741 | 741 | 741 | 741 | 741 | 732 | 689 | 694 | 678 | 700 | 720 | 699 | 693 | 680 | 634 | 706 | 733 | 721 |
| 25 | D | 737 | 756 | 748 | 733 | 735 | 738 | 690 | 660 | 463 | 380 | 388 | 412 | 438 | 579 | 707 | 745 | 655 | 662 | 705 | 667 | 881 | 724 | 731 | 726 | 644 |
| 26 | D | 757 | 179 | 737 | 748 | 746 | 727 | 722 | 720 | 724 | 724 | 724 | 588 | 480 | 677 | 110 | 764 | 733 | 722 | 716 | 715 | 716 | 716 | 712 | 717 | 711 |
| 27 |  | 727 | 736 | 735 | 735 | 733 | 727 | 725 | 693 | 668 | 607 | 644 | 628 | 638 | 602 | 705 | 724 | 710 | 716 | 704 | 7 Cl | 701 | 715 | 721 | 712 | 696 |
| 28 |  | 723 | 126 | 731 | 734 | 734 | 734 | 732 | 731 | 731 | 725 | 725 | 724 | 725 | 727 | 728 | 731 | 726 | 721 | 709 | 708 | 713 | 110 | 711 | 719 | 724 |
| 29 | 0 | 725 | 730 | 734 | 732 | 732 | 732 | 732 | 732 | 732 | 727 | 727 | 729 | 732 | 736 | 741 | 741 | 736 | 725 | 711 | 704 | 7,14 | 710 | 720 | 731 | 721 |
| 30 |  | 724 | 727 | 735 | 735 | 726 | 723 | 725 | 730 | 724 | 697 | 664 | 747 | 745 | 744 | 742 | 737 | 732 | 723 | 719 | 715 | 716 | 123 | 724 | 727 | 725 |
| 31 |  | 734 | 737 | 738 | 739 | 741 | 737 | 734 | 731 | 728 | 719 | 710 | 709 | 720 | 714 | 744 | 736 | 725 | 735 | 726 | 715 | 711 | 717 | 721 | 723 | 727 |
| MEAN | A | 729 | 734 | 735 | 736 | 737 | 737 | 732 | 724 | 716 | 704 | 7 C 2 | 700 | 701 | 712 | 726 | 732 | 725 | 717 | 709 | 706 | 711 | 716 | 718 | 724 | 720 |
| MEAN | 0 | 728 | 733 | 734 | 734 | 733 | 733 | 733 | 732 | 732 | 730 | 730 | 730 | 730 | 734 | 735 | 734 | 728 | 719 | 712 | 711 | 712 | 718 | 723 | 729 | 728 |
| MEAN | D | 729 | 745 | 745 | 746 | 749 | 747 | 724 | 696 | 669 | 639 | 638 | 579 | 606 | 687 | 724 | 739 | 713 | 700 | 698 | 689 | 767 | 715 | 716 | 722 | 701 |


| HOUR | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| UT | TO | T0 | TO | TO | TO | TO | 10 | ro | 10 | 10 | T0 | T0 | TO | 16 | 10 | 10 | 10 | 10 | T0 | 10 | TC | T0 | TC | to mean |
| DAY | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |





$\begin{array}{rllllllllllllllllllllllllllllllllllll}Q & 12.4 & 12.4 & 13.4 & 13.5 & 13.2 & 13.0 & 12.4 & 12.7 & 13.2 & 13.5 & 13.5 & 14.2 & 15.2 & 16.4 & 15.7 & 16.7 & 17.5 & 18.5 & 17.2 & 15.4 & 13.5 & 12.0 & 11.8 & 12.0 \\ 12.5 & 13.1 & 13.6 & 13.8 & 13.8 & 13.1 & 12.6 & 12.5 & 15.6 & 15.1 & 20.5 & 21.6 & 28.5 & 27.5 & 22.5 & 20.1 & 18.5 & 18.3 & 15.1 & 4.8 & 4.1 & 6.9 & 11.4 & 11.9 \\ 12.3 & 13.6 & 14.8 & 13.3 & 11.9 & 13.8 & 12.5 & 5.8 & 16.8 & 14.3 & 13.8 & 15.8 & 15.6 & 17.0 & 16.6 & 16.8 & 19.0 & 18.6 & 16.8 & 15.3 & 11.8 & 10.6 & 10.8 & 10.3 \\ 10.8 & 12.1 & 14.0 & 14.8 & 13.8 & 13.6 & 12.5 & 13.8 & 13.6 & 13.6 & 13.8 & 14.8 & 15.3 & 15.5 & 17.0 & 17.5 & 18.6 & 18.6 & 16.6 & 14.1 & 12.5 & 12.3 & 11.8 & 11.4\end{array}$






13.9



















## VERTICAL INTENSITY

| HOUR <br> UT |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 28 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | то | TO | TO | 10 | 10 | TO | TO | T0 | 10 | J0 | 10 | 10 | TO | TC | TC | 10 | 10 | 10 | T0 | 10 | 10 | 10 | 10 | 10 | PEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |  |
| 1 |  | 688 | 687 | 683 | 676 | 671 | 670 | 666 | 654 | 649 | 617 | 578 | 631 | 655 | 650 | 629 | 643 | 647 | 652 | 653 | 658 | 664 | 667 | 670 | 667 | 655 |
| 2 |  | 666 | 666 | 666 | 667 | 671 | 670 | 666 | 665 | 665 | 664 | 659 | 649 | 653 | 658 | 655 | 666 | 669 | 670 | 673 | 669 | 663 | 666 | 667 | 667 | 665 |
| 3 | 0 | 667 | 665 | 665 | 662 | 662 | 664 | 664 | 665 | 665 | 665 | 662 | 662 | 662 | 657 | 660 | 661 | 664 | 666 | 668 | 668 | 667 | 666 | 666 | 666 | 664 |
| 4 |  | 662 | 660 | 662 | 662 | 662 | 662 | 662 | 657 | 656 | 656 | 656 | 651 | 648 | 656 | 659 | 665 | 666 | 666 | 665 | 667 | 666 | 666 | 666 | 666 | 661 |
| 5 |  | 666 | 660 | 660 | 660 | 656 | 660 | 6 E1 | 661 | 661 | 661 | 660 | 659 | 656 | 656 | 656 | 659 | 662 | 665 | 666 | 666 | 661 | 665 | 662 | 662 | 661 |
| 6 | 0 | 661 | 661 | 660 | 660 | 660 | 660 | 660 | 660 | 660 | 660 | 660 | 659 | 659 | 659 | 659 | 660 | 660 | 664 | 665 | 665 | 665 | 661 | 66 C | 660 | 661 |
| 7 |  | 661 | 660 | 658 | 658 | 658 | 658 | 657 | 657 | 657 | 649 | 649 | 607 | 489 | 624 | 662 | 663 | 661 | 663 | 661 | 657 | 662 | 665 | 665 | 667 | 649 |
| 8 |  | 674 | 671 | 674 | 680 | 693 | 681 | 673 | 637 | 636 | 649 | 677 | 673 | 668 | 661 | 665 | 668 | 669 | 669 | 669 | 669 | 673 | 672 | 672 | 672 | 669 |
| 9 |  | 678 | 680 | 678 | 672 | 669 | 674 | 672 | 669 | 668 | 666 | 666 | 666 | 663 | 662 | 661 | 667 | 668 | 669 | 669 | E69 | 669 | 667 | 669 | 668 | 669 |
| 10 | 0 | 667 | 667 | 666 | 663 | 665 | 666 | 666 | 665 | $6 \in 6$ | 669 | 668 | 662 | 645 | 648 | 660 | 660 | 662 | 666 | 667 | 666 | 667 | 667 | 669 | 668 | 664 |
| 11 |  | 667 | 663 | 664 | 664 | 664 | 664 | 667 | 668 | $6 \in 7$ | 670 | 668 | 668 | 663 | 657 | 656 | 661 | 658 | 659 | 658 | 662 | tet | 666 | 668 | 664 | 664 |
| 12 |  | 670 | 667 | 664 | 664 | 664 | 667 | 667 | 670 | $6 \in 4$ | 659 | 603 | 600 | 632 | 637 | 626 | 616 | 625 | 633 | 650 | 662 | 670 | 672 | 672 | 672 | 651 |
| 13 | 0 | 670 | 667 | 667 | 667 | 663 | 663 | 663 | 663 | 661 | 656 | 643 | 637 | 658 | 658 | 659 | 661 | 663 | 663 | 662 | 667 | 667 | 667 | 668 | 667 | 662 |
| 14 |  | 668 | 676 | 679 | 679 | 674 | 670 | 655 | 621 | 615 | 662 | 623 | 633 | 669 | 662 | 662 | 661 | 661 | 661 | 661 | 663 | 664 | 668 | 672 | 686 | 660 |
| 15 | D | 692 | 693 | 697 | 697 | 704 | 681 | 685 | 682 | 671 | 652 | 639 | 653 | 647 | 651 | 669 | 663 | 663 | 662 | 660 | 669 | 669 | 664 | 67 C | 674 | 671 |
| 16 |  | 674 | 676 | 671 | 679 | 691 | 704 | 716 | 675 | 674 | 647 | 627 | 647 | 601 | 568 | 608 | 648 | 663 | 669 | 668 | 669 | 604 | 665 | 665 | 670 | 660 |
| 17 | D | 674 | 680 | 719 | 712 | 752 | 741 | 719 | 683 | 644 | 550 | 574 | 639 | 612 | 634 | 659 | 647 | 659 | 657 | 683 | 679 | 683 | 688 | 686 | 698 | 670 |
| 18 | D | 711 | 691 | 687 | 682 | 693 | 687 | 647 | 591 | 649 | 640 | 647 | 506 | 589 | 627 | 632 | 664 | 660 | 668 | 674 | 681 | 687 | 683 | 681 | 682 | 657 |
| 19 |  | 692 | 699 | 681 | 683 | 677 | 680 | 683 | 681 | 647 | 555 | 559 | 623 | 641 | 644 | 663 | 668 | 663 | 662 | 669 | 685 | 682 | 673 | 671 | 673 | 661 |
| 20 |  | 671 | 674 | 679 | 683 | 688 | 693 | 695 | 676 | 688 | 659 | 658 | 658 | 634 | 647 | 650 | 651 | 664 | 662 | 663 | 669 | 670 | 670 | 67 C | 673 | 668 |
| 21 |  | 680 | 681 | 676 | 674 | 673 | 664 | 635 | 646 | $6 \in 2$ | 654 | 628 | 658 | 659 | 658 | 662 | 664 | 668 | 668 | 669 | 669 | 669 | 67 C | 668 | 665 | 663 |
| 22 |  | 664 | 664 | 664 | 664 | 659 | 659 | 659 | 662 | 642 | 623 | 662 | 668 | 660 | 660 | 682 | 664 | 664 | 667 | 668 | 6 70 | 685 | 665 | 664 | 663 | 661 |
| 23 |  | 668 | 665 | 665 | 664 | 668 | 668 | 671 | 670 | 665 | 663 | 660 | 658 | 650 | 654 | 658 | 665 | 665 | 657 | 656 | 658 | 659 | 658 | 658 | 662 | 662 |
| 24 |  | 664 | 659 | 659 | 659 | 659 | 659 | 659 | 658 | 658 | 658 | 657 | 651 | 644 | 589 | 534 | 527 | 552 | 599 | 641 | 663 | 676 | 111 | 687 | 699 | 643 |
| 25 | D | 718 | 778 | 715 | 682 | 691 | 694 | 657 | 612 | 539 | 536 | 710 | 536 | 509 | 563 | 561 | 634 | 623 | 657 | 681 | 691 | 711 | 705 | 692 | 686 | 649 |
| 26 | 0 | 740 | 754 | 687 | 704 | 699 | 675 | 663 | 659 | 658 | 660 | 662 | 577 | 515 | 585 | 599 | 682 | 675 | 670 | 670 | 668 | 673 | 674 | 673 | 680 | 663 |
| 27 |  | 682 | 680 | 675 | 676 | 675 | 671 | 669 | 597 | 576 | 555 | 567 | 601 | 591 | 586 | 644 | 645 | 658 | 665 | 671 | 676 | 680 | 682 | 686 | 682 | 645 |
| 28 |  | 688 | 687 | 694 | 682 | 671 | 671 | 668 | 665 | 665 | 662 | 651 | 663 | 663 | 662 | 660 | 669 | 665 | 663 | 663 | 662 | 668 | 673 | 674 | 673 | 669 |
| 29 | 0 | 670 | 668 | 670 | 668 | 665 | 663 | 663 | 659 | 662 | 662 | 660 | 659 | 658 | 658 | 663 | 665 | 662 | 662 | 663 | 668 | 669 | 668 | 667 | 664 | 664 |
| 30 |  | 665 | 668 | 668 | 667 | 664 | 667 | 670 | 662 | 647 | 580 | 524 | 646 | 662 | 659 | 659 | 662 | 660 | 659 | 659 | 660 | 662 | 663 | 662 | 662 | 652 |
| 31 |  | 662 | 660 | 660 | 662 | 662 | 662 | 662 | 659 | 657 | 640 | 626 | 595 | 622 | 591 | 612 | 615 | 628 | 634 | 651 | 659 | 663 | 668 | 67 C | 663 | 645 |
|  |  |  |  |  |  |  |  |  |  |  |  |  | , |  |  |  |  |  |  |  |  |  |  |  |  |  |
| MEAN | A | 677 | 678 | 675 | 673 | 675 | 673 | 668 | 656 | 651 | 639 | 638 | 636 | 632 | 638 | 644 | 653 | 656 | 659 | 664 | 668 | 670 | 671 | 671 | 672 | 660 |
| MEAN | 0 | 667 | 665 | 665 | 664 | 663 | 663 | 663 | 662 | 663 | 662 | 659 | 656 | 657 | 656 | 660 | 661 | 662 | 664 | 665 | 667 | 617 | 666 | 666 | 665 | 663 |
| MEAN | D | 107 | 719 | 701 | 695 | 708 | 696 | 674 | 646 | 636 | 608 | 646 | 582 | 575 | 612 | 624 | 658 | 656 | 663 | 674 | 677 | 685 | 683 | 686 | 684 | 662 |




| $\begin{aligned} & \text { HOUR } \\ & \text { UT } \end{aligned}$ |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 2 C | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | T0 | TO | TO | TO | 10 | TO | T0 | TO | 10 | T0 | T0 | T0 | To | 10 | 10 | 70 | T0 | TO | T0 | 10 | 10 | 10 | 10 | 10 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 12 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |  |
| 1 | 0 | 659 | 662 | 662 | 662 | 660 | 660 | 659 | 659 | 658 | 659 | 659 | 658 | 658 | 658 | 660 | 682 | 658 | 659 | 667 | 663 | 659 | 66 C | 665 | 663 | 660 |
| 2 | D | 659 | 659 | 659 | 659 | 659 | 659 | 659 | 659 | 638 | 639 | 638 | 627 | 636 | 639 | 658 | 638 | 648 | 639 | 640 | 591 | 695 | 707 | $7 \mathrm{C6}$ | 676 | 654 |
| 3 | D | 669 | 673 | 683 | 723 | 705 | 663 | 597 | 598 | 611 | 587 | 591 | 522 | 601 | 487 | 593 | 654 | 663 | 667 | 665 | 681 | 695 | 722 | 691 | 691 | 643 |
| 4 |  | 681 | 683 | 679 | 679 | 680 | 680 | 688 | 693 | 686 | 676 | 687 | 687 | 674 | 671 | 669 | 670 | 664 | 665 | 668 | 665 | 659 | 662 | 668 | 682 | 676 |
| 5 |  | 692 | 719 | 698 | 680 | 681 | 682 | 681 | 657 | 663 | 669 | 632 | 634 | 647 | 659 | 663 | 664 | 664 | 665 | 669 | 674 | 671 | 676 | 674 | 675 | 670 |
| 6 |  | 677 | 677 | 693 | 707 | 706 | 719 | 724 | 691 | 670 | 635 | 593 | 671 | 673 | 673 | 670 | 673 | 673 | 675 | 679 | 677 | 671 | 674 | 683 | 695 | 678 |
| 7 |  | 683 | 682 | 673 | 669 | 669 | 670 | 671 | 667 | 674 | 671 | 660 | 601 | 624 | 650 | 660 | 657 | 658 | 680 | 668 | 660 | 665 | 670 | 685 | 683 | 664 |
| 8 |  | 683 | 693 | 685 | 683 | 685 | 694 | 685 | 671 | 670 | 668 | 668 | 662 | 667 | 660 | 659 | 659 | 659 | 658 | 669 | 669 | 673 | 674 | 671 | 670 | 672 |
| 9 | 0 | 671 | 671 | 670 | 670 | 669 | 668 | 664 | 663 | $6 \in 9$ | 669 | 667 | 665 | 660 | 660 | 659 | 659 | 662 | 668 | 671 | 669 | 668 | 664 | 665 | 669 | 666 |
| 10 |  | 670 | 670 | 671 | 671 | 669 | 662 | 663 | 658 | 638 | 611 | 609 | 624 | 651 | 648 | 664 | 658 | 659 | 669 | 670 | 670 | 669 | 671 | 7 CE | 712 | 661 |
| 11 | 0 | 768 | 760 | 794 | 697 | 683 | 687 | 535 | 486 | 467 | 310 | 374 | 772 | 811 | 640 | 561 | 642 | 647 | 676 | 705 | 734 | 733 | 688 | 704 | 693 | 649 |
| 12 |  | 686 | 687 | 687 | 688 | 696 | 695 | 694 | 689 | 690 | 692 | 686 | 683 | 677 | 676 | 676 | 678 | 677 | 674 | 675 | 674 | 675 | 675 | 68 C | 702 | 684 |
| 13 |  | 702 | 699 | 695 | 687 | 686 | 687 | 675 | 696 | 651 | 636 | 651 | 672 | 672 | 659 | 634 | 641 | 661 | 669 | 674 | 672 | 680 | 678 | 672 | 681 | 672 |
| 14 |  | 671 | 680 | 678 | 686 | 683 | 682 | 677 | 674 | 671 | 670 | 647 | 623 | 635 | 641 | 661 | 671 | 672 | 670 | 672 | 674 | 674 | 672 | 674 | 687 | 669 |
| 15 | D | 683 | 684 | 689 | 710 | 686 | 694 | 699 | 687 | 674 | 623 | 598 | 649 | 660 | 658 | 663 | 661 | 658 | 660 | 665 | 672 | 674 | 684 | 687 | 683 | 671 |
| 16 |  | 696 | 684 | 683 | 682 | 681 | 677 | 671 | 666 | 590 | 659 | 661 | 636 | 586 | 625 | 659 | 660 | 672 | 669 | 670 | 671 | 676 | 674 | 672 | 669 | 662 |
| 17 | 0 | 665 | 663 | 663 | 664 | 664 | 671 | 669 | 665 | 666 | 661 | 663 | 663 | 664 | 660 | 664 | 669 | 671 | 671 | 668 | 672 | 672 | 672 | 671 | 661 | 666 |
| 18 | 0 | 660 | 660 | 660 | 660 | 660 | 660 | 660 | 660 | 680 | 660 | 660 | 660 | 660 | 659 | 660 | 663 | 665 | 663 | 663 | ce5 | 664 | 661 | 661 | 660 | 661 |
| 19 |  | 660 | 661 | 661 | 668 | 676 | 686 | 683 | 671 | 661 | 660 | 659 | 647 | 582 | 574 | 619 | 635 | 648 | 659 | 665 | 661 | 670 | 671 | 669 | 663 | 655 |
| 20 |  | 660 | 660 | 660 | 668 | 689 | 684 | 671 | 661 | 658 | 645 | 645 | 635 | 628 | 645 | 649 | 653 | 653 | 646 | 643 | 645 | 652 | 660 | 668 | 671 | 656 |
| 21 |  | 671 | 672 | 668 | 660 | 660 | 664 | 653 | 657 | 658 | 659 | 658 | 659 | 658 | 658 | 660 | 660 | 660 | 658 | 660 | 660 | 681 | 663 | CE 2 | 862 | 661 |
| 22 | 0 | 659 | 658 | 659 | 659 | 659 | 659 | 660 | 659 | 653 | 652 | 651 | 651 | 648 | 641 | 647 | 649 | 652 | 657 | 657 | 659 | 659 | 661 | 666 | 664 | 656 |
| 23 |  | 664 | 660 | 660 | 659 | 660 | 676 | 645 | 647 | 657 | 648 | 610 | 593 | 604 | 588 | 640 | 657 | 657 | 653 | 651 | 653 | 659 | 863 | 664 | 864 | 647 |
| 24 |  | 664 | 660 | 660 | 660 | 660 | 668 | 665 | 658 | 6C9 | 625 | 654 | 652 | 653 | 655 | 657 | 659 | 659 | 658 | 657 | 660 | 660 | 663 | 663 | 663 | 656 |
| 25 |  | 663 | 664 | 669 | 669 | 660 | 660 | 659 | 658 | 645 | 651 | 652 | 642 | 643 | 657 | 660 | 664 | Et5 | 661 | 660 | $6 \in 0$ | 664 | 670 | 670 | 669 | 660 |
| 26 |  | 666 | 663 | 668 | 672 | 712 | 684 | 670 | 630 | 528 | 587 | 645 | 655 | 649 | 645 | 652 | 659 | 660 | 651 | 643 | 657 | 661 | 674 | 676 | 672 | 653 |
| 27 | D | 664 | 668 | 677 | 672 | 689 | 676 | 663 | 622 | 640 | 660 | 657 | 648 | 648 | 636 | 598 | 513 | 571 | 664 | 670 | 681 | 682 | 687 | 682 | 686 | 652 |
| 28 |  | 683 | 676 | 683 | 681 | 686 | 695 | 623 | 569 | 624 | 649 | 669 | 668 | 654 | 653 | 654 | 659 | 647 | 651 | 657 | 657 | 661 | 675 | 687 | 694 | 661 |
| MEAN | A | 676 | 677 | 678 | 677 | 678 | 677 | 663 | 653 | 642 | 637 | 637 | 649 | 651 | 642 | 649 | 653 | 657 | 662 | 665 | 666 | 672 | 674 | 677 | 677 | 662 |
| MEAN | 0 | 663 | 663 | 663 | 663 | 663 | 664 | 663 | 661 | $6 \in 1$ | 660 | 660 | 659 | 658 | 656 | 658 | 660 | 662 | 663 | 665 | 666 | 664 | 664 | 6et | 663 | 662 |
| MEAN | 0 | 689 | 689 | 701 | 692 | 684 | 676 | 631 | 610 | 606 | 564 | 571 | 644 | 671 | 612 | 614 | 622 | 638 | 661 | 669 | 672 | 696 | 698 | 694 | 686 | 654 |


| HOUR UT |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | ro | 10 | T0 | 10 | TC | TO | T0 | T0 | 10 | 10 | 10 | T0 | T0 | TC | 10 | 10 | 10 | 10 | T0 | 10 | 10 | 10 | T0 | 10 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |  |
| 1 |  | 688 | 707 | 716 | 721 | 721 | 724 | 723 | 724 | 726 | 724 | 727 | 726 | 725 | 724 | 726 | 723 | 700 | 654 | 700 | 700 | 703 | 708 | 719 | 711 | 713 |
| 2 |  | 707 | 732 | 768 | 777 | 726 | 721 | 723 | 723 | 723 | 723 | 721 | 679 | 636 | 704 | 731 | 732 | 727 | 715 | 706 | 704 | 708 | 711 | 712 | 715 | 718 |
| 3 | 0 | 724 | 725 | 731 | 732 | 731 | 732 | 732 | 734 | 734 | 734 | 735 | 735 | 735 | 734 | 734 | 734 | 724 | 720 | 708 | 700 | 700 | 701 | 705 | 714 | 724 |
| 4 | 0 | 723 | 726 | 734 | 734 | 134 | 734 | 734 | 734 | 734 | 735 | 736 | 736 | 736 | 735 | 739 | 736 | 727 | 716 | 711 | 705 | 713 | 717 | 7 C 6 | 710 | 727 |
| 5 |  | 713 | 726 | 734 | 732 | 734 | 735 | 740 | 737 | 744 | 740 | 736 | 668 | 714 | 746 | 746 | 741 | 736 | 725 | $7 \mathrm{C9}$ | 7 CO | 708 | 713 | 723 | 732 | 726 |
| 6 |  | 721 | 728 | 742 | 735 | 744 | 745 | 747 | 737 | 735 | 730 | 670 | 690 | 746 | 745 | 737 | 721 | 709 | 678 | 699 | 699 | 698 | 694 | 708 | 725 | 720 |
| 7 |  | 724 | 734 | 727 | 740 | 758 | 770 | 757 | 749 | 746 | 721 | 723 | 734 | 730 | 678 | 645 | 710 | 726 | 698 | 665 | 689 | 703 | 715 | 7 CS | 727 | 720 |
| 8 |  | 721 | 739 | 756 | 758 | 755 | 739 | 732 | 732 | 726 | 677 | 732 | 700 | 703 | 738 | 735 | 726 | 723 | 709 | 699 | 701 | 709 | 710 | 715 | 703 | 722 |
| 9 |  | 723 | 734 | 737 | 736 | 741 | 136 | 741 | 734 | 732 | 713 | 744 | 736 | 708 | 697 | 688 | 723 | 736 | 718 | 697 | 701 | 714 | 721 | 715 | 725 | 723 |
| 10 | 0 | 734 | 732 | 735 | 736 | 734 | 741 | 742 | 741 | 732 | 711 | 741 | 736 | 735 | 737 | 741 | 741 | 738 | 734 | 727 | 715 | 715 | 713 | 713 | 721 | 731 |
| 11 |  | 726 | 736 | 735 | 746 | 746 | 746 | 743 | 728 | 690 | 645 | 616 | 581 | 603 | 714 | 731 | 727 | 746 | 730 | 710 | 678 | 705 | 726 | 796 | 876 | 715 |
| 12 | 0 | 904 | 856 | 925 | 865 | 843 | 737 | 384 | 481 | $4 ¢ 7$ | 350 | 354 | 702 | 739 | 701 | 701 | 678 | 645 | 668 | 711 | 709 | 124 | 720 | 725 | 729 | 680 |
| 13 |  | 726 | 745 | 743 | 730 | 731 | 730 | 736 | 733 | 727 | 727 | 726 | 722 | 725 | 731 | 726 | 718 | 715 | 719 | 717 | 714 | 714 | 720 | 725 | 725 | 726 |
| 14 |  | 732 | 733 | 733 | 727 | 733 | 735 | 735 | 735 | 735 | 735 | 732 | 735 | 735 | 735 | 727 | 720 | 716 | 714 | 693 | 691 | 701 | 690 | 722 | 728 | 724 |
| 15 |  | 745 | 749 | 815 | 805 | 814 | 729 | 716 | 689 | 417 | 509 | 566 | 550 | 647 | 690 | 696 | 671 | 719 | 725 | 704 | 714 | 721 | 721 | 121 | 735 | 690 |
| 16 |  | 731 | 722 | 730 | 737 | 750 | 720 | 611 | 567 | 538 | 354 | 515 | 758 | 743 | 747 | 757 | 756 | 742 | 725 | 715 | 712 | 712 | 720 | 735 | 750 | 689 |
| 17 | D | 791 | 923 | 933 | 736 | 813 | 856 | 787 | 739 | 721 | 613 | 690 | 677 | 272 | 637 | 758 | 746 | 660 | 613 | 670 | 706 | 716 | 772 | 728 | 724 | 720 |
| 18 |  | 724 | 731 | 737 | 755 | 756 | 736 | 648 | 649 | 679 | 638 | 668 | 728 | 743 | 745 | 745 | 733 | 720 | 680 | 716 | 712 | 712 | 702 | 726 | 715 | 712 |
| 19 |  | 733 | 745 | 735 | 736 | 738 | 736 | 737 | 727 | 671 | 745 | 746 | 746 | 746 | 746 | 748 | 745 | 735 | 716 | 705 | 705 | 719 | 725 | 712 | 747 | 731 |
| 20 |  | 853 | 996 | 973 | 732 | 725 | 724 | 724 | 693 | $7 \in 1$ | 662 | 655 | 746 | 731 | 724 | 709 | 699 | 669 | 647 | 671 | 691 | 694 | 741 | $77 E$ | 788 | 741 |
| 21 |  | 766 | 736 | 757 | 736 | 738 | 755 | 725 | 657 | 7 C8 | 687 | 683 | 670 | 732 | 742 | 733 | 742 | 732 | 712 | 702 | 690 | 689 | 710 | 728 | 715 | 719 |
| 22 |  | 736 | 745 | 745 | 757 | 733 | 733 | 738 | 737 | 7C7 | 635 | 671 | 658 | 689 | 700 | 7 CO | 710 | 718 | 719 | 691 | 687 | 691 | 717 | 72: | 727 | 711 |
| 23 | D | 724 | 722 | 724 | 733 | 735 | 735 | 736 | 736 | 737 | 737 | 741 | 747 | 745 | 747 | 736 | 712 | 706 | 704 | 629 | 644 | 677 | 795 | 1092 | 1016 | 750 |
| 24 | D | 815 | 708 | 801 | 944 | 965 | 746 | 688 | 583 | 385 | -204 | 54 | 244 | 534 | 738 | 748 | 735 | 730 | 719 | 710 | 717 | 72 C | 720 | 716 | 711 | 634 |
| 25 | D | 709 | 701 | 706 | 707 | 707 | 710 | 712 | 489 | 368 | 484 | 7 Cl | 735 | 667 | 663 | 626 | 695 | 701 | 690 | 673 | 690 | 717 | 722 | 745 | 776 | 671 |
| 26 |  | 742 | 733 | 712 | 716 | 720 | 717 | 721 | 721 | 725 | 728 | 690 | 688 | 724 | 725 | 691 | 701 | 717 | 697 | 690 | 704 | 7.78 | 722 | 724 | 733 | 715 |
| 27 | 0 | 725 | 720 | 727 | 729 | 721 | 725 | 730 | 728 | 735 | 736 | 733 | 737 | 736 | 738 | 738 | 739 | 738 | 722 | 712 | 712 | 712 | 712 | 717 | 721 | 727 |
| 28 | C | 727 | 731 | 735 | 735 | 732 | 747 | 746 | 736 | 728 | 738 | 742 | 743 | 742 | 738 | 735 | 738 | 720 | 717 | 722 | 711 | 712 | 712 | 718 | 727 | 731 |
| 29 |  | 731 | 733 | 737 | 735 | 735 | 738 | 740 | 735 | 706 | 670 | 726 | 743 | 711 | 712 | 707 | 705 | 722 | 710 | 721 | 715 | 707 | 727 | 745 | 784 | 725 |
| 30 |  | 779 | 721 | 727 | 735 | 733 | 130 | 732 | 735 | 716 | 712 | 735 | 735 | 735 | 733 | 733 | 732 | 712 | 677 | 669 | 679 | 70C | 725 | 711 | 732 | 722 |
| 31 |  | 726 | 746 | 733 | 738 | 746 | 746 | 745 | 738 | 706 | 714 | 722 | 735 | 737 | 729 | 733 | 746 | 728 | 700 | 660 | 681 | 695 | 698 | 71 C | 726 | 722 |
| MEAN | A | 743 | 749 | 759 | 749 | 751 | 739 | 716 | 699 | 676 | 639 | $t \in 9$ | 694 | 697 | 722 | 723 | 724 | 717 | 702 | 697 | 699 | 707 | 719 | 736 | 744 | 716 |
| MEAN | 0 | 726 | 127 | 732 | 733 | 730 | 736 | 737 | 734 | 734 | 731 | 738 | 737 | 737 | 735 | 737 | 738 | 729 | 722 | 716 | 709 | 711 | 711 | 712 | 719 | 728 |
| MEAN | D | 789 | 782 | 818 | 797 | 813 | 757 | $6 \in 1$ | 606 | 536 | 396 | $5 C 8$ | 621 | 591 | 697 | 714 | 714 | 689 | 679 | 679 | 693 | 111 | 746 | 8 Cz | 791 | 691 |


| HOUR |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | ¢ | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| DAY UT |  | T0 | TO | 10 | T0 | TO | TO | 10 | T0 | 10 | T0 | 10 | TO | 10 | TC | T0 | 15 | 10 | 10 | 10 | 10 | 10 | 10 | 10 | TC | MEAN |
|  |  | 1 | 2 | 3 | 4 | 5 | 8 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |  |
| 1 |  | 10.2 | 10.4 | 12.2 | 13.4 | 13.4 | 13.4 | 13.4 | 13.4 | 12.7 | 13.1 | 13.7 | 14.6 | 14.9 | 15.1 | 17.4 | 18.7 | 17.1 | 10.0 | 3.4 | 7.5 | 8.7 | 10.2 | 9.C | 11.4 | 12.4 |
| 2 |  | 10.2 | 9.4 | 14.2 | 7.2 | 13.7 | 12.7 | 12.4 | 13.6 | 13.2 | 13.7 | 14.9 | 11.5 | 11.0 | 10.9 | 18.7 | 20.1 | 20.6 | 19.1 | 16.2 | 15.4 | 13.7 | 12.6 | 12.4 | 12.4 | 13.7 |
| 3 | $Q$ | 12.2 | 12.2 | 12.2 | 12.4 | 12.9 | 12.9 | 12.6 | 12.2 | 12.4 | 13.6 | 13.7 | 13.9 | 13.6 | 14.2 | 15.6 | 18.2 | 19.4 | 19.2 | 17.2 | 15.4 | 13.6 | 11.9 | 10.5 | 11.5 | 13. 3 |
| 4 | 0 | 11.9 | 11.9 | 11.9 | 12.0 | 12.2 | 12.2 | 12.4 | 12.6 | 12.6 | 12.4 | 13.1 | 13.1 | 13.6 | 13.4 | 15.4 | 18.4 | 18.7 | 16.6 | 15.2 | 11.2 | 9.7 | 6.7 | 5.9 | 5.9 | 12.4 |
| 5 |  | 9.9 | 11.7 | 12.0 | 12.6 | 12.6 | 12.2 | 11.9 | 11.9 | 12.0 | 12.2 | 13.6 | 16.9 | 18.7 | 18.6 | 20.9 | 20.4 | 18.7 | 19.4 | 16.6 | 15.1 | 12.2 | 10.5 | 9.5 | 7.5 | 14.1 |
| 6 |  | 10.4 | 9.2 | 8.7 | 10.7 | 10.5 | 11.5 | 11.4 | 12.2 | 15.2 | 15.2 | 17.1 | 21.1 | 15.6 | 16.1 | 18.4 | 16.9 | 14.9 | 11.7 | 12.4 | 11.5 | 10.5 | 8.9 | 7.5 | 7.7 | 12.7 |
| 7 |  | 8.5 | 8.7 | 11.9 | 12.0 | 8.7 | 10.7 | 14.2 | 12.7 | 16.6 | 12.4 | 11.9 | 13.4 | 15.6 | 9.4 | 10.4 | 17.2 | 20.7 | 19.2 | 12.2 | 8.4 | 5.4 | 6.0 | 8.7 | 7.4 | 11.8 |
| 8 |  | 8.4 | 8.4 | 7.2 | 10.4 | 15.1 | 12.7 | 12.6 | 14.2 | 13.9 | 14.9 | 16.9 | 17.2 | 12.0 | 15.1 | 17.1 | 18.9 | 19.9 | 18.9 | 14.9 | 14.4 | 12.0 | 11.9 | 10.7 | 9.4 | 13.6 |
| 9 |  | 8.9 | 8.7 | 8.4 | 7.5 | 8.7 | 12.4 | 13.2 | 12.4 | 15.1 | 19.1 | 18.4 | 16.6 | 20.2 | 17.6 | 21.6 | 20.6 | 16.9 | 19.4 | 15.6 | 14.4 | 13.7 | 12.2 | 12.2 | 10.7 | 14.3 |
| 10 | 0 | 8.7 | 9.9 | 9.9 | 8.5 | 10.7 | 10.0 | 12.4 | 11.9 | 14.2 | 18.9 | 14.4 | 13.7 | 13.9 | 14.1 | 15.7 | 17.2 | 18.7 | 19.4 | 19.1 | 15.2 | 12.7 | 12.6 | $12 . C$ | 11.4 | 13.6 |
| 11 |  | 10.0 | 8.5 | 9.9 | 10.9 | 10.2 | 8.7 | 17.2 | 12.0 | 25.4 | 26.6 | 29.9 | 28.1 | 42.9 | 24.4 | 20.2 | 18.6 | 18.4 | 18.9 | 17.1 | 18.7 | 12.6 | 10.5 | 7.5 | 7.9 | 17.3 |
| 12 | 0 | 7.2 | 6.9 | 1.2 | 3.0 | $-5.2$ | 1.4 | 13.4 | 23.7 | 33.6 | 18.2 | 26.9 | 19.1 | 14.9 | 17.6 | 16.1 | 17.6 | 14.1 | 17.9 | 17.1 | 14.1 | 13.2 | 12.0 | 10.2 | 9.2 | 13.5 |
| 13 |  | 10.7 | 18.7 | 12.0 | 11.5 | 12.0 | 12.0 | 14.2 | 12.7 | 12.7 | 14.1 | 14.4 | 13.7 | 13.6 | 16.6 | 18.7 | 20.6 | 20.7 | 18.7 | 16.1 | 13.7 | 10.4 | 10.4 | 8.7 | 8.5 | 14.0 |
| 14 |  | 7.4 | 5.2 | 5.9 | 9.0 | 12.0 | 11.4 | 12.4 | 12.4 | 13.2 | 13.7 | 14.2 | 16.6 | 15.4 | 16.6 | 20.6 | 22.1 | 19.7 | 19.9 | 14.1 | 12.7 | 10.4 | 9.0 | 5.5 | 5.7 | 12.7 |
| 15 |  | 3.4 | 2.0 | 10.7 | 2.0 | 7.0 | 14.2 | 11.5 | 15.4 | 12.7 | 34.1 | 26.9 | 28.1 | 27.2 | 23.4 | 23.7 | 15.9 | 15.9 | 20.1 | 12.0 | 16.0 | 10.4 | 11.2 | 11.7 | $10 \cdot 5$ | 15.0 |
| 16 |  | 12.0 | 12.0 | 12.0 | 11.4 | 13.4 | 24.6 | 5.0 | 17.4 | 17.2 | 36.8 | 29.8 | 17.1 | 20.6 | 23.2 | 19.2 | 19.2 | 19.4 | 20.4 | 18.2 | 15.9 | 12.6 | 11.5 | 9.5 | 9.2 | 17.0 |
| 17 | D | 2.5 | 6.5 | 3.9 | 9.9 | 4.9 | 9.2 | 10.2 | 12.0 | 12.7 | 15.1 | 19.2 | 19.9 | 22.2 | 18.7 | 20.7 | 25.2 | 26.9 | 7.2 | 2.4 | 8.4 | 13.6 | 9.9 | 11.2 | 11.9 | 12. 7 |
| 18 |  | 12.4 | 12.6 | 12.0 | 14.4 | 14.1 | 15.1 | 18.2 | 21.4 | 21.6 | 10.9 | 17.4 | 12.7 | 15.7 | 17.2 | 20.1 | 20.7 | 22.1 | 16.7 | 14.4 | 15.7 | 13.7 | 11.7 | $9 . \mathrm{C}$ | 12.9 | 15.5 |
| 19 |  | 12.0 | 12.0 | 11.9 | 12.0 | 12.2 | 11.9 | 11.7 | 22.1 | 17.6 | 15.4 | 12.6 | 13.7 | 14.2 | 16.1 | 19.9 | 21.9 | 22.2 | 21.6 | 18.4 | 14.4 | 13.6 | 8.9 | 2.C | -4.1 | 13.9 |
| 20 |  | 3.5 | -6.2 | -6.0 | 11.9 | 12.4 | 12.4 | 10.4 | 20.2 | 8.7 | 10.5 | 16.6 | 15.1 | 15.6 | 18.2 | 18.7 | 24.4 | 23.9 | 16.6 | 8.2 | 8.4 | 8.2 | 7.0 | 3.2 | 3.4 | 11.1 |
| 21 |  | 7.4 | 7.5 | 4.0 | 9.2 | 11.7 | 12.0 | 18.7 | 10.5 | 18.2 | 14.1 | 11.9 | 12.0 | 12.2 | 14.7 | 18.7 | 21.9 | 24.1 | 23.9 | 20.4 | 17.2 | 9.0 | 6.7 | 5.4 | 5.5 | 13.2 |
| 22 |  | 5.0 | 5.4 | 5.9 | 12.0 | 11.5 | 13.2 | 12.6 | 12.7 | 26.9 | 24.9 | 25.7 | 20.7 | 15.2 | 14.9 | 18.7 | 19.9 | 21.9 | 22.1 | 20.7 | 13.2 | 10.4 | 7.2 | 5.4 | 4.7 | 14.6 |
| 23 | D | 5.9 | 8.9 | 11.0 | 11.0 | 11.9 | 12.0 | 12.7 | 12.6 | 13.7 | 13.6 | 13.4 | 14.4 | 15.2 | 16.7 | 19.1 | 23.6 | 20.4 | 22.1 | 36.8 | 33.6 | 34.1 | 32.1 | 8.7 | -8.3 | 16.5 |
| 24 | 0 | 5.0 | 4.7 | 34.5 | -34.7 | -8.2 | -2.3 | -9.7 | 12.7 | 33.4 | 40.8 | 75.8 | 37.6 | 20.6 | 15.2 | 20.4 | 25.1 | 25.4 | 24.4 | 22.7 | 2 C .2 | 18.7 | 16.9 | 15.4 | 13.6 | 15.0 |
| 25 | 0 | 12.6 | 12.0 | 11.9 | 13.6 | 13.6 | 14.1 | 13.6 | 19.9 | 24.4 | 30.4 | 22.2 | 18.2 | 23.7 | 24.4 | 23.7 | 21.9 | 21.7 | 18.4 | 13.6 | 10.4 | 10.4 | 11.5 | 12.7 | 16.2 | 17.3 |
| 26 |  | 11.9 | 14.2 | 12.4 | 12.6 | 12.9 | 12.7 | 14.1 | 16. 2 | 20.9 | 14.4 | 14.6 | 11.2 | 14.4 | 14.7 | 14.2 | 17.1 | 21.2 | 16.4 | 16.9 | 13.4 | 11.5 | 9.4 | 8.7 | 8.7 | 13.9 |
| 27 | 0 | 9.7 | 10.4 | 10.4 | 11.4 | 12.2 | 12.0 | 11.7 | 12.2 | 14.4 | 15.2 | 14.9 | 14.4 | 14.1 | 14.7 | 16.1 | 18.7 | 19.2 | 20.1 | 18.7 | 16.9 | 13.6 | 12.6 | 10.7 | 10.5 | 13.9 |
| 28 | 0 | 10.2 | 10.4 | 10.7 | 11.7 | 11.7 | 14.6 | 11.9 | 12.6 | 13.1 | 13.6 | 13.7 | 13.4 | 13.7 | 13.6 | 14.9 | 17.2 | 19.9 | 19.2 | 17.1 | 16.6 | 14.1 | 12.2 | 11.2 | 10.0 | 13.6 |
| 29 |  | 8.7 | 8.5 | 8.7 | 10.4 | 11.0 | 11.5 | 12.2 | 18.2 | 20.9 | 21.2 | 20.4 | 15.9 | 13.7 | 14.9 | 14.1 | 16.7 | 18.2 | 16.1 | 15.4 | 16.1 | 15.7 | 11.9 | 9.5 | 10.2 | 14.2 |
| 30 |  | 3.9 | 9.0 | 10.7 | 12.0 | 15.4 | 13.4 | 13.4 | 12.6 | 10.5 | 13.4 | 14.1 | 14.1 | 13.9 | 15.6 | 18.7 | 21.9 | 24.1 | 25.7 | 14.2 | 9.4 | 8.5 | 9.2 | 8.5 | 7.4 | 13.3 |
| 31 |  | 9.4 | 8.9 | 13.7 | 13.9 | 10.2 | 10.2 | 9.9 | 10.7 | 10.9 | 10.9 | 11.4 | 12.0 | 12.6 | 12.4 | 18.9 | 22.6 | 23.6 | 23.7 | 18.6 | 9.0 | 7. 5 | 9.4 | 10.0 | 10.2 | 12.9 |





| HOU |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | T | T0 | TO | T0 | T0 | 10 | TO | T0 | T0 | 10 | 10 | 10 | TC | T0 | T0 | TC | IC | T0 | T0 | T0 | 10 | T0 | 10 | 10 | 10 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |  |
| 1 |  | 676 | 664 | 665 | 665 | 661 | 661 | 660 | 660 | 660 | 660 | 659 | 660 | 660 | 658 | 660 | 660 | 660 | 651 | 648 | 648 | 659 | 664 | 681 | 683 | 662 |
| 2 |  | 705 | 712 | 711 | 741 | 701 | 672 | 661 | 660 | $6 \in 1$ | 659 | 648 | 622 | 590 | 636 | 658 | 670 | 669 | 664 | 666 | 669 | 672 | 672 | 671 | 670 | 669 |
| 3 | 0 | 666 | 663 | 664 | 664 | 663 | 663 | 660 | 660 | 660 | 660 | 660 | 660 | 658 | 658 | 659 | 660 | 660 | 664 | 663 | 663 | 664 | 664 | 664 | 663 | 662 |
| 4 | 0 | 661 | 660 | 660 | 660 | 660 | 660 | 660 | 659 | 659 | 659 | 659 | 658 | 658 | 657 | 660 | 660 | 659 | 657 | 651 | 660 | 664 | 69C | 685 | 681 | 663 |
| 5 |  | 670 | 660 | 660 | 660 | 659 | 659 | 659 | 657 | 658 | 660 | 655 | 593 | 577 | 631 | 640 | 645 | 643 | 649 | 651 | 658 | 659 | 66C | 68 C | 665 | 650 |
| 6 |  | 663 | 663 | 671 | 671 | 675 | 672 | 668 | 637 | 649 | 647 | 552 | 564 | 642 | 654 | 658 | 648 | 648 | 648 | 661 | 661 | 661 | 666 | 666 | 671 | 651 |
| 7 |  | 672 | 694 | 696 | 700 | 701 | 727 | 707 | 695 | 680 | 646 | 634 | 652 | 648 | 588 | 540 | 583 | 629 | 636 | 651 | 659 | 683 | 689 | 669 | 681 | 661 |
| 8 |  | 680 | 692 | 704 | 696 | 694 | 700 | 677 | 675 | 652 | 599 | 647 | 634 | 629 | 663 | 669 | 664 | 664 | 664 | 664 | 668 | 672 | 671 | 678 | 686 | 668 |
| 9 |  | 693 | 684 | 684 | 684 | 696 | 696 | 670 | 660 | 629 | 610 | 660 | 653 | 616 | 587 | 578 | 634 | 672 | 668 | 660 | 672 | 674 | 672 | 663 | 659 | 657 |
| 10 | 0 | 665 | 660 | 661 | 671 | 676 | 675 | 676 | 674 | 652 | 604 | 657 | 660 | 660 | 66 C | 660 | 659 | 657 | 655 | 648 | 659 | 659 | 66 C | 66 C | 660 | 660 |
| 11 |  | 660 | 663 | 664 | 675 | 669 | 688 | 686 | 665 | $6 C 9$ | 574 | 612 | 507 | 488 | 580 | 615 | 646 | 669 | 663 | 657 | 689 | 748 | 743 | 736 | 728 | 650 |
| 12 | 0 | 681 | 719 | 612 | 667 | 731 | 648 | 555 | 541 | 640 | 731 | 662 | 682 | 673 | 649 | 648 | 637 | 640 | 664 | 685 | 682 | 684 | 676 | 677 | 678 | 661 |
| 13 |  | 677 | 695 | 689 | 676 | 671 | 666 | 666 | 661 | 665 | 665 | 660 | 637 | 647 | 662 | 666 | 662 | 660 | 660 | 666 | 672 | 673 | 683 | 68¢ | 689 | 669 |
| 14 |  | 684 | 689 | 707 | 701 | 687 | 682 | 676 | 673 | 670 | 662 | 643 | 648 | 658 | 656 | 654 | 653 | 653 | 655 | 661 | 666 | 673 | 677 | 685 | 687 | 671 |
| 15 |  | 700 | 724 | 747 | 770 | 762 | 682 | 689 | 684 | 587 | 551 | 636 | 551 | 573 | 576 | 561 | 558 | 599 | 649 | 656 | 673 | 676 | 689 | 685 | 685 | 653 |
| 16 |  | 676 | 671 | 671 | 677 | 696 | 661 | 634 | 694 | 746 | 632 | 519 | 662 | 660 | 671 | 678 | 675 | 670 | 669 | 666 | 665 | 670 | 671 | 673 | 684 | 666 |
| 17 | D | 697 | 753 | 768 | 717 | 701 | 585 | 696 | 683 | 665 | 589 | 6 Cl | 614 | 548 | 561 | 685 | 682 | 641 | 600 | 636 | 673 | 699 | 731 | 68 E | 673 | 662 |
| 18 |  | 670 | 672 | 677 | 697 | 711 | 7 CO | 575 | 593 | 618 | 569 | 576 | 635 | 662 | 673 | 673 | 666 | 661 | 658 | 664 | 666 | 673 | 684 | 685 | 677 | 656 |
| 19 |  | 672 | 673 | 669 | 671 | 667 | 665 | 665 | 620 | 575 | 652 | 664 | 662 | 664 | 664 | 666 | 661 | 661 | 661 | 661 | 664 | 666 | 671 | 673 | 695 | 661 |
| 20 |  | 730 | 709 | 730 | 705 | 673 | 685 | 672 | 575 | 685 | 637 | 623 | 675 | 661 | 661 | 661 | 66C | 649 | 849 | 652 | 661 | 675 | 707 | 738 | 744 | 676 |
| 21 |  | 721 | 709 | 721 | 706 | 708 | 735 | 675 | 495 | 610 | 610 | 608 | 612 | 653 | 670 | 670 | 673 | 673 | 667 | 662 | 672 | 675 | 685 | 701 | 681 | 666 |
| 22 |  | 684 | 690 | 700 | 721 | 697 | 673 | 669 | 662 | 593 | 555 | 597 | 613 | 591 | 612 | 623 | 623 | 649 | 658 | 660 | 661 | 667 | 688 | 694 | 694 | 653 |
| 23 | D | 690 | 684 | 666 | 662 | 669 | 665 | 865 | 654 | 654 | 648 | 650 | 660 | 660 | 659 | 658 | 641 | 630 | 636 | 638 | 636 | 672 | 701 | 635 | 413 | 648 |
| 24 | D | 334 | 478 | 435 | 519 | 576 | 532 | 653 | 624 | 731 | 702 | 1116 | 1079 | 700 | 709 | 724 | 735 | 712 | 717 | 769 | 711 | 706 | 703 | 7 CC | 696 | 679 |
| 25 | D | 696 | 690 | 691 | 691 | 691 | 695 | 683 | 660 | 728 | 658 | 640 | 697 | 649 | 653 | 642 | 671 | 667 | 673 | 673 | 685 | 684 | 685 | 708 | 728 | 681 |
| 26 |  | 701 | 706 | 684 | 678 | 682 | 684 | 678 | 676 | 658 | 677 | 629 | 601 | 642 | 673 | 655 | 66 C | 673 | 670 | 675 | 673 | 677 | 687 | 693 | 695 | 672 |
| 27 | Q | 696 | 684 | 677 | 682 | 678 | 685 | 682 | 671 | 650 | 658 | 660 | 661 | 669 | 673 | 675 | 677 | 677 | 676 | 676 | 676 | 676 | 676 | 676 | 673 | 674 |
| 28 | 0 | 676 | 673 | 673 | 673 | 673 | 673 | 677 | 675 | 672 | 670 | 667 | 669 | 670 | 669 | 670 | 670 | 671 | 666 | 666 | 670 | 667 | 662 | 664 | 664 | 670 |
| 29 |  | 665 | 664 | 664 | 664 | 665 | 672 | 687 | 646 | 617 | 588 | 613 | 658 | 642 | 646 | 649 | 642 | 666 | 664 | 672 | 682 | 676 | 684 | 701 | 750 | 661 |
| 30 |  | 732 | 684 | 677 | 675 | 693 | 677 | 677 | 671 | 647 | 623 | 659 | 661 | 666 | 670 | 672 | 673 | 672 | 667 | 676 | 685 | 684 | 69 C | 684 | 683 | 675 |
| 31 |  | 679 | 685 | 701 | 684 | 669 | 665 | 666 | 647 | 6C1 | 608 | 619 | 626 | 640 | 650 | 653 | 667 | 664 | 669 | 670 | 678 | 678 | 677 | 673 | 673 | 660 |
| MEAN | A | 673 | 680 | 677 | 681 | 682 | 671 | 665 | 649 | 651 | 634 | 648 | 651 | 637 | 646 | 651 | 655 | 659 | 660 | 663 | 669 | $67 t$ | 683 | 683 | 678 | 663 |
| MEAN | 0 | 673 | 668 | 667 | 670 | 670 | 671 | 671 | 668 | 659 | 650 | 661 | 662 | 663 | 663 | 665 | 665 | 665 | 664 | 661 | 665 | $t \in E$ | 671 | 671 | 668 | 666 |
| MEAN | D | 620 | 665 | 635 | 651 | 674 | 625 | 650 | 632 | 683 | 666 | 732 | 747 | 646 | 646 | 671 | 673 | 658 | 658 | 689 | 677 | 685 | 699 | 681 | 638 | 666 |


|  |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 2 C | 21 | 22 | 23 | MEAN |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | T | T0 | TO | 10 | T0 | TO | TO | T0 | T0 | 10 | T0 | 10 | T0 | 10 | T0 | 10 | TO | 10 | 10 | T0 | 10 | TO | T0 | IC | T0 |  |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 22 | 24 |  |
| 1 | D | 735 | 741 | 743 | 749 | 747 | 760 | 777 | 779 | 743 | 629 | 591 | 699 | 714 | 748 | 758 | 742 | 690 | 616 | 658 | E66 | 657 | 722 | 775 | 710 | 715 |
| 2 |  | 731 | 732 | 728 | 733 | 733 | 735 | 733 | 735 | 735 | 735 | 726 | 724 | 721 | 714 | 735 | 717 | 668 | 635 | 673 | 691 | 706 | 724 | 758 | 821 | 723 |
| 3 |  | 896 | 909 | 760 | 782 | 732 | 715 | 708 | 693 | 711 | 726 | 728 | 725 | 711 | 729 | 726 | 715 | 690 | 683 | 671 | 693 | 700 | 704 | 718 | 730 | 731 |
| 4 |  | 732 | 738 | 742 | 747 | 756 | 746 | 727 | 716 | 613 | 616 | 643 | 638 | 624 | 701 | 749 | 731 | 727 | 710 | 689 | 684 | 695 | 704 | 694 | 725 | 702 |
| 5 |  | 737 | 725 | 732 | 742 | 737 | 740 | 660 | 662 | 694 | 676 | 718 | 740 | 739 | 739 | 741 | 739 | 714 | 712 | 701 | 704 | 701 | 689 | 71C | 726 | 716 |
| 6 |  | 746 | 746 | 756 | 751 | 750 | 743 | 741 | 735 | 736 | 746 | 743 | 743 | 739 | 733 | 730 | 721 | 725 | 707 | 688 | 683 | 678 | 719 | 709 | 732 | 729 |
| 7 |  | 802 | 778 | 779 | 835 | 814 | 772 | 659 | 607 | 685 | 701 | 719 | 701 | 639 | 655 | 702 | 735 | 702 | 690 | 674 | 704 | 701 | 712 | 707 | 733 | 717 |
| 8 |  | 736 | 745 | 738 | 735 | 726 | 722 | 725 | 726 | 726 | 726 | 711 | 731 | 720 | 710 | 724 | 724 | 717 | 711 | 706 | 701 | 754 | 711 | 717 | 700 | 720 |
| 9 |  | 724 | 722 | 736 | 745 | 755 | 814 | 811 | 735 | 725 | 663 | 635 | 635 | 643 | 657 | 681 | 670 | 671 | 693 | 683 | 676 | 720 | 706 | 714 | 733 | 706 |
| 10 | 0 | 716 | 725 | 729 | 735 | 737 | 753 | 757 | 646 | 727 | 721 | 698 | 706 | 737 | 732 | 724 | 724 | 704 | 676 | 690 | 706 | 706 | 712 | 717 | 727 | 717 |
| 11 |  | 715 | 736 | 737 | 742 | 756 | 746 | 770 | 779 | 617 | 650 | 678 | 690 | 669 | 750 | 757 | 740 | 716 | 897 | 692 | 7 Cl | 711 | 723 | 722 | 723 | 717 |
| 12 |  | 725 | 727 | 728 | 732 | 733 | 737 | 734 | 736 | 737 | 739 | 742 | 738 | 744 | 743 | 748 | 743 | 731 | 716 | 712 | 715 | 126 | 759 | 727 | 795 | 736 |
| 13 | D | 856 | 888 | 813 | 734 | 765 | 827 | 798 | 779 | 772 | 739 | 678 | 663 | 653 | 598 | 593 | 644 | 667 | 628 | 634 | 672 | 719 | 793 | 861 | 881 | 736 |
| 14 |  | 868 | 1056 | 803 | 701 | 703 | 719 | 710 | 720 | 723 | 715 | 715 | 682 | 656 | 727 | 731 | 699 | 705 | 688 | 688 | 703 | 731 | 775 | 761 | 773 | 740 |
| 15 |  | 794 | 740 | 737 | 764 | 773 | 737 | 664 | 716 | 566 | 640 | 613 | 534 | 634 | 738 | 736 | 737 | 111 | 700 | 690 | 691 | 699 | 712 | 713 | 720 | 698 |
| 16 |  | 723 | 738 | 744 | 756 | 780 | 783 | 545 | 650 | 700 | 726 | 692 | 607 | 612 | 723 | 722 | 713 | 710 | 681 | 695 | 692 | 713 | $76 C$ | 759 | 780 | 709 |
| 17 | D | 791 | 847 | 820 | 715 | 723 | 758 | 539 | 567 | 582 | 628 | 546 | 584 | 625 | 624 | 658 | 613 | 651 | 687 | 676 | 670 | 127 | 728 | 748 | 785 | 679 |
| 18 |  | 822 | 835 | 893 | 759 | 737 | 717 | 645 | 680 | 727 | 733 | 727 | 711 | 678 | 716 | 729 | 726 | 717 | 701 | 695 | 694 | 695 | 723 | 723 | 710 | 729 |
| 19 | 0 | 736 | 738 | 739 | 726 | 728 | 732 | 734 | 734 | 736 | 736 | 738 | 739 | 737 | 713 | 736 | 734 | 716 | 694 | 690 | 702 | 706 | 716 | 727 | 716 | 725 |
| 20 |  | 747 | 728 | 733 | 726 | 736 | 737 | 739 | 738 | 737 | 737 | 740 | 743 | 736 | 736 | 738 | 736 | 720 | 702 | 701 | 701 | 710 | 702 | 716 | 719 | 727 |
| 21 | 0 | 741 | 727 | 715 | 728 | 736 | 736 | 738 | 734 | 736 | 740 | 744 | 744 | 747 | 749 | 749 | 747 | 736 | 725 | 719 | 716 | 709 | 710 | 726 | 721 | 732 |
| 22 |  | 738 | 746 | 756 | 760 | 760 | 770 | 779 | 783 | 746 | 756 | 749 | 702 | 747 | 758 | 758 | 761 | 743 | 728 | 719 | 116 | 706 | 711 | 721 | 725 | 743 |
| 23 | 0 | 728 | 742 | 736 | 739 | 744 | 743 | 740 | 741 | 749 | 749 | 747 | 748 | 734 | 718 | 746 | 747 | 726 | 720 | 715 | 716 | 712 | 712 | 715 | 733 | 734 |
| 24 |  | 736 | 756 | 742 | 742 | 759 | 747 | 756 | 752 | 750 | 752 | 752 | 752 | 754 | 759 | 762 | 759 | 736 | 733 | 716 | 710 | 716 | 721 | 725 | 730 | 742 |
| 25 |  | 782 | 737 | 736 | 744 | 739 | 739 | 754 | 752 | 752 | 749 | 750 | 743 | 730 | 736 | 734 | 726 | 733 | 723 | 710 | 711 | 713 | 723 | 747 | 743 | 738 |
| 26 | 0 | 739 | 748 | 747 | 746 | 739 | 742 | 743 | 747 | 747 | 749 | 750 | 748 | 746 | 747 | 748 | 738 | 736 | 718 | 718 | 711 | 123 | 722 | 721 | 743 | 738 |
| 27 |  | 757 | 769 | 743 | 737 | 747 | 744 | 739 | 738 | 746 | 726 | 681 | 717 | 753 | 746 | 717 | 738 | 737 | 716 | 715 | 117 | 717 | 726 | 728 | 746 | 733 |
| 28 | D | 749 | 756 | 759 | 777 | 803 | 583 | 613 | 164 | 303 | 715 | 386 | 508 | 481 | 330 | 581 | 736 | 768 | 753 | 739 | 747 | 740 | 747 | 747 | 739 | 634 |
| 29 |  | 734 | 732 | 730 | 725 | 727 | 721 | 729 | 738 | 739 | 733 | 727 | 736 | 726 | 723 | 739 | 713 | 695 | 708 | 718 | 701 | 706 | 738 | 778 | 827 | 731 |
| 30 | D | 769 | 772 | 803 | 813 | 814 | 591 | 650 | 725 | 572 | 572 | 680 | 713 | 665 | 593 | 605 | 648 | 715 | 720 | 717 | 722 | 73 e | 762 | 76: | 750 | 703 |





| HOUR |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 2 C | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | T | T0 | T0 | T0 | T0 | T0 | T0 | TO | T0 | 10 | T0 | TO | T0 | T0 | 10 | 10 | 10 | T0 | T0 | 10 | T0 | 10 | TO | TC | T0 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 11 | 18 | 19 | 20 | 21 | 22 | 22 | 24 |  |
| 1 | D | 10.0 | 9.0 | 9.5 | 8.9 | 11.9 | 6.5 | 8.2 | 11.4 | 11.4 | 14.4 | 17.6 | 21.9 | 25.2 | 18.7 | 20.1 | 21.9 | 27.1 | 17.1 | 20.6 | 10.9 | 3.2 | 4.9 | 11.7 | 7.7 | 13.7 |
| 2 |  | 6.5 | 9.0 | 10.4 | 9.0 | 10.5 | 10.7 | 11.4 | 12.0 | 12.9 | 13.6 | 13.7 | 18.2 | 15.2 | 15.1 | 22.1 | 25.4 | 23.4 | 14.2 | 8.0 | 13.7 | 14.9 | 7.0 | 3.2 | 1.7 | 12.6 |
| 3 |  | 2.5 | -3.8 | 4.0 | 6.7 | 10.7 | 11.5 | 13.7 | 11.7 | 12.2 | 14.1 | 13.7 | 13.7 | 12.9 | 16.6 | 20.4 | 24.2 | 25.4 | 22.6 | 20.6 | 18.6 | 10.7 | 8.2 | 5.5 | 7.0 | 12.7 |
| 4 |  | 5.5 | 7.5 | 10.7 | 13.7 | 11.0 | 9.9 | 10.7 | 12.6 | 11.2 | 9.0 | 18.1 | 13.4 | 13.7 | 13.9 | 18.2 | 20.1 | 22.2 | 23.9 | 21.7 | 17.7 | 14.1 | 10.9 | 7.4 | 7.5 | 13.6 |
| 5 |  | 8.0 | 10.7 | 11.4 | 12.2 | 12.9 | 15.4 | 3.9 | 19.7 | 18.1 | 20.6 | 20.7 | 17.1 | 17.9 | 18.1 | 19.1 | 20.2 | 21.6 | 18.2 | 14.9 | 13.6 | 10.9 | 8.5 | 6.5 | 5.4 | 14.4 |
| 6 |  | 5.2 | 6.2 | 6.2 | 5.0 | 4.7 | 8.9 | 8.4 | 10.5 | 14.2 | 11.7 | 10.5 | 10.9 | 11.5 | 13.1 | 16.9 | 19.2 | 18.4 | 20.4 | 18.6 | 12.9 | 6.5 | 5.0 | 4.4 | 1.2 | 10.4 |
| 7 |  | . 5 | 3.0 | -0.0 | 4.5 | 5.2 | 2.2 | 13.2 | 6.7 | 18.4 | 16.4 | 12.5 | 13.2 | 13.2 | 16.4 | 18.4 | 19.2 | 18.7 | 15.4 | 13.2 | 11.3 | t. 8 | 7.2 | 8.1 | 4.3 | 10.3 |
| 8 |  | 5.5 | 4.7 | 6.2 | 10.3 | 10.3 | 10.7 | 10.3 | 11.7 | 13.0 | 13.2 | 11.7 | 11.8 | 13.0 | 13.2 | 14.5 | 15.5 | 15.4 | 15.9 | 14.4 | 13.2 | 10.5 | 8.3 | 5.7 | 8.3 | 11.1 |
| 9 |  | 3.1 | 7.9 | 7.9 | 7.6 | 7.1 | 1.9 | 6.7 | 11.9 | 14.6 | 21.6 | 24.1 | 26.8 | 31.3 | 26.8 | 24.9 | 17.3 | 15.3 | 13.1 | 11.9 | 8.4 | 7.1 | 3.7 | 7.5 | 7.1 | 13.2 |
| 10 | 0 | 9.7 | 8.2 | 8.7 | 9.4 | 8.6 | 8.2 | 8.2 | 7.7 | 16.4 | 17.8 | 14.8 | 18.1 | 17.8 | 16.9 | 17.9 | 18.8 | 19.6 | 11.9 | 7.7 | 7.4 | 8.2 | 4.4 | 2.5 | 1.7 | 11.3 |
| 11 |  | 4.2 | 8.2 | 7.9 | 8.7 | 6.2 | 7.4 | 4.4 | 3.1 | 19.6 | 22.6 | 21.4 | 17.1 | 22.6 | 20.1 | 19.8 | 18.9 | 19.6 | 17.3 | 11.7 | 9.6 | 9.1 | 8.6 | 9.4 | 8.6 | 12.8 |
| 12 |  | 8.6 | 8.7 | 9.6 | 9.9 | 9.9 | 9.2 | 9.9 | 10.1 | 10.2 | 14.4 | 11.6 | 10.7 | 13.6 | 16.1 | 17.8 | 18.3 | 19.6 | 20.1 | 12.6 | 11.1 | 11.1 | 14.8 | 6.4 | 7.9 | 12.2 |
| 13 | D | -0.1 | $-1.6$ | 3.4 | 6.4 | 6.1 | $-2.3$ | 5.4 | . 4 | 5.1 | 8.2 | 14.9 | 18.4 | 19.9 | 24.8 | 36.5 | 33.3 | 31.1 | 31.0 | 13.3 | 10.4 | 13.6 | 13.1 | 7.1 | 4.4 | 12.6 |
| 14 |  | 1.1 | 13.8 | 6.4 | 9.9 | 9.9 | 9.4 | 10.2 | 11.2 | 10.2 | 11.6 | 12.6 | 12.7 | 16.4 | 17.9 | 20.3 | 23.4 | 22.3 | 20.3 | 15.3 | 10.7 | $12 . t$ | 10.6 | 5.1 | 1.9 | 11.2 |
| 15 |  | 2.4 | 5.2 | 8.4 | 10.7 | 14.8 | 13.8 | 8.4 | 11.4 | 3.9 | 10.2 | 14.4 | 6.6 | 17.9 | 22.4 | 23.4 | 23.1 | 21.4 | 18.1 | 11.6 | 10.1 | 6.6 | 6.6 | 6.4 | 6.7 | 11.9 |
| 16 |  | 6.4 | 6.4 | 7.6 | 6.6 | 5.2 | 5.4 | -0.1 | 13.4 | 14.4 | 13.3 | 14.9 | 19.8 | 16.9 | 20.6 | 23.8 | 24.4 | 22.3 | 21.6 | 10.4 | 9.7 | 10.t | 5.4 | 2.7 | -0.3 | 11.7 |
| 17 | D | . 4 | -3.1 | -2.3 | 11.7 | 11.2 | 6.7 | $-3.3$ | 11.4 | 18.4 | 13.6 | 12.4 | 23.6 | 24.4 | 23.1 | 23.3 | 25.3 | 19.3 | 16.6 | 11.6 | 4.2 | 5.2 | 4.4 | 2.7 | 3.1 | 11.0 |
| 18 |  | 2.1 | -0.7 | -0.4 | 8.3 | 10.0 | 20.7 | 11.3 | 14.7 | 12.8 | 12.3 | 11.3 | 11.5 | 12.6 | 11.8 | 16.3 | 17.7 | 18.5 | 18.3 | 13.1 | 11.0 | 6.5 | 4.6 | 3.6 | 5.8 | 10.6 |
| 19 | 0 | 4.6 | 9.5 | 9.5 | 9.8 | 12.0 | 12.6 | 11.3 | 11.0 | 11.5 | 11.5 | 11.5 | 11.8 | 12.0 | 14.7 | 18.7 | 21.5 | 21.5 | 18.7 | 14.8 | 10.1 | 7.1 | 5.8 | 4.5 | 5.1 | 11.7 |
| 20 |  | 3.6 | 8.0 | 8.1 | 10.1 | 11.1 | 10.8 | 15.2 | 13.5 | 12.8 | 12.0 | 12.6 | 13.0 | 13.3 | 16.2 | 18.5 | 21.3 | 23.2 | 22.3 | 16.5 | 15.5 | 11.5 | 7.5 | 5.6 | 6.3 | 12.9 |
| 21 | 0 | 6.0 | 6.8 | 10.1 | 11.5 | 11.5 | 11.5 | 12.1 | 12.0 | 11.6 | 11.6 | 10.8 | 11.5 | 13.1 | 14.8 | 16.7 | 19.8 | 21.5 | 21.3 | 17.3 | 11.6 | 7.3 | 5.3 | $4 . t$ | 4.3 | 11.9 |
| 22 |  | 3.5 | 3.6 | 4.5 | 5.3 | 6.1 | 5.1 | 5.3 | 9.6 | 13.3 | 15.0 | 9. 8 | 8.1 | 16.0 | 16.3 | 16.5 | 19.8 | 21.7 | 22.3 | 18.8 | 13.5 | 10.0 | 7.1 | 6.2 | 6.3 | 11.0 |
| 23 | 0 | $7 \cdot 5$ | 9.8 | 11.1 | 9.8 | 11.1 | 11.8 | 14.3 | 11.5 | 13.1 | 11.3 | 11.5 | 11.6 | 9.8 | 13.1 | 17.8 | 20.2 | 22.2 | 21.5 | 16.0 | 14.8 | 10.3 | 6.8 | 5.1 | 4.3 | 12.4 |
| 24 |  | 4.5 | 6.5 | 9.3 | 11.8 | 8.1 | 5.5 | 17.3 | 11.3 | 11.3 | 11.3 | 11.8 | 13.c | 14.8 | 18.0 | 19.3 | 20.8 | 22.0 | 20.8 | 16.7 | 13.8 | 8.6 | 7.3 | 7.C | 7.5 | 12.4 |
| 25 |  | 4.3 | 11.3 | 9.5 | 9.8 | 9.8 | 11.5 | 15.3 | 14.5 | 11.3 | 11.0 | 11.0 | 11.3 | 11.5 | 15.5 | 17.7 | 18.7 | 18.7 | 17.8 | 14.3 | 10.0 | 8.0 | 6.8 | 6.8 | 8.1 | 11.8 |
| 26 | 0 | 8.8 | 11.3 | 14.8 | 9.8 | 9.8 | 10.8 | 11.5 | 11.5 | 11.5 | 10.5 | 11.3 | 12.8 | 13.3 | 20.2 | 20.0 | 20.3 | 19.7 | 19.7 | 18.0 | 10.5 | 6.6 | 5.3 | 6.1 | 6.5 | 12.5 |
| 27 |  | 7.5 | 8.0 | 13.7 | 15.5 | 14.3 | 13.7 | 14.3 | 15.0 | 13.0 | 11.5 | 16.0 | 16.7 | 16.0 | 16.7 | 18.0 | 19.2 | 18.3 | 18.2 | 14.7 | 8.8 | 6.6 | 5.1 | 4.6 | 5.3 | 12.9 |
| 28 | 0 | 6.0 | 6.2 | 6.7 | 6.4 | 3.0 | -25.4 | -9.0 | 4.0 | . 5 | 21.4 | 48.6 | 48.3 | 44.8 | 55.5 | 26.2 | 20.2 | 22.2 | 19.6 | 8.5 | 7.9 | 6.7 | 8.2 | 9.7 | 8.9 | 14.8 |
| 29 |  | 9.5 | 8.2 | 9.5 | 9.7 | 9.5 | 10.4 | 12.9 | 11.4 | 11.7 | 13.4 | 13.6 | 16.2 | 18.2 | 21.6 | 23.2 | 25.7 | 23.1 | 18.1 | 14.2 | 11.4 | 5.9 | 4.2 | 2.5 | 4.2 | 12.9 |
| 30 | 0 | 3.4 | 2.9 | 3.5 | 1.5 | 6.9 | 2.7 | 13.0 | 14.1 | 11.4 | 10.0 | 11.9 | 12.0 | 16.4 | 9.5 | 13.2 | 12.5 | 12.9 | 12.7 | 12.9 | 6.2 | 3.4 | 5.4 | 6.7 | 5.9 | 8.8 |
| MEAN | A | 5.0 | 5.5 | 7.5 | 9.0 | 9.3 | 7.9 | 9.2 | 11.0 | 12.3 | 13.6 | 15.0 | 15.7 | 17.2 | 18.6 | 20.0 | 20.9 | 20.9 | 19.0 | 14.5 | 11.3 | 8.7 | 7.0 | 5.9 | 5.4 | 12.1 |
| MEAN | C | 7.3 | 9.1 | 10.9 | 10.1 | 10.6 | 11.0 | 11.5 | 10.7 | 12.8 | 12.5 | 12.0 | 13.2 | 13.2 | 15.9 | 18.2 | 20.1 | 20.9 | 18.6 | 14.8 | 10.9 | 7.9 | 5.5 | 4.7 | 4.4 | 12.0 |
| MEAN | D | 3.9 | 2.7 | 4.2 | 7.0 | 7.8 | $-2.3$ | 2.9 | 8.3 | 9.4 | 13.5 | 21.1 | 24.9 | 26.2 | 26.3 | 23.9 | 22.6 | 22.5 | 19.4 | 13.4 | 7.9 | 6.4 | 7.2 | 7.E | 6.0 | 12.2 |


| HOUR |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | T | TO | T0 | TO | 10 | T0 | TO | 10 | T0 | T0 | T0 | TO | T0 | 10 | TO | TO | 10 | 10 | ro | TO | 10 | T0 | T0 | TC | ro | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |  |
| 1 | D | 670 | 666 | 671 | 687 | 700 | 701 | 713 | 715 | 662 | 570 | 565 | 587 | 622 | 660 | 670 | 667 | 662 | 641 | 664 | 754 | 749 | 731 | 75 C | 688 | 674 |
| 2 |  | 693 | 695 | 685 | 688 | 683 | 673 | 676 | 672 | 666 | 662 | 649 | 624 | 644 | 632 | 652 | 659 | 653 | 649 | 654 | 672 | 723 | 760 | 754 | 772 | 679 |
| 3 |  | 723 | 719 | 730 | 737 | 702 | 884 | 661 | 625 | 649 | 666 | 672 | 666 | 647 | 662 | 670 | 664 | 665 | 678 | 673 | 709 | 712 | 701 | 705 | 700 | 684 |
| 4 |  | 697 | 713 | 713 | 659 | 699 | 709 | 650 | 661 | 585 | 552 | 567 | 597 | 588 | 634 | 678 | 675 | 683 | 683 | 679 | 681 | 691 | 693 | 675 | 693 | 661 |
| 5 |  | 685 | 682 | 673 | 675 | 672 | 673 | 548 | 581 | 636 | 619 | 634 | 658 | 661 | 665 | 669 | 664 | 654 | 676 | 670 | 677 | 681 | 677 | 677 | 677 | 658 |
| 6 |  | 690 | 689 | 687 | 694 | 712 | 693 | 675 | 673 | 6 CB | 660 | 670 | 664 | 664 | 661 | 660 | 658 | 661 | 659 | 658 | 665 | 665 | 677 | 687 | 713 | 673 |
| 7 |  | 753 | 734 | 754 | 750 | 701 | 628 | 684 | 638 | 637 | 649 | 654 | 640 | 569 | 575 | 613 | 664 | 672 | 667 | 675 | 702 | 673 | 676 | 672 | 683 | 669 |
| 8 |  | 697 | 706 | 701 | 695 | 688 | 673 | 672 | 670 | $6 \in 2$ | 653 | 619 | 660 | 660 | 652 | 653 | 656 | 658 | 661 | 662 | 664 | 671 | 676 | 69C | 673 | 670 |
| 9 |  | 674 | 673 | 677 | 685 | 701 | 733 | 714 | 695 | 660 | 579 | 511 | 543 | 549 | 55 C | 544 | 547 | 565 | 624 | 660 | 674 | 714 | 696 | 677 | 677 | 638 |
| 10 | 0 | 673 | 673 | 673 | 673 | 674 | 683 | 695 | 594 | 650 | 638 | 623 | 601 | 649 | 661 | 657 | 666 | 672 | 660 | 659 | 672 | 685 | 685 | 69 C | 696 | 663 |
| 11 |  | 694 | 677 | 678 | 686 | 695 | 696 | 7 C 2 | 617 | 598 | 623 | 606 | 592 | 554 | 638 | 674 | 685 | 688 | 685 | 682 | 678 | 676 | 671 | 674 | 674 | 660 |
| 12 |  | 674 | 673 | 671 | 671 | 671 | 674 | 676 | 676 | 672 | 666 | 670 | 665 | 666 | 667 | 674 | 674 | 673 | 676 | 673 | 673 | 671 | 674 | 674 | 703 | 673 |
| 13 | D | 787 | 855 | 806 | 712 | 713 | 706 | 654 | 629 | 691 | 678 | 639 | 618 | 598 | 554 | 519 | 539 | 592 | 638 | 666 | 713 | 738 | 790 | BC7 | 807 | 685 |
| 14 |  | 792 | 775 | 749 | 688 | 678 | 679 | 674 | 674 | 674 | 666 | 654 | 635 | 618 | 662 | 673 | 667 | 674 | 676 | 668 | 680 | 704 | 753 | 751 | 756 | 693 |
| 15 |  | 774 | 741 | 704 | 722 | 700 | 672 | 691 | 643 | 464 | 543 | 607 | 619 | 542 | 655 | 671 | 679 | 678 | 676 | 686 | 678 | 676 | 676 | 674 | 674 | 660 |
| 16 |  | 674 | 680 | 686 | 708 | 729 | 708 | 582 | 661 | 627 | 647 | 637 | 607 | 606 | 648 | 654 | 659 | 672 | 674 | 676 | 673 | 690 | 748 | 725 | 726 | 671 |
| 17 | D | 753 | 771 | 815 | 721 | 692 | 672 | 688 | 574 | 594 | 636 | 576 | 591 | 539 | 506 | 570 | 611 | 650 | E74 | 673 | 685 | 695 | 694 | 703 | 719 | 658 |
| 18 |  | 741 | 759 | 708 | 716 | 721 | 626 | 527 | 570 | 650 | 665 | 665 | 655 | 644 | 667 | 676 | 684 | 686 | 685 | 677 | 674 | 670 | 676 | 696 | 694 | 672 |
| 19 | $Q$ | 698 | 701 | 685 | 673 | 666 | 665 | 663 | 663 | 663 | 663 | 663 | 665 | 662 | 650 | 654 | 662 | 666 | 665 | 661 | 661 | 662 | 666 | 675 | 680 | 668 |
| 20 |  | 696 | 689 | 682 | 670 | 666 | 666 | 673 | 671 | 662 | 661 | 661 | 661 | 659 | 655 | 659 | 660 | 661 | 655 | 650 | 650 | 653 | 659 | 677 | 698 | 666 |
| 21 | 0 | 715 | 690 | 677 | 674 | 672 | 671 | 671 | 668 | 661 | 660 | 654 | 665 | 665 | 663 | 661 | 659 | 659 | 661 | 654 | 650 | 650 | 655 | 672 | 677 | 667 |
| 22 |  | 684 | 668 | 661 | 660 | 660 | 660 | 673 | 663 | 650 | 655 | 653 | 613 | 631 | 662 | 862 | 663 | 654 | 660 | 659 | 659 | 653 | 661 | 666 | 667 | 654 |
| 23 | 0 | 664 | 671 | 665 | 665 | 666 | 672 | 666 | 648 | 658 | 661 | 659 | 661 | 652 | 622 | 637 | 652 | 652 | 650 | 653 | 652 | 659 | 66 C | 661 | 666 | 657 |
| 24 |  | 667 | 683 | 696 | 684 | 694 | 637 | 673 | 667 | 662 | 661 | 661 | 661 | 661 | 661 | 660 | 660 | 652 | 655 | 653 | 650 | 652 | 652 | 659 | 666 | 664 |
| 25 |  | 705 | 707 | 676 | 667 | 664 | 672 | 629 | 631 | 662 | 662 | 661 | 650 | 635 | 641 | 641 | 638 | 647 | 658 | 660 | 664 | 671 | 673 | 683 | 682 | 662 |
| 26 | 0 | 673 | 676 | 673 | 661 | 660 | 661 | 660 | 660 | $6 \in 0$ | 660 | 654 | 647 | 650 | 652 | 656 | 660 | 661 | 660 | 660 | 662 | 670 | 675 | $67 t$ | 684 | 663 |
| 27 |  | 685 | 701 | 700 | 676 | 672 | 677 | 669 | 661 | $6 \pm 4$ | 634 | 553 | 549 | 643 | 638 | 616 | 625 | 648 | 659 | 664 | E61 | 665 | 664 | $66 C$ | 660 | 652 |
| 28 | D | 661 | 660 | 861 | 669 | 684 | 369 | 572 | 660 | 873 | 811 | 782 | 782 | 654 | 750 | 613 | 675 | 723 | 677 | 671 | 664 | 671 | 671 | 672 | 672 | 679 |
| 29 |  | 673 | 672 | 673 | 672 | 673 | 673 | 673 | 673 | 673 | 672 | 670 | 673 | 670 | 661 | 667 | 661 | 653 | 649 | 654 | 660 | 670 | 694 | 708 | 760 | 674 |
| 30 | D | 721 | 724 | 718 | 753 | 744 | 572 | 576 | 652 | 6 Cl | 447 | 579 | 616 | 597 | 578 | 581 | 623 | 665 | 679 | 685 | 695 | 696 | 702 | 718 | 690 | 651 |
| MEAN | A | 703 | 704 | 698 | 690 | 688 | 663 | 656 | 650 | 650 | 641 | 636 | 635 | 627 | 639 | 643 | 652 | 660 | 664 | 666 | 675 | 682 | 690 | 694 | 698 | 667 |
| MEAN | 0 | 685 | 682 | 675 | 669 | 668 | 670 | 671 | 647 | 659 | 657 | 651 | 648 | 656 | 650 | 653 | 660 | 662 | 659 | 657 | 659 | 665 | 668 | 676 | 681 | 664 |
| MEAN | D | 719 | 735 | 734 | 708 | 707 | 604 | 640 | 646 | 6E8 | 628 | 628 | 639 | 602 | 610 | 590 | 623 | 659 | 662 | 672 | 702 | 710 | 718 | 730 | 715 | 670 |


| HOU |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | JT | T0 | T0 | T0 | T0 | T0 | TO | 10 | 10 | TO | T0 | 10 | 10 | 10 | 10 | TC | T0 | T0 | T0 | TO | T0 | T0 | T0 | 1 C | 10 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |  |
| 1 |  | 769 | 765 | 749 | 749 | 756 | 736 | 723 | 690 | 651 | 702 | 731 | 725 | 731 | 723 | 726 | 713 | 713 | 700 | 691 | 705 | 732 | 736 | 727 | 736 | 126 |
| 2 | 0 | 738 | 756 | 741 | 752 | 749 | 744 | 737 | 738 | 720 | 620 | 748 | 749 | 716 | 666 | 691 | 710 | 702 | 715 | 678 | 696 | 709 | 749 | 77 C | 749 | 723 |
| 3 |  | 732 | 738 | 747 | 747 | 757 | 743 | 681 | 586 | 636 | 691 | 666 | 649 | 694 | 713 | 658 | 690 | 706 | 698 | 702 | 715 | 725 | 713 | 73? | 730 | 702 |
| 4 |  | 746 | 747 | 739 | 758 | 742 | 742 | 741 | 738 | 744 | 730 | 719 | 734 | 736 | 739 | 737 | 726 | 713 | 717 | 700 | 705 | 713 | 722 | 725 | 747 | 732 |
| 5 |  | 771 | 758 | 742 | 747 | 741 | 743 | 746 | 747 | 747 | 742 | 741 | 715 | 671 | 667 | 731 | 725 | 718 | 713 | 697 | 702 | 694 | 722 | 731 | 753 | 128 |
| 6 |  | 744 | 740 | 759 | 767 | 758 | 691 | 749 | 748 | 747 | 747 | 741 | 730 | 721 | 736 | 749 | 744 | 736 | 716 | 707 | 712 | 723 | 728 | 716 | 738 | 735 |
| 7 | 0 | 769 | 769 | 764 | 753 | 752 | 747 | 751 | 747 | 620 | 691 | 147 | 744 | 748 | 751 | 748 | 744 | 740 | 733 | 730 | 731 | 725 | 72C | 715 | 727 | 736 |
| 8 |  | 736 | 752 | 752 | 752 | 749 | 754 | 760 | 749 | 749 | 748 | 751 | 756 | 758 | 764 | 747 | 762 | 760 | 747 | 749 | 742 | 741 | 738 | 758 | 736 | 750 |
| 9 |  | 743 | 750 | 760 | 758 | 749 | 760 | 747 | 746 | 653 | 709 | 746 | 751 | 736 | 763 | 763 | 747 | 737 | 725 | 718 | 713 | 713 | 758 | 757 | 740 | 739 |
| 10 |  | 767 | 741 | 762 | 759 | 773 | 779 | 785 | 622 | 634 | 732 | 748 | 721 | 757 | 747 | 751 | 742 | 740 | 721 | 722 | 731 | 727 | 731 | 730 | 748 | 736 |
| 11 | 0 | 761 | 758 | 757 | 746 | 749 | 747 | 749 | 746 | 743 | 727 | 751 | 750 | 758 | 759 | 758 | 750 | 744 | 731 | 734 | 728 | 720 | 720 | 723 | 733 | 743 |
| 12 |  | 740 | 755 | 753 | 753 | 751 | 750 | 751 | 752 | 749 | 761 | 759 | 762 | 768 | 774 | 779 | 770 | 758 | 735 | 745 | 735 | 737 | 744 | 783 | 792 | 757 |
| 13 | D | 815 | 918 | 877 | 835 | 940 | 780 | 772 | 548 | 438 | 379 | 327 | 367 | 243 | 499 | 571 | 627 | 665 | 686 | 752 | 770 | 813 | 830 | 998 | 1034 | 687 |
| 14 | 0 | 1029 | 1019 | 875 | 804 | 766 | 631 | 687 | 616 | 642 | 571 | 630 | 706 | 747 | 728 | 680 | 659 | 677 | 711 | 706 | 706 | 737 | 844 | 1028 | 1358 | 773 |
| 15 | D | 1196 | 1007 | 1111 | 993 | 823 | 645 | 619 | 701 | 543 | 77 | 113 | 133 | -78 | -97 | -223 | 34 | 150 | 468 | 655 | 785 | 813 | 88 : | 982 | 1103 | 560 |
| 16 | D | 1063 | 1019 | 939 | 719 | 687 | 660 | 265 | 447 | 678 | 247 | 469 | 530 | 568 | 737 | 743 | 750 | 737 | 735 | 737 | 724 | 721 | 733 | 735 | 762 | 684 |
| 17 |  | 763 | 792 | 836 | 872 | 871 | 838 | 495 | 567 | 668 | 658 | 683 | 678 | 671 | 704 | 737 | 747 | 738 | 729 | 711 | 104 | 723 | 757 | 758 | 766 | 728 |
| 18 |  | 973 | 862 | 776 | 748 | 770 | 749 | 510 | 687 | 6 C 5 | 547 | 606 | 742 | 770 | 770 | 748 | 750 | 745 | 726 | 720 | 708 | 703 | 721 | 751 | 729 | 726 |
| 19 |  | 759 | 738 | 743 | 741 | 742 | 748 | 749 | 749 | 748 | 750 | 748 | 724 | 659 | 676 | 710 | 765 | 747 | 741 | 728 | 723 | 714 | 717 | 744 | 748 | 734 |
| 20 |  | 781 | 780 | 780 | 747 | 748 | 747 | 729 | 748 | 751 | 747 | 757 | 755 | 753 | 761 | 757 | 769 | 772 | 755 | 735 | 748 | 735 | 725 | 732 | 769 | 753 |
| 21 |  | 771 | 789 | 792 | 781 | 783 | 757 | 730 | 701 | 710 | 670 | 516 | 504 | 589 | 669 | 589 | 702 | 752 | 737 | 740 | 735 | 742 | 730 | 754 | 770 | 709 |
| 22 |  | 773 | 758 | 762 | 761 | 750 | 747 | 754 | 752 | 745 | 691 | 617 | 561 | 582 | 667 | 720 | 724 | 760 | 769 | 759 | 737 | 733 | 728 | 737 | 748 | 722 |
| 23 |  | 764 | 772 | 755 | 750 | 748 | 748 | 748 | 729 | 749 | 7 CO | 677 | 726 | 669 | 747 | 755 | 749 | 745 | 726 | 728 | 737 | 738 | 743 | 748 | 749 | 737 |
| 24 |  | 763 | 761 | 758 | 759 | 788 | 809 | 804 | 735 | 730 | 734 | 754 | 750 | 745 | 704 | 692 | 730 | 750 | 728 | 723 | 726 | 727 | 747 | 775 | 813 | 750 |
| 25 |  | 872 | 811 | 762 | 747 | 737 | 743 | 747 | 747 | 749 | 748 | 750 | 759 | 765 | 761 | 758 | 748 | 737 | 717 | 714 | 720 | 737 | 743 | $75 ?$ | 759 | 753 |
| 26 | 0 | 759 | 760 | 752 | 752 | 743 | 747 | 750 | 753 | 757 | 759 | 748 | 742 | 765 | 769 | 766 | 751 | 735 | 716 | 702 | 703 | 723 | 737 | 751 | 754 | 746 |
| 27 | 0 | 761 | 758 | 755 | 755 | 750 | 750 | 752 | 753 | 757 | 750 | 749 | 745 | 754 | 754 | 750 | 753 | 748 | 731 | 723 | 724 | 728 | 734 | 757 | 759 | 748 |
| 28 |  | 763 | 763 | 759 | 762 | 760 | 765 | 765 | 757 | 740 | 739 | 721 | 755 | 759 | 758 | 748 | 735 | 717 | 728 | 723 | 719 | 724 | 718 | 737 | 726 | 743 |
| 29 | 0 | 751 | 755 | 751 | 752 | 748 | 751 | 755 | 750 | 757 | 751 | 749 | 742 | 745 | 740 | 747 | 731 | 726 | 713 | 712 | 714 | 726 | 720 | 762 | 781 | 743 |
| 30 |  | 761 | 770 | 758 | 755 | 766 | 769 | 755 | 750 | 688 | 723 | 757 | 72C | 682 | 750 | 754 | 727 | 690 | 737 | 739 | 735 | 737 | 739 | 755 | 751 | 740 |
| 31 |  | 783 | 780 | 763 | 783 | 758 | 690 | 750 | 748 | 722 | 730 | 748 | 737 | 685 | 716 | 738 | 753 | 138 | 742 | 734 | 739 | 745 | 737 | 755 | 779 | 744 |
| MEAN | A | 804 | 795 | 785 | 770 | 765 | 742 | 711 | 705 | 697 | 664 | 676 | 683 | 673 | 697 | 696 | 711 | 713 | 718 | 720 | 725 | 732 | 744 | 771 | 793 | 729 |
| MEAN | Q | 760 | 760 | 756 | 752 | 748 | 748 | 751 | 750 | 727 | 736 | 749 | 745 | 754 | 755 | 754 | 746 | 739 | 725 | 720 | 720 | 724 | 726 | 742 | 751 | 743 |
| ME AN | [ | 968 | 944 | 909 | 821 | 793 | 692 | 616 | 610 | 604 | 379 | 457 | 497 | 439 | 506 | 492 | 556 | 586 | 663 | 705 | 736 | 759 | 809 | 9 C 3 | 1001 | 685 |


| $\begin{aligned} & \text { HOUR } \\ & \text { UT } \end{aligned}$ |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 2 C | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | TO | TO | TO | 10 | TC | T0 | 10 | T0 | T0 | TO | 10 | T0 | T0 | TC | 10 | Ta | 10 | T0 | TO | T0 | 10 | 10 | 10 | T0 | PEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |  |
| 1 |  | 4.2 | 10.2 | 9.7 | 9.7 | 14.6 | 11.9 | 11.0 | 7.5 | 9.9 | 16.6 | 14.6 | 15.1 | 15.7 | 17.7 | 20.7 | 20.9 | 20.2 | 19.4 | 13.2 | 8.7 | 6.7 | 5.5 | 6.4 | 6.4 | 12.4 |
| 2 | 0 | 7.2 | 6.2 | 7.4 | 13.2 | 14.4 | 13.2 | 13.2 | 12.5 | 10.4 | 7.2 | 16.6 | 13.0 | 14.7 | 15.6 | 20.4 | 25.7 | 28.6 | 15.6 | 24.6 | 2.7 | 3.7 | 4.7 | 5.9 | 4.9 | 12.6 |
| 3 |  | 8.9 | 11.0 | 11.2 | 11.4 | 16.4 | 31.1 | 21.2 | 14.7 | 15.1 | 18.2 | 15.6 | 17.2 | 21.6 | 16.4 | 20.6 | 18.4 | 10. 2 | 16.7 | 10.9 | 7.4 | 7.5 | 6.5 | 4.7 | 6.2 | 14.5 |
| 4 |  | 6.7 | 7.5 | 9.7 | 9.7 | 19.6 | 9.7 | 9.7 | 10.5 | 13.0 | 12.0 | 12.5 | 14.4 | 16.6 | 18.4 | 20.6 | 20.7 | 22.2 | 18.7 | 14.4 | 8.7 | $8 . C$ | 8.0 | 6.4 | 3.0 | 12.5 |
| 5 |  | 4.4 | 7.2 | 8.0 | 8.4 | 10.2 | 10.4 | 9.9 | 11.4 | 11.4 | 10.0 | 9.7 | 8.0 | 10.0 | 9.9 | 16.4 | 21.4 | 21.1 | 19.4 | 13.2 | 9.7 | $5 . C$ | 4.5 | 4.4 | 5.5 | 10.4 |
| 6 |  | 6.4 | 6.7 | 8.0 | 8.0 | 11.7 | 8.7 | 21.4 | 16.2 | 11.5 | 11.0 | 11.5 | 13.0 | 14.2 | 17.1 | 17.6 | 2C.9 | 20.2 | 20.4 | 15.6 | 11.0 | 9.2 | 6.5 | 5.7 | 3.5 | 12.3 |
| 7 | 0 | 3.6 | 4.6 | 5.4 | 6.3 | 10.3 | 10.4 | 10.6 | 10.9 | 9.3 | 16.3 | 13.1 | 12.8 | 14.8 | 16.6 | 17.8 | 19.5 | 19.5 | 18.6 | 15.8 | 12.6 | 9.6 | 8.3 | 7.6 | 6.3 | 11.7 |
| 8 |  | 6.3 | 6.3 | 8.3 | 8.3 | 9.3 | B. 3 | 10.6 | 11.4 | 11.3 | 12.3 | 12.9 | 12.9 | 16.0 | 16.3 | 16.5 | 21.3 | 18.3 | 18.8 | 11.3 | 9.9 | 8.3 | 8.6 | 7.5 | 9.8 | 11.7 |
| 9 |  | 8.4 | 6.6 | 7.9 | 10.8 | 13.1 | 11.3 | 13.8 | 14.6 | 29.1 | 20.3 | 15.5 | 13.6 | 17.3 | 18.1 | 20.1 | 20.8 | 19.6 | 19.8 | 14.8 | 12.4 | 7.9 | 7.3 | 6.5 | 4.6 | 14.0 |
| 10 |  | 5.6 | 7.4 | 8.1 | 10.3 | 12.9 | 12.9 | 9.9 | 15.8 | 14.6 | 11.8 | 10.9 | 11.1 | 14.5 | 17.3 | 19.5 | 19.8 | 20.1 | 20.0 | 10.9 | 8.3 | 7.3 | 7.8 | 8.3 | 7.9 | 12.2 |
| 11 | 0 | 7.1 | 9.3 | 9.6 | 9.9 | 11.3 | 12.4 | 10.3 | 12.4 | 15.0 | 17.1 | 14.1 | 12.9 | 15.8 | 18.1 | 19.6 | 21.1 | 21.6 | 19.6 | 14.5 | 12.8 | 9.9 | 8.1 | 6.6 | 6.3 | 13.2 |
| 12 |  | 7.9 | 9.6 | 11.4 | 11.4 | 11.8 | 10.4 | 11.1 | 12.9 | 14.3 | 12.9 | 11.6 | 11.1 | 14.0 | 18.0 | 21.0 | 21.6 | 21.3 | 19.0 | 14.6 | 15.3 | 7.6 | 8.1 | 5.1 | 1.8 | 12.7 |
| 13 | 0 | -0.1 | -6.1 | 1.9 | 4.9 | 4.6 | 12.1 | 2.1 | 7.4 | 30.3 | 32.8 | 41.3 | 45.7 | 26.6 | 43.5 | 44.0 | 30.5 | 27.5 | 22.5 | 11.4 | 8.4 | 9.4 | 5.3 | 5.8 | 1.6 | 17.2 |
| 14 | D | $-1.7$ | -1.1 | $-1.2$ | 8.3 | 14.3 | 13.6 | 8.6 | 12.9 | 18.8 | 18.6 | 12.4 | 14.0 | 17.3 | 20.3 | 26.3 | 24.6 | 21.8 | 16.0 | 11.6 | 25.6 | 17.C | 10.3 | -1.2 | -7.6 | 12.5 |
| 15 |  | 14.6 | 13.9 | 51.7 | 4.8 | 32.1 | -6.8 | 1.6 | 1.6 | 4.3 | 78.2 | 52.7 | 47.9 | 49.0 | 33.8 | 46.7 | 50.4 | 32.5 | 32.3 | 17.0 | 19.6 | 24.5 | 19.6 | 13.6 | 13.8 | 15.5 |
| 16 | D | 9.8 | 3.3 | -3.2 | 2.6 | -1.4 | -4.9 | -1.2 | -4.4 | 14.5 | 15.1 | 9.4 | 18.1 | 15.3 | 15.8 | 19.5 | 22.6 | 22.8 | 22.3 | 17.1 | 12.4 | 7.9 | 6.6 | 6.4 | 6.1 | 9.7 |
| 17 |  | 7.6 | 7.3 | 9.3 | . 8 | 4.4 | 5.1 | 14.6 | 13.3 | 14.0 | 18.3 | 12.1 | 13.8 | 17.3 | 21.1 | 24.5 | 23.3 | 21.8 | 20.0 | 16.3 | 10.4 | 5.9 | 3.6 | 2.3 | - 8 | 12.0 |
| 18 |  | -4.1 | -0.4 | 7.8 | 7.4 | 6.6 | 7.1 | -7.1 | 9.9 | 11.8 | 18.0 | 21.6 | 16.0 | 15.5 | 19.8 | 26.1 | 29.0 | 26.3 | 26.1 | 14.6 | 6.1 | 7.9 | 6.8 | 5.1 | 5.4 | 11.8 |
| 19 |  | 6.3 | 9.4 | 9.1 | 10.4 | 11.6 | 11.1 | 11.6 | 11.8 | 12.4 | 12.1 | IC. 3 | 11.6 | 12.8 | 20.1 | 22.1 | 19.6 | 19.6 | 16.0 | 12.8 | 10.4 | 6.1 | 4.3 | 4.2 | 4.1 | 11.7 |
| 20 |  | 6.3 | 9.4 | 11.1 | 10.3 | 9.6 | 12.8 | 16.6 | 14.6 | 12.9 | 11.6 | 10.1 | 10.9 | 16.0 | 19.5 | 21.8 | 23.8 | 21.3 | 18.1 | 14.1 | 8.9 | 8.8 | 6.3 | 6.3 | 6.8 | 12.8 |
| 21 |  | 7.9 | 7.6 | 11.1 | 13.8 | 15.0 | 17.8 | 26.1 | 19.6 | 17.6 | 15.1 | 30.0 | 39.3 | 33.8 | 24.5 | 22.6 | 22.3 | 21.3 | 19.8 | 16.8 | 13.3 | 12.8 | 7.8 | $6 \cdot 3$ | 5.6 | 17.8 |
| 22 |  | 4.4 | 6.3 | 7.3 | 15.0 | 10.1 | 9.6 | 10.1 | 12.9 | 12.8 | 14.1 | 14.0 | 31.8 | 35.0 | 30.0 | 29.0 | 19.6 | 20.3 | 17.3 | 15.8 | 10.3 | 8.8 | 6.9 | 6.4 | 6.3 | 14.8 |
| 23 |  | 7.4 | 7.6 | 9.9 | 11.6 | 11.3 | 11.1 | 12.1 | 18.3 | 21.3 | 14.1 | 21.0 | 15.1 | 25.0 | 27.0 | 22.1 | 22.8 | 21.1 | 18.1 | 14.1 | 14.1 | 9.6 | 8.6 | 6.8 | 5.6 | 14.8 |
| 24 |  | 6.3 | 8.1 | 8.1 | 8.4 | 6.3 | 2.1 | 9.6 | 11.1 | 12.4 | 14.8 | 13.3 | 14.6 | 14.8 | 17.8 | 17.8 | 17.8 | 20.8 | 17.8 | 11.4 | 6.8 | 1.9 | 3.6 | 1.4 | 3.3 | 10.4 |
| 25 |  | 5.3 | 9.6 | 11.1 | 12.1 | 8.8 | 8.3 | 9.3 | 9.4 | 9.3 | 7.9 | 8.8 | 12.3 | 15.5 | 18.6 | 21.1 | 21.1 | 20.6 | 19.3 | 10.3 | 7.6 | 4.9 | 6.3 | 6.8 | 7.6 | 11.3 |
| 26 | 0 | 9.3 | 9.6 | 12.6 | 12.4 | 9.9 | 9.4 | 9.3 | 9.4 | 9.6 | 8.4 | 9.9 | 12.4 | 16.1 | 20.0 | 20.5 | 20.3 | 19.6 | 16.8 | 12.6 | 7.9 | 6.6 | 6.6 | $6 \cdot 3$ | 7.3 | 11.8 |
| 27 | 0 | 8.1 | 8.1 | 7.9 | 8.1 | 9.1 | 9.4 | 9.8 | 9.8 | 11.1 | 12.9 | 14.1 | 15.1 | 17.8 | 19.6 | 18.0 | 19.6 | 21.0 | 18.6 | 15.5 | 13.5 | 9.9 | 8.3 | 6.3 | 6.4 | 12.4 |
| 28 |  | 6.3 | 6.6 | 8.1 | 8.3 | 9.4 | 8.9 | 4.4 | 6.8 | 14.8 | 12.1 | 2 C .1 | 19.3 | 19.5 | 20.3 | 24.6 | 23.0 | 16.6 | 11.3 | 7.8 | 6.8 | 7.9 | 6.3 | 4.4 | 6.4 | 11.7 |
| 29 | 0 | 6.4 | 8.0 | 8.2 | 8.9 | 9.4 | 9.7 | 9.5 | 9.5 | 11.0 | 9.9 | 11.5 | 11.0 | 16.4 | 19.6 | 21.6 | 19.6 | 20.2 | 18.1 | 15.4 | 8.5 | 7.0 | 4.9 | 2.8 | 3.5 | 11.3 |
| 30 |  | 5.5 | 4.9 | 6.7 | 7.0 | 7.4 | 6.7 | 8.9 | 7.9 | 8.2 | 14.2 | 9.7 | 7.4 | 12.9 | 21.9 | 24.4 | 26.6 | 19.7 | 11.2 | 12.0 | 11.0 | 8.7 | 6.2 | 5.2 | 6.2 | 10.9 |
| 31 |  | 4.4 | 5.2 | 7.9 | 5.9 | 11.4 | 25.4 | 11.9 | 11.2 | 19.6 | 15.2 | 11.2 | 12.5 | 13.4 | 20.6 | 23.2 | 20.6 | 20.9 | 16.4 | 15.7 | 17.2 | 12.5 | 8.4 | 5.2 | 3.0 | 13.3 |





| HaU |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | UT | 10 | ro | T0 | T0 | T0 | TO | TO | T0 | 10 | 50 | T0 | T0 | T0 | TC | TO | TC | 10 | T0 | T0 | T0 | TC | T0 | T0 | 10 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |  |
| 1 |  | 696 | 699 | 689 | 689 | 641 | 667 | 649 | 557 | 576 | 602 | 648 | 655 | 661 | 660 | 661 | 662 | 670 | 673 | 666 | 662 | 676 | 681 | 673 | 673 | 658 |
| 2 | D | 673 | 683 | 683 | 695 | 676 | 688 | 675 | 673 | 643 | 553 | 637 | 673 | 649 | 611 | 623 | 635 | 644 | 644 | 681 | 672 | 699 | 730 | 728 | 685 | 665 |
| 3 |  | 682 | 679 | 677 | 673 | 683 | 590 | 579 | 517 | 517 | 594 | 577 | 561 | 591 | 635 | 595 | 626 | 656 | 671 | 677 | 679 | 685 | 687 | 693 | 693 | 634 |
| 4 |  | 688 | 673 | 671 | 682 | 687 | 673 | 673 | 667 | 652 | 656 | 624 | 640 | 659 | 661 | 662 | 662 | 666 | 661 | 659 | 661 | 667 | 676 | 679 | 687 | 666 |
| 5 |  | 717 | 697 | 673 | 673 | 673 | 662 | 661 | 662 | 660 | 659 | 661 | 638 | 591 | 576 | 628 | 652 | 661 | 662 | 662 | 667 | 672 | 679 | 685 | 709 | 662 |
| 6 |  | 697 | 684 | 687 | 696 | 690 | 561 | 599 | 640 | 667 | 667 | 661 | 652 | 642 | 649 | 664 | 669 | 672 | 669 | 666 | 670 | 673 | 673 | 676 | 685 | 663 |
| 7 | 0 | 705 | 707 | 709 | 721 | 721 | 703 | 683 | 681 | 590 | 601 | 643 | 661 | 664 | 672 | 672 | 665 | 661 | 660 | 659 | 653 | 653 | 656 | $66 C$ | 681 | -69 |
| 8 |  | 666 | 675 | 676 | 689 | 694 | 687 | 696 | 685 | 671 | 662 | 666 | 664 | 661 | 661 | 653 | 65 C | 661 | 660 | 660 | 655 | 652 | 659 | 676 | 683 | 669 |
| 9 |  | 684 | 676 | 679 | 685 | 700 | 720 | 687 | 667 | 551 | 600 | 637 | 664 | 650 | 675 | 675 | 664 | 655 | 649 | 658 | 659 | 661 | 675 | 697 | 703 | 665 |
| 10 |  | 693 | 667 | 677 | 700 | 718 | 695 | 683 | 540 | 581 | 611 | 640 | 634 | 661 | 660 | 659 | 664 | 669 | 672 | 673 | 677 | 688 | 673 | 675 | 675 | 662 |
| 11. | 0 | 673 | 675 | 677 | 671 | 672 | 673 | 669 | 650 | 636 | 566 | 628 | 644 | 659 | 658 | 653 | 649 | 652 | 653 | 653 | 655 | 661 | 671 | 675 | 676 | 656 |
| 12 |  | 673 | 678 | 678 | 676 | 671 | 670 | 669 | 667 | 660 | 655 | 649 | 660 | 669 | 672 | 672 | 665 | 659 | 649 | 647 | 649 | 655 | 667 | 691 | 721 | 668 |
| 13 | D | 754 | 768 | 697 | 703 | 706 | 707 | 618 | 721 | 655 | 711 | 653 | 658 | 636 | 517 | 512 | 524 | 613 | 696 | 707 | 709 | 735 | 747 | 771 | 712 | 676 |
| 14 | D | 685 | 634 | 707 | 735 | 658 | 481 | 648 | 640 | 596 | 445 | 520 | 607 | 656 | 661 | 647 | 628 | 649 | 655 | 667 | 685 | 748 | 753 | 701 | 613 | 642 |
| 15 | D | 661 | 729 | 321 | 289 | 551 | 666 | 703 | 697 | 576 | 640 | 452 | 682 | 806 | 435 | 666 | 516 | 547 | 650 | 709 | 793 | 815 | 780 | 78 C | 669 | 631 |
| 16 | D | 646 | 697 | 625 | 526 | 593 | 718 | 735 | 790 | 705 | 532 | 578 | 525 | 573 | 675 | 685 | 697 | 691 | 689 | 693 | 693 | 691 | 702 | 719 | 728 | 663 |
| 17 |  | 734 | 748 | 778 | 778 | 770 | 694 | 626 | 636 | 635 | 620 | 646 | 636 | 626 | 624 | 655 | 683 | 691 | 693 | 691 | 693 | 694 | 707 | 112 | 732 | 688 |
| 18 |  | 791 | 741 | 734 | 723 | 724 | 672 | 547 | 660 | 664 | 596 | 536 | 641 | 678 | 688 | 675 | 675 | 673 | 673 | 672 | 681 | 684 | 694 | 7 Cs | 694 | 676 |
| 19 |  | 709 | 693 | 684 | 679 | 685 | 682 | 678 | 673 | 666 | 671 | 666 | 647 | 593 | 576 | 606 | 661 | 664 | 661 | 662 | 673 | 678 | 676 | 683 | 685 | 665 |
| 20 |  | 705 | 712 | 707 | 685 | 682 | 644 | 599 | 650 | 656 | 661 | 676 | 672 | 672 | 673 | 664 | 656 | 671 | 671 | 664 | 670 | 672 | 682 | 685 | 708 | 672 |
| 21 |  | 723 | 734 | 731 | 736 | 730 | 672 | 635 | 813 | 623 | 576 | 470 | 476 | 546 | 564 | 555 | 617 | 659 | 676 | 685 | 681 | 693 | 705 | 715 | 723 | 647 |
| 22 |  | 700 | 684 | 685 | 689 | 683 | 682 | 685 | 676 | 646 | 555 | 461 | 449 | 449 | 514 | 587 | 635 | 654 | 673 | 677 | 683 | 673 | 667 | 673 | 675 | 632 |
| 23 |  | 683 | 687 | 689 | 697 | 687 | 683 | 670 | 614 | 647 | 612 | 557 | 618 | 563 | 636 | 665 | 673 | 672 | 662 | 658 | 660 | 671 | 675 | 681 | 673 | 655 |
| 24 |  | 673 | 669 | 666 | 667 | 687 | 619 | 687 | 664 | 644 | 624 | 659 | 664 | 660 | 635 | 614 | 632 | 659 | 660 | 652 | 656 | 661 | 672 | 688 | 708 | 659 |
| 25 |  | 753 | 701 | 697 | 693 | 673 | 672 | 671 | 667 | 661 | 649 | 658 | 667 | 664 | 665 | 661 | 660 | 661 | 660 | 662 | 660 | 672 | 683 | 695 | 699 | 675 |
| 26 | 0 | 694 | 685 | 677 | 671 | 664 | 667 | 669 | 667 | 664 | 660 | 630 | 606 | 649 | 660 | 661 | 660 | 656 | 658 | 652 | 642 | 649 | 660 | 667 | 673 | 660 |
| 27 | 0 | 673 | 673 | 669 | 662 | 662 | 661 | 661 | 661 | 661 | 661 | 661 | 652 | 659 | 652 | 655 | 656 | 655 | 648 | 650 | 652 | 654 | 659 | 661 | 672 | 660 |
| 28 |  | 672 | 665 | 664 | 664 | 664 | 671 | 685 | 671 | 648 | 649 | 631 | 648 | 661 | 666 | 649 | 646 | 646 | 649 | 658 | 658 | 661 | 667 | $67 E$ | 673 | 660 |
| 29 | 0 | 673 | 671 | 669 | 664 | 661 | 662 | 664 | 662 | 656 | 659 | 659 | 652 | 649 | 649 | 660 | 659 | 660 | 653 | 656 | 652 | 656 | 661 | 682 | 705 | 662 |
| 30 |  | 702 | 699 | 685 | 676 | 685 | 697 | 679 | 658 | 567 | 597 | 652 | 626 | 561 | 637 | 660 | 650 | 635 | 646 | 664 | 670 | 672 | 672 | 683 | 685 | 657 |
| 31 |  | 694 | 696 | 694 | 696 | 650 | 542 | 659 | 659 | 612 | 622 | 659 | 647 | 578 | 608 | 636 | 664 | 675 | 671 | 664 | 673 | 677 | 702 | 718 | 117 | 659 |
| MEAN | A | 696 | 693 | 676 | 674 | 679 | 861 | 659 | 654 | 632 | 618 | 616 | 630 | 634 | 630 | 643 | 647 | 657 | 663 | 668 | 672 | 681 | 687 | 694 | 69C | 661 |
| MEAN | 0 | 684 | 682 | 680 | 678 | 676 | 674 | 669 | 664 | 642 | 629 | 644 | 643 | 656 | 658 | 660 | 658 | 657 | 654 | 654 | 651 | 655 | 662 | 669 | 677 | 662 |
| MEAN | D | 684 | 702 | 607 | 590 | 636 | 652 | 676 | 704 | 635 | 576 | 568 | 629 | 664 | 580 | 627 | 600 | 629 | 667 | 691 | 710 | 738 | 742 | 74 C | 681 | 655 |


| HOUR UT |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | T0 | TO | T0 | 15 | 10 | T0 | 10 | T0 | 10 | 10 | 10 | 50 | T0 | 10 | TC | 10 | 10 | TC | T0 | 10 | 10 | 10 | 10 | T0 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |  |
| 1 |  | 759 | 781 | 788 | 780 | 759 | 757 | 747 | 744 | 744 | 744 | 747 | 747 | 737 | 737 | 744 | 748 | 739 | 727 | 701 | 704 | 723 | 726 | 734 | 747 | 744 |
| 2 |  | 753 | 764 | 764 | 780 | 760 | 757 | 732 | 654 | 740 | 751 | 753 | 745 | 735 | 749 | 749 | 739 | 723 | 708 | 695 | 717 | 724 | 726 | 73 E | 751 | 738 |
| 3 |  | 774 | 754 | 758 | 745 | 750 | 753 | 757 | 749 | 744 | 753 | 753 | 754 | 760 | 758 | 759 | 747 | 737 | 726 | 718 | 714 | 726 | 742 | 762 | 751 | 748 |
| 4 |  | 754 | 751 | 766 | 769 | 750 | 750 | 758 | 737 | 748 | 753 | 749 | 735 | 712 | 733 | 758 | 762 | 745 | 718 | 695 | 7 CO | 707 | 711 | 734 | 750 | 739 |
| 5 |  | 760 | 775 | 193 | 759 | 748 | 757 | 750 | 144 | 750 | 751. | 748 | 750 | 763 | 754 | 749 | 741 | 742 | 734 | 733 | 735 | 739 | 728 | 732 | 747 | 749 |
| 6 | 0 | 749 | 755 | 755 | 754 | 755 | 755 | 757 | 757 | 755 | 757 | 759 | 758 | 761 | 759 | 759 | 739 | 733 | 730 | 724 | 728 | 742 | 750 | 75 | 771 | 751 |
| 7 |  | 780 | 779 | 768 | 764 | 773 | 776 | 774 | 769 | 764 | 751 | 719 | 700 | 599 | 702 | 729 | 720 | 727 | 734 | 737 | 737 | 745 | 749 | $75 \%$ | 773 | 74.3 |
| 8 |  | 783 | 783 | 789 | 764 | 753 | 810 | 807 | 791 | 783 | 781 | 770 | 781 | 791 | 791 | 780 | 771 | 748 | 713 | 750 | 741 | 735 | 781 | 769 | 768 | 772 |
| 9 |  | 755 | 784 | 778 | 791 | 764 | 761 | 750 | 750 | 755 | 751 | 740 | 128 | 699 | 706 | 741 | 718 | 687 | 690 | 714 | 720 | 761 | 784 | 847 | 862 | 751 |
| 10 |  | 759 | 801 | 806 | 768 | 731 | 750 | 779 | 716 | 617 | 677 | 689 | 729 | 714 | 719 | 755 | 755 | 713 | 692 | 706 | 723 | 124 | 724 | 725 | 747 | 730 |
| 11 |  | 752 | 769 | 748 | 738 | 744 | 759 | 758 | 759 | $6 \in 0$ | 150 | 768 | 764 | 762 | 758 | 759 | 759 | 763 | 741 | 114 | 711 | 722 | 735 | 790 | 743 | 747 |
| 12 | 0 | 771 | 804 | 905 | 1054 | 934 | 758 | 655 | 740 | 554 | 627 | 700 | 672 | 729 | 754 | 734 | 732 | 718 | 719 | 701 | 714 | 723 | 751 | 751 | 757 | 748 |
| 13 | D | 758 | 781 | 811 | 876 | 750 | 744 | 790 | 171 | 756 | 149 | 746 | 745 | 673 | 660 | 682 | 712 | 701 | 692 | 694 | 704 | 727 | 770 | 774 | 808 | 745 |
| 14 | D | 761 | 761 | 770 | 758 | 772 | 777 | 760 | 662 | 665 | 771 | 774 | 775 | 603 | 494 | 714 | 756 | 741 | 727 | 731 | 740 | 743 | 748 | 774 | 751 | 730 |
| 15 |  | 758 | 760 | 780 | 769 | 756 | 750 | 746 | 754 | 760 | 764 | 758 | 653 | 616 | 673 | 724 | 771 | 771 | 740 | 709 | 715 | 738 | 746 | 738 | 749 | 737 |
| 16 | D | 754 | 802 | 783 | 793 | 796 | 796 | 766 | 752 | 555 | 607 | 762 | 750 | 752 | 743 | 687 | 704 | 723 | 729 | 735 | 736 | 7.31 | 748 | 765 | 766 | 739 |
| 17 | D | 801 | 899 | 916 | 813 | 749 | 746 | 744 | 742 | 752 | 746 | 688 | 763 | 779 | 775 | 771 | 745 | 735 | 691 | 673 | 704 | 727 | 725 | 731 | 738 | 756 |
| 18 | 0 | 750 | 748 | 750 | 749 | 744 | 743 | 745 | 748 | 7E1 | 754 | 758 | 760 | 769 | 764 | 757 | 754 | 733 | 719 | 717 | 718 | 724 | 735 | 748 | 748 | 745 |
| 19 |  | 745 | 753 | 751 | 759 | 748 | 751 | 750 | 757 | 762 | 759 | 748 | 768 | 766 | 763 | 760 | 752 | 765 | 758 | 740 | 727 | 721 | 745 | 755 | 750 | 752 |
| 20 |  | 782 | 805 | 769 | 768 | 768 | 751 | 745 | 749 | 633 | 690 | 716 | 714 | 739 | 751 | 759 | 766 | 771 | 760 | 745 | 137 | 737 | 738 | 161 | 766 | 747 |
| 21 |  | 769 | 770 | 762 | 753 | 758 | 761 | 758 | 747 | 744 | 726 | 722 | 722 | 734 | 724 | 740 | 762 | 750 | 740 | 734 | 747 | 739 | 735 | 745 | 760 | 746 |
| 22 | 0 | 759 | 763 | 760 | 758 | 751 | 749 | 750 | 750 | 750 | 751 | 752 | 753 | 768 | 774 | 770 | 762 | 139 | 724 | 724 | 724 | 728 | 737 | 743 | 757 | 750 |
| 23 |  | 764 | 770 | 760 | 762 | 759 | 758 | 750 | 751 | 750 | 749 | 750 | 769 | 759 | 757 | 769 | 739 | 737 | 750 | 754 | 748 | 750 | 759 | 765 | 781 | 757 |
| 24 |  | 783 | 174 | 799 | 796 | 761 | 763 | 737 | 759 | 738 | 742 | 741 | 718 | 699 | 731 | 717 | 745 | 726 | 723 | 733 | 734 | 747 | 768 | 761 | 757 | 748 |
| 25 |  | 760 | 771 | 763 | 748 | 740 | 762 | 770 | 750 | 748 | 739 | 750 | 738 | 723 | 696 | 714 | 728 | 692 | 679 | 717 | 720 | 737 | 742 | 763 | 773 | 738 |
| 26 |  | 783 | 769 | 748 | 751 | 758 | 760 | 759 | 753 | 755 | 747 | 742 | 714 | 709 | 692 | 686 | 763 | 721 | 723 | 721 | 724 | 723 | 726 | 733 | 744 | 735 |
| 27 |  | 742 | 754 | 775 | 769 | 749 | 749 | 757 | 750 | 748 | 749 | 742 | 723 | 720 | 749 | 755 | 742 | 751 | 745 | 737 | 737 | 742 | 748 | 741 | 737 | 746 |
| 28 | 0 | 761 | 751 | 748 | 749 | 757 | 755 | 759 | 757 | 759 | 758 | 757 | 758 | 757 | 759 | 758 | 758 | 751 | 743 | 735 | 729 | 729 | 728 | 717 | 734 | 748 |
| 29 | 0 | 750 | 768 | 758 | 771 | 758 | 757 | 758 | 759 | 758 | 751 | 750 | 745 | 753 | 770 | 772 | 770 | 747 | 712 | 699 | 703 | 713 | 727 | $74 C$ | 759 | 748 |
| 30 |  | 759 | 754 | 759 | 759 | 750 | 753 | 759 | 757 | 753 | 761 | 761 | 765 | 773 | 778 | 769 | 759 | 728 | 714 | 723 | 726 | 729 | 751 | 764 | 769 | 753 |
| MEAN | A | 763 | 775 | 779 | 779 | 761 | 759 | 754 | 746 | 725 | 739 | 744 | 740 | 728 | 732 | 744 | 745 | 735 | 723 | 720 | 724 | 732 | 743 | 754 | 760 | 746 |
| MEAN | Q | 754 | 757 | 754 | 756 | 753 | 752 | 754 | 754 | 755 | 754 | 755 | 755 | 761 | 765 | 763 | 757 | 741 | 726 | 720 | 720 | 728 | 735 | 741 | 754 | 748 |
| MEAN | 0 | 769 | 809 | 837 | 859 | 800 | 764 | 743 | 733 | 656 | 700 | 734 | 741 | 707 | 685 | 718 | 730 | 724 | 111 | 707 | 720 | 730 | 748 | 755 | 764 | 744 |


| HOU |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | UT | T0 | T0 | T0 | T0 | 10 | 10 | T0 | TO | 10 | 10 | 10 | T0 | 10 | 10 | 1 C | 10 | 10 | TO | T0 | 10 | 1 C | 10 | IC | 10 | mean |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |  |
| 1 |  | 4.5 | 4.2 | 8.9 | 6.4 | 8.0 | 10.9 | 12.0 | 9.7 | 10.0 | 10.9 | 1 C .7 | 11.4 | 14.7 | 16.4 | 20.1 | 21.4 | 20.4 | 18.2 | 13.6 | 12.2 | 8.7 | 6.4 | 6.4 | 6.4 | 11.4 |
| 2 |  | 7.5 | 8.0 | 8.0 | 8.5 | 13.2 | 8.5 | 6.9 | 8.0 | 11.9 | 12.0 | 10.5 | 11.2 | 13.9 | 20.1 | 22.4 | 24.2 | 22.4 | 19.9 | 14.1 | t. 9 | 3.5 | -0.1 | 1.7 | 4.9 | 11.2 |
| 3 |  | 3.4 | 6.7 | 7.9 | 9.5 | 8.0 | 8.5 | 8.0 | 7.7 | 7.0 | 8.2 | 8.0 | 10.2 | 13.2 | 16.6 | 20.9 | 22.1 | 22.7 | 18.7 | 9.7 | 8.4 | 6.4 | 1.9 | 1.2 | 3.0 | 9.9 |
| 4 |  | 4.2 | 7.5 | 8.9 | 7.9 | 6.7 | 7.2 | 6.4 | 13.2 | 14.6 | 8.5 | 8.5 | 12.2 | 17.9 | 24.2 | 23.9 | 23.1 | 18.6 | 19.7 | 14.2 | 11.4 | 8.5 | 5.0 | 4.5 | 6.2 | 11.8 |
| 5 |  | 5.0 | 6.0 | 8.2 | 11.0 | 9.2 | 9.5 | 9.5 | 9.2 | 7.9 | 9.7 | 8.5 | 11.9 | 16.2 | 19.7 | 23.6 | 26.9 | 23.2 | 10.6 | 14.9 | 10.2 | 7.9 | 4.7 | 4.5 | 4.9 | 11.1 |
| 6 | 0 | 6.2 | 8.0 | 10.0 | 11.4 | 11.2 | 10.2 | 9.7 | 8.0 | 8.0 | 9.0 | 10.9 | 13. 2 | 17.7 | 21.7 | 23.2 | 24.6 | 24.7 | 15.7 | 13.2 | 8.4 | 3.5 | 3.0 | 1.5 | 1.7 | 11.5 |
| 7 |  | 2.9 | 5.0 | 6.5 | 4.9 | 5.2 | 4.7 | 6.9 | 7.5 | 7.7 | 6.7 | 11.5 | 16.4 | 14.1 | 18.4 | 23.1 | 25.2 | 21.4 | 16.1 | 10.0 | 6.9 | 5.9 | 5.5 | 5.5 | 5.9 | 10.2 |
| 8 |  | 8.2 | 7.7 | 10.0 | 11.2 | 10.5 | 6.7 | 4.4 | 9.7 | 10.0 | 8.7 | 12.7 | 13.0 | 21.6 | 23.2 | 24.7 | 27.6 | 27.1 | 21.7 | 7.7 | 12.0 | 3.2 | . 0 | 1.5 | 2.2 | 11.9 |
| 9 |  | 1.9 | 1.7 | 5.9 | 8.0 | 6.7 | 6.9 | 6.4 | 7.5 | 7.9 | 6.9 | 8.5 | 13.9 | 17.7 | 22.6 | 30.1 | 30.6 | 27.7 | 24.1 | 12.2 | 6.4 | 5.2 | 1.5 | 1.C | 1.4 | 10.9 |
| 10 |  | 7.9 | 4.9 | 6.9 | 7.0 | 7.5 | 4.4 | 9.9 | 6.7 | 10.5 | 12.9 | 13.0 | 13.4 | 13.2 | 21.2 | 24.7 | 23.7 | 24.6 | 19.4 | 15.2 | 11.0 | 6.0 | 2.4 | 3.2 | 4.4 | 11.4 |
| 11 |  | 6.0 | 8.4 | 11.7 | 9.7 | 8.5 | 11.9 | 10.9 | 7.4 | 4.9 | 16.6 | 11.5 | 13.0 | 15.6 | 17.9 | 19.7 | 20.2 | 21.4 | 20.7 | 16.7 | 8.9 | 4.9 | 1.5 | - 5 | 4.5 | 11.4 |
| 12 | D | 2.7 | 2.9 | -8.5- | 18.8 | . 4 | 14.1 | 14.1 | 7.4 | 14.1 | 22.9 | 15.1 | 12.7 | 15.6 | 19.9 | 23.4 | 22.4 | 21.4 | 19.1 | 16.2 | 4.9 | 2.5 | 3.0 | 5.2 | 6.2 | 9.9 |
| 13 | D | 5.5 | 5.5 | 4.4 | -0.8 | 10.5 | 16.2 | 8.5 | 6.5 | 7.2 | 8.2 | 11.0 | 16.4 | 18.4 | 21.7 | 6.9 | 24.4 | 25.6 | 21.1 | 13.9 | 5.5 | 4.4 | 6.7 | 6.2 | . 4 | 10.6 |
| 14 | D | . 6 | 1.0 | 6.3 | 14.3 | 13.8 | 8.1 | 4.8 | 2.8 | 10.1 | 8.0 | 6.8 | 10.6 | 13.8 | 29.0 | 29.2 | 26.0 | 25.3 | 17.8 | 16.5 | 13.5 | 9.8 | 9.6 | 9.1 | 7.5 | 12.3 |
| 15 |  | 6.6 | 7.8 | 9.1 | 11.3 | 11.3 | 9.5 | 9.5 | 9.6 | 16.3 | 11.0 | 6.0 | 12.0 | 13.7 | 23.7 | 28.2 | 23.5 | 22.0 | 21.2 | 15.7 | 9.5 | 5.6 | 5.C | 6.6 | 7.0 | 12.6 |
| 16 | 0 | 8.1 | 8.5 | 12.0 | 10.5 | 8.5 | 8.5 | 21.2 | 13.5 | 18.8 | 31.2 | 12.1 | 11.0 | 16.5 | 20.0 | 24.8 | 24.5 | 23.5 | 17.8 | 14.5 | 9.8 | 4.5 | 5.3 | 6. 6 | 5.6 | 14.0 |
| 17 | D | 4.5 | 3.3 | 9.1 | 9.0 | 8.1 | 10.1 | 17.3 | 24.0 | 10.0 | 7.3 | 8.5 | 9.8 | 17.3 | 21.0 | 23.5 | 23.3 | 25.7 | 24.8 | 15.8 | 6.3 | 6.5 | 6.8 | 6.8 | 6.8 | 12.7 |
| 18 | 0 | 8.1 | 9.6 | 10.0 | 9.8 | 10.0 | 9.3 | 10.1 | 11.5 | 10.6 | 10.5 | 11.0 | 13.0 | 14.7 | 15.7 | 18.2 | 21.2 | 20.7 | 16.8 | 7.6 | 6.0 | 5.0 | 4.5 | 4.6 | 6.6 | 11.0 |
| 19 |  | 8.5 | 8.6 | 9.5 | 10.1 | 8.5 | 9.0 | 9.3 | 7.8 | 13.0 | 14.7 | 16.0 | 13.7 | 16.2 | 16.7 | 17.2 | 18.0 | 16.5 | 14.8 | 13.0 | 8.1 | 6.0 | 2.6 | 5.3 | 6.5 | 11.2 |
| 20 |  | 5.0 | 9.8 | 11.0 | 11.6 | 18.2 | 12.1 | 14.7 | 9.8 | 18.2 | 12.3 | 14.7 | 14.5 | 18.2 | 18.2 | 21.8 | 22.7 | 20.3 | 16.5 | 10.0 | 8.3 | 6.0 | 4.3 | 3.1 | 5.0 | 12.8 |
| 21 |  | 7.3 | 9.5 | 9.8 | 10.0 | 10.3 | 13.1 | 16.8 | 11.8 | 10.0 | 6.6 | 11.8 | 16.7 | 20.3 | 21. 1 | 20.7 | 23.3 | 21.5 | 18.2 | 16.3 | 11.1 | 9.8 | 7.6 | 6.8 | 7.8 | 13.3 |
| 22 | 0 | 8.5 | 10.1 | 11.3 | 11.3 | 9.8 | 9.8 | 9.3 | 9.1 | 9.5 | 9.8 | 9.8 | 13.0 | 16.2 | 16.8 | 17.2 | 20.2 | 18.8 | 16.2 | 14.0 | 9.8 | 7.6 | 6.3 | 6.1 | 6.1 | 11.5 |
| 23 |  | 6.1 | 6.8 | 8.6 | 8.3 | 8.1 | 8.3 | 9.0 | 9.1 | B. 5 | 9.5 | 12.8 | 14.7 | 14.8 | 17.3 | 19.3 | 22.3 | 20.0 | 14.8 | 11.1 | 9.5 | 7.8 | 4.6 | 4.C | 4.0 | 10.8 |
| 24 |  | 5.0 | 5.0 | 9.6 | 9.6 | 8.5 | 13.3 | 12.5 | 11.3 | 14.7 | 11.5 | 10.6 | 11.1 | 12.8 | 20.C | 22.2 | 18.2 | 21.3 | 18.0 | 11.5 | 5.6 | 5.8 | 4.6 | 4.6 | 4.6 | 11.3 |
| 25 |  | 6.3 | 7.3 | 9.3 | 9.6 | 9.8 | 9.6 | 9.5 | 9.6 | 7.8 | 9.5 | 11.8 | 12.8 | 15.7 | 14.2 | 18.3 | 21.5 | 24.8 | 18.5 | B. 1 | 7.0 | 5.0 | 3.3 | 2.1 | 2.1 | 10.6 |
| 26 |  | $-0.0$ | 5.5 | 9.5 | 8.1 | 8.6 | 8.6 | 8.1 | 8.3 | 8.6 | 8.1 | 9.5 | 6.8 | 11.5 | 14.8 | 16.2 | 13.5 | 13.3 | 16.5 | 14.5 | 11.6 | 6.3 | 5.6 | 5.1 | 4.5 | 9.3 |
| 27 |  | 5.5 | 6.6 | 8.6 | 11.8 | 10.8 | 9.0 | 10.6 | 10.1 | 9.1 | 8.8 | 9.1 | 11.5 | 15.0 | 17.7 | 20.3 | 21.5 | 18.7 | 18.0 | 13.7 | 11.3 | 9.3 | 7.1 | 6.6 | 6.8 | 11.6 |
| 28 | 0 | 6.1 | 6.5 | 8.1 | 9.0 | 9.0 | 9.5 | 10.1 | 9.5 | 9.5 | E. 8 | 8.1 | 9.6 | 12.6 | 14.8 | 17.3 | 19.2 | 19.8 | 18.2 | 15.7 | 8.3 | 5.C | 2.8 | 3.1 | 4.5 | 10.2 |
| 29 | 0 | 6.3 | 7.8 | 9.8 | 9.6 | 9.8 | 9.0 | 8.5 | 9.6 | 10.3 | 11.3 | 11.8 | 13.3 | 18.3 | 20.0 | 21.5 | 23.5 | 22.8 | 20.3 | 14.3 | 9.5 | 6.3 | 4.1 | 4.6 | 5.0 | 12.0 |
| 30 |  | 7.5 | 9.8 | 10.8 | 9.3 | 8.3 | 8.6 | 10.5 | 10.8 | 10.6 | 9.0 | 10.0 | 13.1 | 15.5 | 16.C | 19.8 | 20.7 | 20.8 | 18.5 | 10.1 | 5.8 | . 5 | $-2.0$ | -1.4 | -0.2 | 10.1 |
| MEAN | A | 5.5 | 6.7 | 8.4 | 8.3 | 9.2 | 9.5 | 10.2 | 9.6 | 10.6 | 11.0 | 10.7 | 12.5 | 15.8 | 19.4 | 21.4 | 22.6 | 21.9 | 18.7 | 13.1 | 8. 8 | 5.9 | 4.1 | 4.2 | 4.7 | 11.4 |
| MEAN | Q | 7.1 | 8.4 | 9.9 | 10.2 | 10.0 | 9.6 | 9.6 | 9.6 | 9.6 | 9.9 | 10.3 | 12.4 | 15.9 | 17.8 | 19.5 | 21.7 | 21.4 | 17.4 | 13.0 | E. 4 | 5.5 | 4.1 | 4.C | 4.8 | 11.2 |
| MEAN | D | 4.3 | $4 \cdot 2$ | 4.7 | 2.8 | 8.3 | 11.4 | 13.2 | 10.8 | 12.0 | 15.5 | 16.7 | 12.1 | 16.3 | 22.3 | 21.6 | 24.1 | 24.3 | 20.1 | 15.4 | 8.0 | 5.5 | 6.3 | 6.7 | 5.3 | 11.9 |


| HOUR |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | T | TO | TO | TO | TO | TO | TO | TO | T0 | 10 | 10 | T0 | T0 | T0 | T'C | TC | TC | T0 | T0 | 10 | 10 | 10 | 10 | 10 | T0 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 2 I | 24 |  |
| 1 |  | 697 | 705 | 709 | 695 | 697 | 697 | 689 | 673 | 670 | 660 | 653 | 660 | 662 | 664 | 662 | 667 | 669 | 664 | 660 | 671 | 683 | 676 | 673 | 672 | 676 |
| 2 |  | 671 | 671 | 671 | 684 | 697 | 703 | 666 | 519 | 624 | 656 | 666 | 649 | 635 | 650 | 667 | 666 | 681 | 658 | 654 | 656 | 659 | 660 | 666 | 681 | 658 |
| 3 |  | 706 | 709 | 707 | 684 | 676 | 672 | 669 | 667 | 659 | 659 | 662 | 665 | 671 | 669 | 659 | 653 | 649 | 650 | 649 | 648 | 659 | 662 | 673 | 697 | 670 |
| 4 |  | 708 | 693 | 688 | 693 | 699 | 690 | 678 | 600 | 611 | 662 | 661 | 646 | 606 | 626 | 650 | 656 | 650 | 646 | 638 | 649 | 680 | 662 | 671 | 677 | 659 |
| 5 |  | 681 | 694 | 711 | 684 | 670 | 671 | 672 | 667 | 661 | 653 | 650 | 647 | 671 | 661 | 652 | 641 | 649 | 649 | 648 | 649 | 658 | 660 | 658 | 662 | 663 |
| 6 | 0 | 664 | 664 | 667 | 671 | 667 | 664 | 662 | 661 | 661 | 661 | 664 | 664 | 664 | 658 | 659 | 649 | 640 | 637 | 636 | 644 | 659 | 670 | 677 | 689 | 660 |
| 7 |  | 700 | 707 | 702 | 696 | 703 | 705 | 697 | 684 | 667 | 655 | 623 | 613 | 541 | 601 | 638 | 649 | 669 | 681 | 675 | 672 | 673 | 675 | 673 | 693 | 666 |
| 8 |  | 720 | 729 | 720 | 695 | 682 | 707 | 689 | 661 | 659 | 649 | 634 | 652 | 665 | 656 | 647 | 650 | 650 | 647 | 636 | 636 | 654 | 707 | 725 | 718 | 675 |
| 9 |  | 697 | 707 | 712 | 699 | 684 | 675 | 661 | 661 | 664 | 661 | 656 | 638 | 614 | 614 | 644 | 643 | 622 | 624 | 640 | 672 | 734 | 777 | 782 | 768 | 677 |
| 10 |  | 709 | 723 | 734 | 711 | 673 | 676 | 683 | 655 | 570 | 583 | 611 | 659 | 654 | 649 | 673 | 676 | 662 | 661 | 656 | 659 | 662 | 671 | 668 | 672 | 665 |
| 11 |  | 673 | 685 | 679 | 665 | 667 | 683 | 673 | 669 | 578 | 624 | 673 | 673 | 671 | 661 | 661 | 660 | E61 | 659 | 659 | 860 | 665 | 670 | 685 | 682 | 664 |
| 12 | D | 696 | 710 | 774 | 745 | 696 | 596 | 608 | 674 | 515 | 621 | 625 | 631 | 660 | 665 | 654 | 655 | 662 | 676 | 684 | 678 | 673 | 686 | 686 | 690 | 665 |
| 13 | D | 688 | 704 | 724 | 701 | 639 | 650 | 713 | 698 | 684 | 676 | 665 | 673 | 626 | 602 | 598 | 614 | 838 | 650 | 648 | 660 | 682 | 722 | 759 | 741 | 673 |
| 14 | D | 696 | 689 | 710 | 700 | 674 | 676 | 698 | 644 | 654 | 673 | 686 | 686 | 618 | 554 | 627 | 677 | 661 | 651 | 662 | 662 | 667 | 695 | 715 | 710 | 670 |
| 15 |  | 697 | 685 | 688 | 690 | 694 | 677 | 672 | 667 | 650 | 671 | 653 | 560 | 537 | 565 | 582 | 656 | 663 | 650 | 648 | 680 | 674 | 673 | 671 | 676 | 652 |
| 16 | 0 | 679 | 700 | 718 | 719 | 719 | 695 | 683 | 636 | 597 | 488 | 618 | 645 | 641 | 631 | 591 | 589 | 626 | 642 | 657 | 663 | 662 | 665 | 68 t | 707 | 652 |
| 17 | D | 724 | 760 | 745 | 722 | 712 | 696 | 633 | 578 | 650 | 650 | 537 | 618 | 674 | 674 | 670 | 653 | 653 | 648 | 647 | 647 | 650 | 654 | $66 ?$ | 673 | 664 |
| 18 | 0 | 679 | 673 | 670 | 666 | 661 | 661 | 661 | 662 | 685 | 667 | 671 | 669 | 669 | 662 | 659 | 658 | 656 | 650 | 647 | 648 | 649 | 658 | 66 C | 661 | 662 |
| 19 |  | 661 | 661 | 660 | 664 | 661 | 661 | 661 | 852 | 647 | 623 | 649 | 670 | 666 | 661 | 654 | 640 | 640 | 649 | 649 | C50 | 659 | 667 | 672 | 678 | 657 |
| 20 |  | 687 | 700 | 693 | 690 | 696 | 616 | 661 | 672 | 479 | 526 | 565 | 588 | 608 | 635 | 635 | 648 | 660 | 660 | 658 | 659 | 664 | 669 | 673 | 673 | 642 |
| 21 |  | 673 | 676 | 672 | 662 | 669 | 675 | 656 | 652 | 652 | 625 | 590 | 597 | 613 | 611 | 637 | 660 | 660 | 659 | 653 | 658 | 664 | 67C | 661 | 670 | 651 |
| 22 | 0 | 671 | 673 | 667 | 662 | 661 | 661 | 661 | 661 | 661 | 661 | 652 | 652 | 666 | 662 | 659 | 656 | 656 | 652 | 650 | 652 | 659 | 662 | 672 | 671 | 661 |
| 23 |  | 664 | 661 | 660 | 661 | 661 | 661 | 659 | 659 | 655 | 647 | 644 | 654 | 652 | 647 | 647 | 637 | 638 | 635 | 640 | 649 | 659 | 672 | 688 | 709 | 657 |
| 24 |  | 712 | 695 | 703 | 684 | 685 | 655 | 613 | 654 | 625 | 652 | 658 | 642 | 607 | 649 | 641 | 660 | 861 | 660 | 655 | 658 | 669 | 684 | 688 | 697 | 663 |
| 25 |  | 683 | 673 | 676 | 671 | 661 | 665 | 676 | 660 | 660 | 637 | 652 | 650 | 640 | 619 | 626 | 654 | 647 | 636 | 635 | 649 | E61 | 685 | 7CC | 696 | 659 |
| 26 |  | 694 | 699 | 683 | 662 | 673 | 673 | $6 \in 1$ | 661 | 660 | 648 | 636 | 608 | 613 | 612 | 575 | 6 C 3 | 640 | 661 | 679 | 664 | 665 | 671 | 672 | 676 | 654 |
| 27 |  | 673 | 678 | 697 | 697 | 683 | 665 | 664 | 662 | 661 | 659 | 649 | 624 | 625 | 659 | 667 | 660 | 661 | 661 | 659 | 659 | 661 | 675 | 685 | 693 | 666 |
| 28 | 0 | 691 | 676 | 671 | 661 | 661 | 661 | 661 | 660 | 650 | 647 | 643 | 652 | 661 | 664 | 662 | 660 | 854 | 649 | 641 | 638 | 649 | 655 | 652 | 659 | 658 |
| 29 | 0 | 664 | 671 | 662 | 670 | 665 | 661 | 660 | 660 | 649 | 649 | 652 | 654 | 656 | 664 | 661 | 661 | 656 | 648 | 641 | 637 | 647 | 649 | 649 | 664 | 656 |
| 30 |  | 676 | 678 | 675 | 670 | 661 | 660 | 660 | 655 | 647 | 658 | 661 | 664 | 667 | 662 | 659 | 659 | 649 | 646 | 638 | 635 | 637 | 649 | 658 | 659 | 658 |
| MEAN | 4 | 688 | 692 | 695 | 686 | 678 | 670 | 667 | 653 | 636 | 640 | 642 | 643 | 638 | 640 | 644 | 650 | 652 | 652 | 651 | 655 | 664 | 675 | 682 | 687 | 662 |
| MEAN | 0 | 674 | 671 | 668 | 666 | 663 | 662 | 661 | 661 | 657 | 657 | 656 | 658 | 663 | 662 | 660 | 657 | 653 | 647 | 643 | 644 | 653 | 659 | 662 | 669 | 659 |
| MEAN | 0 | 696 | 713 | 734 | 117 | 688 | 663 | 667 | 646 | 620 | 622 | 626 | 651 | 644 | 625 | 628 | 637 | 648 | 653 | 660 | 662 | 667 | 684 | 702 | 704 | 665 |



D $=23.5$ DEGREES EAST PLUS TABULAR VALUES IN MINUTES

| HOURUT |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 2 C | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | T0 | TO | TO | 10 | TO | TO | 10 | T0 | TO | T0 | T0 | T0 | T0 | T0 | 10 | 10 | 10 | 10 | 10 | 10 | TC | 10 | T0 | 10 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |  |
| 1 | D | 2.5 | 4.6 | 7.8 | 5.5 | 4.3 | 2.0 | 2.6 | -1.4 | 15.0 | 9.6 | 9.8 | 14.7 | 16.5 | 26.2 | 28.0 | 27.8 | 25.8 | 22.5 | 15.5 | 8.6 | $\epsilon . \varepsilon$ | 1.5 | 2. 8 | 4.6 | 11.0 |
| 2 |  | 7.8 | 8.1 | 7.8 | 11.5 | 10.0 | 10.0 | 8.0 | 9.8 | 8.3 | 8.1 | 10.1 | 13.5 | 17.8 | 20.5 | 22.3 | 22.5 | 20.2 | 18.3 | 16.0 | 11.3 | 6.8 | 4.0 | 3.5 | 6.8 | 11.8 |
| 3 |  | 8.1 | 8.5 | 10.0 | 10.1 | 9.5 | 9.3 | 9.5 | 8.6 | 9.6 | 9.8 | 11.3 | 14.7 | 17.7 | 20.3 | 21.0 | 23.2 | 23.0 | 18.8 | 11.3 | 4.6 | 1.3 | 1.8 | 4.5 | 6.5 | 11.4 |
| 4 | 0 | 7.8 | 8.5 | 9.0 | 8.3 | 8.0 | 8.1 | 8.5 | 9.0 | 9.3 | 10.0 | 11.3 | 13.0 | 15.8 | 19.2 | 20.0 | 21.3 | 21.8 | 20.2 | 15.2 | 8.1 | 4.1 | . 3 | . 6 | 3.3 | 10.9 |
| 5 | 0 | 5.5 | 7.1 | 9.0 | 9.0 | 9.5 | 8.5 | 7.8 | 8.1 | 8.5 | 10.1 | 12.5 | 12.1. | 14.8 | 19.7 | 22.0 | 23.3 | 23.2 | 19.8 | 14.8 | 8.0 | 4.5 | 1.1 | $-1.4$ | 2.0 | 10.8 |
| 6 |  | 3.0 | 5.0 | $7 \cdot 3$ | 8.0 | 8.1 | 8.1 | 7.5 | 7.1 | 8.1 | 9.6 | 12.0 | 14.7 | 15.2 | 18.3 | 21.5 | 21.7 | 21.3 | 20.0 | 16.5 | 11.3 | 7.6 | 5.0 | 3.1 | 2.3 | 10.9 |
| 7 |  | 1.5 | 3.1 | 6.3 | 7.8 | 8.1 | 8.1 | 8.6 | 8.8 | 9.3 | 11.3 | 13.1 | 16.2 | 20.8 | 22.5 | 23.2 | 20.0 | 23.8 | 19.0 | 13.7 | 10.0 | 6.0 | 1.3 | -0.c | 1.1 | 11.0 |
| 8 |  | 3.1 | 6.2 | 7.9 | 8.2 | 8.1 | 9.1 | 7.7 | 8.4 | 8.9 | 10.2 | 12.1 | 13.1 | 13.8 | 17.8 | 19.8 | 20.1 | 20.3 | 19.6 | 13.6 | 9.1 | 6.6 | 3.4 | 2.5 | 4.6 | 10.6 |
| 9 |  | 6.6 | 6.7 | 8.2 | 7.9 | 9.2 | 9.1 | 7.4 | 10.7 | 11.7 | 10.6 | 12.4 | 15.3 | 18.6 | 19.8 | 19.9 | 22.8 | 23.4 | 21.6 | 15.8 | 6.6 | 2.6 | -0.3 | 1.2 | 4.7 | 11.4 |
| 10 |  | 8.1 | 6.7 | 9.7 | 9.1 | 7.7 | 7.6 | 6.4 | 7.6 | 6.4 | 8.4 | 9.1 | 11.9 | 14.9 | 16.4 | 19.8 | 19.4 | 21.1 | 18.6 | 12.9 | 8.7 | 4.2 | 2.1 | 3.7 | 5.2 | 10.2 |
| 11 |  | 7.1 | 8.9 | 10.2 | 10.1 | 9.2 | 9.1 | 9.1 | 10.1 | 11.9 | 9.9 | 10.6 | 12.1 | 14.8 | 16.9 | 17.3 | 20.6 | 22.1 | 17.1 | 11.2 | E. 4 | 4.4 | 1.9 | 3.6 | 5.6 | 10.8 |
| 12 |  | 6.9 | 6.6 | 5.4 | 5.6 | 5.2 | 11.6 | 7.2 | 10.1 | 10.2 | 14.1 | 11.4 | 13.3 | 17.1 | 21.4 | 20.3 | 23.4 | 24.9 | 22.4 | 16.4 | 11.7 | 6.6 | 6.2 | 6.4 | 5.1 | 12.1 |
| 13 | D | 7.1 | 8.2 | 9.9 | 9.1 | 6.1 | 7.2 | 11.1 | 10.1 | 16.8 | 21.3 | 14.9 | 13.3 | 13.8 | 17.1 | 21.6 | 21.8 | 19.3 | 17.4 | 19.4 | 13.9 | . 2 | -1.9 | 1.2 | 4.7 | 11.8 |
| 14 | 0 | 8.1 | 11.6 | 12.4 | 10.2 | 21.4 | 13.4 | 11.4 | 19.9 | 16.1 | 12.4 | 10.7 | 8.7 | 13.3 | 18.3 | 21.8 | 22.9 | 21.4 | 18.3 | 10.9 | 6.7 | 3.6 | 5.2 | 5.7 | 7.2 | 13.0 |
| 15 |  | 10.1 | 12.9 | 13.4 | 11.2 | 9.9 | 9.6 | 9.7 | 9.9 | 13.8 | 11.4 | 7.1 | 7.4 | 10.9 | 16.9 | 22.3 | 24.6 | 22.9 | 20.4 | 17.1 | 12.1 | 7.7 | 6.4 | 6.4 | 7.4 | 12.6 |
| 16 |  | 8.7 | 10.4 | 12.1 | 13.4 | 15.4 | 11.6 | 11.4 | 10.1 | 8.7 | 8.4 | 9.1 | 17.8 | 17.4 | 22.8 | 23.1 | 22.4 | 21.6 | 14.8 | 15.1 | 8.2 | 7.4 | 9.6 | 8.1 | 9.2 | 13.2 |
| 17 |  | 9.1 | 10.4 | 12.4 | 11.4 | 11.2 | 13.3 | 11.4 | 9.4 | 8.7 | 8. 9 | 8.9 | 11.9 | 14.6 | 16.1 | 19.9 | 19.9 | 18.6 | 15.3 | 12.9 | 8.2 | 6.4 | 4.4 | 4.9 | 5.1 | 11.4 |
| 18 |  | 5.9 | 7.7 | 8.6 | 9.4 | 9.6 | 9.9 | 10.2 | 10.6 | 13.1 | 12.9 | 10.1 | 15.3 | 16.6 | 16.8 | 17.8 | 18.8 | 19.9 | 18.1 | 13.6 | 9.9 | 6.6 | 6.1 | 7.4 | 8.1 | 11.8 |
| 19 | 0 | 8.4 | 8.9 | 9.4 | 9.7 | 9.9 | 10.1 | 12.4 | 11.6 | 13.3 | 11.1 | 10.4 | 11.9 | 14.6 | 15.4 | 16.8 | 18.4 | 17.6 | 14.1 | 8.4 | 5.1 | 5.1 | 5.1 | 4.7 | 5.2 | 10.7 |
| 20 | 0 | 6.9 | 8.2 | 8.6 | 9.9 | 9.6 | 11.2 | 10.1 | 9.6 | 9.7 | 10.7 | 11.2 | 11.1 | 13.4 | 16.9 | 19.9 | 22.8 | 22.6 | 18.1 | 14.3 | 8.9 | 4.6 | 3.4 | 3.2 | 5.1 | 11.3 |
| 21 |  | 8.1 | 9.9 | 9.9 | 9.7 | 8.7 | 8.4 | 9.6 | 8.7 | 8.7 | 8.6 | 10.1 | 11.6 | 13.1 | 16.3 | 21.3 | 20.6 | 18.4 | 16.9 | 7.4 | 3.1 | 1.7 | 2.2 | 3.4 | 7.4 | 10.2 |
| 22 |  | 7.9 | 8.6 | 8.6 | 8.6 | 7.2 | 6.1 | 6.9 | 7.9 | 11.1 | 11.2 | 11.2 | 13.3 | 16.4 | 19.9 | 21.1 | 19.9 | 21.6 | 19.9 | 14.6 | 10.6 | 9.7 | 8.2 | 6.7 | 5.2 | 11.7 |
| 23 |  | 6.7 | 6.2 | 5.7 | 6.7 | 8.4 | 8.9 | 9.7 | 9.7 | 9.9 | 10.1 | 8.6 | 11.4 | 13.4 | 15.3 | 16.9 | 16.8 | 16.9 | 17.3 | 8.4 | 7.1 | 7.9 | 7.7 | 6.1 | 8.9 | 10.2 |
| 24 |  | 8.7 | 8.4 | 8.4 | 8.2 | 8.6 | 9.9 | 9.7 | 11.9 | 10.7 | 10.4 | 11.6 | 13.3 | 15.6 | 17.4 | 19.8 | 21.9 | 19.9 | 17.9 | 15.6 | 12.9 | 11.7 | 9.9 | 9.4 | 9.1 | 12.5 |
| 25 |  | 8.6 | 8.1 | 8.9 | 8.2 | 8.4 | 11.2 | 10.2 | 10.7 | 9.6 | 9.9 | 11.7 | 13.3 | 14.8 | 15.1 | 16.6 | 16.4 | 16.4 | 16.3 | 13.1 | 8.6 | 6.1 | 5.9 | 5.2 | 7.7 | 10.9 |
| 26 | D | 7.9 | 8.4 | 6.7 | 6.7 | 10.7 | 7.4 | 6.6 | 8.2 | 9.9 | 10.2 | 11.7 | 12.9 | 15.8 | 19.9 | 18.8 | 29.6 | 26.6 | 23.4 | 20.1 | 13.9 | 10.1 | 6.6 | 6.2 | 10.9 | 12.9 |
| 27 | D | 49.8 | 47.5 | 13.4 | 2.7 | 3.6 | 16.3 | 12.2 | 10.9 | 35.3 | 22.9 | 15.1 | 16.4 | 18.6 | 22.9 | 22.3 | 22.6 | 21.8 | 21.8 | 18.4 | 9.9 | 5.9 | 6.2 | 7.2 | 7.9 | 18.0 |
| 28 |  | 10.2 | 11.2 | 11.9 | 11.4 | 10.1 | 11.6 | 13.1 | 3.1 | 9.7 | 11.4 | 11.6 | 11.7 | 18.6 | 18.1 | 19.6 | 19.8 | 20.4 | 18.6 | 18.6 | 14.3 | 11.6 | 10.1 | 8.5 | 9.1 | 13.0 |
| 29 | 0 | 8.7 | 8.6 | 9.2 | 9.2 | 9.7 | 10.2 | 10.2 | 13.3 | 11.4 | 11.4 | 12.1 | 13.4 | 15.6 | 17.9 | 19.8 | 23.1 | 23.3 | 18.3 | 11.7 | 6.9 | 3.6 | 4.6 | 4.9 | 4.7 | 11.7 |
| 30 |  | 5.4 | 8.6 | 8.4 | 8.2 | 8.2 | 8.1 | 8.2 | 8.1 | 8.7 | 10.6 | 11.1 | 11.4 | 12.1 | 13.4 | 15.3 | 19.9 | 21.4 | 22.1 | 10.7 | 3.6 | . 4 | -0.1 | 5.4 | 7.1 | 9.8 |
| 31 |  | 8.9 | 9.6 | 9.4 | 10.4 | 9.4 | 9.7 | 8.7 | 9.2 | 9.6 | 11.6 | 10.6 | 12.7 | 17.3 | 17.3 | 21.6 | 21.3 | 20.9 | 17.6 | 13.8 | 7.9 | 5.2 | 4.9 | 3.7 | 5.2 | 11.5 |
| MEAN | A | 8.5 | 9.4 | 9.2 | 8.9 | 9.1 | 9.5 | 9.1 | 9.4 | 11.4 | 11.2 | 11.1 | 13.0 | 15.5 | 18.5 | 20.4 | 21.6 | 21.4 | 18.9 | 14.1 | 8.9 | 5.7 | 4.3 | 4.5 | 6.0 | 11.6 |
| MEAN | 0 | 7.5 | 8.3 | 9.0 | 9.2 | 9.3 | 9.6 | 9.8 | 10.3 | 10.4 | 10.7 | 11.5 | 12.3 | 14.8 | 17.8 | 19.7 | 21.8 | 21.7 | 18.1 | 12.9 | 7.4 | 4.4 | 2.9 | 2.4 | 4.1 | 11.1 |
| MEAN | D | 15.1 | 16.1 | 10.1 | 6.9 | 9.2 | 9.3 | 8.8 | 9.6 | 18.6 | 15.3 | 12.5 | 13.2 | 15.6 | 20.9 | 22.5 | 25.0 | 23.0 | 20.7 | 16.9 | 10.6 | 5.3 | 3.5 | 4.4 | $7 \cdot 1$ | 13.3 |


| HOU |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 2 C | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | JT | T0 | TO | TC | ro | T0 | TO | 10 | T0 | TO | 10 | T0 | 10 | 10 | TC | 10 | 10 | T0 | 10 | TO | 10 | T0 | T0 | TC | T0 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 22 | 24 |  |
| 1 | D | 661 | 671 | 673 | 667 | 672 | 683 | 685 | 493 | 636 | 036 | 613 | 637 | 619 | 652 | 649 | 644 | 638 | 646 | 649 | ES5 | 685 | 671 | 683 | 685 | 650 |
| 2 |  | 709 | 695 | 697 | 711 | 685 | 662 | 624 | 602 | 647 | 635 | 660 | 666 | 666 | 661 | 661 | 658 | 652 | 647 | 650 | 652 | 648 | 656 | 659 | 660 | 661 |
| 3 |  | 662 | 667 | 672 | 672 | 664 | 661 | 6 60 | 659 | 660 | 661 | 661 | 664 | 660 | 655 | 648 | 648 | 648 | 649 | 648 | 644 | 644 | 647 | 650 | 662 | 657 |
| 4 | Q | 672 | 672 | 663 | 659 | 657 | 657 | 657 | 659 | 657 | 658 | 660 | 661 | 660 | 660 | 659 | 655 | 648 | 648 | 651 | 651 | ts 1 | 652 | 658 | 660 | 658 |
| 5 | 0 | 663 | 670 | 670 | 664 | 661 | 663 | $6 \in 1$ | 658 | 657 | 653 | 660 | 653 | 642 | 648 | 658 | 655 | 655 | 649 | 642 | 636 | 639 | 643 | 647 | 654 | 654 |
| 6 |  | 660 | 660 | 658 | 657 | 655 | 655 | 653 | 658 | 658 | 660 | 660 | 659 | 659 | 655 | 649 | 640 | 636 | 637 | 640 | 637 | 639 | 640 | 647 | 651 | 651 |
| 7 |  | 653 | 653 | 654 | 658 | 660 | 672 | 663 | 658 | 654 | 655 | 636 | 643 | 645 | 646 | 647 | 639 | 636 | 634 | 635 | 629 | 635 | 647 | $66 C$ | 672 | 649 |
| 8 |  | 678 | 670 | 660 | 657 | 660 | 666 | 658 | 657 | 651 | 648 | 648 | 653 | 659 | 651 | 649 | 649 | 648 | 649 | 658 | 654 | 658 | 666 | 672 | 684 | 659 |
| 9 |  | 696 | 712 | 722 | 722 | 707 | 710 | 682 | 663 | 634 | 660 | 658 | 659 | 655 | 648 | 648 | 657 | 654 | 651 | 653 | 654 | 672 | 674 | 672 | 671 | 672 |
| 10 |  | 670 | 675 | 700 | 696 | 689 | 681 | 672 | 664 | 659 | 634 | 610 | 637 | 653 | 657 | 649 | 641 | 660 | 660 | 661 | 663 | 658 | 659 | 671 | 681 | 663 |
| 11 |  | 684 | 682 | 684 | 672 | 660 | 658 | 658 | 659 | 649 | 648 | 651 | 657 | 658 | 65 E | 659 | 660 | 655 | 646 | 647 | 649 | 659 | 671 | 682 | 695 | 663 |
| 12 |  | 711 | 743 | 746 | 759 | 773 | 734 | 696 | 645 | 525 | 625 | 658 | 659 | 671 | 664 | 652 | 649 | 658 | 659 | 658 | 651 | 655 | 682 | 704 | 696 | 678 |
| 13 | D | 681 | 692 | 720 | 702 | 699 | 598 | 656 | 596 | 523 | 482 | 598 | 636 | 660 | 670 | 671 | 670 | 659 | 649 | 659 | 671 | 681 | 696 | 696 | 696 | 654 |
| 14 | D | 694 | 696 | 695 | 711 | 684 | 676 | 655 | 622 | 517 | 570 | 645 | 663 | 636 | 613 | 660 | 659 | 660 | 668 | 659 | 658 | 663 | 670 | 684 | 686 | 659 |
| 15 |  | 678 | 680 | 678 | 674 | 668 | 663 | 660 | 651 | 625 | 613 | 634 | 615 | 643 | 666 | 660 | 661 | 659 | 658 | 658 | 659 | 663 | 671 | 681 | 687 | 659 |
| 16 |  | 686 | 683 | 684 | 690 | 686 | 675 | 668 | 664 | 663 | 655 | 529 | 574 | 639 | 645 | 659 | 654 | 654 | 652 | 649 | 659 | 663 | 672 | 678 | 672 | 656 |
| 17 |  | 668 | 675 | 672 | 671 | 677 | 665 | 660 | 661 | 651 | 642 | 648 | 659 | 663 | 655 | 658 | 660 | 653 | 653 | 660 | 666 | 661 | 665 | 67 C | 669 | 662 |
| 18 |  | 661 | 661 | 660 | 660 | 660 | 660 | 660 | 655 | 652 | 642 | 624 | 595 | 647 | 635 | 636 | 651 | 651 | 651 | 655 | 655 | 655 | 653 | 66 C | 663 | 650 |
| 19 | $c$ | 660 | 660 | 659 | 659 | 659 | 659 | 652 | 637 | 641 | 639 | 637 | 653 | 660 | 658 | 654 | 654 | 655 | 655 | 655 | 665 | 684 | 659 | 664 | 665 | 655 |
| 20 | 0 | 661 | 661 | 660 | 659 | 659 | 659 | 653 | 652 | 653 | 654 | 655 | 655 | 651 | 652 | 649 | 651 | 643 | 641 | 642 | 645 | 651 | 657 | 658 | 660 | 653 |
| 21 |  | 664 | 665 | 664 | 657 | 654 | 654 | 653 | 653 | 653 | 654 | 653 | 655 | 654 | 648 | 642 | 636 | 636 | 647 | 642 | 653 | 659 | 665 | 672 | 684 | 655 |
| 22 |  | 685 | 691 | 682 | 670 | 659 | 673 | 698 | 674 | 681 | 674 | 657 | 665 | 667 | 660 | 660 | 654 | 648 | 650 | 647 | 648 | 650 | 66C | 664 | 676 | 666 |
| 23 |  | 677 | 657 | 653 | 657 | 653 | 654 | 652 | 651 | 652 | 651 | 647 | 6.39 | 648 | 654 | 660 | 664 | 659 | 656 | 658 | 659 | 657 | 660 | 677 | 688 | 658 |
| 24 |  | 680 | 667 | 659 | 653 | 654 | 658 | 657 | 656 | 653 | 656 | 657 | 658 | 659 | 653 | 650 | 648 | 647 | 641 | 642 | 646 | 648 | 654 | 658 | 653 | 655 |
| 25 |  | 654 | 657 | 667 | 676 | 679 | 671 | 641 | 657 | $6 \in 0$ | 654 | 654 | 653 | 657 | 658 | 659 | 658 | 658 | 659 | 659 | 658 | 658 | 659 | 665 | 667 | 660 |
| 26 | D | 668 | 663 | 677 | 698 | 693 | 685 | 667 | 658 | 657 | 658 | 658 | 662 | 653 | 641 | 569 | 589 | 623 | 629 | 624 | 634 | 642 | 648 | 664 | 722 | 653 |
| 27 | D | 604 | 703 | 539 | 648 | 683 | 658 | 659 | 654 | 658 | 611 | 622 | 646 | 614 | 628 | 662 | 676 | 665 | 664 | 663 | 693 | 682 | 674 | 665 | 668 | 652 |
| 28 |  | 675 | 682 | 674 | 671 | 671 | 669 | 654 | 564 | 599 | 651 | 670 | 673 | 675 | 671 | 667 | 665 | 663 | 660 | 657 | 663 | 663 | 663 | 665 | 662 | 859 |
| 29 | c | 658 | 659 | 658 | 658 | 659 | 659 | 659 | 659 | 659 | 658 | 652 | 657 | 658 | 657 | 662 | 662 | 659 | 656 | 652 | 650 | 653 | 648 | $65 ?$ | 656 | 657 |
| 30 |  | 667 | 670 | 668 | 662 | 659 | 659 | 659 | 659 | 658 | 659 | 660 | 659 | 658 | 659 | 654 | 647 | 640 | 646 | 657 | 651 | 668 | 669 | 675 | 691 | 661 |
| 31 |  | 701 | 685 | 664 | 671 | 662 | 659 | 659 | 660 | 653 | 647 | 646 | 646 | 657 | 659 | 652 | 650 | 650 | 645 | 645 | C52 | 656 | 664 | 67 C | 671 | 659 |
| MEAN | A | 672 | 677 | 672 | 676 | 673 | 666 | $6 \in 2$ | 644 | 641 | 640 | 643 | 649 | 653 | 653 | 652 | 652 | 651 | 650 | 651 | 654 | 657 | 662 | 665 | 674 | 658 |
| MEAN | 0 | 663 | 665 | 662 | 660 | 659 | 659 | 656 | 653 | 653 | 652 | 653 | 656 | 654 | 655 | 656 | 656 | 652 | 650 | 649 | 649 | 651 | 652 | 651 | 659 | 656 |
| ME AN | 0 | 662 | 685 | 661 | 685 | 686 | 660 | 673 | 605 | 610 | 591 | 627 | 649 | 636 | 641 | 642 | 648 | 649 | 651 | 651 | 662 | 671 | 672 | 675 | 691 | 654 |


| HDURUT |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | T0 | T0 | T0 | 10 | T0 | 10 | TO | T0 | 10 | T0 | 10 | 10 | 10 | 10 | 10 | 10 | TO | T0 | 10 | TC | 10 | T0 | TC | TO | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |  |
| 1 | 0 | 761 | 758 | 759 | 755 | 753 | 751 | 747 | 754 | 756 | 755 | 748 | 739 | 739 | 743 | 748 | 746 | 733 | 724 | 703 | 695 | 698 | 711 | 737 | 750 | 740 |
| 2 |  | 748 | 749 | 749 | 749 | 750 | 749 | 751 | 753 | 754 | 756 | 758 | 762 | 767 | 774 | 759 | 765 | 755 | 733 | 717 | 713 | 715 | 717 | 732 | 748 | 747 |
| 3 | D | 757 | 767 | 779 | 765 | 753 | 754 | 761 | 762 | 7E2 | 753 | 755 | 731 | 729 | 741 | 740 | 740 | 729 | 711 | 688 | 726 | 733 | 754 | 791 | 781 | 748 |
| 4 |  | 783 | 806 | 847 | 768 | 755 | 710 | 733 | 741 | 739 | 711 | 617 | 683 | 746 | 760 | 751 | 738 | 703 | 695 | 689 | 712 | 724 | 738 | 7EE | 758 | 736 |
| 5 |  | 761 | 760 | 767 | 767 | 767 | 734 | 748 | 750 | 748 | 748 | 749 | 727 | 673 | 747 | 762 | 754 | 747 | 733 | 722 | 716 | 717 | 724 | 736 | 749 | 742 |
| 6 |  | 759 | 786 | 780 | 755 | 757 | 756 | 749 | 754 | 752 | 755 | 755 | 747 | 757 | 760 | 758 | 749 | 738 | 728 | 724 | 725 | 727 | 727 | 734 | 756 | 749 |
| 7 |  | 757 | 758 | 760 | 759 | 757 | 758 | 757 | 763 | 758 | 766 | 765 | 768 | 765 | 757 | 743 | 746 | 740 | 728 | 716 | 704 | 715 | 727 | 763 | 767 | 750 |
| 8 |  | 787 | 765 | 751 | 748 | 753 | 752 | 758 | 767 | 756 | 760 | 757 | 634 | 740 | 747 | 755 | 752 | 727 | 716 | 719 | 721 | 721 | 747 | 738 | 771 | 743 |
| 9 |  | 763 | 756 | 784 | 775 | 747 | 747 | 748 | 749 | 750 | 756 | 756 | 755 | 747 | 738 | 746 | 757 | 737 | 724 | 723 | 135 | 734 | 737 | $75 t$ | 758 | 749 |
| 10 |  | 771 | 765 | 756 | 755 | 756 | 756 | 754 | 748 | 633 | 686 | 755 | 752 | 736 | 735 | 737 | 737 | 732 | 715 | 713 | 720 | 126 | 735 | 745 | 754 | 736 |
| 11 | 0 | 755 | 755 | 754 | 751 | 755 | 754 | 755 | 756 | 758 | 763 | 757 | 761 | 756 | 767 | 766 | 763 | 746 | 737 | 728 | 732 | 739 | 743 | 754 | 763 | 753 |
| 12 | D | 769 | 791 | 767 | 783 | 821 | 767 | 768 | 757 | 623 | 766 | 723 | 490 | 686 | 732 | 745 | 747 | 716 | 665 | 133 | 748 | 755 | 763 | 755 | 753 | 734 |
| 13 |  | 748 | 757 | 746 | 755 | 764 | 745 | 745 | 747 | 673 | 714 | 755 | 748 | 748 | 750 | 753 | 744 | 726 | 708 | 704 | 727 | 747 | 747 | 767 | 763 | 741 |
| 14 |  | 764 | 747 | 754 | 760 | 757 | 756 | 738 | 692 | 755 | 734 | 655 | 699 | 701 | 686 | 706 | 734 | 744 | 724 | 715 | 723 | 734 | 737 | 744 | 747 | 729 |
| 15 |  | 755 | 757 | 756 | 756 | 759 | 756 | 756 | 748 | 757 | 755 | 755 | 757 | 766 | 765 | 765 | 757 | 745 | 735 | 735 | 735 | 735 | 747 | 746 | 746 | 752 |
| 16 |  | 749 | 754 | 757 | 759 | 758 | 757 | 757 | 757 | 763 | 756 | 754 | 758 | 765 | 773 | 775 | 766 | 734 | 732 | 726 | 728 | 735 | 738 | 738 | 750 | 752 |
| 17 |  | 766 | 785 | 788 | 796 | 806 | 777 | 761 | 746 | 745 | 747 | 756 | 756 | 756 | 759 | 755 | 737 | 722 | 704 | 706 | 711 | 724 | 736 | 745 | 748 | 751 |
| 18 |  | 755 | 764 | 755 | 746 | 754 | 756 | 757 | 758 | 759 | 757 | 764 | 767 | 760 | 744 | 714 | 737 | 747 | 727 | 716 | 724 | 733 | 742 | 755 | 756 | 748 |
| 19 | D | 775 | 765 | 763 | 749 | 756 | 765 | 754 | 751 | 736 | 702 | 722 | 748 | 745 | 755 | 764 | 753 | 714 | 713 | 696 | 703 | 745 | 755 | 756 | 805 | 745 |
| 20 |  | 735 | 736 | 755 | 753 | 754 | 759 | 709 | 652 | 721 | 124 | 755 | 756 | 746 | 717 | 737 | 739 | 719 | 708 | 703 | 709 | 725 | 733 | 755 | 764 | 732 |
| 21 |  | 764 | 756 | 739 | 754 | 755 | 756 | 755 | 755 | 757 | 757 | 757 | 754 | 745 | 734 | 733 | 735 | 714 | 718 | 719 | 719 | 724 | 744 | 747 | 763 | 744 |
| 22 |  | 736 | 755 | 751 | 755 | 760 | 758 | 757 | 761 | 764 | 766 | 766 | 760 | 755 | 750 | 757 | 748 | 735 | 733 | 722 | 724 | 746 | 724 | 746 | 767 | 750 |
| 23 |  | 780 | 757 | 755 | 777 | 838 | 788 | 757 | 766 | 767 | 724 | 633 | 674 | 715 | 736 | 745 | 749 | 726 | 715 | 723 | 725 | 731 | 735 | 756 | 781 | 744 |
| 24 |  | 773 | 759 | 755 | 755 | 753 | 756 | 756 | 757 | 757 | 756 | 751 | 745 | 746 | 749 | 765 | 757 | 744 | 724 | 717 | 721 | 726 | 733 | 745 | 763 | 748 |
| 25 | 0 | 758 | 758 | 756 | 766 | 757 | 758 | 755 | 754 | 755 | 756 | 756 | 756 | 757 | 755 | 750 | 736 | 717 | 706 | 704 | 713 | 717 | 726 | 743 | 749 | 744 |
| 26 | D | 757 | 765 | 760 | 758 | 764 | 765 | 766 | 765 | 766 | 716 | 635 | 734 | 716 | 766 | 778 | 765 | 743 | 725 | 727 | 734 | 747 | 769 | 745 | 784 | 748 |
| 27 | 0 | 808 | 850 | 981 | 1066 | 716 | 799 | 770 | 744 | 683 | 628 | 609 | 656 | 727 | 747 | 743 | 736 | 725 | 715 | 700 | 716 | 748 | 753 | 763 | 768 | 756 |
| 28 |  | 756 | 765 | 765 | 767 | 766 | 746 | 755 | 753 | 748 | 744 | 747 | 755 | 754 | 744 | 736 | 732 | 720 | 706 | 693 | 702 | 716 | 725 | 735 | 743 | 740 |
| 29 | 0 | 749 | 756 | 764 | 757 | 758 | 757 | 756 | 759 | $7 \in 0$ | 758 | 757 | 756 | 760 | 756 | 749 | 744 | 736 | 717 | 704 | 701 | 706 | 717 | 727 | 747 | 744 |
| 30 | 0 | 755 | 756 | 757 | 757 | 760 | 766 | 768 | 755 | 756 | 763 | 761 | 765 | 765 | 750 | 758 | 756 | 744 | 728 | 721 | 713 | 716 | 717 | 738 | 757 | 749 |
| 31 |  | 766 | 767 | 765 | 764 | 764 | 765 | 766 | 746 | 748 | 755 | 759 | 757 | 754 | 754 | 751 | 745 | 716 | 703 | 704 | 714 | 726 | 743 | $75 C$ | 758 | 747 |
| MEAN | A | 762 | 765 | 770 | 770 | 162 | 757 | 754 | 749 | 741 | 741 | 734 | 731 | 743 | 748 | 750 | 747 | 731 | 718 | 713 | 719 | 129 | 737 | 145 | 760 | 745 |
| ME AN | 0 | 756 | 757 | 758 | 757 | 757 | 757 | 756 | 756 | 757 | 759 | 756 | 756 | 756 | 754 | 754 | 749 | 735 | 722 | 712 | 711 | 715 | 723 | 74 C | 753 | 746 |
| MEAN | D | 773 | 788 | 810 | 824 | 762 | 770 | 764 | 756 | 714 | 713 | 689 | 672 | 721 | 748 | 754 | 748 | 725 | 706 | 709 | 725 | 745 | 759 | 762 | 778 | 746 |


| HOU |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 20 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | J | 10 | 10 | T0 | TC | 10 | TO | TO | TO | 10 | 10 | 10 | T0 | T0 | TC | 10 | 1 C | 10 | T0 | то | 10 | 10 | T0 | TO | 10 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |  |
| 1 | 0 | 8.4 | 9.5 | 10.1 | 10.0 | 10.3 | 10.5 | 10.6 | 11.1 | 11.4 | 11.1 | 11.1 | 12.1 | 13.8 | 15.9 | 20. 1 | 22.5 | 22.5 | 20.3 | 14.6 | 9.5 | 5.2 | 3.1 | 3.2 | 5.0 | 11.8 |
| 2 |  | 6.9 | 8.9 | 10.5 | 10.1 | 10.0 | 10.1 | 10.5 | 10.5 | 10.6 | 10.5 | 12.1 | 14.0 | 17.9 | 20.8 | 22.1 | 25.8 | 24.8 | 23.2 | 16.4 | 9.3 | 1.1 | $-1.3$ | . 8 | 3.4 | 12.0 |
| 3 | D | 6.8 | 7.7 | 7.9 | 6.1 | 8.7 | 8.7 | 9.5 | 10.0 | 9.5 | 16.1 | 15.6 | 14.0 | 18.2 | 23.8 | 25.8 | 24.3 | 22.7 | 19.3 | 10.5 | 6.4 | 2.4 | 1.4 | 2.3 | 2.1 | 11.7 |
| 4 |  | 3.1 | 3.2 | 8.5 | 15.8 | 10.1 | 11.1 | 8.0 | 8.0 | 7.6 | 4.7 | 8.0 | 15.0 | 15.1 | 20.1 | 22.7 | 24.1 | 22.1 | 14.8 | 13.4 | 8.7 | 5.2 | 7.2 | 7.6 | 8.4 | 11.4 |
| 5 |  | 9.2 | 10.5 | 9.8 | 18.2 | 11.1 | 16.3 | 10.9 | 9.7 | 10.5 | 11.6 | 11.8 | 11.3 | 11.9 | 18.7 | 20.9 | 22.1 | 22.1 | 16.1 | 10.0 | 6.1 | 4.5 | 3.5 | 5.8 | 8.4 | 12.1 |
| 6 |  | 8.9 | 8.2 | 11.8 | 9.2 | 12.2 | 15.1 | 11.3 | 8.9 | 9.7 | 10.0 | 10.1 | 11.6 | 16.3 | 17.9 | 18.5 | 21.4 | 19.6 | 16.4 | 9.7 | 3.9 | $-0.2$ | $-1.0$ | 1.9 | 4.0 | 10.6 |
| 7 |  | 6.6 | 7.7 | 7.9 | 8.4 | 8.9 | 11.6 | 17.5 | 14.6 | 13.0 | 11.4 | 13.0 | 13.5 | 18.0 | 20.0 | 21.3 | 19.6 | 16.7 | 13.2 | 11.3 | 6.6 | 4.7 | 3.4 | 5.5 | 8.5 | 11.8 |
| 8 |  | 11.1 | 13.4 | 11.4 | 9.2 | 8.4 | 8.5 | 8.9 | 12.9 | 20.8 | 16.6 | 11.6 | 11.9 | 19.8 | 23.7 | 25.6 | 20.9 | 18.2 | 13.5 | 10.5 | 6.4 | 5.0 | 7.1 | 5.8 | 6.9 | 12.8 |
| 9 |  | 10.1 | 10.5 | 11.6 | 15.0 | 11.3 | 8.4 | 9.3 | 13.2 | 18.4 | 12.6 | 11.8 | 10.0 | 14.8 | 19.5 | 19.3 | 18.5 | 16.7 | 12.4 | 9.8 | 6.1 | 6.9 | 7.2 | 9.8 | 11.6 | 12.3 |
| 10 |  | 11.4 | 11.4 | 11.9 | 11.6 | 13.2 | 11.6 | 10.0 | 9.2 | 6.4 | 8.2 | 13.0 | 13.2 | 17.5 | 21.3 | 20.9 | 21.1 | 18.2 | 17.5 | 12.6 | 10.1 | 8.C | 6.9 | 6.8 | 7.1 | 12.5 |
| 11 | 0 | 8.4 | 9.8 | 10.0 | 10.0 | 9.3 | 9.8 | 10.1 | 10.3 | 10.3 | 10.0 | 11.4 | 13.8 | 17.7 | 19.2 | 21.1 | 21.6 | 19.6 | 18.2 | 11.3 | 6.8 | 8.2 | 7.7 | 8. C | 8.4 | 12.1 |
| 12 | D | 8.4 | 8.0 | 7.9 | 10.0 | 10.5 | 22.1 | 11.9 | 10.0 | 5.6 | 18.7 | 8.7 | 15.0 | 21.1 | 19.3 | 18.0 | 21.4 | 19.2 | 7.9 | . 2 | 3.9 | 3.5 | 6.6 | 8.4 | 9.5 | 11.5 |
| 13 |  | 10.3 | 8.9 | 9.7 | 11.4 | 11.3 | 8.5 | 7.4 | 8.5 | $-1.5$ | 5.2 | 10.5 | 10.3 | 16.3 | 19.5 | 18.7 | 17.7 | 17.2 | 16.1 | 10.1 | 5.2 | 5.2 | 6.1 | 8.5 | 10.6 | 10.5 |
| 14 |  | 11.8 | 11.6 | 10.1 | 10.0 | 9.7 | 11.4 | 10.1 | 11.3 | 11.6 | 8.7 | 10.9 | 13.8 | 11.6 | 14.5 | 19.8 | 21.7 | 19.8 | 16.7 | 12.1 | 5.3 | 3.5 | 5.3 | 7.2 | 8.4 | 11.5 |
| 15 |  | 8.5 | 9.5 | 9.5 | 9.5 | 9.5 | 9.7 | 10.0 | 11.6 | 11.4 | 11.8 | 12.9 | 13.5 | 13.7 | 16.3 | 18.2 | 18.0 | 18.0 | 16.3 | 13.4 | 8.2 | 7.1 | 6.8 | 6.6 | 8.1 | 11.6 |
| 16 |  | 10.1 | 10.0 | 10.0 | 10.1 | 10.1 | 10.1 | 10.3 | 11.4 | 11.8 | 12.2 | 9.2 | 13.5 | 15.0 | 16.7 | 17.9 | 17.7 | 16.7 | 15.1 | 8.7 | 3.5 | 4.2 | 4.8 | 5.6 | 8.2 | 11.0 |
| 17 |  | 10.2 | 9.9 | 9.2 | 3.4 | 2.3 | 9.9 | 6.5 | 11.2 | 11.2 | 13.3 | 12.1 | 13.1 | 15.4 | 17.6 | 19.1 | 19.5 | 18.4 | 16.2 | 11.5 | 7.0 | 4.6 | 4.9 | 5.1 | 6.8 | 10.8 |
| 18 |  | 8.3 | 8.4 | 11.5 | 8.4 | 8.4 | 8.8 | 9.7 | 9.9 | 10.0 | 9.9 | 12.5 | 11.5 | 13.7 | 16.5 | 16.2 | 20.8 | 21.5 | 19.1 | 13.4 | 6.7 | 5.7 | 6.2 | 6.1 | 8.3 | 11.3 |
| 19 | D | 8.1 | 8.3 | 10.0 | 7.9 | 8.1 | 15.0 | 14.5 | 11.7 | 9.9 | 9.6 | 5.7 | 15.4 | 19.5 | 21.0 | 20.8 | 22.3 | 19.4 | 11.5 | 9.6 | t. 2 | 3.6 | -1.1 | 5.1 | 5.2 | 11.1 |
| 20 |  | 6.5 | 8.4 | 9.9 | 13.1 | 10.4 | 11.3 | 8.1 | 10.0 | 18.6 | 13.9 | 13.7 | 14.1 | 16.3 | 16.2 | 19.2 | 18.3 | 17.8 | 13.4 | 9.7 | 7.3 | 6.3 | 6.5 | 6.3 | 8.4 | 11.8 |
| 21 |  | 9.4 | 9.4 | 9.1 | 9.9 | 18.6 | 9.9 | 8.8 | 9.6 | 9.9 | 11.2 | 11.7 | 13.1 | 14.5 | 16.0 | 17.4 | 20.5 | 17.4 | 10.8 | 14.4 | 11.7 | 7.9 | 8.1 | $8 \cdot 3$ | 8.1 | 11.9 |
| 22 |  | 8.6 | 7.5 | 7.8 | 8.1 | 9.1 | 9.2 | 9.9 | 10.5 | 11.2 | 11.7 | 12.1 | 13.3 | 16.2 | 18.3 | 19.7 | 19.5 | 19.7 | 16.2 | 8.3 | 4.1 | 2.3 | 2.6 | $3 . \varepsilon$ | 4.7 | 10.6 |
| 23 |  | 3.3 | 4.1 | 6.3 | 4.9 | 3.8 | 6.5 | 7.0 | 12.9 | 12.3 | 10.5 | 6.3 | 11.7 | 16.5 | 23.6 | 22.8 | 19.2 | 16.5 | 13.9 | 11.3 | 2.4 | 7.C | 7.1 | 8.1 | 8.3 | 10.5 |
| 24 |  | 8.6 | 8.4 | 9.6 | 11.7 | 9.9 | 9.7 | 9.6 | 9.9 | 10.7 | 13.1 | 13.4 | 19.9 | 21.3 | 23.1 | 24.4 | 24.c | 21.3 | 19.7 | 13.1 | 8.6 | 5.5 | 5.2 | 5.4 | 6.8 | 13.0 |
| 25 | 0 | 9.2 | 11.8 | 13.1 | 8.4 | 8.3 | 8.3 | 9.4 | 8.4 | 9.9 | 11.5 | 12.1 | 12.9 | 14.1 | 14.9 | 17.8 | 19.2 | 19.7 | 18.3 | 13.6 | 8.9 | 6.3 | 5.1 | 6.2 | 7.9 | 11.5 |
| 26 | D | 8.6 | 8.6 | 9.2 | 9.4 | 8.8 | 8.3 | 8.6 | 11.5 | 11.7 | 5.2 | 4.6 | 17.8 | 17.9 | 18.1 | 23.2 | 24.2 | 22.4 | 17.6 | 11.3 | 6.5 | 3.4 | 3.4 | 4.7 | 3.3 | 11.2 |
| 27 | D | 1.7 | -4.8 | 6.8 | 10.0 | 3.3 | 13.3 | 8.1 | 7.1 | 12.8 | 21.0 | 2 C .7 | 17.8 | 14.7 | 19.5 | 20.3 | 18.4 | 15.2 | 14.9 | 8.4 | 4.2 | 5.4 | 8.4 | 9.7 | 10.5 | 11.2 |
| 28 |  | 11.7 | 11.0 | 8.4 | 7.3 | 13.1 | 11.8 | 11.7 | 11.3 | 11.3 | 11.5 | 12.0 | 14.4 | 16.3 | 18.1 | 20.2 | 21.3 | 20.8 | 17.4 | 10.2 | 1.8 | 3.4 | 4.7 | 6.8 | 8.6 | 11.9 |
| 29 | 0 | 9.9 | 10.2 | 10.0 | 9.7 | 9.7 | 9.6 | 9.9 | 10.0 | 10.8 | 11.8 | 12.8 | 13.6 | 16.2 | 18.4 | 22.6 | 23.7 | 23.4 | 18.1 | 12.8 | 6.8 | 3.9 | 3.3 | 4.7 | 6.8 | 12.0 |
| 30 | c | 8.6 | 9.9 | 9.6 | 9.6 | 9.9 | 9.7 | 12.0 | 11.5 | 9.6 | 11.7 | 12.8 | 12.9 | 14.5 | 14.1 | 19.4 | 21.2 | 22.9 | 2C. 7 | 15.0 | 9.9 | 6.0 | 3.8 | 4.7 | 6.5 | 11.9 |
| 31 |  | 8.3 | 8.9 | 9.1 | 9.2 | 9.9 | 10.2 | 11.2 | 14.9 | 17.9 | 13.7 | 12.9 | 13.1 | 12.9 | 17.8 | 20.8 | 23.7 | 23.1 | 16.0 | 11.0 | 5.1 | 3.3 | 3.1 | 2.5 | 3.6 | 11.8 |
| MEAN | A | 8.4 | 8.7 | 9.6 | 9.9 | 9.6 | 10.8 | 10.0 | 10.7 | 11.1 | 11.6 | 11.5 | 13.6 | 16.1 | 18.7 | 20.5 | 21.1 | 19.8 | 16.2 | 11.2 | 6.7 | $4=8$ | 4.7 | 5.8 | 7.2 | 11.6 |
| ME AN | 0 | 8.9 | 10.2 | 10.6 | 9.5 | 9.5 | 9.6 | 10.4 | 10.3 | 10.4 | 11.2 | 12.0 | 13.1 | 15.3 | 16.5 | 20.2 | 21.6 | 21.6 | 19.1 | 13.5 | 8.4 | 5.9 | 4.6 | 5.4 | 6.9 | 11.9 |
| MEAN | D | 6.7 | 5.6 | 8.4 | 8.7 | 7.9 | 13.5 | 10.5 | 10.0 | 9.9 | 14.1 | 11.0 | 16.0 | 18.3 | 20.4 | 21.6 | 22.1 | 19.8 | 14.2 | 8.0 | 5.4 | 3.7 | 3.8 | 6.C | 6.1 | 11.3 |


| HOU |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 1 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | T | T0 | T0 | T0 | 10 | T0 | T0 | 10 | T0 | 10 | T0 | 10 | T0 | 10 | TC | TC | TC | T0 | TC | T0 | 10 | 10 | 10 | 10 | T0 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |  |
| 1 | 0 | 666 | 659 | 657 | 653 | 653 | 653 | 653 | 653 | 652 | 646 | 637 | 634 | 634 | 634 | 642 | 644 | 644 | 646 | 650 | 6.50 | 650 | 651 | 655 | 658 | 649 |
| 2 |  | 659 | 664 | 663 | 661 | 662 | 662 | 651 | 652 | 651 | 651 | 651 | 653 | 654 | 654 | 650 | 646 | 648 | 648 | 643 | 641 | 643 | 645 | 651 | 654 | 652 |
| 3 | D | 653 | 655 | 661 | 663 | 659 | 652 | 651 | 650 | 648 | 634 | 644 | 634 | 618 | 623 | 625 | 623 | 628 | 630 | 633 | 646 | 651 | 668 | 701 | 718 | 649 |
| 4 |  | 737 | 751 | 747 | 711 | 679 | 607 | 644 | 653 | 644 | 610 | 515 | 588 | 644 | 670 | 670 | 656 | 653 | 654 | 667 | 673 | 671 | 674 | 672 | 663 | 661 |
| 5 |  | 662 | 669 | 677 | 695 | 689 | 619 | 652 | 660 | 657 | 653 | 654 | 628 | 574 | 626 | 645 | 660 | 659 | 659 | 651 | 653 | 658 | 858 | 659 | 667 | 653 |
| 6 |  | 669 | 683 | 897 | 683 | 661 | 659 | 657 | 659 | 659 | 659 | 659 | 651 | 660 | 660 | 659 | 652 | 652 | 654 | 656 | 655 | 652 | 641 | 642 | 653 | 660 |
| 7 |  | 654 | 653 | 653 | 655 | 659 | 661 | 643 | 632 | 652 | 659 | 658 | 659 | 654 | 651 | 650 | 649 | 648 | 649 | 643 | 647 | 658 | 67c | 688 | 708 | 656 |
| B |  | 715 | 696 | 678 | 660 | 658 | 656 | 658 | 650 | 611 | 624 | 640 | 525 | 586 | 623 | 634 | 659 | 660 | 659 | 659 | 646 | 643 | 659 | 668 | 677 | 648 |
| 9 |  | 680 | 689 | 707 | 725 | 678 | 665 | 659 | 642 | 633 | 641 | 652 | 634 | 631 | 618 | 617 | 640 | 646 | 649 | 650 | 658 | 654 | 668 | 676 | 686 | 658 |
| 10 |  | 682 | 678 | 677 | 678 | 681 | 689 | 681 | 654 | 552 | 517 | 624 | 644 | 632 | 612 | 605 | 630 | 657 | 659 | 668 | 676 | 672 | 670 | 668 | 662 | 649 |
| 11 | 0 | 660 | 659 | 659 | 659 | 659 | 659 | 659 | 659 | 659 | 659 | 658 | 659 | 659 | 659 | 657 | 656 | 653 | 653 | 648 | 642 | 646 | 648 | 65 C | 658 | 656 |
| 12 | D | 668 | 676 | 710 | 724 | 715 | 641 | 658 | 660 | 520 | 612 | 611 | 425 | 552 | 604 | 626 | 644 | 651 | 633 | 650 | 658 | 651 | 659 | 668 | 669 | 637 |
| 13 |  | 669 | 670 | 667 | 670 | 677 | 669 | 643 | 651 | 498 | 526 | 624 | 643 | 649 | 652 | 659 | 659 | 660 | 663 | 660 | 665 | 669 | 677 | 686 | 678 | 649 |
| 14 |  | 672 | 670 | 668 | 668 | 669 | 672 | 636 | 557 | 632 | 611 | 493 | 576 | 584 | 584 | 620 | 649 | 660 | 664 | 667 | 668 | 662 | 665 | 666 | 667 | 637 |
| 15 |  | 667 | 660 | 659 | 659 | 659 | 660 | 661 | 658 | 650 | 659 | 659 | 660 | 659 | 659 | 659 | 659 | 659 | 659 | 651 | 648 | 650 | 658 | 662 | 668 | 659 |
| 16 |  | 666 | 659 | 659 | 659 | 657 | 657 | 654 | 651 | 650 | 639 | 619 | 630 | 650 | 658 | 657 | 654 | 648 | 641 | 638 | 641 | 651 | 861 | 67 C | 675 | 652 |
| 17 |  | 681 | 698 | 724 | 753 | 171 | 726 | 696 | 673 | 658 | 655 | 662 | 660 | 659 | 661 | 661 | 659 | 859 | 655 | 655 | 660 | 668 | 670 | 669 | 667 | 679 |
| 18 |  | 667 | 678 | 690 | 670 | 659 | 658 | 652 | 651 | 650 | 644 | 640 | 652 | 659 | 649 | 611 | 610 | 636 | 640 | 640 | 647 | $65 ?$ | 659 | 655 | 659 | 651 |
| 19 | D | 669 | 676 | 685 | 690 | 679 | 681 | 653 | 650 | 602 | 513 | 491 | 581 | 611 | 624 | 643 | 650 | 636 | 657 | 667 | 678 | 6.76 | 725 | 759 | 675 | 651 |
| 20 |  | 665 | 668 | 687 | 691 | 697 | 690 | 602 | 494 | 584 | 592 | 611 | 659 | 659 | 640 | 648 | 662 | 670 | 671 | 669 | 668 | 670 | 672 | 676 | 678 | 651 |
| 21 |  | 673 | 673 | 669 | 670 | 660 | 658 | 656 | 655 | 656 | 658 | 659 | 659 | 654 | 640 | 630 | 633 | 641 | 633 | 641 | 653 | 655 | 659 | $66 C$ | 671 | 655 |
| 22 |  | 659 | 662 | 659 | 659 | 659 | 659 | 658 | 658 | 658 | 659 | 652 | 643 | 633 | 642 | 649 | 652 | 658 | 655 | 649 | 649 | 650 | 651 | $65 ?$ | 659 | 653 |
| 23 |  | 670 | 668 | 660 | 667 | 696 | 686 | 666 | 651 | 669 | 642 | 563 | 538 | 575 | 623 | 642 | 655 | 670 | 670 | 668 | 676 | 687 | 688 | 682 | 687 | 654 |
| 24 |  | 685 | 690 | 688 | 679 | 671 | 661 | 661 | 660 | 660 | 660 | 643 | 642 | 653 | 646 | 658 | 659 | 657 | 652 | 650 | 650 | 655 | 659 | $66 C$ | 667 | 661 |
| 25 | 0 | 670 | 676 | 671 | 670 | 669 | 670 | 660 | 643 | 649 | 652 | 654 | 659 | 660 | 660 | 660 | 660 | 660 | 660 | 654 | 656 | 630 | 662 | 663 | 661 | 661 |
| 26 | D | 661 | 661 | 660 | 680 | 660 | 660 | 661 | 653 | 662 | 617 | 427 | 550 | 553 | 584 | 635 | 653 | 660 | 664 | 660 | 660 | 680 | 661 | 662 | 677 | 636 |
| 27 | D | 717 | 735 | 737 | 605 | 498 | 687 | 690 | 663 | 637 | 475 | 545 | 594 | 624 | 644 | 645 | 659 | 660 | 660 | 660 | 680 | 687 | 689 | 681 | 691 | 648 |
| 28 |  | 690 | 694 | 698 | 721 | 678 | 600 | 670 | 667 | $6 \in 0$ | 649 | 668 | 675 | 672 | 664 | 660 | 660 | 664 | 661 | 660 | 660 | 602 | 673 | 680 | 678 | 669 |
| 29 | 0 | 670 | 662 | 663 | 663 | 662 | 661 | 680 | 660 | 661 | 661 | 661 | 661 | 660 | 660 | 653 | 650 | 652 | 654 | 652 | 659 | 66 C | 666 | 67 C | 671 | 661 |
| 30 | 0 | 669 | 661 | 660 | 660 | 661 | 662 | 669 | 670 | 654 | 661 | 660 | 681 | 662 | 652 | 660 | 681 | 666 | 662 | 660 | 660 | $6 \in 2$ | 665 | 666 | 664 | 662 |
| 31 |  | 660 | 660 | 660 | 660 | 660 | 659 | 659 | 614 | 622 | 643 | 660 | 662 | 668 | 668 | 667 | 666 | 660 | 650 | 651 | 660 | $6 E 5$ | 672 | 679 | 681 | 659 |
| MEAN | A | 674 | 676 | 679 | 676 | 668 | 661 | 657 | 645 | 634 | 625 | 619 | 624 | 634 | 640 | 645 | 651 | 655 | 654 | 654 | 657 | 660 | 666 | 671 | 673 | 654 |
| MEAN | 0 | 667 | 664 | 662 | 661 | 661 | 661 | $6 \in 0$ | 657 | 655 | 656 | 654 | 655 | 655 | 653 | 654 | 654 | 655 | 655 | 653 | 653 | 656 | 659 | 661 | 662 | 658 |
| MEAN | D | 674 | 681 | 691 | 668 | 642 | 664 | 662 | 655 | 614 | 570 | 544 | 557 | 592 | 616 | 635 | 646 | 651 | 649 | 654 | 665 | 669 | 680 | 694 | 686 | 644 |

## HORIZONTAL INTENSITY

| HOUR |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 2 C | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | UT | 10 | T0 | T0 | 10 | 10 | TO | 10 | T0 | 10 | 10 | T0 | 10 | 10 | 10 | 10 | 10 | 10 | 10 | 10 | 10 | 10 | T0 | TC | 10 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 22 | 24 |  |
| 1 | 0 | 736 | 756 | 762 | 763 | 754 | 755 | 757 | 755 | 756 | 764 | 760 | 759 | 761 | 761 | 757 | 746 | 729 | 709 | 694 | 706 | 719 | 733 | 744 | 746 | 745 |
| 2 | 0 | 753 | 760 | 762 | 763 | 763 | 763 | 765 | 763 | 757 | 756 | 761 | 763 | 760 | 765 | 763 | 746 | 728 | 706 | 695 | 706 | 722 | 736 | 745 | 757 | 748 |
| 3 |  | 766 | 765 | 764 | 765 | 764 | 764 | 765 | 765 | 765 | 764 | 766 | 757 | 763 | 764 | 756 | 746 | 726 | 719 | 724 | 726 | 134 | 733 | 752 | 763 | 753 |
| 4 |  | 756 | 756 | 756 | 755 | 756 | 759 | 759 | 739 | 765 | 759 | 770 | 766 | 764 | 756 | 752 | 739 | 724 | 714 | 714 | 730 | 745 | 757 | 754 | 747 | 750 |
| 5 |  | 749 | 752 | 755 | 765 | 765 | 765 | 770 | 770 | 766 | 764 | 765 | 754 | 703 | 654 | 383 | 588 | 698 | 734 | 735 | 729 | 773 | 821 | 872 | 878 | 738 |
| 6 | D | 805 | 744 | 790 | 784 | 753 | 715 | 673 | 755 | 764 | 729 | 585 | 503 | 743 | 736 | 750 | 732 | 735 | 726 | 726 | 732 | 746 | 757 | 752 | 745 | 728 |
| 7 |  | 757 | 756 | 745 | 742 | 754 | 753 | 753 | 753 | 682 | 677 | 735 | 657 | 714 | 733 | 755 | 734 | 733 | 723 | 695 | 714 | 739 | 756 | 771 | 785 | 734 |
| 8 |  | 760 | 777 | 785 | 810 | 891 | 1016 | 746 | 848 | 818 | 736 | 725 | 784 | 774 | 744 | 727 | 743 | 745 | 732 | 723 | 725 | 741 | 745 | 754 | 757 | 775 |
| 9 |  | 751 | 753 | 741 | 750 | 746 | 755 | 695 | 732 | 763 | 754 | 752 | 726 | 671 | 631 | 692 | 721 | 722 | 733 | 733 | 732 | 735 | 748 | 752 | 746 | 731 |
| 10 |  | 754 | 757 | 754 | 748 | 750 | 755 | 753 | 754 | 754 | 754 | 754 | 754 | 746 | 733 | 717 | 725 | 735 | 716 | 716 | 725 | 737 | 734 | 738 | 756 | 742 |
| 11 |  | 781 | 760 | 784 | 782 | 753 | 747 | 744 | 713 | 653 | 715 | 756 | 739 | 746 | 728 | 741 | 746 | 726 | 725 | 724 | 722 | 745 | 755 | 750 | 765 | 741 |
| 12 |  | 765 | 739 | 747 | 756 | 751 | 768 | 760 | 756 | 763 | 736 | 756 | 746 | 756 | 747 | 744 | 736 | 722 | 714 | 721 | 724 | 733 | 744 | 753 | 754 | 745 |
| 13 | 0 | 756 | 755 | 755 | 755 | 753 | 754 | 756 | 755 | 745 | 736 | 755 | 744 | 756 | 757 | 754 | 735 | 719 | 706 | 722 | 724 | 724 | 746 | 756 | 947 | 754 |
| 14 |  | 941 | 990 | 889 | 794 | 760 | 742 | 731 | 774 | 726 | 648 | 651 | 682 | 674 | 683 | 723 | 722 | 623 | 630 | 721 | 724 | 725 | 746 | $79 \epsilon$ | 819 | 746 |
| 15 |  | 940 | 982 | 893 | 788 | 765 | 742 | 742 | 776 | 122 | 747 | 651 | 684 | 672 | 682 | 722 | 722 | 624 | 630 | 695 | 705 | 703 | 726 | 753 | 764 | 743 |
| 16 |  | 757 | 755 | 747 | 747 | 747 | 746 | 756 | 736 | 732 | 733 | 753 | 744 | 742 | 756 | 755 | 747 | 748 | 734 | 732 | 733 | 744 | 751 | 754 | 757 | 746 |
| 17 |  | 755 | 755 | 754 | 755 | 761 | 762 | 763 | 765 | 765 | 760 | 757 | 692 | 761 | 764 | 751 | 744 | 744 | 733 | 714 | 714 | 738 | 741 | 746 | 748 | 748 |
| 18 | 0 | 765 | 766 | 780 | 781 | 791 | 789 | 777 | 769 | 764 | 744 | 745 | 716 | 706 | 701 | 741 | 754 | 726 | 675 | 703 | 724 | 747 | 763 | 756 | 774 | 748 |
| 19 |  | 780 | 773 | 773 | 766 | 777 | 776 | 764 | 756 | 754 | 725 | 736 | 756 | 746 | 741 | 746 | 739 | 733 | 732 | 719 | 718 | 724 | 734 | 746 | 756 | 749 |
| 20 |  | 755 | 750 | 757 | 756 | 755 | 751 | 757 | 733 | 662 | 706 | 757 | 749 | 734 | 724 | 734 | 726 | 761 | 710 | 733 | 734 | 734 | 748 | 745 | 755 | 739 |
| 21 |  | 765 | 757 | 757 | 762 | 766 | 761 | 763 | 755 | 737 | 761 | 764 | 765 | 761 | 755 | 746 | 735 | 733 | 732 | 735 | 741 | 750 | 755 | 755 | 756 | 753 |
| 22 | 0 | 746 | 755 | 756 | 757 | 756 | 762 | 756 | 761 | 766 | 769 | 755 | 756 | 763 | 764 | 756 | 747 | 737 | 743 | 733 | 735 | 749 | 755 | 756 | 755 | 754 |
| 23 |  | 753 | 756 | 757 | 758 | 760 | 762 | 765 | 764 | 763 | 767 | 772 | 775 | 773 | 745 | 734 | 745 | 746 | 727 | 723 | 730 | 843 | 744 | 753 | 756 | 753 |
| 24 |  | 754 | 763 | 758 | 756 | 769 | 764 | 765 | 755 | 756 | 746 | 736 | 757 | 756 | 756 | 754 | 742 | 727 | 712 | 715 | 723 | 742 | 753 | $75 \pm$ | 752 | 749 |
| 25 |  | 754 | 746 | 757 | 758 | 745 | 763 | 752 | 749 | 754 | 758 | 758 | 754 | 755 | 75C | 740 | 714 | 713 | 723 | 714 | 729 | 727 | 731 | 755 | 756 | 744 |
| 26 | Q | 747 | 757 | 756 | 755 | 755 | 758 | 763 | 165 | 752 | 704 | 764 | 766 | 763 | 762 | 756 | 745 | 733 | 722 | 713 | 719 | 725 | 735 | 752 | 754 | 747 |
| 27 |  | 760 | 759 | 759 | 759 | 764 | 763 | 764 | 764 | $7 E 4$ | 764 | 764 | 764 | 772 | 765 | 763 | 763 | 737 | 727 | 724 | 723 | 728 | 748 | 764 | 763 | 755 |
| 28 | D | 783 | 776 | 773 | 768 | 765 | 768 | 778 | 776 | 775 | 766 | 755 | 251 | 556 | 640 | 660 | 722 | 740 | 712 | 652 | 702 | 740 | 752 | 783 | 765 | 715 |
| 29 | D | 773 | 780 | 773 | 769 | 776 | 807 | 779 | 473 | 186 | 148 | 333 | 544 | 652 | 628 | 463 | 543 | 725 | 711 | 729 | $7 \mathrm{C7}$ | 740 | 787 | 847 | 978 | 652 |
| 30 | D | 899 | 853 | 736 | 825 | 814 | 784 | 834 | 441 | 2 C 4 | 186 | 258 | 33 | 255 | 529 | 705 | 647 | 669 | 679 | 714 | 745 | 784 | 746 | 755 | 756 | 619 |
| MEAN | A | 777 | 777 | 769 | 766 | 766 | 769 | 757 | 739 | 711 | 703 | 712 | 688 | 717 | 722 | 718 | 723 | 722 | 713 | 716 | 723 | 738 | 749 | 764 | 771 | 738 |
| MEAN | 6 | 748 | 757 | 758 | 759 | 756 | 758 | 759 | 760 | 755 | 746 | 759 | 758 | 761 | 762 | 757 | 744 | 729 | 717 | 712 | 718 | 728 | 741 | 755 | 792 | 750 |
| MEAN | D | 805 | 784 | 771 | 785 | 780 | 773 | 768 | 643 | 539 | 515 | 535 | 409 | 582 | 647 | 664 | 680 | 719 | 700 | 705 | 722 | 751 | 761 | 775 | 804 | 692 |


| HOUR |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 2 C | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| U |  | T0 | T0 | T0 | T0 | T0 | T0 | T0 | 10 | 10 | T0 | T0 | 10 | T0 | TC | 10 | TO | 10 | 10 | 10 | T0 | T0 | T0 | TC | 10 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 22 | 24 |  |
| 1 |  | 8.4 | 9.6 | 9.6 | 9.7 | 9.1 | 8.9 | 8.4 | 9.6 | 10.0 | 10.0 | 10.7 | 11.5 | 13.1 | 16.5 | 19.9 | 21.8 | 21.5 | 20.2 | 13.4 | 8.4 | 3.6 | 3.3 | 5.1 | 8.1 | 11.3 |
| 2 |  | 8.3 | 8.4 | 8.4 | 8.6 | 9.9 | 8.9 | 9.4 | 8.3 | 9.9 | 11.5 | 12.5 | 13.1 | 15.4 | 16.8 | 19.2 | 21.3 | 22.9 | 19.5 | 11.8 | 7.5 | 3.6 | 3.6 | 5.1 | 7.0 | 11.3 |
| 3 |  | 8.3 | 8.4 | 8.4 | 8.4 | 9.2 | 9.9 | 10.0 | 10.0 | 10.2 | 11.2 | 11.5 | 13.3 | 17.1 | 19.4 | 20.8 | 19.7 | 21.0 | 17.1 | 11.5 | 7.6 | 6.7 | 8.3 | 7.3 | 6.8 | 11.8 |
| 4 |  | 6.8 | 6.7 | 4.9 | 6.5 | 6.5 | 9.7 | 9.6 | 10.0 | 9.9 | 10.7 | 11.7 | 13.1 | 14.4 | 16.0 | 18.1 | 19.2 | 17.9 | 11.7 | 6.5 | 3.4 | 1.8 | 4.7 | T.E | 10.2 | 9.9 |
| 5 |  | 10.8 | 9.7 | 8.3 | 8.3 | 8.4 | 9.4 | 9.7 | 11.5 | 12.8 | 14.4 | 13.9 | 12.1 | 8.6 | 11.5 | 14.5 | 19.1 | 11.5 | 8.3 | 6.8 | 3.1 | 2.2 | 5.4 | 9.5 | 11.3 | 10.1 |
| 6 |  | 8.6 | 7.6 | 6.8 | 19.5 | 10.2 | 19.4 | 19.2 | 17.3 | 13.1 | 13.4 | 18.3 | 16.3 | 13.9 | 16.5 | 18.1 | 19.4 | 14.9 | 14.4 | 7.3 | 4.2 | 4.9 | 8.3 | 7.5 | 8.4 | 12.8 |
| 7 |  | 8.4 | 9.6 | 9.9 | 8.6 | 9.1 | 9.7 | 10.5 | 12.9 | 22.9 | 22.9 | 11.5 | 5.1 | 13.4 | 18.1 | 18.4 | 17.6 | 17.6 | 11.8 | 4.4 | 4.4 | 1.5 | 3.8 | 8.4 | 5.9 | 11.1 |
| 8 |  | 9.1 | 10.0 | 13.1 | 14.4 | 6.0 | 7.1- | 10.7 | -27.0 | 21.5 | 26.6 | 22.8 | 14.4 | 14.9 | 19.1 | 17.9 | 14.7 | 15.2 | 12.1 | 8.4 | 5.2 | 5.1 | 5.5 | 8.2 | 11.3 | 10.2 |
| 9 |  | 12.8 | 12.8 | 11.3 | 11.0 | 9.9 | 11.2 | . 1 | 11.7 | 11.3 | 12.8 | 13.1 | 9.6 | 11.2 | 12.8 | 16.2 | 17.8 | 16.0 | 13.1 | 7.5 | 5.4 | 5.9 | 7.3 | 9.2 | 10.7 | 10.8 |
| 10 |  | 14.7 | 15.5 | 10.7 | 13.4 | 13.1 | 8.3 | 8.1 | 8.4 | 10.2 | 11.5 | 11.8 | 12.0 | 14.1 | 15.0 | 14.7 | 13.7 | 14.5 | 12.8 | 3.3 | 3.1 | 4.2 | 5.2 | 8.1 | 10.0 | 10.7 |
| 11 |  | 9.2 | 11.2 | 11.0 | 12.8 | 8.4 | 8.1 | 8.6 | 9.9 | 15.8 | 16.2 | 14.7 | 14.9 | 16.0 | 14.9 | 16.5 | 17.6 | 16.3 | 11.2 | 10.2 | 3.6 | - 7 | 3.6 | 8.3 | 9.9 | 11.2 |
| 12 |  | 11.0 | 11.5 | 10.4 | 9.9 | 11.5 | 14.7 | 9.9 | 8.3 | 10.5 | 7.0 | 12.9 | 13.1 | -1 | 15.2 | 17.9 | 18.1 | 16.2 | 15.5 | 9.9 | 9.9 | 5.9 | 7.C | 9.7 | 10.7 | 11.1 |
| 13 |  | 11.7 | 11.3 | 9.9 | 9.9 | 11.3 | 9.4 | 9.1 | 9.7 | 8.8 | . 5 | 13.1 | 13.1 | 16.6 | 17.9 | 17.9 | 19.7 | 19.5 | 14.9 | 9.9 | 6.7 | 4.1 | 6.2 | 8.1 | 8.4 | 11.2 |
| 14 |  | 9.9 | 10.2 | 11.0 | 13.3 | 11.3 | 10.7 | 9.9 | 9.9 | 10.0 | 12.3 | 7.9 | 14.5 | 16.3 | 18.9 | 20.5 | 21.6 | 20.8 | 13.6 | 9.1 | 10.2 | 4.2 | 3.0 | 2.2 | 6.7 | 11.6 |
| 15 |  | 3.3 | 9.3 | 11.4 | 14.4 | 12.8 | 8.2 | 19.3 | 1.6 | 14.8 | 16.5 | 17.0 | 18.2 | 26.7 | 27.8 | 25.7 | 15.7 | 3.2 | -0.5 | 4.1 | 7.2 | 7.8 | 6.7 | 7.4 | 10.6 | 12.1 |
| 16 |  | 10.1 | 8.5 | 11.4 | 23.9 | 11.1 | 16.1 | 12.8 | 10.4 | 15.1 | 12.8 | 12.4 | 13.3 | 16.4 | 17.2 | 19.1 | 19.1 | 18.6 | 16.1 | 13.0 | 11.2 | 9.8 | 10.1 | 9.8 | 9.8 | 13.7 |
| 17 |  | 9.5 | 8.5 | 9.1 | 8.8 | 9.8 | 9.8 | 9.9 | 9.9 | 10.7 | 12.4 | 13.3 | 23.0 | 28.8 | 23.9 | 24.3 | 21.7 | 17.8 | 18.6 | 3.5 | 3.5 | 4.5 | 4.0 | 4.5 | 6.7 | 12.4 |
| 18 | ) | 5.4 | 5.9 | 9.9 | 7.5 | 5.4 | 9.9 | 6.9 | 10.9 | 8.7 | 12.4 | 11.1 | 9.8 | 9.6 | 13.2 | 18.3 | 15.9 | 16.5 | 9.9 | 2.2 | 1.9 | 6.4 | 6.7 | 5.9 | 5.6 | 9.0 |
| 19 |  | 7.0 | 5.8 | 9.6 | 11.6 | 16.2 | 15.3 | 10.6 | 9.8 | 11.1 | 9.9 | 11.4 | 12.8 | 12.2 | 14.0 | 16.4 | 16.1 | 16.5 | 14.8 | 14.0 | 12.2 | 9.8 | 9.1 | 8.8 | 8.3 | 11.8 |
| 20 |  | 8.3 | 8.2 | 9.9 | 12.7 | 11.1 | 13.8 | 13.6 | 11.4 | 15.3 | 18.6 | 13.8 | 14.9 | 13.0 | 14.4 | 17.5 | 16.2 | 11.6 | 13.3 | 8.5 | 9.5 | 8.8 | 7.6 | 7.7 | 8.2 | 12.0 |
| 21 |  | 8.5 | 8.2 | 8.2 | 8.8 | 9.6 | 11.2 | 10.4 | 7.8 | 6.9 | 11.1 | 11.6 | 14.0 | 13.8 | 14.9 | 16.2 | 15.6 | 13.6 | 13.5 | 9.8 | 9.3 | 9.1 | 9.0 | 8.3 | 8.5 | 10.7 |
| 22 | Q | 8.8 | 8.8 | 9.1 | 8.8 | 9.8 | 9.1 | 2.9 | 10.4 | 12.2 | 13.5 | 14.8 | 16.2 | 16.4 | 16.1 | 16.2 | 16.9 | 16.4 | 14.6 | 12.0 | 9.8 | 8.2 | 7.7 | 8. 3 | 9.8 | 11.5 |
| 23 |  | 9.6 | 9.5 | 9.3 | 9.0 | 9.6 | 10.1 | 9.8 | 9.1 | 11.1 | 11.9 | 13.0 | 13.8 | 14.4 | 12.7 | 13.0 | 17.5 | 15.3 | 12.2 | 8.0 | 6.9 | 8.2 | 5.3 | 6.E | 8.2 | 10.6 |
| 24 |  | 9.8 | 8.5 | 8.2 | 9.1 | 9.5 | 11.4 | 8.5 | 9.5 | 12.4 | 13.2 | 16.5 | 17.7 | 17.0 | 16.2 | 18.0 | 18.2 | 18.2 | 17.3 | 13.0 | 11.1 | 7.C | 7.2 | 7.8 | 8.8 | 12.2 |
| 25 |  | 9.3 | 9.8 | 8.3 | 9.8 | 17.3 | 11.4 | 7.4 | 9.8 | 9.8 | 11.4 | 12.7 | 13.8 | 14.6 | 16.1 | 17.8 | 14.6 | 11.6 | 12.7 | 12.8 | 9.5 | 6.1 | 4.6 | 4.5 | 6.4 | 10.9 |
| 26 | Q | 9.5 | 9.6 | 9.9 | 9.9 | 10.1 | 10.4 | 11.2 | 19.4 | 11.6 | 7.8 | 14.8 | 14.6 | 14.4 | 16.1 | 17.6 | 19.6 | 20.9 | 18.0 | 14.3 | 11.4 | 9.8 | 8.3 | 8.6 | 8.0 | 12.7 |
| 27 |  | 8.5 | 8.7 | 9.3 | 9.8 | 9.8 | 10.1 | 11.1 | 11.1 | 11.1 | 11.4 | 11.9 | 12.5 | 13.0 | 14.9 | 16.5 | 20.1 | 20.7 | 16.4 | 12.2 | 10.7 | 7.5 | 3.7 | 1.1 | 1.4 | 11.0 |
| 28 | 0 | . 8 | 3.2 | 9.1 | 9.3 | 9.5 | 8.3 | 8.0 | 9.8 | 10.1 | 15.9 | 14.9 | 14.8 | 35.9 | 37.3 | 29.1 | 24.8 | 22.5 | 20.1 | 8.7 | 3.2 | 4.0 | 4.9 | 4.2 | 7.7 | 13.2 |
| 29 | - | 9.6 | 11.1 | 9.6 | 18.2 | 12.7 | 7.8 | 6.6 | 4.8 | -12.8 | 3.2 | 11.2 | 32.8 | 24.1 | 34.1 | 38.4 | 20.6 | 9.6 | 12.5 | 7.2 | 4.9 | 6.7 | 6.7 | 9.8 | 26.7 | 13.2 |
| 30 | - | 12.2 | 6.6 | -7.9 | 6.7 | 6.6 | 5.3 | 5.6 | -3.6- | -45.1 | 40.9 | 47.0 | 39.4 | 36.0 | 9.6 | 12.4 | 14.6 | 14.8 | 11.2 | 18.3 | 12.7 | 13.2 | 9.6 | 10.t | 12.2 | 12.0 |
| MEAN | - | 8.9 | 9.1 | 8.9 | 11.1 | 10.2 | 10.5 | 8.9 | 8.4 | 9.3 | 13.5 | 14.5 | 15.3 | 16.4 | 17.6 | 18.9 | 18.3 | 16.5 | 13.9 | 9.4 | 7.3 | 6.0 | 6.2 | 7.3 | 9.1 | 11.5 |
| MEAN | 0 | 9.3 | 9.6 | 9.4 | 9.4 | 10.0 | 9.4 | 6.2 | 11.5 | 10.5 | 8.7 | 13.2 | 13.7 | 15.2 | 16.7 | 18.2 | 19.9 | 20.2 | 17.4 | 12.3 | 8.7 | 5. 8 | 5.8 | 6.5 | $8 \cdot 3$ | 11.6 |
| MEAN | 0 | 7.3 | 6.9 | 5.5 | 12.2 | 8.9 | 10.2 | 9.3 | 7.8 | -5.2 | 17.1 | 20.5 | 22.6 | 23.9 | 22.1 | 23.3 | 19.0 | 15.7 | 13.6 | 8.7 | 5.4 | 7.C | 7.3 | 7.E | 12.1 | 12.0 |


| HOUR UT |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 1 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 10 | TO | T0 | T0 | T0 | TO | TO | TO | 10 | ro | 10 | T0 | 10 | 10 | TC | 15 | 10 | TC | TO | 10 | 10 | 10 | T0 | T0 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 22 | 24 |  |
| 1 | 0 | 670 | 652 | 664 | 665 | 671 | 670 | 661 | 660 | 644 | 655 | 657 | 660 | 662 | 664 | 665 | 665 | 661 | 660 | 646 | 647 | 646 | 651 | 655 | 660 | 659 |
| 2 | 0 | 659 | 660 | 660 | 661 | 660 | 660 | 661 | 661 | $6 E 5$ | 666 | 666 | 664 | 660 | 660 | 660 | 660 | 656 | 655 | 647 | 647 | 646 | 651 | cec | 660 | 659 |
| 3 |  | 656 | 656 | 657 | 656 | 656 | 656 | 655 | 655 | 654 | 653 | 651 | 636 | 638 | 650 | 655 | 657 | 655 | 647 | 646 | 646 | 646 | 651 | 655 | 662 | 652 |
| 4 |  | 666 | 667 | 671 | 679 | 689 | 670 | 660 | 660 | 660 | 660 | 660 | 659 | 660 | 656 | 656 | 656 | 653 | $64 t$ | 646 | 655 | 651 | 656 | 66 C | 660 | 661 |
| 5 |  | 656 | 653 | 652 | 653 | 654 | 655 | 660 | 668 | 6 68 | 658 | 644 | 632 | 546 | 472 | 505 | 426 | 596 | 683 | 693 | 709 | 716 | 733 | 759 | 773 | 644 |
| 6 | D | 723 | 679 | 721 | 717 | 696 | 568 | 468 | 642 | 670 | 644 | 521 | 586 | 641 | 649 | 664 | 660 | 661 | 669 | 668 | 674 | 676 | 692 | 695 | 675 | 652 |
| 7 |  | 678 | 684 | 675 | 670 | 665 | 665 | 666 | 651 | 564 | 560 | 642 | 578 | 617 | 630 | 660 | 669 | 683 | 671 | 672 | 686 | 703 | 712 | 726 | 736 | 661 |
| 8 |  | 711 | 711 | 717 | 727 | 709 | 546 | 530 | 471 | 661 | 661 | 644 | 689 | 699 | 676 | 662 | 678 | 684 | 685 | 689 | 687 | 641 | 676 | 671 | 674 | 664 |
| 9 |  | 675 | 680 | 675 | 673 | 671 | 666 | 507 | 613 | 612 | 664 | E60 | 642 | 613 | 595 | 598 | 614 | 659 | 673 | 674 | 676 | 679 | 687 | 696 | 691 | 652 |
| 10 |  | 695 | 696 | 688 | 688 | 685 | 676 | 668 | 669 | 665 | 665 | 667 | 667 | 669 | 660 | 652 | 645 | 651 | 660 | 663 | 662 | 671 | 674 | 671 | 669 | 670 |
| 11 |  | 690 | 715 | 754 | 736 | 711 | 688 | 662 | 613 | 559 | 624 | 661 | 661 | 664 | 656 | 669 | 671 | 670 | 670 | 671 | 669 | 672 | 672 | 612 | 671 | 671 |
| 12 |  | 679 | 671 | 670 | 672 | 678 | 627 | 656 | 661 | 662 | 635 | 653 | 655 | 659 | 662 | 662 | 666 | 666 | 664 | 669 | 672 | 67C | 671 | 67 C | 669 | 663 |
| 13 | 0 | 665 | 665 | 665 | 665 | 669 | 669 | 662 | 664 | 647 | 624 | 652 | 631 | 650 | 661 | 661 | 661 | 661 | 665 | 660 | 659 | 661 | 666 | 666 | 668 | 659 |
| 14 |  | 665 | 666 | 671 | 671 | 667 | 666 | 664 | 660 | 653 | 624 | $6 \mathrm{C4}$ | 631 | 645 | 644 | 647 | 66C | 657 | 651 | 650 | 664 | 658 | 70 C | 728 | 753 | 662 |
| 15 |  | 755 | 709 | 602 | 721 | 697 | 690 | 689 | 627 | 646 | 630 | 621 | 622 | 630 | 601 | 601 | 552 | 572 | 587 | 653 | 684 | 681 | 684 | 692 | 709 | 652 |
| 16 |  | 708 | 691 | 698 | 690 | 684 | 681 | 670 | 650 | 648 | 674 | 664 | 651 | 670 | 679 | 677 | 676 | 675 | 675 | 679 | 675 | 675 | 675 | 675 | 671 | 675 |
| 17 |  | 670 | 668 | 667 | 664 | 666 | 665 | 668 | 668 | 648 | 660 | 649 | 552 | 627 | 636 | 632 | 641 | 650 | 651 | 660 | 646 | 651 | 66 C | $66 t$ | 666 | 652 |
| 18 | D | 676 | 682 | 708 | 693 | 707 | 706 | 657 | 679 | 666 | 648 | 644 | 641 | 622 | 653 | 612 | 654 | 660 | 660 | 678 | 668 | c97 | 703 | 685 | 715 | 671 |
| 19 |  | 715 | 717 | 726 | 694 | 644 | 645 | 656 | 672 | 670 | 633 | 632 | 657 | 662 | 664 | 667 | 675 | 676 | 674 | 670 | 670 | 670 | 670 | 676 | 676 | 671 |
| 20 |  | 672 | 669 | 670 | 671 | 674 | 676 | 665 | 636 | 545 | 582 | 651 | 653 | 646 | 635 | 631 | 642 | 655 | 666 | 672 | 677 | 673 | 672 | 676 | 675 | 653 |
| 21 |  | 672 | 671 | 672 | 677 | 677 | 669 | 672 | 654 | 625 | 652 | 656 | 656 | 661 | 662 | 661 | 662 | 663 | 666 | 666 | 684 | 6E9 | 671 | 671 | 676 | 664 |
| 22 | 0 | 676 | 675 | 674 | 673 | 676 | 669 | 710 | 628 | 641 | 663 | 654 | 653 | 661 | 662 | 665 | 666 | 670 | 671 | 671 | 671 | 67C | 668 | 663 | 661 | 666 |
| 23 |  | 665 | 665 | 665 | 665 | 665 | 665 | 663 | 665 | 666 | 665 | 664 | 660 | 661 | 634 | 606 | 622 | 637 | 649 | 656 | 669 | 680 | 699 | 7C8 | 684 | 662 |
| 24 |  | 673 | 671 | 677 | 667 | 690 | 693 | 685 | 685 | 680 | 662 | 633 | 651 | 656 | 665 | 665 | 666 | 669 | 666 | 672 | 661 | 671 | 666 | 664 | 665 | 669 |
| 25 |  | 670 | 672 | 671 | 679 | 683 | 689 | 612 | 636 | 673 | 671 | 662 | 661 | 663 | 661 | 656 | 641 | 647 | 652 | 663 | 670 | 680 | 681 | 681 | 678 | 665 |
| 26 | 0 | 665 | 669 | 667 | 670 | 668 | 669 | 670 | 669 | 661 | 596 | 641 | 664 | 663 | 663 | 664 | 666 | 663 | 661 | 689 | 693 | 694 | 698 | 7CC | 699 | 669 |
| 27 |  | 699 | 699 | 699 | 699 | 699 | 699 | 699 | 699 | 699 | 699 | 699 | 699 | 698 | 698 | 698 | 698 | 698 | 697 | 694 | 697 | 701 | 694 | 697 | 693 | 698 |
| 28 | D | 707 | 740 | 722 | 699 | 693 | 694 | 697 | 703 | 652 | 688 | 690 | 458 | 440 | 571 | 614 | 674 | 669 | 688 | 683 | 693 | 705 | 735 | 767 | 730 | 673 |
| 29 | D | 733 | 729 | 724 | 734 | 722 | 743 | 739 | 545 | 739 | 549 | 573 | 730 | 729 | 667 | 606 | 553 | 648 | 666 | 704 | 716 | 723 | 732 | 758 | 537 | 679 |
| 30 | D | 434 | 504 | 453 | 535 | 723 | 742 | 693 | 722 | 926 | 823 | 694 | 798 | 718 | 609 | 666 | 710 | 699 | 697 | 751 | 750 | 758 | 122 | 723 | 728 | 691 |
| MEAN | A | 676 | 676 | 674 | 679 | 682 | 669 | 654 | 650 | $6 \in 3$ | 650 | 647 | 647 | 648 | 643 | 645 | 646 | 659 | 664 | 672 | 675 | 679 | 684 | 689 | 683 | 665 |
| MEAN | 0 | 667 | 664 | 666 | 667 | 669 | 667 | 673 | 657 | 651 | 641 | 654 | 655 | 660 | 662 | 663 | 664 | 662 | 662 | 663 | 663 | 684 | 667 | 67 C | 67 J | 663 |
| MEAN | D | 654 | 667 | 665 | 676 | 708 | 691 | 651 | 658 | 740 | 670 | 625 | 643 | 630 | 630 | 633 | 650 | 667 | ¢ 76 | 697 | 100 | 110 | 717 | 72E | 677 | 673 |


| HOUR <br> UT |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |  |
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|  |  | TO | TO | 10 | T0 | T0 | T0 | TO | 10 | 10 | 10 | T0 | 10 | 10 | 10 | TC | 10 | T0 | TC | T0 | 10 | T0 | TO | 10 | T0 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |  |
| 1 | D | 776 | 752 | 757 | 757 | 760 | 764 | 583 | 625 | 672 | 638 | 527 | 529 | 581 | 744 | 744 | 733 | 740 | 732 | 729 | 729 | 727 | 726 | 743 | 737 | 700 |
| 2 | 0 | 758 | 767 | 755 | 752 | 755 | 721 | 672 | 454 | 124 | 56 | 292 | 432 | 506 | 722 | 593 | 654 | 631 | 766 | 743 | 747 | 735 | 752 | 751 | 746 | 620 |
| 3 | 0 | 744 | 750 | 736 | 744 | 745 | 702 | 712 | 731 | 684 | 687 | $7 \mathrm{C9}$ | 648 | 579 | 621 | 602 | 637 | 701 | 742 | 725 | 734 | 744 | 744 | 756 | 752 | 705 |
| 4 |  | 752 | 745 | 753 | 753 | 752 | 740 | 755 | 752 | 746 | 704 | 733 | 725 | 736 | 751 | 747 | 755 | 742 | 712 | 714 | 736 | 731 | 741 | 747 | 752 | 740 |
| 5 |  | 745 | 746 | 752 | 759 | 753 | 756 | 765 | 758 | 755 | 740 | 719 | 741 | 762 | 754 | 756 | 750 | 754 | 731 | 721 | 721 | 730 | 734 | 733 | 747 | 745 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 6 | D | 756 | 755 | 752 | 756 | 765 | 773 | 765 | 748 | 746 | 735 | 671 | 714 | 721 | 724 | 717 | 735 | 711 | 683 | 682 | 701 | 724 | 732 | 733 | 745 | 731 |
| 7 |  | 752 | 765 | 765 | 776 | 775 | 756 | 724 | 715 | 734 | 733 | 744 | 751 | 745 | 745 | 749 | 744 | 733 | 728 | 717 | 719 | 725 | 733 | 733 | 744 | 742 |
| 8 | 0 | 749 | 751 | 755 | 758 | 756 | 760 | 760 | 760 | 7E7 | 768 | 768 | 766 | 762 | 756 | 756 | 753 | 752 | 742 | 729 | 728 | 734 | 742 | 745 | 748 | 753 |
| 9 |  | 745 | 755 | 761 | 761 | 756 | 768 | 753 | 755 | 756 | 761 | 761 | 762 | 762 | 761 | 756 | 754 | 755 | 742 | 735 | 740 | 732 | 725 | 743 | 764 | 753 |
| 10 | D | 765 | 777 | 775 | 796 | 832 | 830 | 797 | 758 | 680 | 590 | 341 | 560 | 639 | 684 | 746 | 152 | 736 | 732 | 721 | 705 | 725 | 733 | 745 | 748 | 715 |
| 11 |  | 754 | 746 | 757 | 758 | 763 | 737 | 743 | 742 | 755 | 722 | 661 | 752 | 717 | 701 | 753 | 752 | 750 | 724 | 722 | 731 | 737 | 743 | 752 | 755 | 739 |
| 12 |  | 766 | 755 | 756 | 762 | 761 | 754 | 746 | 604 | 701 | 744 | 744 | 731 | 699 | 122 | 713 | 711 | 734 | 734 | 735 | 741 | 748 | 757 | 76E | 767 | 735 |
| 13 |  | 747 | 747 | 748 | 747 | 750 | 754 | 754 | 745 | 751 | 750 | 726 | 725 | 752 | 738 | 746 | 752 | 739 | 733 | 716 | 725 | 736 | 733 | 743 | 753 | 742 |
| 15 | 0 | 752 | 754 | 755 | 754 | 754 | 754 | 753 | 754 | 755 | 756 | 755 | 757 | 756 | 753 | 745 | 743 | 732 | 722 | 714 | 716 | 722 | 733 | 742 | 745 | 745 |
|  | 0 | 749 | 752 | 753 | 752 | 752 | 752 | 749 | 747 | 746 | 748 | 744 | 738 | 753 | 762 | 759 | 752 | 743 | 727 | 719 | 722 | 733 | 742 | 74E | 746 | 745 |
| 16 |  | 751 | 752 | 753 | 753 | 754 | 754 | 736 | 756 | 765 | 763 | 763 | 762 | 762 | 754 | 750 | 742 | 726 | 723 | 732 | 731 | 722 | 734 | 736 | 742 | 747 |
| 17 |  | 742 | 743 | 748 | 753 | 748 | 751 | 746 | 746 | 753 | 755 | 755 | 762 | 762 | 762 | 756 | 753 | 744 | 735 | 733 | 732 | 735 | 741 | 732 | 736 | 747 |
| 18 |  | 738 | 743 | 744 | 745 | 752 | 754 | 763 | 754 | 750 | 723 | 681 | 743 | 766 | 754 | 753 | 752 | 745 | 734 | 722 | 733 | 745 | 754 | 752 | 754 | 744 |
| 19 |  | 763 | 763 | 758 | 762 | 766 | 763 | 761 | 761 | 754 | 773 | 763 | 734 | 641 | 716 | 751 | 745 | 734 | 722 | 722 | 725 | 739 | 752 | 744 | 741 | 744 |
| 20 |  | 744 | 745 | 754 | 755 | 755 | 757 | 758 | 756 | 755 | 759 | 756 | 762 | 763 | 762 | 759 | 755 | 751 | 743 | 724 | 725 | 733 | 735 | 736 | 743 | 750 |
| 21 |  | 753 | 754 | 755 | 758 | 759 | 762 | 7Є1 | 759 | 723 | 714 | 773 | 765 | 762 | 760 | 753 | 732 | 723 | 733 | 735 | $7 \pm 2$ | 740 | 749 | 748 | 745 | 748 |
| 22 |  | 753 | 754 | 753 | 754 | 753 | 765 | 765 | 761 | 755 | 737 | 762 | 755 | 754 | 749 | 753 | 745 | 734 | 718 | 715 | 721 | 732 | 739 | 742 | 743 | 746 |
| 23 |  | 749 | 753 | 753 | 753 | 756 | 758 | 756 | 754 | 757 | 760 | 762 | 761 | 760 | 761 | 755 | 754 | 745 | 736 | 726 | 733 | 737 | 727 | 746 | 743 | 750 |
| 24 |  | 755 | 751 | 745 | 747 | 764 | 766 | 775 | 744 | 743 | 716 | 755 | 721 | 683 | 742 | 757 | 745 | 745 | 741 | 733 | 735 | 739 | 753 | 744 | 753 | 744 |
| 25 |  | 757 | 766 | 757 | 750 | 752 | 752 | 758 | 753 | 752 | 753 | 752 | 753 | 757 | 759 | 759 | 757 | 751 | 742 | 724 | 722 | 732 | 723 | 734 | 742 | 748 |
| 26 | 0 | 748 | 752 | 755 | 754 | 753 | 753 | 754 | 753 | 751 | 756 | 755 | 755 |  |  | 759 |  |  | 738 | 731 | 722 | 732 | 741 | 744 | 751 | 749 |
| 27 |  | 754 | 761 | 765 | 762 | 761 | 761 | 764 | 764 | 754 | 751 | 760 | 762 | 753 | 745 | 764 | 764 | 753 | 742 | 732 | 724 | 711 | 703 | 734 | 735 | 749 |
| 28 |  | 753 | 752 | 753 | 755 | 764 | 761 | 760 | 755 | 753 | 757 | 756 | 761 | 762 | 755 | 754 | 745 | 733 | 132 | 722 | 720 | 715 | 722 | 733 | 741 | 747 |
| 29 |  | 743 | 752 | 753 | 752 | 757 | 782 | 764 | 759 | 753 | 754 | 761 | 762 | 762 | 764 | 762 | 753 | 743 | 731 | 719 | 712 | 721 | 731 | 738 | 744 | 748 |
| 30 | 0 | 752 | 753 | 755 | 759 | 758 | 757 | 761 | 762 | 755 | 754 | 754 | 755 | 760 | 759 | 756 | 751 | 743 | 731 | 722 | 725 | 735 | 744 | $75 C$ | 753 | 750 |
| 31 |  | 760 | 162 | 761 | 752 | 753 | 751 | 742 | 739 | 719 | 732 | 713 | 682 | 703 | 732 | 762 | 754 | 751 | 740 | 724 | 720 | 122 | 732 | 734 | 744 | 737 |
| ME AN | A | 752 | 754 | 755 | 757 | 759 | 757 | 747 | 733 | 722 | 713 | 707 | 720 | 722 | 741 | 742 | 741 | 736 | 732 | 724 | 726 | 732 | 737 | 142 | 747 | 737 |
| MEAN | 0 | 750 | 753 | 755 | 756 | 755 | 755 | 756 | 755 | 755 | 757 | 755 | 754 | 757 | 758 | 755 | 751 | 744 | 732 | 723 | 723 | 731 | 74C | 74: | 749 | 748 |
| MEAN | D | 760 | 760 | 755 | 761 | 771 | 758 | 706 | 663 | 581 | 541 | 5C8 | 577 | 605 | 699 | 680 | 702 | 704 | 731 | 720 | 723 | 731 | 737 | 745 | 745 | 694 |


| HOUR <br> UT |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 1 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 2 C | 21 | 22 | 23 |  |
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|  |  | TO | T0 | T0 | T0 | TO | T0 | 10 | T0 | TO | T0 | T0 | T0 | T0 | 10 | T0 | 10 | 10 | T0 | 10 | 10 | 10 | 10 | 10 | 10 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 22 | 24 |  |
| 1 | D | 12.4 | 13.3 | 17.3 | 12.2 | 14.4 | 13.0 | 7.5 | 17.0 | 19.1 | 10.9 | 19.3 | 20.6 | 13.0 | 14.4 | 16.7 | 17.8 | 19.6 | 10.3 | 10.4 | 11.7 | 12.8 | 12.7 | 11.4 | 9.8 | 14.1 |
| 2 | D | 10.6 | 24.9 | 11.1 | 9.6 | 11.7 | 15.9 | 2.1 | 25.2 | 50.5 | 42.5 | 38.4 | 35.9 | 5.6 | 9.6 | 7.8 | 10.9 | 10.6 | 11.2 | 13.5 | 11.9 | 10.1 | 11.4 | 11.2 | 11.4 | 16.8 |
| 3 | 0 | 11.4 | 12.0 | 26.5 | 20.9 | 11.6 | 13.0 | 9.9 | 11.9 | 5.8 | 6.2 | 11.4 | 18.0 | 6.2 | -0.7 | -6.5 | -4.5 | 5.3 | 14.6 | 8.8 | 11.6 | 10.1 | 11.2 | 10.7 | 11.2 | 9.9 |
| 4 |  | 11.4 | 12.8 | 11.7 | 11.6 | 12.5 | 10.3 | 13.3 | 12.8 | 13.0 | 7.5 | 14.0 | 14.8 | 12.7 | 14.1 | 13.3 | 15.9 | 17.5 | 15.6 | 12.0 | 11.7 | 11.2 | 11.1 | 9.6 | 9.8 | 12.5 |
| 5 |  | 12.2 | 10.9 | 10.3 | 11.2 | 11.1 | 16.2 | 14.4 | 11.2 | 12.0 | 16.1 | 15.9 | 16.5 | 13.2 | 13.0 | 14.4 | 16.7 | 16.9 | 18.0 | 16.4 | 9.6 | 8.5 | 6.7 | 8.2 | 8.5 | 12.8 |
| 6 | D | 9.5 | 9.6 | 11.6 | 19.9 | 10.6 | 11.6 | 13.8 | 8.8 | 11.2 | 12.0 | 5.3 | 11.6 | 11.6 | 14.1 | 9.8 | 10.6 | 13.3 | 6.7 | -0.5 | -3 | 3.2 | 4.1 | 6.7 | 9.5 | 9.4 |
| 7 |  | 10.6 | 9.6 | 8.7 | 20.1 | 11.1 | 11.6 | 16.2 | 9.3 | 10.4 | 1 C .9 | 11.6 | 13.0 | 12.0 | 12.8 | 15.6 | 16.5 | 15.9 | 14.8 | 12.4 | 9.5 | 7.4 | 6.2 | 6.6 | 7.5 | 11.7 |
| 8 | 0 | 9.1 | 10.6 | 10.4 | 10.6 | 11.2 | 11.2 | 11.4 | 11.4 | 13.0 | 12.0 | 12.0 | 12.2 | 12.5 | 13.8 | 13.0 | 14.3 | 14.9 | 14.0 | 11.6 | 8.2 | 6.7 | 7.0 | 7.4 | 8.2 | 11.1 |
| 9 |  | 9.3 | 9.9 | 10.1 | 10.3 | 10.9 | 11.6 | 8.8 | 9.6 | 11.6 | 11.4 | 11.6 | 12.8 | 12.0 | 13.2 | 14.3 | 15.4 | 18.2 | 14.9 | 14.8 | 9.9 | 9.6 | 4.3 | 7.8 | 9.3 | 11.3 |
| 10 | D | 8.7 | 8.2 | 9.5 | 13.3 | 10.1 | 9.6 | 13.6 | 11.9 | 14.0 | 27.3 | 46.5 | 24.1 | 21.2 | 12.0 | 16.2 | 14.3 | 9.6 | 8.2 | 12.4 | 8.3 | 6.7 | 8.6 | 8.1 | 9.9 | 13.8 |
| 11 |  | 9.8 | 9.9 | 11.6 | 11.1 | 10.1 | 14.8 | 14.3 | 13.3 | 13.5 | 11.6 | 9.5 | 12.8 | 22.8 | 14.6 | 19.3 | 17.7 | 17.5 | 14.9 | 9.9 | 8.0 | 6.4 | 6.6 | 9.3 | 9.8 | 12.5 |
| 12 |  | 9.6 | 10.4 | 14.4 | 10.1 | 10.1 | 9.8 | 9.9 | -3.7 | 13.3 | 13.6 | 19.1 | 20.9 | 20.4 | 24.3 | 16.5 | 9.9 | 9.8 | 12.7 | 12.8 | 8.5 | 8.2 | 8.2 | 9.5 | 9.9 | 12.0 |
| 13 |  | 9.3 | 9.5 | 10.1 | 9.8 | 10.0 | 11.3 | 7.2 | 7.1 | 8.7 | 10.1 | 7.4 | 15.6 | 14.8 | 13.7 | 15.1 | 16.4 | 15.1 | 12.2 | B. 8 | 6.1 | 4. 2 | 5.3 | 7.1 | 8.4 | 10.1 |
| 14 | 0 | 8.7 | 9.0 | 10.0 | 10.1 | 10.0 | 10.0 | 10.0 | 9.8 | 10.0 | 10.1 | 10.5 | 11.3 | 11.6 | 12.2 | 13.8 | 15.3 | 15.6 | 13.2 | 8.0 | 4.3 | 3.8 | 4.3 | 7.1 | 8.7 | 9.9 |
| 15 | 0 | 8.8 | 10.0 | 10.5 | 10.3 | 10.5 | 10.3 | 4.0 | 8.7 | 10.1 | 11.9 | 10.8 | 10.3 | 16.9 | 16.9 | 15.6 | 16.6 | 16.7 | 15.3 | 12.1 | 9.3 | 8.7 | 8.7 | $9 . C$ | 10.0 | 11. 3 |
| 16 |  | 9.0 | 8.8 | 9.0 | 9.2 | 8.7 | 7.2 | 2.4 | 8.4 | 10.5 | 10.5 | 11.6 | 11.9 | 12.1 | 12.9 | 14.6 | 16.7 | 15.6 | 7.1 | 4.0 | 4.0 | 1.0 | 1.6 | 3.8 | 5.3 | 8.6 |
| 17 |  | 7.1 | 8.4 | 8.8 | 8.7 | 8.7 | 9.0 | 8.8 | 10.3 | 10.5 | 10.8 | 11.1 | 11.9 | 11.9 | 12.1 | 13.5 | 15.3 | 16.9 | 15.1 | 12.1 | 8.7 | 6.6 | 4.2 | 3. 5 | 3.8 | 9.9 |
| 18 |  | 5.0 | 7.0 | 8.6 | 8.7 | 9.7 | 8.6 | 19.8 | 8.7 | 11.6 | 12.4 | 13.6 | 12.0 | 12.1 | 12.0 | 12.3 | 14.5 | 14.9 | 13.6 | 10.5 | 7.1 | 6.8 | 6-3 | 8.4 | 7.1 | 10.5 |
| 19 |  | 6.5 | 6.6 | 6.8 | 6.6 | 6.3 | 6.8 | 8.6 | 6.3 | 6.6 | 11.5 | 13.6 | 17.1 | 13.6 | 16.5 | 13.1 | 13.4 | 14.9 | 13.1 | 7.3 | E. 3 | 5.5 | 5.4 | 7. C | 8.4 | 9.5 |
| 20 |  | 8.1 | 8.7 | 8.4 | 8.4 | 8.6 | 8.9 | 8.7 | 10.2 | 10.4 | 10.8 | 11.5 | 11.3 | 11.8 | 12.0 | 13.7 | 15.0 | 15.2 | 15.0 | 13.1 | 9.7 | 7.1 | 7.0 | 7.C | 8.7 | 10.4 |
| 21 |  | 7.6 | 8.4 | 8.6 | 8.9 | 9.2 | 10.0 | 10.2 | 10.0 | 11.8 | 18.4 | 16.6 | 13.6 | 13.2 | 13.6 | 15.2 | 16.5 | 11.2 | 10.2 | 8.1 | 4.6 | 5.c | 5.5 | 8.3 | 10.0 | 10.6 |
| 22 |  | 8.6 | 8.6 | 8.5 | 8.8 | 9.9 | 13.3 | 7.0 | 8.6 | 10.1 | 9.8 | 12.0 | 13.8 | 16.4 | 13.6 | 11.9 | 14.8 | 14.8 | 14.1 | 10.3 | 7.5 | 7.2 | 9.0 | 9.1 | 8.8 | 10.7 |
| 23 |  | 8.6 | 7.2 | 9.1 | 8.5 | 9.3 | 10.4 | 12.8 | 7.8 | 11.7 | 10.1 | 1 C .7 | 11.1 | 11.4 | 11.5 | 12.5 | 13.3 | 14.0 | 13.6 | 8.8 | 6.5 | 5.9 | 7.8 | 7.2 | 8.5 | 9.9 |
| 24 |  | 7.2 | 9.3 | 10.4 | 11.4 | 10.7 | 5.3 | 13.0 | 16.5 | 16.4 | 15.1 | 11.9 | 15.1 | 13.5 | 11.7 | 14.9 | 16.0 | 13.5 | 12.2 | 8.6 | 8.0 | $8 . E$ | 8.8 | 8.6 | 8.3 | 11.5 |
| 25 |  | 8.3 | 8.5 | 8.6 | 8.8 | 9.8 | 14.9 | 8.3 | 9.8 | 10.3 | 10.1 | 11.4 | 12.0 | 11.5 | 11.9 | 13.1 | 14.8 | 14.9 | 14.6 | 12.0 | 9.3 | 8.3 | 8.3 | 7.2 | 8.6 | 10.6 |
| 26 | 0 | 8.5 | 8.7 | 8.9 | 9.3 | 9.3 | 8.7 | 14.7 | 14.0 | 13.0 | 10.2 | 1 C .3 | 11.6 | 11.6 | 11.9 | 13.4 | 15.0 | 16.3 | 16.3 | 13.0 | 10.0 | 7.9 | 6.6 | 6.8 | 7.6 | 11. C |
| 27 |  | 8.1 | 8.5 | 8.5 | 8.9 | 8.7 | 8.9 | 9.7 | 9.8 | 10.6 | 13.0 | 12.9 | 11.9 | 11.9 | 10.5 | 13.2 | 16.4 | 16.6 | 16.6 | 14.7 | 11.8 | 9.8 | 5.c | 3.2 | 5.2 | 10.6 |
| 28 |  | 4.2 | 5.2 | 6.6 | 7.1 | 8.7 | 9.5 | 11.4 | 11.6 | 13.2 | 13.4 | 11.0 | 11.1 | 11.4 | 12.7 | 13.4 | 15.1 | 15.0 | 13.0 | 11.9 | 8.1 | 5.2 | 3.2 | 5.2 | 6.8 | 9.7 |
| 29 |  | 8.4 | 8.6 | 8.8 | 11.2 | 11.8 | 9.9 | 9.9 | 8.6 | 9.9 | 9.9 | 1 C .2 | 11.2 | 11.3 | 11.5 | 12.6 | 13.4 | 14.2 | 13.6 | 12.8 | 8.3 | 5.2 | 5.1 | 6.1 | 8.0 | 10.0 |
| $30$ | $c$ | 8.6 | 9.4 | 9.7 | 9.7 | 9.9 | 9.9 | 11.7 | 9.7 | 8.4 | 9.6 | 1 C .2 | 11.0 | 11.3 | 12.5 | 12.9 | 14.6 | 14.9 | 14.7 | 11.7 | 9.7 | 8.0 | 7.8 | 8.1 | 8.3 | 10.5 |
| 31 |  | 8.3 | 9.1 | 9.9 | 11.2 | 13.1 | 9.9 | 10.9 | 13.1 | 17.1 | 14.9 | 12.9 | 9.7 | 16.3 | 14.6 | 13.3 | 13.3 | 13.6 | 14.9 | 11.7 | 9.9 | 8.1 | 8. C | 7.6 | 8.1 | 11.6 |
| MEAN | A | 8.8 | 9.7 | 10.4 | 10.9 | 10.3 | 10.7 | 10.5 | 10.6 | 12.8 | 13.1 | 14.0 | 14.4 | 13.2 | 12.9 | 13.2 | 14.3 | 14.6 | 13.4 | 10.8 | 8.3 | 1.2 | 6.5 | 7.6 | 8.5 | 11.1 |
| MEAN | 0 | 8.8 | 9.5 | 9.9 | 10.0 | 10.2 | 10.0 | 10.3 | 10.7 | 10.9 | 10.8 | 1 C .8 | 11.3 | 12.8 | 13.5 | 13.8 | 15.1 | 15.7 | 14.7 | 11.3 | 8.3 | 7.0 | 6.9 | 7.7 | 8.5 | 10.8 |
| MEAN | D | 10.5 | 13.6 | 15.2 | 15.2 | 11.7 | 12.6 | 9.4 | 15.0 | 20.1 | 19.8 | 24.2 | 22.0 | 11.5 | 9.9 | 8.8 | 9.8 | 11.7 | 10.2 | 8.9 | 8.7 | 8.6 | 9.2 | 8.6 | 10.4 | 12.8 |


| HOUR <br> UT |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | TO | TO | 10 | TO | T0 | 10 | T0 | TO | 10 | 10 | T0 | 10 | TO | TC | T0 | 10 | T0 | 10 | T0 | T0 | 10 | TO | TC | TO | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |  |
| 1 | D | 739 | 753 | 750 | 738 | 736 | 727 | 613 | 610 | 685 | 644 | 662 | 562 | 645 | 680 | 698 | 699 | 722 | 723 | 723 | 722 | 724 | 732 | 742 | 741 | 698 |
| 2 | D | 736 | 748 | 747 | 727 | 724 | 624 | 619 | 575 | 571 | 761 | 618 | 557 | 604 | 610 | 544 | 687 | 702 | 747 | 743 | 732 | 733 | 737 | 74 C | 748 | 681 |
| 3 | 0 | 742 | 740 | 728 | 717 | 731 | 694 | 676 | 682 | 693 | 642 | 658 | 614 | 581 | 565 | 541 | 560 | 635 | 702 | 720 | 719 | 712 | 712 | 72 C | 717 | 675 |
| 4 |  | 721 | 723 | 721 | 719 | 708 | 686 | 709 | 709 | 707 | 645 | 679 | 685 | 684 | 694 | 707 | 112 | 713 | 712 | 710 | 712 | 113 | 716 | 725 | 724 | 705 |
| 5 |  | 727 | 726 | 716 | 721 | 721 | 722 | 717 | 716 | 686 | 656 | 653 | 681 | 701 | 702 | 712 | 712 | 716 | 717 | 718 | 715 | 719 | 718 | 71 C | 716 | 708 |
| 6 | D | 717 | 718 | 728 | 726 | 751 | 750 | 726 | 710 | 708 | 690 | 716 | 663 | 664 | 676 | 680 | 693 | 704 | 719 | 726 | 724 | $72 t$ | 717 | 7 CS | 716 | 711 |
| 7 |  | 714 | 728 | 742 | 769 | 742 | 728 | 702 | 645 | 685 | 693 | 697 | 704 | 709 | 110 | 713 | 712 | 711 | 710 | 709 | 704 | 710 | 713 | 713 | 713 | 712 |
| 8 | 0 | 713 | 709 | 709 | 709 | 709 | 709 | 709 | 709 | 690 | 706 | 707 | 706 | 705 | 705 | 705 | 705 | 703 | 704 | 703 | 704 | 706 | 713 | 72 C | 716 | 707 |
| 9 |  | 710 | 714 | 710 | 710 | 709 | 707 | 695 | 704 | 769 | 704 | 705 | 700 | 703 | 704 | 710 | 711 | 708 | 705 | 701 | 693 | 691 | 700 | 7 C 7 | 706 | 705 |
| 10 | D | 707 | 717 | 740 | 782 | 710 | 692 | 712 | 710 | 662 | 624 | 582 | 633 | 609 | 683 | 688 | 679 | 673 | 687 | 710 | 727 | 759 | 748 | 73 E | 725 | 695 |
| 11 |  | 728 | 741 | 745 | 726 | 717 | 709 | 681 | 690 | 760 | 676 | 618 | 671 | 644 | 596 | 652 | 686 | 717 | 712 | 708 | 708 | 717 | 722 | 715 | 710 | 696 |
| 12 |  | 719 | 727 | 746 | 721 | 727 | 727 | 718 | 521 | 634 | 662 | 662 | 643 | 591 | 551 | 568 | 616 | 654 | 700 | 718 | 717 | 717 | 118 | 717 | 711 | 674 |
| 13 |  | 711 | 710 | 710 | 709 | 710 | 718 | 709 | 673 | 710 | 701 | 617 | 597 | 662 | 688 | 700 | 701 | 701 | 700 | 697 | 699 | 700 | 704 | 707 | 709 | 693 |
| 14 | 0 | 664 | 663 | 663 | 663 | 663 | 663 | 662 | 662 | 661 | 662 | 663 | 663 | 661 | 662 | 661 | 664 | 665 | 666 | 660 | 660 | 66.4 | 665 | bet | 666 | 663 |
| 15 | 0 | 666 | 665 | 664 | 665 | 669 | 666 | 629 | 649 | 637 | 645 | 633 | 631 | 636 | 645 | 654 | 660 | 656 | 668 | 666 | 665 | 686 | 666 | 666 | 665 | 655 |
| 16 |  | 664 | 665 | 664 | 664 | 665 | 653 | 609 | 633 | $6 \in 2$ | 664 | 663 | 662 | 657 | 656 | 654 | 655 | 656 | 653 | 651 | 655 | 657 | 664 | 666 | 676 | 657 |
| 17 |  | 675 | 670 | 663 | 663 | 664 | 665 | 665 | 664 | 662 | 656 | 648 | 663 | 657 | 656 | 656 | 661 | 659 | 657 | 656 | 659 | 665 | 666 | 674 | 698 | 663 |
| 18 |  | 696 | 681 | 673 | 665 | 663 | 671 | 647 | 662 | 673 | 632 | 626 | 641 | 664 | 663 | 663 | 665 | 671 | 671 | 665 | 662 | 662 | 660 | 657 | 662 | 662 |
| 19 |  | 662 | 663 | 665 | 666 | 665 | 663 | 672 | 599 | 584 | 664 | 672 | 647 | 559 | 590 | 646 | 665 | 664 | 665 | 665 | 669 | 672 | 675 | 673 | 671 | 651 |
| 20 |  | 671 | 665 | 665 | 672 | 673 | 673 | 671 | 665 | 664 | 664 | 663 | 662 | 661 | 662 | 664 | 665 | 664 | 664 | 665 | 663 | 665 | 672 | 665 | 665 | 666 |
| 21 |  | 667 | 665 | 663 | 664 | 663 | 663 | 664 | 654 | 6 CS | 578 | 645 | 672 | 665 | 663 | 662 | 656 | 653 | 656 | 671 | 672 | 671 | 668 | 665 | 663 | 657 |
| 22 |  | 663 | 664 | 663 | 668 | 662 | 680 | 690 | 671 | 670 | 626 | 644 | 644 | 644 | 655 | 664 | 663 | 664 | 668 | 672 | 672 | 667 | 664 | 664 | 664 | 663 |
| 23 |  | 666 | 667 | 666 | 666 | 664 | 667 | 678 | 662 | 668 | 669 | 664 | 664 | 662 | 663 | 664 | 666 | 667 | 664 | 660 | 662 | tet | 672 | 672 | 670 | 666 |
| 24 |  | 662 | 670 | 672 | 696 | 700 | 665 | 693 | 652 | 672 | 631 | 652 | 647 | 579 | 628 | 653 | 653 | E63 | 665 | 664 | 666 | 670 | 671 | 667 | 669 | 661 |
| 25 |  | 667 | 663 | 663 | 664 | 670 | 657 | 672 | 669 | 663 | 659 | 649 | 661 | 660 | 661 | 661 | 663 | 663 | 662 | 661 | 659 | 661 | 662 | 668 | 667 | 663 |
| 26 | 0 | 664 | 663 | 663 | 662 | 663 | 664 | 862 | 657 | EE 2 | 670 | 670 | 668 | 663 | 662 | 663 | 669 | 670 | 669 | 661 | 662 | 663 | 663 | be4 | 663 | 664 |
| 27 |  | 663 | 663 | 663 | 663 | 665 | 666 | 669 | 670 | 669 | 652 | 641 | 662 | 653 | 643 | 653 | 663 | 669 | 670 | 671 | 672 | 678 | 681 | 691 | 680 | 665 |
| 28 |  | 683 | 684 | 687 | 695 | 690 | 679 | 670 | 668 | 671 | 671 | 672 | 670 | 663 | 662 | 666 | 667 | 663 | 663 | 663 | 665 | 671 | 675 | 67 C | 669 | 672 |
| 29 |  | 668 | 667 | 669 | 671 | 671 | 669 | 662 | 661 | 661 | 661 | 664 | 665 | 863 | 663 | 665 | 669 | 671 | 670 | 672 | 670 | 689 | 669 | 67 C | 669 | 667 |
| 30 | 0 | 669 | 667 | 664 | 663 | 662 | 662 | 661 | 660 | 662 | 662 | 661 | 661 | 660 | 661 | 662 | 664 | 689 | 669 | 669 | 664 | E62 | 661 | 662 | 662 | 663 |
| 31 |  | 661 | 661 | 661 | 669 | 669 | 670 | 669 | 632 | 603 | 611 | 593 | 622 | 574 | 604 | 630 | 648 | 668 | 671 | 669 | 669 | 671 | 677 | 677 | 672 | 648 |
| MEAN | A | 691 | 692 | 693 | 694 | 691 | 684 | 675 | 859 | 663 | 661 | 655 | 652 | 648 | 654 | 660 | 671 | 678 | 684 | 685 | 685 | 688 | 69 C | 69 C | 690 | 676 |
| MEAN | 0 | 675 | 673 | 672 | 672 | 673 | 673 | 664 | 667 | 682 | 669 | 666 | 666 | 665 | 667 | 669 | 672 | 673 | 675 | 672 | 671 | 672 | 673 | 675 | 675 | 670 |
| MEAN | 0 | 728 | 735 | 739 | 738 | 730 | 697 | 669 | 657 | 660 | 672 | 647 | 606 | 621 | 643 | 630 | 664 | 687 | 716 | 724 | 725 | 730 | 129 | 725 | 729 | 692 |


| HOUR <br> UT |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 2 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | T0 | ro | TO | T0 | T0 | T0 | TO | T0 | 10 | T0 | TO | T0 | TO | TC | T0 | 10 | T0 | 10 | T0 | TO | T0 | T0 | T0 | 10 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 22 | 24 | Mean |
| 1 | 0 | 751 | 750 | 752 | 753 | 753 | 754 | 754 | 755 | 756 | 757 | 760 | 761 | 762 | 762 | 764 | 757 | 745 | 735 | 731 | 722 | 723 | 732 | 741 | 744 | 749 |
| 2 |  | 747 | 751 | 752 | 753 | 753 | 754 | 753 | 753 | 750 | 745 | 754 | 762 | 764 | 762 | 744 | 702 | 700 | 731 | 729 | 721 | 731 | 733 | 751 | 754 | 744 |
| 3 | D | 762 | 764 | 746 | 754 | 765 | 766 | 753 | 707 | 623 | 685 | 752 | 754 | 752 | 742 | 732 | 713 | 745 | 753 | 735 | 732 | 724 | 730 | 743 | 747 | 737 |
| 4 |  | 742 | 751 | 754 | 743 | 751 | 753 | 752 | 752 | 742 | 701 | 692 | 734 | 760 | 757 | 757 | 759 | 753 | 742 | 730 | 721 | 719 | 722 | 731 | 742 | 740 |
| 5 |  | 743 | 742 | 752 | 761 | 764 | 764 | 760 | 753 | 754 | 764 | 763 | 765 | 763 | 763 | 752 | 741 | 751 | 751 | 742 | 740 | 741 | 742 | 75 C | 754 | 753 |
| 6 | $c$ | 761 | 761 | 761 | 759 | 760 | 760 | 759 | 764 | 763 | 764 | 764 | 765 | 765 | 763 | 761 | 753 | 745 | 741 | 739 | 739 | 748 | 749 | 753 | 764 | 757 |
| 7 |  | 768 | 769 | 753 | 757 | 751 | 742 | 733 | 731 | 679 | 731 | 730 | 741 | 722 | 764 | 770 | 767 | 761 | 750 | 741 | 742 | 739 | 733 | 734 | 742 | 744 |
| 8 |  | 753 | 753 | 754 | 749 | 741 | 744 | 722 | 739 | 751 | 744 | 751 | 751 | 761 | 763 | 753 | 730 | 744 | 711 | 700 | 710 | 740 | 742 | 754 | 760 | 743 |
| 9 | D | 749 | 763 | 760 | 765 | 772 | 554 | 575 | 710 | 630 | 239 | 359 | 584 | 639 | 700 | 494 | 737 | 744 | 749 | 689 | 721 | 741 | 751 | 75 5 | 761 | 664 |
| 10 | D | 760 | 754 | 753 | 764 | 803 | 808 | 918 | 769 | 751 | 814 | 802 | 745 | 558 | 621 | 725 | 753 | 750 | 720 | 703 | 669 | 694 | 752 | 743 | 749 | 745 |
| 11 |  | 760 | 751 | 752 | 751 | 744 | 750 | 751 | 731 | 732 | 725 | 723 | 733 | 754 | 752 | 733 | 722 | 744 | 741 | 732 | 724 | 733 | 74C | 758 | 758 | 741 |
| 12 |  | 751 | 740 | 763 | 761 | 765 | 770 | 761 | 754 | 750 | 740 | 751 | 760 | 756 | 757 | 760 | 752 | 734 | 720 | 724 | 730 | 733 | 741 | 744 | 743 | 748 |
| 13 |  | 753 | 763 | 760 | 762 | 760 | 759 | 757 | 750 | 745 | 749 | 759 | 756 | 751 | 760 | 758 | 753 | 749 | 740 | 732 | 731 | 733 | 742 | 748 | 751 | 751 |
| 14 | 0 | 762 | 760 | 760 | 762 | 760 | 760 | 760 | 759 | 758 | 754 | 759 | 759 | 757 | 754 | 752 | 750 | 742 | 737 | 730 | 731 | 733 | 740 | $74 t$ | 748 | 752 |
| 15 | 6 | 751 | 752 | 753 | 754 | 754 | 754 | 754 | 754 | 754 | 754 | 755 | 757 | 757 | 756 | 756 | 751 | 746 | 743 | 740 | 741 | 743 | 748 | 75 C | 753 | 751 |
| 16 |  | 750 | 764 | 764 | 764 | 764 | 764 | 763 | 763 | 760 | 760 | 763 | 764 | 763 | 763 | 763 | 762 | 760 | 741 | 740 | 741 | 746 | 749 | 751 | 760 | 757 |
| 17 |  | 763 | 769 | 767 | 767 | 770 | 770 | 764 | 763 | 762 | 762 | 763 | 762 | 760 | 760 | 760 | 759 | 753 | 744 | 743 | 745 | 749 | 750 | 745 | 758 | 759 |
| 18 |  | 759 | 763 | 771 | 764 | 763 | 769 | 762 | 760 | 760 | 759 | 763 | 762 | 762 | 767 | 765 | 764 | 753 | 741 | 740 | 743 | 740 | 739 | 742 | 752 | 757 |
| 19 |  | 759 | 762 | 763 | 763 | 764 | 163 | 760 | 754 | 760 | 763 | 762 | 762 | 751 | 746 | 760 | 762 | 759 | 748 | 733 | 737 | 728 | 719 | 737 | 739 | 752 |
| 20 |  | 750 | 760 | 763 | 762 | 762 | 760 | 759 | 759 | $7 \in 0$ | 759 | 760 | 762 | 760 | 760 | 760 | 759 | 756 | 751 | 746 | 742 | 741 | 745 | 745 | 752 | 756 |
| 21 | 0 | 759 | 759 | 759 | 760 | 760 | 759 | 758 | 759 | 760 | 762 | 762 | 760 | 760 | 762 | 757 | 755 | 758 | 751 | 743 | 740 | 741 | 743 | 75C | 752 | 756 |
| 22 |  | 760 | 762 | 768 | 765 | 779 | 786 | 790 | 770 | 765 | 764 | 763 | 764 | 763 | 762 | 760 | 762 | 757 | 748 | 742 | 732 | 740 | 753 | 759 | 754 | 761 |
| 23 |  | 759 | 762 | 763 | 763 | 762 | 764 | 762 | 762 | 762 | 764 | 765 | 766 | 764 | 766 | 764 | 758 | 745 | 742 | 727 | 725 | 732 | 741 | 742 | 751 | 754 |
| 24 |  | 759 | 761 | 758 | 757 | 758 | 758 | 753 | 757 | 758 | 718 | 739 | 765 | 769 | 768 | 758 | 762 | 759 | 746 | 739 | 739 | 737 | 740 | 745 | 750 | 752 |
| 25 |  | 759 | 765 | 766 | 765 | 763 | 765 | 761 | 161 | 750 | 759 | 759 | 731 | 751 | 766 | 762 | 75 C | 741 | 748 | 732 | 731 | 134 | 738 | 735 | 749 | 752 |
| 26 |  | 758 | 773 | 773 | 782 | 773 | 779 | 771 | 759 | 752 | 752 | 753 | 759 | 759 | 758 | 756 | 762 | 750 | 718 | 720 | 731 | 739 | 730 | 745 | 758 | 753 |
| 27 | D | 759 | 762 | 759 | 761 | 772 | 771 | 729 | 559 | 513 | 289 | 627 | 616 | 615 | 630 | 719 | 670 | 750 | 731 | 716 | 717 | 741 | 750 | 749 | 739 | 685 |
| 28 |  | 751 | 763 | 769 | 766 | 757 | 756 | 751 | 756 | 699 | 721 | 762 | 759 | 751 | 748 | 759 | 761 | 758 | 749 | 736 | 730 | 718 | 736 | 73 C | 739 | 747 |
| 29 |  | 761 | 758 | 752 | 757 | 759 | 752 | 741 | 738 | 729 | 751 | 738 | 749 | 731 | 750 | 739 | 756 | 728 | 710 | 721 | 750 | 722 | 74C | 745 | 740 | 742 |
| 30 | D | 740 | 759 | 762 | 759 | 754 | 728 | 639 | 627 | 610 | 691 | 758 | 761 | 752 | 751 | 752 | 729 | 696 | 698 | 728 | 730 | 737 | 732 | 738 | 746 | 724 |
| MEAN | A | 755 | 759 | 759 | 760 | 762 | 755 | 751 | 741 | 728 | 715 | 737 | 746 | 741 | 748 | 745 | 747 | 746 | 738 | 730 | 730 | 734 | 74C | 746 | 750 | 744 |
| MEAN | 0 | 757 | 757 | 757 | 758 | 758 | 758 | 757 | 758 | 758 | 758 | 760 | 761 | 760 | 759 | 758 | 753 | 747 | 741 | 736 | 735 | 738 | 742 | 74 E | 752 | 753 |
| MEAN | D | 754 | 760 | 756 | 760 | 773 | 725 | 723 | 674 | 625 | 544 | 660 | 692 | 663 | 689 | 685 | 720 | 737 | 730 | 714 | 714 | 727 | 743 | $74 \in$ | 749 | 711 |


| HOUR UT |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | T0 | T0 | 10 | TO | TC | TO | T0 | T0 | 10 | 10 | T0 | T0 | 10 | TC | 10 | 10 | 10 | T0 | 10 | 10 | 10 | 10 | TC | 10 | NEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |  |
| 1 | 0 | B.0 | 8.3 | 10.1 | 9.6 | 9.9 | 9.7 | 9.7 | 9.7 | 9.9 | 9.9 | 10.1 | 10.4 | 11.2 | 11.3 | 12.9 | 15.0 | 18.3 | 18.1 | 15.0 | 11.5 | 8.4 | 8.1 | 8.C | 7.8 | 10.9 |
| 2 |  | 8.0 | 4.8 | 8.5 | 9.5 | 10.0 | 10.0 | 10.1 | 10.9 | 14.6 | 14.9 | 8.3 | 10.6 | 11.1 | 10.1 | 8.5 | 6.7 | 4.8 | 7.4 | 12.8 | 13.0 | 8.5 | 8.C | 7.5 | 8.3 | 9.5 |
| 3 | 0 | 8.3 | 6.4 | 9.5 | 9.0 | 9.6 | 8.3 | 14.5 | 16.2 | 12.8 | 14.5 | 1 C .8 | 11.2 | 11.1 | 8.7 | 11.4 | 9.8 | 10.3 | 15.3 | 14.6 | 11.6 | 11.9 | 9.6 | 8.2 | 8.0 | 10.9 |
| 4 |  | 8.2 | 8.7 | 8.5 | 10.8 | 10.0 | 9.8 | 10.9 | 13.2 | 13.0 | 9.8 | 7.9 | 11.6 | 9.1 | 8.5 | 10.8 | 13.3 | 14.6 | 15.9 | 11.7 | 9.6 | 8.2 | 6.7 | 6.2 | 6.9 | 10.2 |
| 5 |  | 6.4 | 8.0 | 9.6 | 9.5 | 10.9 | 10.0 | 9.6 | 10.0 | 11.2 | 10.1 | 9.8 | 10.0 | 11.4 | 11.4 | 10.8 | 8.3 | 11.6 | 13.3 | 11.4 | 9.8 | 8.5 | 8.0 | $8 . \mathrm{C}$ | 8.2 | 9.8 |
| 6 | 0 | 8.4 | 9.0 | 9.4 | 9.7 | 9.5 | 9.9 | 9.9 | 8.2 | 8.1 | 9.2 | 9.5 | 10.0 | 10.3 | 11.0 | 11.6 | 13.2 | 14.4 | 12.6 | 10.0 | 9.5 | 7.6 | 7.4 | 7.8 | 6.5 | 9.7 |
| 7 |  | 6.6 | 6.5 | 10.0 | 8.2 | 6.1 | 9.4 | 11.3 | 14.4 | 12.7 | 19.7 | 10.7 | 10.8 | 14.4 | 14.2 | 16.1 | 16.5 | 12.9 | 13.2 | 7.8 | 7.8 | 6.0 | 5.8 | 6.3 | 8.2 | 10.6 |
| 8 |  | 9.5 | 9.7 | 9.9 | 9.7 | 11.8 | 8.1 | 12.6 | 11.1 | 8.7 | 8.1 | 7.6 | 8.2 | 10.8 | 11.3 | 10.7 | 4.7 | 14.4 | 13.1 | 3.6 | 6.5 | 4.7 | 1.6 | 4.5 | 5.2 | 8.6 |
| 9 | D | 8.4 | 10.0 | 11.1 | 10.0 | 8.1 | 1.8 | 28.2 | 14.8 | 13.4 | 9.5 | 8.1 | 11.3 | 23.9 | 17.7 | 19.5 | 9.5 | 8.1 | 14.7 | 1.6 | -1.4 | 3.1 | 5.0 | 7.8 | 8.2 | 10.5 |
| 10 | D | 9.4 | 9.6 | 10.9 | 10.7 | 13.5 | 6.7 | 28.7 | 11.4 | 7.2 | $-6.7$ | 2.5 | 5.9 | 19.3 | 15.4 | 17.8 | 19.6 | 18.9 | 12.8 | 9.9 | 3.6 | 1.7 | B.C | 8.1 | 9.4 | 10.6 |
| 11 |  | 8.0 | 9.6 | 9.8 | 11.0 | 12.5 | 11.5 | 9.6 | 6.4 | 11.0 | 7.8 | 11.5 | 8.1 | 9.6 | 11.7 | 12.3 | 11.5 | 15.9 | 14.4 | 11.4 | 1C.4 | 9.6 | 8.0 | 7.7 | 8.1 | 10.3 |
| 12 |  | 6.4 | 10.9 | 10.6 | 10.3 | 13.5 | 12.5 | 9.8 | 9.7 | 9.3 | 6.1 | 9.5 | 11.1 | 10.9 | 10.0 | 12.4 | 15.4 | 17.9 | 14.6 | 9.7 | 8.8 | 7.9 | 6.4 | 7.6 | 7.7 | 10.4 |
| 13 |  | 7.9 | 8.2 | 9.5 | 9.8 | 10.0 | 10.0 | 9.8 | 8.5 | 9.2 | 10.9 | 10.1 | 11.3 | 13.4 | 12.7 | 12.5 | 16.1 | 14.0 | 11.4 | 7.9 | 7.9 | 7.6 | 6.3 | $6 . E$ | 7.7 | 10.0 |
| 14 | 0 | 7.6 | 8.0 | 9.0 | 9.5 | 9.7 | 9.8 | 9.8 | 10.0 | 10.0 | 9.7 | 10.8 | 10.9 | 11.1 | 11.3 | 12.5 | 14.0 | 14.5 | 14.0 | 11.1 | 9.0 | 7.7 | 6.4 | 7.6 | 7.7 | 10.1 |
| 15 | 0 | 7.9 | 8.7 | 9.2 | 9.3 | 9.5 | 9.5 | 9.5 | 9.5 | 9.5 | 9.7 | 9.7 | 10.0 | 10.8 | 10.9 | 11.9 | 13.5 | 15.4 | 14.0 | 11.1 | 9.3 | 7.9 | 7.9 | 7.7 | 8.2 | 10.0 |
| 16 |  | 7.9 | 9.3 | 9.7 | 9.5 | 9.5 | 9.8 | 10.3 | 9.7 | 10.1 | 9.8 | 10.6 | 10.8 | 10.8 | 11.1 | 12.2 | 14.2 | 14.6 | 15.9 | 10.9 | 9.3 | 7.6 | 6.4 | 7.4 | 7.6 | 10.3 |
| 17 |  | 8.0 | 8.2 | 9.3 | 9.5 | 9.7 | 9.7 | 9.7 | 9.7 | 9.8 | 9.8 | 11.1 | 10.9 | 11.1 | 11.3 | 12.2 | 13.7 | 15.9 | 14.5 | 9.5 | 9.5 | 8.4 | 6.4 | 6.6 | 7.7 | 10.1 |
| 18 |  | 8.4 | 8.0 | 8.2 | 9.5 | 9.8 | 9.7 | 9.7 | 10.5 | 11.3 | 10.9 | 12.4 | 12.5 | 12.7 | 12.1 | 12.2 | 14.2 | 15.6 | 15.9 | 9.5 | 7.9 | 8.0 | 8.2 | 7.7 | 7.6 | 10.5 |
| 19 |  | 7.9 | 8.8 | 9.2 | 9.3 | 9.5 | 9.5 | 11.7 | 9.7 | 11.1 | 9.8 | 10.9 | 12.5 | 9.8 | 7.4 | 10.9 | 13.7 | 13.8 | 12.4 | 7.9 | 6.3 | t. 6 | 4.7 | 8.2 | 9.2 | 9.6 |
| 20 |  | 8.3 | 9.8 | 11.8 | 9.6 | 9.8 | 9.9 | 9.8 | 10.7 | 9.4 | 11.2 | 11.4 | 11.2 | 10.9 | 11.0 | 11.8 | 12.8 | 12.6 | 12.6 | 11.2 | 10.4 | 10.1 | 9.4 | 8.1 | 9.1 | 10.5 |
| 21 | 0 | 9.1 | 8.9 | 9.4 | 9.8 | 9.6 | 9.4 | 9.6 | 9.6 | 9.6 | 9.9 | 11.0 | 11.2 | 11.0 | 11.4 | 11.2 | 11.5 | 13.1 | 14.1 | 12.3 | 11.0 | 9.4 | 7.7 | 7.5 | 8.0 | 10.2 |
| 22 |  | 9.4 | 9.8 | 9.4 | 9.8 | 8.1 | 6.4 | 7.2 | 7.5 | 6.7 | 7.8 | 8.3 | 9.8 | 11.2 | 12.5 | 11.4 | 13.0 | 14.6 | 15.1 | 10.9 | 8.6 | 5.9 | 4.1 | 6.5 | 7.8 | 9.2 |
| 23 |  | 9.4 | 9.4 | 9.8 | 9.9 | 9.8 | 9.4 | 9.4 | 9.1 | 9.4 | 9.4 | 9.8 | 10.2 | 11.0 | 11.4 | 12.5 | 14.4 | 15.7 | 14.6 | 7.7 | 4.9 | 4.4 | 5.9 | $7 . C$ | 8.1 | 9.7 |
| 24 |  | 9.6 | 9.8 | 10.1 | 9.9 | 9.9 | 9.8 | 9.9 | 9.1 | 9.4 | 3.5 | 6.4 | 9.8 | 11.5 | 12.5 | 9.9 | 14.3 | 14.4 | 12.5 | 9.9 | 8.0 | 7.8 | 6.4 | 6.5 | 8.1 | 9.5 |
| 25 |  | 9.3 | 9.6 | 9.8 | 9.9 | 9.8 | 9.4 | 13.0 | 13.1 | 11.7 | 9.8 | 9.9 | 8.1 | 11.2 | 15.4 | 14.4 | 14.7 | 13.0 | 15.5 | 9.6 | 8.1 | 7.5 | 6.2 | 3.5 | 3.0 | 10.2 |
| 26 |  | 4.7 | 6.5 | 5.8 | 6.1 | 10.0 | 12.7 | 10.0 | 9.9 | 9.5 | 9.5 | 9.7 | 11.0 | 11.1 | 11.1 | 11.5 | 15.8 | 12.9 | 2.0 | $-1.1$ | 1.0 | 5.6 | 7.6 | 8.1 | 9.0 | 8.3 |
| 27 | D | 10.0 | 11.1 | 11.8 | 11.3 | 16.3 | 29.0 | 16.0 | 11.5 | 8.2 | 6.5 | 20.6 | 18.9 | 5.0 | 11.1 | 11.3 | 12.9 | 12.3 | 11.0 | 6.6 | -1.4 | 4.7 | 7.1 | 6.6 | 7.6 | 11.1 |
| 28 |  | 9.7 | 9.9 | 11.1 | 12.9 | 14.8 | 11.3 | 16.0 | 22.1 | 7.9 | 5.0 | 5.9 | 11.0 | 11.0 | 0.2 | 11.3 | 13.4 | 15.2 | 14.7 | 12.6 | 8.1 | 4.7 | 4.5 | 6. 3 | 5.7 | 10.7 |
| 29 |  | 7.9 | 8.9 | 9.4 | 11.5 | 11.5 | 11.3 | 14.4 | 22.9 | 13.1 | 11.1 | 5.3 | 5.7 | 11.5 | 1.8 | 8.2 | 13.1 | 12.1 | 13.2 | 14.2 | 11.0 | 8.2 | 6.5 | 7.8 | 6.5 | 10.3 |
| 30 | D | 7.9 | 13.7 | 11.0 | 15.0 | 13.1 | 12.9 | 8.1 | 7.4 | 13.2 | 11.3 | 7.9 | 9.4 | 10.7 | 10.3 | 10.5 | 8.1 | -1.3 | 1.8 | 5.7 | 8.4 | 8.1 | 7.9 | 9.5 | 9.7 | 9.2 |
| MEAN | A | 8.2 | 8.9 | 9.7 | 10.0 | 10.5 | 10.2 | 12.0 | 11.2 | 10.4 | 9.3 | 9.7 | 10.5 | 11.6 | 11.2 | 12.1 | 12.9 | 13.4 | 13.0 | 9.6 | 7.9 | 7.2 | 6.7 | 7.2 | 7.7 | 10.1 |
| MEAN | 0 | 8.2 | 8.6 | 9.4 | 9.6 | 9.6 | 9.7 | 9.7 | 9.4 | 9.4 | 9.7 | 10.2 | 10.5 | 10.9 | 11.2 | 12.0 | 13.5 | 15.1 | 14.6 | 11.9 | 10.1 | 8.2 | 7.5 | 7.7 | 7.6 | 10.2 |
| MEAN | 0 | 8.8 | 10.2 | 10.8 | 11.2 | 12.1 | 11.8 | 19.1 | 12.3 | 11.0 | 7.0 | 10.0 | 11.3 | 14*0 | 12.7 | 14.1 | 12.0 | 9.7 | 11.1 | 7.7 | 4.2 | 5.9 | 7.5 | $8 . C$ | 8.6 | 10.5 |


| $\begin{aligned} & \text { HOUR } \\ & \text { UT } \end{aligned}$ |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 10 | 10 | 10 | T0 | TC | TO | TO | T0 | T0 | T0 | T0 | T0 | 10 | 1 C | 10 | T0 | 10 | 10 | T0 | 10 | 10 | T0 | 1 C | T0 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 22 | 24 |  |
| 1 | 0 | 673 | 672 | 670 | 669 | 667 | 663 | 661 | 661 | 661 | 660 | 660 | 661 | 660 | 661 | 663 | 664 | 666 | 664 | 667 | 668 | 668 | 667 | 667 | 668 | 665 |
| 2 |  | 668 | 677 | 671 | 672 | 667 | 668 | 667 | 655 | 631 | 615 | 633 | 647 | 659 | 658 | 651 | 634 | 642 | 658 | 666 | 674 | 671 | 669 | 68 C | 706 | 660 |
| 3 | 0 | 724 | 717 | 687 | 880 | 693 | 668 | 693 | 649 | 594 | 602 | 658 | 668 | 660 | 659 | 648 | 655 | 669 | 677 | 678 | 679 | 690 | 696 | 689 | 681 | 671 |
| 4 |  | 670 | 669 | 677 | 690 | 697 | 678 | 668 | 651 | 638 | 595 | 547 | 615 | 658 | 667 | 670 | 672 | 673 | 672 | 670 | 677 | 675 | 679 | 680 | 679 | 661 |
| 5 |  | 677 | 675 | 670 | 676 | 677 | 681 | 670 | 667 | 666 | 648 | 660 | 660 | 659 | 660 | 658 | 649 | 659 | 657 | 653 | 657 | 659 | 660 | 665 | 660 | 663 |
| 6 | 0 | 659 | 659 | 659 | 659 | 660 | 660 | 660 | 649 | 654 | 657 | 658 | 658 | 659 | 659 | 660 | 660 | 660 | 659 | 658 | 657 | 657 | 659 | 657 | 658 | 658 |
| 7 |  | 658 | 659 | 666 | 669 | 673 | 673 | 651 | 628 | 535 | 557 | 574 | 601 | 547 | 640 | 664 | 663 | 658 | 660 | 666 | 670 | 678 | 681 | 686 | 686 | 643 |
| 8 |  | 688 | 675 | 673 | 668 | 667 | 674 | 599 | 628 | 637 | 621 | 629 | 641 | 658 | 66 C | 648 | 619 | 641 | 649 | 665 | 671 | 688 | 715 | 712 | 718 | 660 |
| 9 | 0 | 700 | 683 | 669 | 676 | 675 | 628 | 537 | 584 | 5¢2 | 603 | 468 | 403 | 586 | 656 | 661 | 104 | 67.3 | 696 | 651 | 658 | 667 | 673 | 67 C | 668 | 633 |
| 10 | D | 667 | 666 | 667 | 688 | 724 | 731 | 675 | 649 | 675 | 646 | 633 | 692 | 525 | 545 | 626 | 666 | 695 | 678 | 683 | 685 | 704 | 706 | 694 | 685 | 667 |
| 11 |  | 687 | 678 | 677 | 675 | 673 | 669 | 658 | 629 | 627 | 634 | 628 | 656 | 657 | 659 | 651 | 657 | 676 | 669 | 668 | 676 | 682 | 675 | 675 | 674 | 663 |
| 12 |  | 677 | 685 | 682 | 674 | 674 | 667 | 671 | 667 | 658 | 633 | 638 | 664 | 666 | 668 | 674 | 674 | 674 | 675 | 674 | 674 | 674 | 676 | 675 | 674 | 670 |
| 13 |  | 674 | 675 | 669 | 667 | 667 | 666 | 666 | 660 | 634 | 637 | 667 | 674 | 665 | 668 | 666 | 662 | 660 | 658 | 657 | 665 | 671 | 674 | 674 | 674 | 665 |
| 14 | c | 675 | 674 | 674 | 674 | 673 | 667 | 666 | 665 | 665 | 664 | 665 | 665 | 665 | 664 | 666 | 669 | 673 | 671 | 670 | 670 | 666 | 665 | 664 | 664 | 668 |
| 15 | 6 | 665 | 665 | 665 | 665 | 665 | 664 | 663 | 663 | $6 \in 3$ | 663 | 663 | 663 | 664 | 664 | 664 | 664 | 665 | 666 | 666 | 665 | 665 | 665 | 665 | 665 | 664 |
| 16 |  | 666 | 666 | 666 | 666 | 666 | 665 | 665 | 665 | 659 | 656 | 681 | 661 | 661 | 661 | 661 | 665 | 666 | 666 | 664 | E 66 | 666 | 665 | 665 | 665 | 664 |
| 17 |  | 665 | 664 | 663 | 662 | 662 | 661 | 661 | 661 | 661 | 659 | 660 | 664 | 664 | 664 | 665 | 666 | 670 | 666 | 665 | 666 | 664 | 663 | 664 | 667 | 664 |
| 18 |  | 665 | 665 | 666 | 664 | 664 | 665 | 666 | 665 | 665 | 662 | 657 | 658 | 657 | 661 | 665 | 667 | 668 | 669 | 664 | 665 | 666 | 667 | 667 | 667 | 664 |
| 19 |  | 666 | 665 | 665 | 665 | 665 | 667 | 675 | 665 | 668 | 666 | 665 | 658 | 649 | 836 | 647 | 655 | 657 | 658 | 658 | 664 | 665 | 674 | 677 | 674 | 663 |
| 20 |  | 675 | 685 | 693 | 680 | 674 | 667 | 666 | 665 | 665 | 658 | 658 | 664 | 664 | 663 | 664 | 666 | 666 | 663 | 661. | ¢ 58 | 658 | 659 | 661 | 664 | 667 |
| 21 | $Q$ | 664 | 661 | 661 | 661 | 661 | 663 | 664 | 664 | 658 | 657 | 660 | 658 | 656 | 657 | 657 | 658 | 659 | 658 | 663 | 665 | 666 | 666 | 668 | 666 | 661 |
| 22 |  | 665 | 664 | 665 | 668 | 684 | 711 | 712 | 687 | 674 | 666 | 665 | 664 | 658 | 656 | 656 | 657 | 658 | 657 | 658 | 658 | cte | 667 | 664 | 666 | 668 |
| 23 |  | 666 | 665 | 664 | 663 | 663 | 661 | 659 | 659 | 659 | 659 | 658 | 658 | 658 | 658 | 658 | 661 | $6 \in 5$ | 664 | 663 | EEG | 668 | 668 | 667 | 669 | 663 |
| 24 |  | 669 | 668 | 668 | 667 | 666 | 665 | 659 | 656 | 649 | 606 | 610 | 648 | 656 | 657 | 650 | 657 | 653 | 659 | 681 | 665 | 667 | 669 | 675 | 671 | 657 |
| 25 |  | 668 | 667 | 666 | 663 | 664 | 666 | 659 | 657 | 654 | 659 | 658 | 628 | 627 | 647 | 658 | 657 | 656 | 658 | 655 | 659 | 667 | 667 | 672 | 678 | 659 |
| 26 |  | 686 | 707 | 706 | 737 | 707 | 694 | 676 | 673 | $6 \in 8$ | 667 | 667 |  |  | 662 | 665 |  | 665 | 638 | 640 | 650 | 675 | 666 | 667 | 666 | 674 |
| 27 | D | 668 | 670 | 669 | 675 | 694 | 641 | 643 | 518 | 489 | 412 | 401 | 595 | 526 | 533 | 563 | 598 | 667 | 649 | 684 | 687 | 681 | 685 | 688 | 699 | 614 |
| 28 |  | 714 | 711 | 705 | 694 | 691 | 687 | 667 | 639 | 627 | 628 | 667 | 667 | 658 | 657 | 666 | 671 | 669 | 667 | 667 | 675 | 675 | 885 | 694 | 679 | 673 |
| 29 |  | 676 | 684 | 682 | 675 | 672 | 672 | 658 | 614 | 629 | 646 | 634 | 658 | 639 | 602 | 634 | 657 | 652 | 657 | 696 | 724 | 715 | 734 | 7CE | 703 | 667 |
| 30 | D | 718 | 687 | 708 | 716 | 694 | 657 | 611 | 607 | 572 | 602 | 666 | 675 | 666 | 667 | 666 | 655 | 649 | 647 | 659 | 685 | 687 | 684 | 678 | 685 | 664 |
| MEAN | A | 676 | 675 | 674 | 675 | 676 | 670 | 658 | 647 | 638 | 631 | 632 | 646 | 643 | 649 | 655 | 659 | 663 | 663 | 665 | 670 | 672 | 676 | 675 | 676 | 661 |
| MEAN | Q | 667 | 666 | 666 | 666 | 665 | 663 | 663 | 660 | 660 | 660 | 661 | 661 | 661 | 661 | 662 | 663 | 665 | 664 | 665 | C65 | 664 | 664 | 664 | 664 | 663 |
| MEAN | D | 695 | 685 | 680 | 687 | 696 | 665 | 632 | 601 | 584 | 573 | 565 | 607 | 592 | 612 | 633 | 656 | 671 | 670 | 671 | 679 | 686 | 689 | 684 | 684 | 650 |



| HCU |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | T | 10 | 10 | 10 | TC | 10 | 10 | T0 | T0 | 10 | 10 | T0 | 10 | T0 | IC | 10 | TC | 10 | T0 | 10 | T0 | TC | T0 | TC | T0 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 22 | 24 |  |
| 1 |  | 9.8 | 10.0 | 10.1 | 10.4 | 11.1 | 10.8 | 9.8 | 10.8 | 9.5 | 10.0 | 11.2 | 8.5 | 8.2 | 10.0 | 11.4 | 11.2 | 11.1 | 11.6 | 11.7 | 11.1 | 9.6 | 8.5 | 8.2 | 8.5 | 10.1 |
| 2 |  | 9.6 | 9.6 | 9.8 | 9.8 | 11.6 | 11.2 | 11.1 | 9.5 | 6.6 | 8.5 | 9.6 | 10.0 | 10.1 | 11.6 | 11.4 | 11.9 | 14.5 | 14.5 | 11.6 | 9.6 | 6.7 | 6.2 | 6.7 | 8.0 | 10.0 |
| 3 |  | 8.5 | 9.8 | 9.8 | 10.0 | 10.1 | 10.3 | 10.0 | 9.8 | 9.3 | 9.6 | 9.8 | 10.C | 10.1 | 11.1 | 11.9 | 13.7 | 15.9 | 14.8 | 13.0 | 11.2 | 9.3 | 6.4 | 6.2 | 5.0 | 10.2 |
| 4 |  | 6.9 | 8.7 | 9.6 | 10.1 | 9.6 | 7.9 | 9.5 | 9.6 | 9.6 | 10.0 | 8.5 | 8.0 | 10.4 | 11.4 | 12.0 | 16.2 | 13.2 | 13.0 | 11.1 | 9.3 | 8.2 | 8.0 | 6.5 | 8.5 | 9.8 |
| 5 | D | 9.6 | 9.8 | 10.1 | 10.4 | 10.0 | 11.4 | 13.3 | 9.8 | 7.4 | 9.5 | 6.9 | 3.2 | 11.7 | 14.6 | 8.2 | 13.0 | 13.3 | -4.5 | -3.1 | 3.3 | 4.8 | 5.4 | 8.2 | 6.1 | 8.C |
| 6 | 0 | 8.1 | 8.4 | 16.0 | 10.1 | 7.0 | 24.7 | 15.0 | 14.4 | 8.1 | 3.4 | 6.8 | 9.6 | 12.8 | 11.7 | 6.5 | . 6.8 | 13.1 | 14.4 | 11.5 | 10.9 | E.e | 8.4 | 8.3 | 9.7 | 10.6 |
| 7 |  | 11.2 | 11.3 | 11.2 | 10.4 | 11.5 | 12.9 | 12.9 | 10.1 | 10.1 | 8.0 | 3.9 | 10.2 | 11.7 | 12.8 | 12.1 | 12.9 | 12.8 | 13.1 | 12.1 | 9.9 | 9.6 | 8.4 | 9.7 | 9.9 | 10.8 |
| 8 |  | 9.9 | 10.1 | 11.8 | 12.0 | 11.2 | 13.3 | 11.2 | 9.1 | 9.9 | 9.7 | IC.2 | 11.2 | 10.9 | 11.3 | 11.3 | 11.7 | 11.8 | 13.4 | 11.5 | 11.0 | 9.9 | 9.6 | 8.4 | 8.9 | 10.8 |
| 9 | D | 9.9 | 9.7 | 12.8 | 14.9 | 10.2 | 10.9 | 11.2 | 10.1 | 9.9 | 10.1 | 1 C .4 | 11.7 | 11.5 | 11.2 | 12.9 | 14.9 | 14.7 | 11.8 | 10.7 | 10.2 | 9.7 | 8.3 | 7.6 | 8.1 | 11.0 |
| 10 |  | 8.4 | 10.1 | 11.0 | 11.2 | 11.0 | 10.5 | 10.2 | 11.0 | 10.1 | 9.7 | 10.1 | 9.9 | 10.4 | 11.3 | 12.3 | 13.1 | 14.1 | 11.0 | 9.7 | 10.1 | 8.6 | 6.8 | 5.5 | 3.8 | 10.0 |
| 11 |  | 6.5 | 8.3 | 10.1 | 12.8 | 11.8 | 12.9 | 11.8 | 11.7 | 12.6 | 9.7 | 13.1 | 12.8 | 12.9 | 14.9 | 19.2 | 17.8 | 18.4 | 16.8 | 13.3 | 11.2 | 8.3 | 6.7 | 6.7 | 6.7 | 12. C |
| 12 |  | 6.9 | 8.4. | 8.2 | 10.5 | 11.4 | 11.6 | 11.6 | 11.9 | 10.2 | 8.2 | 10.0 | 11.4 | 8.2 | 9.8 | 11.6 | 13.4 | 14.8 | 15.0 | 13.9 | 1 C .2 | 8.2 | 6.5 | 7.1 | 8.4 | 10.3 |
| 13 | G | 7.9 | 8.5 | 10.0 | 10.2 | 11.0 | 11.6 | 10.0 | 8.9 | 9.7 | 9.7 | 9.8 | 10.3 | 12.3 | 11.6 | 11.9 | 13.0 | 14.7 | 14.8 | 13.4 | 11.1 | 8.5 | 0.1 | 6.9 | 7.1 | 10.4 |
| 14 |  | 8.2 | 8.5 | 9.7 | 10.0 | 10.0 | 10.2 | 10.0 | 9.8 | 9.8 | 10.2 | 10.3 | 10.3 | 11.4 | 11.9 | 13.4 | 11.8 | 15.1 | 15.0 | 12.7 | 11.3 | 8.4 | 6.8 | $6 . t$ | 6.8 | 10.3 |
| 15 |  | 8.4 | 9.7 | 10.2 | 11.3 | 11.3 | 11.3 | 10.2 | 10.2 | 10.0 | 8.5 | 6.8 | 12.1 | 12.9 | 11.6 | 12.9 | 13.5 | 16.3 | 16.6 | 11.6 | 9.7 | 7.9 | 6.8 | 6.8 | 6.3 | 10.5 |
| 16 | 0 | 6.8 | 8.1 | 8.4 | 11.3 | 11.8 | 11.3 | 11.4 | 18.2 | 8.2 | 10.3 | 10.2 | 11.6 | 11.1 | 10.5 | 12.1 | 12.7 | 12.1 | 14.7 | 13.4 | 11.3 | 8.4 | 6.3 | 6.8 | 7.7 | 10.6 |
| 17 |  | 7.9 | 8.2 | 9.8 | 10.3 | 11.6 | 11.6 | 11.4 | 11.1 | 11.0 | 11.4 | 12.4 | 11.4 | 11.8 | 11.9 | 12.1 | 13.9 | 14.5 | 14.2 | 12.2 | 1 C .2 | 10.C | 9.0 | 8.7 | 8.7 | 11.1 |
| 18 |  | 8.9 | 9.8 | 10.3 | 11.0 | 10.8 | 10.5 | 10.3 | 10.2 | 10.2 | 10.3 | 10.2 | 11.C | 10.8 | 11.1 | 11.3 | 11.9 | 13.2 | 13.5 | 12.9 | 11.6 | 9.5 | 8.1 | 7.5 | 8.1 | 10.5 |
| 19 |  | 8.5 | 9.7 | 10.0 | 10.2 | 10.2 | 11.3 | 10.0 | 10.2 | 10.3 | 11.0 | 11.4 | 11.8 | 13.0 | 11.6 | 12.1 | 13.2 | 13.5 | 13.2 | 11.6 | 10.3 | 9.8 | 8.9 | 8.4 | 7.6 | 10.7 |
| 20 | 0 | 8.4 | 8.7 | 9.8 | 10.2 | 10.2 | 10.0 | 10.3 | 10.2 | 10.2 | 10.3 | 11.3 | 11.6 | 11.6 | 11.4 | 11.6 | 11.9 | 13.2 | 13.4 | 10.3 | 10.2 | 9.5 | 8.2 | 8.2 | 7.6 | 10.3 |
| 21 | 0 | 7.9 | 7.6 | 8.9 | 10.2 | 10.2 | 10.0 | 9.3 | 10.0 | 9.8 | 10.0 | 1 C .3 | 11.C | 11.0 | 11.3 | 11.4 | 12.7 | 13.0 | 13.2 | 12.6 | 11.4 | 10.2 | 9.7 | 8.4 | 8.7 | 10.4 |
| 22 |  | 8.1 | 9.1 | 9.9 | 10.1 | 10.1 | 9.9 | 1.0 | 12.9 | 11.8 | 9.7 | 10.2 | 12.9 | 10.7 | 11.3 | 14.9 | 16.2 | 14.7 | 12.8 | 10.1 | 9.6 | 8.8 | 8.1 | 8.t | 9.7 | 10.7 |
| 23 | D | 9.9 | 10.1 | 11.2 | 10.2 | 12.8 | 9.7 | 11.5 | 10.1 | 9.7 | 9.9 | 18.1 | 16.3 | 15.0 | 13.1 | 6.5 | 11.2 | 12.8 | 8.3 | . 7 | 4.9 | 5.1 | 6.5 | 8.2 | 9.6 | 10.1 |
| 24 |  | 8.4 | 13.1 | 13.3 | 12.8 | 10.1 | 9.7 | 9.7 | 10.5 | 10.1 | 11.2 | 11.0 | 8.9 | 12.3 | 11.3 | 13.3 | 14.1 | 13.4 | 12.5 | 10.4 | 2. 3 | 5.7 | 5.5 | 6.5 | 8.4 | 10.4 |
| 25 |  | 9.9 | 11.2 | 10.5 | 11.5 | 19.2 | 18.1 | 11.3 | 9.7 | 3.8 | 13.1 | 10.5 | 13.4 | 12.9 | 11.5 | 9.9 | 12.0 | 9.9 | 8.4 | 5.7 | 5.2 | 4.7 | 6.7 | 7.3 | 8.9 | 10.2 |
| 26 |  | 10.4 | 10.7 | 10.2 | 10.1 | 10.2 | 11.2 | 12.1 | 9.7 | 11.3 | 10.5 | 9.9 | 8.4 | 11.8 | 12.9 | 13.8 | 13.3 | 9.6 | 6.2 | 11.2 | 8.3 | 4.9 | 6.2 | 8.1 | 8.6 | 10.0 |
| 27 |  | 10.7 | 11.5 | 9.3 | 14.1 | 8.3 | 12.9 | 11.5 | 10.9 | 8.0 | 9.1 | -1.1 | 11.2 | 12.0 | 12.9 | 12.8 | 13.8 | 14.7 | 13.1 | 13.1 | 12.3 | 11.5 | 11.5 | 10.7 | 10.7 | 11.1 |
| 28 |  | 10.1 | 9.7 | 9.9 | 10.7 | 11.3 | 10.9 | 9.9 | 9.9 | 9.7 | 10.5 | 9.6 | 9.9 | 11.3 | 11.0 | 11.3 | 12.9 | 13.3 | 12.3 | 11.0 | 10.1 | 8.4 | 9.2 | 9.7 | 9.7 | 10.5 |
| 29 |  | 10.1 | 10.5 | 11.5 | 11.8 | 11.2 | 11.2 | 1 C .9 | 10.2 | 8.1 | 9.6 | 11.5 | 11.5 | 11.7 | 11.8 | 12.8 | 12.6 | 12.6 | 13.1 | 12.9 | 11.7 | 11.C | 10.2 | 9.5 | 9.7 | 11.2 |
| 30 | 0 | 9.9 | 10.1 | 10.1 | 9.9 | 11.7 | 9.9 | 10.5 | 10.9 | 10.9 | 10.7 | 9.7 | 11.3 | 11.2 | 11.5 | 11.3 | 12.6 | 14.2 | 14.9 | 14.6 | 13.4 | 11.2 | 9.9 | 9.6 | 9.7 | 11.2 |
| 31 | 0 | 9.7 | 9.9 | 10.2 | 10.9 | 11.0 | 10.4 | 9.9 | 10.2 | 10.4 | 10.2 | 5.7 | 11.2 | 9.9 | 11.2 | 11.3 | 12.6 | 14.6 | 14.6 | 14.4 | 12.8 | 11.0 | 9.7 | 8.3 | 8.6 | 10.9 |
| MEAN | A | 8.9 | 9.6 | 10.5 | $1 \mathrm{C}$. | 10.9 | 11.6 | 10.8 | 10.7 | 9.5 | 9.8 | 9.8 | 10.7 | 11.4 | 11.7 | 11.9 | 13.0 | 13.7 | 12.6 | 11.0 | 10.0 | 8.6 | 7.9 | 7.5 | 8.2 | 10.5 |
| MEAN | C | 8.8 | 9.0 | 9.8 | 10.2 | 10.8 | 10.4 | 10.0 | 10.0 | 10.2 | 10.2 | 10.2 | 11.1 | 11.0 | 11.4 | 11.5 | 12.6 | 13.9 | 14.2 | 13.0 | 11.8 | 10.1 | 9.1 | 8.3 | 8.3 | 10.7 |
| MEAN | D | 8.9 | 9.2 | 11.7 | 11.4 | 10.3 | 13.6 | 12.5 | 12.5 | 8.7 | 8.6 | 1C. 5 | 10.5 | 12.4 | 12.2 | 9.2 | 11.7 | 13.2 | 8.9 | 6.6 | 8.1 | 7.3 | 7.0 | 7.8 | 8.2 | 10.1 |

## TABLE 36 MEANOOK

| $\begin{aligned} & \text { HOUF } \\ & \text { UI } \end{aligned}$ |  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | TO | TO | T0 | T0 | 10 | 10 | TO | TO | 10 | 70 | 10 | T0 | T0 | 10 | TC | 1 C | 10 | T0 | 10 | 10 | TC | T0 | TC | 10 | MEAN |
| DAY |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |  |
| 1 |  | 688 | 678 | 675 | 670 | 667 | 666 | 666 | 665 | 856 | 650 | 649 | 631 | 620 | 646 | 657 | 649 | 646 | 645 | 647 | 659 | 675 | 675 | 675 | 675 | 660 |
| 2 |  | 672 | 669 | 669 | 670 | 671 | 674 | 669 | 657 | 622 | 651 | 659 | 659 | 651 | 649 | 659 | 668 | 672 | 667 | 668 | 671 | 674 | 674 | 675 | 675 | 664 |
| 3 |  | 676 | 675 | 676 | 673 | 671 | 672 | 671 | 670 | $6 \in 9$ | 669 | 669 | 669 | 668 | 669 | 670 | 876 | 674 | 670 | 669 | 670 | 670 | 669 | 674 | 676 | 671 |
| 4 |  | 669 | 669 | 670 | 672 | 674 | 676 | 670 | 667 | 666 | 660 | 650 | 629 | 646 | 629 | 611 | 643 | 648 | 659 | 660 | 659 | 659 | 66 C | 662 | 664 | 657 |
| 5 | D | 666 | 666 | 665 | 665 | 667 | 676 | 657 | 643 | 660 | 639 | 641 | 498 | 518 | 560 | 587 | 620 | 641 | 611 | 631 | 658 | 669 | 696 | 690 | 689 | 638 |
| 6 | D | 705 | 716 | 745 | 725 | 648 | 651 | 707 | 672 | 660 | 592 | 647 | 660 | 658 | 640 | 601 | 641 | 659 | 667 | 672 | 676 | 673 | 679 | 684 | 678 | 66'7 |
| 7 |  | 677 | 676 | 668 | 667 | 670 | 673 | 674 | 660 | 662 | 648 | 631 | 650 | 658 | 660 | 666 | 667 | 667 | 667 | 668 | 669 | 669 | 67 C | 672 | 669 | 665 |
| 8 |  | 668 | 668 | 669 | 672 | 671 | 670 | 668 | 667 | $6 \pm 6$ | 660 | 666 | 664 | 663 | 664 | 664 | 665 | 666 | 666 | 660 | 666 | 667 | 667 | 668 | 669 | 686 |
| 9 | D | 669 | 673 | 679 | 688 | 669 | 668 | 668 | 667 | 667 | 065 | 663 | 658 | 641 | 647 | 647 | 658 | 660 | 660 | 665 | 6e8 | 669 | 668 | 667 | 668 | 665 |
| 10 |  | 669 | 669 | 668 | 668 | 667 | 667 | 668 | 666 | 661 | 661 | 667 | 662 | 665 | 667 | 668 | 669 | 668 | 666 | 664 | 668 | 668 | 669 | 678 | 709 | 669 |
| 11 |  | 697 | 687 | 686 | 680 | 680 | 681 | 616 | 579 | 660 | 668 | 672 | 677 | 671 | 652 | 648 | 663 | 670 | 671 | 660 | 664 | 664 | 665 | 665 | 673 | 665 |
| 12 |  | 674 | 674 | 676 | 687 | 695 | 687 | 677 | 668 | 668 | 666 | 665 | 662 | 660 | 660 | 665 | 669 | 669 | 669 | 668 | 669 | 668 | 667 | 668 | 669 | 671 |
| 13 | Q | 670 | 669 | 669 | 670 | 670 | 670 | 666 | 653 | 666 | 667 | 667 | 668 | 667 | 661 | 661 | 662 | 664 | 662 | 665 | 668 | 668 | 669 | 668 | 669 | 666 |
| 14 |  | 669 | 667 | 667 | 668 | 667 | 667 | 666 | 665 | 662 | 661 | 661 | 661 | 660 | 661 | 661 | 660 | 661 | 661 | 665 | 668 | 648 | 667 | 675 | 671 | 665 |
| 15 |  | 668 | 669 | 669 | 669 | 668 | 667 | 666 | 665 | Etl | 641 | 611 | 652 | 660 | 661 | 660 | 665 | 662 | 663 | 663 | 668 | 675 | 676 | $6 E 5$ | 671 | 662 |
| 16 | 0 | 680 | 689 | 690 | 688 | 677 | 674 | 678 | 613 | 650 | 654 | 671 | 660 | 659 | 661 | 659 | 632 | 642 | 652 | 667 | 674 | 672 | 674 | 673 | 672 | 665 |
| 17 |  | 678 | 679 | 680 | 673 | 67 C | 670 | 669 | 669 | 668 | 661 | 653 | 656 | 669 | 668 | 669 | 669 | 668 | 662 | 662 | 669 | 672 | 671 | 671 | 672 | 668 |
| 18 |  | 671 | 671 | 670 | 669 | 668 | 668 | 667 | 667 | 667 | 665 | 663 | 664 | 663 | 663 | 663 | 664 | 665 | 666 | 666 | 669 | 664 | 662 | $6 C 2$ | 669 | 666 |
| 19 |  | 669 | 668 | 669 | 670 | 670 | 670 | 669 | 868 | 667 | 664 | 663 | 662 | 661 | 663 | 663 | 668 | 668 | 669 | 651 | 651 | 649 | 645 | 645 | 645 | 662 |
| 20 | 0 | 645 | 646 | 645 | 645 | 646 | 646 | 648 | 647 | 646 | 644 | 645 | 643 | 643 | 644 | 643 | 644 | 645 | 644 | 649 | 651 | 648 | 644 | 645 | 648 | 645 |
| 21 | Q | 651 | 652 | 656 | 656 | 654 | 652 | 649 | 647 | 646 | 646 | 645 | 645 | 644 | 644 | 645 | 646 | 646 | 645 | 648 | 646 | 645 | 646 | $64 t$ | 646 | 648 |
| 22 |  | 650 | 645 | 645 | 644 | 645 | 646 | 643 | 636 | 663 | 657 | 653 | 645 | 634 | 616 | 627 | 626 | 633 | 636 | 645 | 646 | 644 | 646 | 651 | 651 | 643 |
| 23 | 0 | 652 | 649 | 649 | 653 | 656 | 654 | 648 | 643 | 620 | 530 | 528 | 561 | 616 | 599 | 581 | 635 | 643 | 644 | 645 | 655 | 660 | 659 | 665 | 667 | 630 |
| 24 |  | 699 | 679 | 663 | 654 | 653 | 653 | 652 | 652 | 652 | 645 | 626 | 606 | 523 | 605 | 637 | 646 | 648 | 648 | 652 | 649 | 649 | 654 | 659 | 660 | 644 |
| 25 |  | 657 | 656 | 659 | 658 | 661 | 641 | 659 | 649 | 617 | 629 | 658 | 647 | 632 | 617 | 625 | 659 | 647 | 647 | 651 | 655 | 654 | 658 | 668 | 662 | 649 |
| 26 |  | 660 | 657 | 657 | 657 | 656 | 655 | 642 | 628 | 621 | 634 | 622 | 626 | 637 | 646 | 647 | 647 | 635 | 636 | 641 | 646 | 649 | 653 | 679 | 682 | 646 |
| 27 |  | 684 | 675 | 684 | 675 | 642 | 663 | 658 | 645 | 628 | 586 | 553 | 557 | 623 | 648 | 651 | 651 | 651 | 658 | 669 | 666 | 6S1 | 661 | 661 | 660 | 646 |
| 28 |  | 654 | 652 | 652 | 654 | 654 | 654 | 651 | 651 | 650 | 647 | 637 | 635 | 649 | 649 | 649 | 648 | 647 | 650 | 655 | 655 | 656 | 857 | 657 | 658 | 651 |
| 29 |  | 659 | 660 | 662 | 658 | 656 | 655 | 654 | 651 | 635 | 617 | 612 | 638 | 651 | 651 | 650 | 651 | 651 | 652 | 658 | 656 | 656 | 657 | 657 | 657 | 650 |
| 30 | 0 | 656 | 655 | 655 | 655 | 656 | 657 | 656 | 655 | 655 | 654 | 647 | 646 | 848 | 650 | 651 | 655 | 656 | 657 | 657 | 657 | 655 | 656 | $65 t$ | 655 | 654 |
| 31 | 0 | 652 | 652 | 653 | 653 | 654 | 654 | 652 | 651 | 6:0 | 648 | 629 | 629 | 641 | 648 | 650 | 650 | 651 | 656 | 657 | 650 | 654 | 657 | 657 | 656 | 650 |
| MEAN | A | 670 | 668 | 669 | 668 | 664 | 664 | 661 | 653 | 653 | 644 | 643 | 639 | 642 | 645 | 646 | 654 | 656 | 656 | 658 | 681 | 602 | 664 | 686 | 667 | 657 |
| MEAN | 0 | 655 | 655 | 656 | 656 | 656 | 656 | 654 | 651 | 652 | 652 | 646 | 646 | 648 | 649 | 650 | 651 | 652 | 653 | 655 | 654 | 654 | 654 | 654 | 655 | 653 |
| MEAN | D | 674 | 679 | 686 | 684 | 663 | 664 | 672 | 648 | 651 | 616 | 630 | 607 | 618 | 621 | 615 | 637 | 649 | 647 | 656 | E66 | 648 | 675 | $67 t$ | 675 | 653 |

HORI 2ONTAL INTENSITY-ALL DAYS

TABLE 37 MEANOOK
$H=12500$ PLUS TARULAR VALUES IN GAFNAS

| U.T. | JAN | FEB | MAR | APR | MAY | JUN | JUL | AUG | SEP | OC $T$ | NOV | CEC | YEAR | SUNMER | EQUINOX | WINTER |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0-1 | 729 | 735 | 743 | 760 | 804 | 763 | 759 | 762 | 777 | 752 | 755 | 762 | 758 | 772 | 758 | 746 |
| 1-2 | 734 | 746 | 749 | 769 | 795 | 775 | 764 | 765 | 777 | 754 | 759 | 765 | 763 | 775 | 762 | 751 |
| 2-3 | 735 | 743 | 759 | 755 | 785 | 779 | 762 | 770 | 769 | 755 | 759 | 766 | 762 | 774 | 760 | 751 |
| 3-4 | 736 | 740 | 749 | 747 | 770 | 779 | 761 | 770 | 766 | 757 | 760 | 767 | 758 | 770 | 755 | 751 |
| 4-5 | 737 | 741 | 751 | 750 | 765 | 761 | 763 | 762 | 766 | 759 | 762 | 766 | 757 | 763 | 757 | 752 |
| 5-6 | 737 | 738 | 739 | 737 | 742 | 759 | 755 | 757 | 769 | 757 | 755 | 764 | 751 | 753 | 750 | 748 |
| 6-7 | 732 | 727 | 716 | 714 | 711 | 754 | 751 | 754 | 757 | 747 | 751 | 764 | 740 | 743 | 733 | 743 |
| 7-8 | 724 | 716 | 699 | 700 | 705 | 746 | 716 | 749 | 739 | 733 | 741 | 761 | 727 | 729 | 718 | 735 |
| 8-9 | 716 | 701 | 676 | 694 | 697 | 725 | 731 | 741 | 711 | 722 | 728 | 759 | 717 | 723 | 701 | 726 |
| 9-10 | 704 | 690 | 639 | 707 | 664 | 739 | 746 | 741 | 703 | 713 | 715 | 753 | 709 | 722 | 691 | 715 |
| 10-11 | 702 | 682 | 669 | 692 | 676 | 744 | 749 | 734 | 712 | 707 | 737 | 751 | 713 | 726 | 695 | 718 |
| 11-12 | 700 | 690 | 694 | 695 | 683 | 740 | 754 | 731 | 688 | 720 | 746 | 751 | 716 | 727 | 699 | 722 |
| 12-13 | 701 | 689 | 697 | 694 | 673 | 728 | 757 | 743 | 717 | 722 | 741 | 756 | 718 | 725 | 707 | 722 |
| 13-14 | 712 | 696 | 722 | 701 | 697 | 732 | 761 | 748 | 722 | 741 | 748 | 757 | 728 | 735 | 721 | 728 |
| 14-15 | 726 | 710 | 723 | 718 | 696 | 744 | 762 | 750 | 718 | 742 | 745 | 759 | 733 | 738 | 725 | 735 |
| 15-16 | 732 | 706 | 724 | 720 | 711 | 745 | 755 | 747 | 723 | 741 | 747 | 762 | 734 | 739 | 727 | 737 |
| 16-17 | 725 | 699 | 717 | 712 | 713 | 735 | 744 | 731 | 722 | 736 | 746 | 760 | 728 | 731 | 722 | 732 |
| 17-18 | 717 | 702 | 702 | 699 | 718 | 723 | 733 | 718 | 713 | 732 | 738 | 751 | 720 | 723 | 712 | 727 |
| 18-19 | 709 | 690 | 697 | 696 | 720 | 720 | 724 | 713 | 716 | 724 | 730 | 747 | 716 | 719 | 709 | 719 |
| 19-20 | 706 | 684 | 699 | 701 | 725 | 724 | 724 | 719 | 723 | 726 | 730 | 745 | 717 | 723 | 712 | 716 |
| 20-21 | 711 | 703 | 707 | 710 | 732 | 732 | 730 | 729 | 738 | 732 | 734 | 744 | 725 | 730 | 721 | 723 |
| 21-22 | 716 | 709 | 719 | 726 | 744 | 743 | 739 | 737 | 749 | 737 | 740 | 747 | 734 | 741 | 733 | 728 |
| 22-23 | 718 | 710 | 736 | 735 | 771 | 754 | 750 | 749 | 764 | 742 | 746 | 752 | 744 | 756 | 744 | 731 |
| 23-24 | 724 | 722 | 744 | 747 | 793 | 760 | 756 | 760 | 777 | 747 | 750 | 759 | 753 | 767 | 754 | 739 |
| MEAN | 720 | 711 | 716 | 720 | 729 | 746 | 748 | 745 | 738 | 737 | 744 | 757 | 734 | 742 | 728 | 733 |

## DECLINATION-ALL DAYS

| U.T. | JAN | FEB | MAR | APR | MAY | JUN | JUL | AUG | SEP | OCT | NCV | DEC | YEAR | SUMMER | EQUINOX | WINTER |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0-1 | 12.5 | 11.0 | 8.7 | 5.0 | 5.1 | 5.5 | 8.5 | 8.4 | 8.9 | 8.8 | 8.2 | 8.9 | 8.3 | 6.9 | 7.9 | 10.1 |
| 1-2 | 13.3 | 11.3 | 9.0 | 5.5 | 5.9 | 6.7 | 9.4 | 8.7 | 9.1 | 9.7 | 8.9 | 9.6 | 8.9 | 7.7 | 8.3 | 10.8 |
| 2-3 | 13.7 | 12.1 | 8.0 | 7.5 | 6.0 | 8.4 | 9.2 | 9.6 | 8.9 | 10.4 | 9.7 | 10.5 | 9.5 | 8.3 | 8.7 | 11.5 |
| 3-4 | 13.9 | 13.6 | 9.2 | 9.0 | 7.3 | 8.3 | 8.9 | 9.9 | 11.1 | 10.9 | 10.0 | 10.9 | 10.2 | 8.6 | 10.0 | 12.1 |
| 4-5 | 14.3 | 12.7 | 10.5 | 9.3 | 9.1 | 9.2 | 9.1 | 9.6 | 10.2 | 10.3 | 10.5 | 10.9 | 10.5 | 9.3 | 10.1 | 12.1 |
| 5-6 | 14.1 | 13.5 | 11.8 | 7.9 | 10.3 | 9.5 | 9.5 | 10.8 | 10.5 | 10.7 | 10.2 | 11.6 | 10.9 | 10.0 | 10.2 | 12.4 |
| 6-7 | 13.3 | 14.5 | 12.0 | 9.2 | 10.3 | 10.2 | 9.1 | 10.0 | 8.9 | 10.5 | 12.0 | 10.8 | 10.9 | 9.9 | 10.1 | 12.7 |
| 7-8 | 12.6 | 13.2 | 14.4 | 11.0 | 11.1 | 9.6 | 9.4 | 10.7 | 8.4 | 10.6 | 11.2 | 10.7 | 11.1 | 10.2 | 11.1 | 11.9 |
| 8-9 | 14.3 | 13.7 | 16.8 | 12.3 | 13.9 | 10.6 | 11.4 | 11.1 | 9.3 | 12.8 | 10.4 | 9.5 | 12.2 | 11.7 | 12.8 | 12.0 |
| 9-10 | 14.3 | 16.4 | 17.8 | 13.6 | 16.4 | 11.0 | 11.2 | 11.6 | 13.5 | 13.1 | 9.3 | 9.8 | 13.2 | 12.5 | 14.5 | 12.4 |
| 10-11 | 15.6 | 17.0 | 19.1 | 15.0 | 15.9 | 10.7 | 11.1 | 11.5 | 14.5 | 14.0 | 9.7 | 9.8 | 13.7 | 12.3 | 15.7 | 13.0 |
| 11-12 | 16.4 | 17.9 | 16.8 | 15.7 | 16.9 | 12.5 | 13.0 | 13.6 | 15.3 | 14.4 | 10.5 | 10.7 | 14.5 | 14.0 | 15.5 | 13.9 |
| 12-13 | 16.6 | 17.8 | 16.8 | 17.2 | 18.5 | 15.8 | 15.5 | 16.1 | 16.4 | 13.2 | 11.6 | 11.4 | 15.6 | 16.5 | 15.9 | 14.3 |
| 13-14 | 16.0 | 17.2 | 16.4 | 18.6 | 20.4 | 19.4 | 18.5 | 18.7 | 17.6 | 12.9 | 11.2 | 11.7 | 16.5 | 19.2 | 16.4 | 14.0 |
| 14-15 | 16.5 | 17.7 | 18.3 | 20.0 | 22.8 | 21.4 | 20.4 | 20.5 | 18.9 | 13.2 | 12.1 | 11.9 | 17.8 | 21.3 | 17.6 | 14.5 |
| 15-16 | 16.8 | 18.4 | 20.0 | 20.9 | 22.9 | 22.6 | 21.6 | 21.1 | 18.3 | 14.3 | 12.9 | 13.0 | 18.6 | 22.1 | 18.4 | 15.3 |
| 16-17 | 16.9 | 19.1 | 20.3 | 20.9 | 21.5 | 21.9 | 21.4 | 19.8 | 16.5 | 14.6 | 13.4 | 13.7 | 18.3 | 21.1 | 18.1 | 15.8 |
| 17-18 | 15.4 | 18.5 | 18.8 | 19.0 | 18.8 | 18.7 | 18.9 | 16.2 | 13.9 | 13.4 | 13.0 | 12.6 | 16.4 | 18.1 | 16.3 | 14.9 |
| 18-19 | 14.3 | 17.5 | 16.0 | 14.5 | 14.1 | 13.1 | 14.1 | 11.2 | 9.4 | 10.8 | 9.6 | 11.0 | 13.0 | 13.1 | 12.7 | 13.1 |
| 19-20 | 12.9 | 13.9 | 14.1 | 11.3 | 10.9 | 8.8 | 8.9 | 6.7 | 7.3 | 8.3 | 7.9 | 10.0 | 10.1 | 8.8 | 10.2 | 11.2 |
| 20-21 | 12.1 | 12.2 | 12.4 | 8.7 | 8.7 | 5.9 | 5.7 | 4.8 | 6.0 | 7.2 | 7.2 | 8.6 | 8.3 | 6.3 | 8.6 | 10.0 |
| 21-22 | 11.7 | 11.1 | 11.1 | 7.0 | 7.1 | 4.1 | 4.3 | 4.7 | 6.2 | 6.9 | 6.7 | 7.9 | 7.4 | 5.1 | 7.8 | 9.4 |
| 22-23 | 11.8 | 10.6 | 9.2 | 5.9 | 5.7 | 4.2 | 4.5 | 5.8 | 7.3 | 7.6 | 7.2 | 7.9 | 7.3 | 5.1 | 7.5 | 9.4 |
| 23-24 | 12.1 | 10.6 | 8.4 | 5.4 | 5.1 | 4.7 | 6.0 | 7.2 | 9.1 | 8.5 | 7.7 | 8.2 | 7.8 | 5.8 | 7.8 | 9.7 |
| MEAN | 14.2 | 14.7 | 14.0 | 12.1 | 12.7 | 11.4 | 11.6 | 11.6 | 11.5 | 11.1 | 10.1 | 10.5 | 12.1 | 11.8 | 12.2 | 12.4 |

## MEAN VALUES OF MAGNETIC ELEMENTS

VERTICAL INTENSITY-ALL DAYS

TABLE 39 MEANDOK
$Z=58000$ PLUS TABULAR VALUES IN GAMMAS
1969

| U.T. | JAN | FEB | MAR | APR | MAY | JUN | JUL | AUG | SEP | CCT | NOV | DEC | YEAR | SUNMER | EQUINDX | WINTER |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0-1 | 677 | 676 | 673 | 703 | 696 | 688 | 672 | 674 | 676 | 691 | 676 | 670 | 681 | 682 | 686 | 675 |
| 1-2 | 678 | 677 | 680 | 704 | 693 | 692 | 677 | 676 | 676 | 692 | 675 | 668 | 682 | 684 | 688 | 675 |
| 2-3 | 675 | 678 | 677 | 698 | 676 | 695 | 672 | 679 | 674 | 693 | 674 | 669 | 680 | 681 | 686 | 674 |
| 3-4 | 673 | 677 | 681 | 690 | 674 | 686 | 676 | 676 | 679 | 694 | 675 | 668 | 679 | 678 | 686 | 673 |
| 4-5 | 675 | 678 | 682 | 688 | 679 | 678 | 673 | 668 | 682 | 691 | 676 | 664 | 678 | 674 | 686 | 673 |
| 5-6 | 673 | 677 | 671 | 663 | 661 | 670 | 666 | 661 | 669 | 684 | 670 | 664 | 669 | 665 | 672 | 671 |
| 6-7 | 668 | 663 | 665 | 656 | 659 | 667 | 662 | 657 | 654 | 675 | 658 | 661 | 662 | 661 | 663 | 663 |
| 7-8 | 656 | 653 | 649 | 650 | 654 | 653 | 644 | 645 | 650 | 659 | 647 | 653 | 651 | 649 | 652 | 652 |
| 8-9 | 651 | 642 | 651 | 650 | 632 | 636 | 641 | 634 | 663 | 663 | 638 | 653 | 646 | 636 | 657 | 646 |
| 9-10 | 639 | 637 | 634 | 641 | 618 | 640 | 640 | 625 | 650 | 661 | 631 | 644 | 638 | 631 | 646 | 638 |
| 10-11 | 638 | 637 | 648 | 636 | 616 | 642 | 643 | 619 | 647 | 655 | 632 | 643 | 638 | 630 | 646 | 638 |
| 11-12 | 636 | 649 | 651 | 635 | 630 | 643 | 649 | 624 | 647 | 652 | 646 | 639 | 642 | 636 | 646 | 642 |
| 12-13 | 632 | 651 | 637 | 627 | 634 | 638 | 653 | 634 | 648 | 648 | 643 | 642 | 640 | 640 | 640 | 642 |
| 13-14 | 638 | 642 | 646 | 639 | 630 | 640 | 653 | 640 | 643 | 654 | 649 | 645 | 643 | 641 | 646 | 643 |
| 14-15 | 644 | 649 | 651 | 643 | 643 | 644 | 652 | 645 | 645 | 660 | 655 | 646 | 648 | 646 | 650 | 648 |
| 15-16 | 653 | 653 | 655 | 652 | 647 | 650 | 652 | 651 | 646 | 671 | 659 | 654 | 654 | 650 | 656 | 655 |
| 16-17 | 656 | 657 | 659 | 660 | 657 | 652 | 651 | 655 | 659 | 678 | 663 | 656 | 658 | 654 | 664 | 658 |
| 17-18 | 659 | 662 | 660 | 664 | 663 | 652 | 650 | 654 | 664 | 684 | 663 | 656 | 661 | 655 | 668 | 660 |
| $18-19$ | 664 | 665 | 663 | 666 | 668 | 651 | 651 | 654 | 672 | 685 | 665 | 658 | 664 | 656 | 671 | 663 |
| 19-20 | 668 | 666 | 669 | 675 | 672 | 655 | 654 | 657 | 675 | 685 | 670 | 661 | 667 | 660 | 676 | 666 |
| 20-21 | 670 | 672 | 676 | 682 | 681 | 664 | 657 | 660 | 679 | 688 | 673 | 662 | 672 | 666 | 681 | 669 |
| 21-22 | 671 | 674 | 683 | 690 | 687 | 675 | 662 | 666 | 684 | 690 | 676 | 664 | 677 | 672 | 687 | 671 |
| 22-23 | 671 | 677 | 683 | 694 | 694 | 682 | 669 | 671 | 689 | 690 | 675 | 666 | 680 | 679 | 689 | 672 |
| 23-24 | 672 | 677 | 678 | 698 | 690 | 687 | 674 | 673 | 683 | 690 | 676 | 667 | 680 | 681 | 687 | 673 |
| MEAN | 660 | 662 | 663 | 667 | 661 | 662 | 658 | 654 | 665 | 676 | 661 | 657 | 662 | 659 | 668 | 660 |

## MEAN VALUES OF MAGNETIC ELEMENTS

HORIZONTAL INTENSITY-QUIET DAYS


## MEAN VALUES OF MAGNETIC ELEMENTS

## DECLINATION-QUIET DAYS

| U.T. | JAN | FEB | MAR | APR | MAY | JUN | JUL | AUG | SEP | CCT | NOV | CEC | YEAR | SUMMER | EQUINOX | WINTER |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0-1 | 12.8 | 11.9 | 10.5 | 7.3 | 6.9 | 7.1 | 7.5 | 8.9 | 9.3 | 8.8 | 8.2 | 8.8 | 9.0 | 7.6 | 9.0 | 10.4 |
| 1-2 | 13.1 | 11.7 | 10.9 | 9.1 | 7.9 | 8.4 | 8.3 | 10.2 | 9.6 | 9.5 | 8.6 | 9.0 | 9.7 | 8.7 | 9.8 | 10.6 |
| 2-3 | 13.7 | 12.2 | 11.0 | 10.9 | 8.8 | 9.9 | 9.0 | 10.6 | 9.4 | 9.9 | 9.4 | 9.8 | 10.4 | 9.6 | 10.3 | 11.3 |
| 3-4 | 13.8 | 12.7 | 11.2 | 10.1 | 9.1 | 10.2 | 9.2 | 9.5 | 9.4 | 10.0 | 9.6 | IC. 2 | 10.4 | 9.5 | 10.2 | 11.6 |
| 4-5 | 13.7 | 12.8 | 11.9 | 10.6 | 10.0 | 10.0 | 9.3 | 9.5 | 10.0 | 10.2 | 9.6 | 10.8 | 10.7 | 9.7 | 10.7 | 11.7 |
| 5-6 | 13.6 | 12.8 | 12.4 | 11.0 | 10.3 | 9.6 | 9.6 | 9.6 | 9.4 | 10.0 | 9.7 | 10.4 | 10.7 | 9.8 | 1 C .7 | 11.6 |
| 6-7 | 13.2 | 12.8 | 12.2 | 11.5 | 9.9 | 9.6 | 9.8 | 10.4 | 8.2 | 10.3 | 9.7 | 10.0 | 10.6 | 9.9 | 10.6 | 11.4 |
| 7-8 | 13.0 | 12.5 | 12.3 | 10.7 | 10.4 | 9.6 | 10.3 | 10.3 | 11.5 | 10.7 | 9.4 | 10.0 | 10.9 | 10.1 | 11.3 | 11.2 |
| 8-9 | 13.3 | 12.8 | 13.3 | 12.8 | 11.2 | 9.6 | 10.4 | 10.4 | 10.5 | 10.9 | 9.4 | 10.2 | 11.2 | 10.4 | 11.9 | 11.4 |
| 9-10 | 13.5 | 13.4 | 14.7 | 12.5 | 12.9 | 9.9 | 10.7 | 11.2 | 8.7 | 10.8 | 9.7 | 10.2 | 11.5 | 11.2 | 11.7 | 11.7 |
| 10-11 | 14.1 | 14.0 | 14.0 | 12.0 | 12.6 | 10.3 | 11.5 | 12.0 | 13.2 | 10.8 | 10.2 | 10.2 | 12.1 | 11.6 | 12.5 | 12.1 |
| 11-12 | 15.0 | 14.7 | 13.7 | 13.2 | 12.9 | 12.4 | 12.3 | 13.1 | 13.7 | 11.3 | 10.5 | 11.1 | 12.8 | 12.7 | 13.0 | 12.8 |
| 12-13 | 14.3 | 14.2 | 13.8 | 13.2 | 16.2 | 15.9 | 14.8 | 15.3 | 15.2 | 12.8 | 10.9 | 11.0 | 14.0 | 15.5 | 13.7 | 12.6 |
| 13-14 | 15.4 | 14.3 | 14.0 | 15.9 | 18.8 | 17.8 | 17.8 | 16.5 | 16.7 | 13.5 | 11.2 | 11.4 | 15.3 | 17.7 | 15.0 | 13.0 |
| 14-15 | 16.2 | 15.6 | 15.5 | 18.2 | 19.5 | 19.5 | 19.7 | 20.2 | 18.2 | 13.8 | 12.0 | 11.5 | 16.7 | 19.7 | 16.4 | 13.8 |
| 15-16 | 17.1 | 17.4 | 18.0 | 20.1 | 20.0 | 21.7 | 21.8 | 21.6 | 19.9 | 15.1 | 13.5 | 12.6 | 18.2 | 21.3 | 18.3 | 15.1 |
| 16-17 | 18.2 | 18.0 | 19.2 | 20.9 | 20.4 | 21.4 | 21.7 | 21.6 | 20.2 | 15.7 | 15.1 | 13.9 | 18.9 | 21.3 | 19.0 | 16.3 |
| 17-18 | 17.9 | 17.4 | 18.9 | 18.6 | 18.3 | 17.4 | 18.1 | 19.1 | 17.4 | 14.7 | 14.6 | 14.2 | 17.2 | 18.2 | 17.4 | 16.0 |
| 18-19 | 16.4 | 16.1 | 17.5 | 14.8 | 14.7 | 13.0 | 12.9 | 13.5 | 12.3 | 11.3 | 11.9 | 13.0 | 13.9 | 13.5 | 13.9 | 14.4 |
| 19-20 | 14.9 | 14.1 | 15.1 | 10.9 | 11.1 | 8.4 | 7.4 | 8.4 | 8.7 | 8.3 | 10.1 | 11.8 | 10.8 | 8.8 | 1 C .8 | 12.7 |
| 20-21 | 13.7 | 12.8 | 12.7 | 7.9 | 8.6 | 5.5 | 4.4 | 5.9 | 5.8 | 7.0 | 8.2 | 10.1 | 8.6 | 6.1 | 8.4 | 11.2 |
| 21-22 | 12.6 | 11.7 | 11.2 | 5.5 | 7.2 | 4.1 | 2.9 | 4.6 | 5.8 | 6.9 | 7.5 | 9.1 | 7.4 | 4.7 | 7.4 | 10.3 |
| 22-23 | 12.3 | 11.6 | 10.1 | 4.7 | 5.9 | 4.0 | 2.4 | 5.4 | 6.9 | 7.7 | 7.7 | 8.3 | 7.3 | 4.4 | 7.3 | 10.0 |
| 23-24 | 12.2 | 11.6 | 9.9 | 4.4 | 6.0 | 4.8 | 4.1 | 6.9 | 8.3 | B. 5 | 7.6 | 8.3 | 7.7 | 5.4 | 7.8 | 10.0 |
| MEAN | 14.3 | 13.7 | 13.5 | 12.0 | 12.1 | 11.2 | 11.1 | 11.9 | 11.6 | 10.8 | 10.2 | 1C. 7 | 11.9 | 11.6 | 12.0 | 12.2 |

## VERTICAL INTENSITY-QUIET DAYS

TABLE 42 MEANOOK
$Z=58000$ PLUS TABULAR VALUES IN GAMNAS

| U.T. | JAN | FEB | MAR | APR | MAY | JUN | JUL | AUG | SEP | OCT | NOV | OEC | YEAR | SUMMER | EQUINOX | WINTER |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0-1 | 667 | 663 | 673 | 685 | 684 | 674 | 663 | 667 | 667 | 675 | 667 | 655 | 670 | 672 | 675 | 663 |
| 1-2 | 665 | 663 | 668 | 682 | 682 | 671 | 665 | 664 | 664 | 673 | 666 | 655 | 668 | 671 | 672 | 662 |
| 2-3 | 665 | 663 | 667 | 675 | 680 | 668 | 662 | 662 | 666 | 672 | 666 | 656 | 667 | 668 | 670 | 662 |
| 3-4 | 664 | 663 | 670 | 669 | 678 | 666 | 660 | 661 | 667 | 672 | 666 | 656 | 666 | 666 | 670 | 662 |
| 4-5 | 663 | 663 | 670 | 668 | 676 | 663 | 659 | 661 | 669 | 673 | 665 | 656 | 665 | 665 | 670 | 662 |
| 5-6 | 663 | 664 | 671 | 670 | 674 | 662 | 659 | 661 | 667 | 673 | 663 | 656 | 665 | 664 | 670 | 662 |
| 6-7 | 663 | 663 | 671 | 671 | 669 | 661 | 656 | 660 | 673 | 664 | 663 | 654 | 664 | 662 | 670 | 661 |
| 7-8 | 662 | 661 | 668 | 647 | 664 | 661 | 653 | 657 | 657 | 667 | 660 | 651 | 659 | 659 | 659 | 659 |
| 8-9 | 663 | 661 | 659 | 659 | 642 | 657 | 653 | 655 | 651 | 662 | 660 | 652 | 656 | 652 | 658 | 659 |
| 9-10 | 662 | 660 | 650 | 657 | 629 | 657 | 652 | 656 | 641 | 669 | 660 | 652 | 654 | 649 | 654 | 659 |
| 10-11 | 659 | 660 | 661 | 651 | 644 | 656 | 653 | 654 | 654 | 666 | 661 | 646 | 655 | 652 | 658 | 657 |
| 11-12 | 656 | 659 | 662 | 648 | 643 | 658 | 656 | 655 | 655 | 666 | 661 | 646 | 655 | 653 | 657 | 655 |
| 12-13 | 657 | 658 | 663 | 656 | 656 | 663 | 654 | 655 | 660 | 665 | 661 | 648 | 658 | 657 | 661 | 656 |
| 13-14 | 656 | 656 | 663 | 650 | 658 | 662 | 655 | 653 | 662 | 667 | 661 | 649 | 658 | 657 | 660 | 655 |
| 14-15 | 660 | 658 | 665 | 653 | 660 | 660 | 656 | 654 | 663 | 669 | 662 | 650 | 659 | 658 | 683 | 658 |
| 15-16 | 661 | 660 | 665 | 660 | 658 | 657 | 656 | 654 | 664 | 672 | 663 | 651 | 660 | 656 | 665 | 659 |
| 16-17 | 662 | 662 | 665 | 662 | 657 | 653 | 652 | 655 | 662 | 673 | 665 | 652 | 660 | 654 | 665 | 660 |
| 17-18 | 664 | 663 | 664 | 659 | 654 | 647 | 650 | 655 | 662 | 675 | 664 | 653 | 659 | 652 | 665 | 661 |
| 18-19 | 665 | 665 | 661 | 657 | 654 | 643 | 649 | 653 | 663 | 672 | 665 | 655 | 658 | 650 | 663 | 663 |
| 19-20 | 667 | 666 | 665 | 659 | 651 | 644 | 649 | 653 | 663 | 671 | 665 | 654 | 659 | 649 | 665 | 663 |
| 20-21 | 667 | 664 | 666 | 665 | 655 | 653 | 651 | 656 | 664 | 672 | 664 | 654 | 661 | 654 | 667 | 662 |
| 21-22 | 666 | 664 | 671 | 668 | 662 | 659 | 652 | 659 | 667 | 673 | 664 | 654 | 663 | 658 | 670 | 662 |
| 22-23 | 666 | 666 | 671 | 676 | 669 | 662 | 656 | 661 | 670 | 675 | 664 | 654 | 666 | 662 | 673 | 662 |
| 23-24 | 665 | 663 | 668 | 681 | 677 | 669 | 659 | 662 | 670 | 675 | 664 | 655 | 667 | 667 | 673 | 662 |
| MEAN | 663 | 662 | 666 | 664 | 662 | 659 | 656 | 658 | 663 | 670 | 663 | 653 | 661 | 659 | 666 | 660 |

mean values of magnetic elements

HORIZONTAL INTENSITY-DISTLRBED DAYS


DECLINATION-DISTURBED DAYS

## TABLE 44 MEANOOK

$D=23.5$ DEGREES EAST PLUS TABULAR VALUES IN MINUTES

| U.T. | JAN | FEB | MAR | APR | MAY | JUN | JUL | AUG | SEP | OCT | NCV | DEC | YEAR | SUMMER | EQUINOX | WINTER |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0-1 | 12.2 | 10.5 | 6.6 | 3.9 | . 1 | 4.3 | 15.1 | 6.7 | 7.3 | 10.5 | 8.8 | 8.9 | 7.9 | 6.5 | 7.1 | 10.1 |
| 1-2 | 14.1 | 12.3 | 7.8 | 2.7 | -2.3 | 4.2 | 16.1 | 5.6 | 6.9 | 13.6 | 10.2 | 9.2 | 8.4 | 5.9 | 7.7 | 11.4 |
| 2-3 | 12.6 | 12.1 | $-1.3$ | 4.2 | -9.4 | 4.7 | 10.1 | 8.4 | 5.5 | 15.2 | 10.8 | 11.7 | 7.0 | 3.4 | 5.9 | 11.8 |
| 3-4 | 13.1 | 13.8 | .6 | 7.0 | -4.0 | 2.8 | 6.9 | 8.7 | 12.2 | 15.2 | 11.2 | 11.4 | 8.2 | 3.6 | 8.7 | 12.4 |
| 4-5 | 13.8 | 10.9 | 3.4 | 7.8 | -0.1 | 8.3 | 9.2 | 7.9 | 8.9 | 11.7 | 12.1 | 10.3 | 8.7 | 6.3 | 7.9 | 11.8 |
| 5-6 | 14.9 | 13.7 | 6.9 | -2.3 | 5.5 | 11.4 | 9.3 | 13.5 | 10.2 | 12.6 | 11.8 | 13.6 | 10.1 | 9.9 | 6.8 | 13.5 |
| 6-7 | 12.6 | 13.2 | 8.0 | 2.9 | 4.9 | 13.2 | 8.8 | 10.5 | 9.3 | 9.4 | 19.1 | 12.5 | 10.4 | 9.3 | 7.4 | 14.3 |
| 7-8 | 10.1 | 13.8 | 16.2 | 8.3 | 6.0 | 10.8 | 9.6 | 10.0 | 7.8 | 15.0 | 12.3 | 12.5 | 11.0 | 9.1 | 11.8 | 12.2 |
| 8-9 | 16.3 | 17.2 | 23.6 | 9.4 | 15.6 | 12.0 | 18.6 | 9.9 | -5.2 | 20.1 | 11.0 | 8.7 | 13.1 | 14.0 | 12.0 | 13.3 |
| 9-10 | 14.8 | 28.1 | 23.6 | 13.5 | 30.4 | 15.5 | 15.3 | 14.1 | 17.1 | 19.8 | 7.0 | 8.6 | 17.3 | 18.8 | 18.5 | 14.6 |
| 10-11 | 22.1 | 28.4 | 31.5 | 21.1 | 26.5 | 10.7 | 12.5 | 11.0 | 20.5 | 24.2 | 10.0 | 1C. 5 | 19.1 | 15.2 | 24.3 | 17.7 |
| 11-12 | 20.1 | 29.9 | 21.8 | 24.9 | 27.7 | 12.1 | 13.2 | 16.0 | 22.6 | 22.0 | 11.3 | 1C. 5 | 19.3 | 17.3 | 22.8 | 17.9 |
| 12-13 | 17.2 | 28.9 | 19.3 | 26.2 | 24.6 | 16.3 | 15.6 | 18.3 | 23.9 | 11.5 | 14.0 | 12.4 | 19.0 | 18.7 | 20.2 | 18.1 |
| 13-14 | 16.5 | 23.4 | 18.5 | 26.3 | 25.8 | 22.3 | 20.9 | 20.4 | 22.1 | 9.9 | 12.7 | 12.2 | 19.2 | 22.3 | 19.2 | 16.2 |
| 14-15 | 16.6 | 21.6 | 20.0 | 23.9 | 31.4 | 21.6 | 22.5 | 21.6 | 23.3 | 8.8 | 14.1 | 9.2 | 19.5 | 24.3 | 19.0 | 15.4 |
| 15-16 | 17.3 | 15.5 | 22.7 | 22.6 | 30.8 | 24.1 | 25.0 | 22.1 | 19.0 | 9.8 | 12.0 | 11.7 | 19.4 | 25.5 | 18.5 | 14.1 |
| 16-17 | 17.3 | 17.2 | 21.7 | 22.5 | 26.6 | 24.3 | 23.0 | 19.8 | 15.7 | 11.7 | 9.7 | 13.2 | 18.6 | 23.4 | 17.9 | 14.3 |
| 17-18 | 14.4 | 20.7 | 18.0 | 19.4 | 21.7 | 20.1 | 20.7 | 14.2 | 13.6 | 10.2 | 11.1 | 8.9 | 16.1 | 19.2 | 15.3 | 13.8 |
| 18-19 | 12.2 | 25.1 | 18.5 | 13.4 | 16.3 | 15.4 | 16.9 | 8.0 | 8.7 | 8.9 | 7.7 | 6.6 | 13.1 | 14.1 | 12.4 | 12.9 |
| 19-20 | 10.9 | 13.9 | 17.3 | 7.9 | 13.8 | 8.0 | 10.6 | 5.4 | 5.4 | 8.7 | 4.2 | 8.1 | 9.5 | 9.5 | 9.8 | 9.3 |
| 20-21 | 11.3 | 10.0 | 18.0 | 6.4 | 12.5 | 5.5 | 5.3 | 3.7 | 7.0 | 8.6 | 5.9 | 7.3 | 8.5 | 6.8 | 10.0 | 8.6 |
| 21-22 | 11.3 | 10.1 | 16.5 | 7.2 | 9.3 | 6.3 | 3.5 | 3.8 | 7.3 | 9.2 | 7.5 | 7.0 | 8.2 | 5.7 | 1 C .0 | 9.0 |
| 22-23 | 12.2 | 9.0 | 11.6 | 7.6 | 6.1 | 6.7 | 4.6 | 6.0 | 7.8 | 9.6 | 8.0 | 7.8 | 8.1 | 5.9 | 9.2 | 9.3 |
| 23-24 | 12.4 | 9.8 | 8.5 | 6.0 | 3.8 | 5.3 | 7.1 | 6.1 | 12.1 | 10.4 | 8.6 | 8.2 | 8.2 | 5.6 | 9.2 | 9.8 |
| MEAN | 14.4 | 17.0 | 15.0 | 12.2 | 13.5 | 11.9 | 13.3 | 11.3 | 12.0 | 12.8 | 10.5 | 10.1 | 12.8 | 12.5 | 13.0 | 13.0 |

## mean values of magnetic elements

VERTICAL INTENSITY-DISTUREED DAYS

TABLE 45 MEANOOK
$Z=58 C 00$ PLUS TABULAR VALUES IN GAMMAS
1969

| U.T. | JAN | FEB | MAR | APR | MAY | JUN | JUL | AUG | SEP | OCT | NCV | DEC | YEAR | SUMMER | EQUINOX | WINTER |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0-1 | 707 | 689 | 620 | 719 | 684 | 696 | 662 | 674 | 654 | 728 | 695 | 674 | 683 | 679 | 680 | 691 |
| 1-2 | 719 | 689 | 665 | 735 | 702 | 713 | 685 | 681 | 667 | 735 | 685 | 679 | 696 | 695 | 701 | 693 |
| 2-3 | 701 | 701 | 635 | 734 | 607 | 734 | 661 | 691 | 665 | 739 | 680 | 686 | 686 | 673 | 693 | 692 |
| 3-4 | 695 | 692 | 651 | 708 | 590 | 717 | 685 | 668 | 676 | 738 | 687 | 684 | 683 | 665 | 693 | 690 |
| 4-5 | 708 | 684 | 674 | 707 | 636 | 688 | 686 | 642 | 708 | 730 | 696 | 663 | 685 | 663 | 705 | 688 |
| 5-6 | 696 | 676 | 625 | 604 | 652 | 663 | 660 | 664 | 691 | 697 | 665 | 664 | 663 | 660 | 654 | 675 |
| 6-7 | 674 | 631 | 650 | 640 | 676 | 667 | 673 | 662 | 651 | 669 | 632 | 672 | 658 | 669 | 653 | 652 |
| 7-8 | 646 | 610 | 632 | 646 | 704 | 646 | 605 | 655 | 658 | 657 | 601 | 648 | 642 | 653 | 648 | 626 |
| 8-9 | 636 | 606 | 683 | 688 | 635 | 620 | 610 | 614 | 740 | 660 | 584 | 651 | 644 | 620 | 693 | 619 |
| 9-10 | 608 | 564 | 666 | 628 | 576 | 622 | 591 | 570 | 670 | 672 | 573 | 616 | 613 | 590 | 659 | 590 |
| 10-11 | 646 | 571 | 732 | 628 | 568 | 626 | 627 | 544 | 625 | 647 | 565 | 630 | 617 | 591 | 658 | 603 |
| 11-12 | 582 | 644 | 747 | 639 | 629 | 651 | 649 | 557 | 643 | 606 | 607 | 607 | 630 | 621 | 658 | 610 |
| 12-13 | 575 | 671 | 646 | 602 | 664 | 644 | 636 | 592 | 630 | 621 | 592 | 618 | 624 | 634 | 625 | 614 |
| 13-14 | 612 | 612 | 646 | 610 | 580 | 625 | 641 | 616 | 630 | 643 | 612 | 621 | 621 | 615 | 632 | 614 |
| 14-15 | 624 | 614 | 671 | 590 | 627 | 628 | 642 | 635 | 633 | 630 | 633 | 615 | 629 | 633 | 631 | 622 |
| 15-16 | 658 | 622 | 673 | 623 | 600 | 637 | 648 | 646 | 650 | 664 | 656 | 637 | 643 | 633 | 653 | 643 |
| 16-17 | 656 | 638 | 658 | 659 | 629 | 648 | 649 | 651 | 667 | 687 | 671 | 649 | 655 | 644 | 668 | 653 |
| 17-18 | 663 | 661 | 658 | 662 | 667 | 653 | 651 | 649 | 676 | 716 | 670 | 647 | 664 | 655 | 678 | 660 |
| 18-19 | 674 | 669 | 669 | 672 | 691 | 660 | 651 | 654 | 697 | 724 | 671 | 656 | 674 | 664 | 690 | 667 |
| 19-20 | 677 | 672 | 677 | 702 | 710 | 662 | 662 | 665 | 700 | 725 | 679 | 666 | 683 | 675 | 701 | 673 |
| 20-21 | 685 | 696 | 689 | 710 | 738 | 667 | 671 | 669 | 710 | 730 | 686 | 668 | 693 | 686 | 710 | 684 |
| 21-22 | 683 | 698 | 699 | 718 | 742 | 684 | 672 | 680 | 717 | 729 | 689 | 675 | 699 | 695 | 716 | 686 |
| 22-23 | 680 | 694 | 681 | 730 | 740 | 702 | 679 | 694 | 725 | 729 | 684 | 676 | 701 | 704 | 716 | 683 |
| 23-24 | 684 | 686 | 638 | 715 | 681 | 704 | 691 | 686 | 677 | 729 | 684 | 675 | 688 | 691 | 690 | 682 |
| MEAN | 662 | 654 | 666 | 670 | 655 | 665 | 654 | 644 | 673 | 692 | 650 | 653 | 661 | 655 | 675 | 655 |

THREE-HOUR RANGE INDICES, MEANOOK, 1969
Table 46

| Jonuary |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | D |  | H |  | Z |  | K |  |
| 1 | 1023 | 1210 | 2113 | 2211 | 2013 | 2110 | 2123 | 2211 |
| 2 | 0200 | 1100 | 0100 | 1200 | 0001 | 0110 | 0201 | 1210 |
| 3 | 0000 | 0100 | 0000 | 1100 | 0000 | 0000 | 0000 | 1100 |
| 4 | 0001 | 1000 | 0001 | 1111 | 0000 | 1000 | 0001 | 1111 |
| 5 | 0200 | 1000 | 0100 | 0000 | 0000 | 0000 | 0200 | 1000 |
| 6 | 0000 | 0110 | 0000 | 0101 | 0000 | 0000 | 0000 | 0101 |
| 7 | 0012 | 3132 | 0114 | 5222 | 0004 | 5001 | 0114 | 5232 |
| 8 | 1131 | 0110 | 1141 | 0111 | 0232 | 0000 | 1242 | 0111 |
| 9 | 1000 | 0010 | 2110 | 0110 | 0000 | 0000 | 2110 | 0110 |
| 10 | 0001 | 2110 | 0010 | 2100 | 0010 | 1000 | 0011 | 2110 |
| 11 | 0010 | 1110 | 0020 | 1111 | 0010 | 0100 | 0020 | 1111 |
| 12 | 1022 | 2210 | 0023 | 3201 | 0013 | 2220 | 1023 | 3211 |
| 13 | 0001 | 0100 | 0001 | 0101 | 0002 | 0000 | 0002 | 0101 |
| 14 | 1221 | 1122 | 1233 | 1112 | 1143 | 1012 | 1243 | 1122 |
| 15 | 2213 | 1122 | 2223 | 2232 | 0212 | 2121 | 2223 | 2232 |
| 16 | 0223 | 3211 | 1223 | 5302 | 0333 | 4200 | 1333 | 5312 |
| 17 | 2324 | 2221 | 3334 | 3333 | 3344 | 3222 | 3344 | 3333 |
| 8 | 1443 | 2211 | 2356 | 4222 | 2455 | 4211 | 2456 | 4222 |
| 19 | 2123 | 2111 | 2234 | 3212 | 2034 | 2011 | 2234 | 3212 |
| 20 | 1321 | 1221 | 2221 | 3231 | 1121 | 2221 | 2321 | 3231 |
| 21 | 1122 | 0100 | 2123 | 0111 | 1222 | 0000 | 2223 | 0111 |
| 22 | 0111 | 0010 | 0033 | 0101 | 0023 | 0000 | 0133 | 0111 |
| 23 | 0000 | 1110 | 0001 | 2111 | 0000 | 1000 | 0001 | 2111 |
| 24 | 0000 | 3221 | 1000 | 3323 | 0000 | 4332 | 1000 | 4333 |
| 25 | 2244 | 5322 | 3266 | 7533 | 3256 | 4332 | 3266 | 7533 |
| 26 | 3213 | 3221 | 4316 | 7312 | 4315 | 5311 | 4316 | 7322 |
| 27 | 0229 | 3211 | 2244 | 5312 | 2144 | 4211 | 2244 | 5312 |
| 28 | 2001 | 0110 | 1111 | 0111 | 1102 | 0000 | 2112 | 0111 |
| 29 | 0000 | 0110 | 1001 | 0102 | 0000 | 0000 | 1001 | 0112 |
| 30 | 0113 | 1110 | 1114 | 1110 | 0024 | 0000 | 1124 | 1110 |
| 31 | 0012 | 2211 | 0012 | 3211 | 0013 | 3211 | 0013 | 3211 |


| D |  | H |  | Z |  | $\begin{aligned} & \text { February } \\ & \text { K } \end{aligned}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0000 | 0110 | 0000 | 0111 | 0000 | 0000 | 0000 | 0111 |
| 0021 | 2463 | 0012 | 2475 | 0022 | 2353 | 0022 | 2475 |
| 4375 | 5432 | 5577 | 7544 | 4475 | 6433 | 5577 | 7544 |
| 2033 | 2322 | 3232 | 3312 | 2122 | 1102 | 3233 | 3322 |
| 2021 | 1111 | 2123 | 1111 | 2133 | 1000 | 2133 | 1111 |
| 1422 | 1111 | 2335 | 0122 | 2334 | 0001 | 2435 | 1122 |
| 1022 | 1121 | 1023 | 2122 | 1013 | 2111 | 1023 | 2122 |
| 2120 | 1211 | 2111 | 1211 | 1121 | 0000 | 2121 | 1211 |
| 0010 | 0110 | 0110 | 1111 | 0000 | 0000 | 0110 | 1111 |
| 1022 | 2113 | 1122 | 2223 | 0033 | 2103 | 1133 | 2223 |
| 3259 | 7633 | 7377 | 7754 | 5268 | 7733 | 7379 | 7754 |
| 2111 | 0121 | 3110 | 0112 | 1100 | 0002 | 3111 | 0122 |
| 1122 | 1112 | 2134 | 3312 | 1233 | 2212 | 223 | 3312 |
| 0101 | 1011 | 2112 | 2112 | 1113 | 3001 | 2113 | 3112 |
| 1322 | 2232 | 2234 | 2323 | 1223 | 1112 | 2334 | 2333 |
| 1231 | 1211 | 2253 | 3211 | 1243 | 3200 | 2253 | 3211 |
| 0111 | 0000 | 0011 | 0111 | 0000 | 0000 | 0111 | 0111 |
| 0000 | 0110 | 0000 | 0101 | 0000 | 0000 | 0000 | 0111 |
| 0101 | 3220 | 0111 | 3211 | 0121 | 4200 | 0121 | 4221 |
| 0101 | 1221 | 0101 | 2322 | 0211 | 2111 | 0211 | 2322 |
| 1031 | 1110 | 2120 | 1211 | 1020 | 0000 | 2131 | 1211 |
| 0011 | 1111 | 0010 | 1212 | 0011 | 1000 | 0011 | 1212 |
| 1232 | 2221 | 1122 | 3212 | 0233 | 3110 | 1233 | 3222 |
| 0111 | 1110 | 1132 | 1111 | 0033 | 0000 | 1133 | 1111 |
| 1011 | 1101 | 1012 | 1201 | 1011 | 1000 | 1012 | 1201 |
| 1232 | 2220 | 2233 | 2221 | 0353 | 1010 | 2353 | 2221 |
| 2230 | 3531 | 1141 | 5543 | 1231 | 4521 | 2241 | 5543 |
| 0241 | 1212 | 2352 | 1323 | 0342 | 1112 | 2352 | 1323 |


| March | D |  | H |  | Z |  | K |  | D |  | H |  | Z |  | April |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1 | 1000 | 2322 |  |  | 3111 | 2322 | 1010 | 0212 | 3111 | 2322 | 0223 | 2343 | 2235 | 4445 | 1234 | 4244 | 2235 | 4445 |
| 2 | 3302 | 2100 | 4303 | 4201 | 3303 | 3000 | 4303 | 4201 | 2102 | 2332 | 3113 | 3424 | 2102 | 2132 | 3113 | 3434 |
| 3 | 0000 | 0110 | 1000 | 0111 | 0000 | 0000 | 1000 | 0111 | 5220 | 2222 | 6322 | 2333 | 5331 | 2122 | 6332 | 2333 |
| 4 | 0000 | 1122 | 0000 | 0123 | 0000 | 0012 | 0000 | 1123 | 3333 | 3221 | 2353 | 4222 | 2343 | 3101 | 3353 | 4222 |
| 5 | 1003 | 2111 | 2114 | 4112 | 1004 | 3000 | 2114 | 4112 | 1152 | 1211 | 3143 | 1213 | 0091 | 0011 | 3153 | 1213 |
| 6 | 1123 | 1210 | 2124 | 1322 | 0034 | 2111 | 2134 | 2322 | 1230 | 2132 | 1130 | 2223 | 1231 | 1012 | 1231 | 2233 |
| 7 | 2221 | 2232 | 2322 | 4332 | 2323 | 4322 | 2323 | 4332 | 3452 | 2221 | 4563 | 4333 | 3542 | 3121 | 4563 | 4333 |
| 8 | 1322 | 2111 | 3324 | 3212 | 2323 | 3001 | 3324 | 3212 | 2101 | 1111 | 2202 | 1112 | 2213 | 1001 | 2213 | 1112 |
| 9 | 1223 | 2201 | 2123 | 3221 | 0133 | 3311 | 2233 | 3321 | 0233 | 3122 | 2344 | 3233 | 1244 | 2332 | 2344 | 3333 |
| 10 | 1122 | 0020 | 2123 | 0111 | 1123 | 0000 | 2123 | 0121 | 0132 | 1211 | 1243 | 2322 | 0143 | 2121 | 1248 | 2322 |
| 11 | 1133 | 4223 | 1134 | 5335 | 0234 | 4233 | 1134 | 5335 | 1142 | 2110 | 2253 | 4321 | 1143 | 4100 | 2253 | 4321 |
| 12 | 5665 | 1321 | 6877 | 3322 | 6665 | 3210 | 6877 | 3322 | 0012 | 2133 | 1100 | 1234 | 0011 | 0013 | 1112 | 2234 |
| 13 | 2021 | 1121 | 2121 | 1111 | 1102 | 1100 | 2122 | 1121 | 3343 | 3323 | 5444 | 4345 | 4343 | 4438 | 5444 | 4445 |
| 14 | 1101 | 2121 | 2101 | 1213 | 1102 | 0011 | 2102 | 2223 | 4111 | 2222 | 7223 | 4333 | 4113 | 3111 | 7223 | 4333 |
| 15 | 3464 | 2211 | 4474 | 3323 | 3455 | 2321 | 4475 | 3323 | 2354 | 3221 | 3355 | 5322 | 2243 | 3110 | 3355 | 5322 |
| 16 | 0356 | 2110 | 1567 | 2222 | 0556 | 2101 | 1567 | 2222 | 1253 | 3222 | 2375 | 5333 | 1363 | 3222 | 2375 | 5333 |
| 17 | 4433 | 5421 | 6545 | 7434 | 4534 | 5333 | 6545 | 7434 | 3264 | 3321 | 4365 | 3434 | 4964 | 4322 | 4365 | 4434 |
| 18 | 0233 | 2211 | 2345 | 1312 | 1244 | 1111 | 2345 | 1312 | 4441 | 2121 | 5452 | 3212 | 5552 | 2112 | 5552 | 3222 |
| 19 | 0032 | 2133 | 2042 | 1234 | 0032 | 0013 | 2042 | 2234 | 2000 | 2121 | 2100 | 2222 | 2000 | 1002 | 2100 | 2222 |
| 20 | 5143 | 1312 | 6345 | 2333 | 4354 | 0123 | 6355 | 2333 | 1020 | 2121 | 2211 | 1222 | 1010 | 0002 | 2221 | 2222 |
| 21 | 3252 | 2121 | 3253 | 2222 | 2253 | 2012 | 3253 | 2222 | 2000 | 1120 | 2010 | 0212 | 2010 | 0002 | 2010 | 1222 |
| 22 | 1332 | 2221 | 2333 | 3222 | 2333 | 3210 | 2333 | 3222 | 0023 | 1220 | 2233 | 3222 | 1033 | 3101 | 2233 | 3222 |
| 23 | 1001 | 2255 | 1011 | 2146 | 1001 | 1137 | 1011 | 2257 | 1120 | 2121 | 2111 | 2212 | 0020 | 2000 | 2121 | 2222 |
| 24 | 6577 | 5321 | 7677 | 6323 | 6667 | 4211 | 7677 | 6323 | 2320 | 1221 | 3311 | 1222 | 2410 | 0102 | 3421 | 1222 |
| 25 | 1154 | 3222 | 3266 | 5233 | 1155 | 4313 | 3266 | 5333 | 2121 | 2121 | 3232 | 1212 | 2131 | 1111 | 3232 | 2222 |
| 26 | 2032 | 2221 | 3123 | 3332 | 2023 | 2112 | 3133 | 3332 | 2010 | 2131 | 2110 | 1222 | 1001 | 0011 | 2110 | 2232 |
| 27 | 1120 | 1011 | 2211 | 0211 | 1021 | 1000 | 2221 | 1211 | 2223 | 1120 | 2214 | 2222 | 2124 | 2201 | 2224 | 2222 |
| 28 | 0110 | 1211 | 1110 | 1222 | 0000 | 0100 | 1110 | 1222 | 1675 | 5421 | 4796 | 7434 | 2785 | 6412 | 4796 | 7434 |
| 29 | 0032 | 2222 | 1034 | 3323 | 0033 | 2313 | 1034 | 3323 | 1111 | 2322 | 4231 | 3234 | 2110 | 1123 | 4231 | 3334 |
| 30 | 2212 | 2222 | 3123 | 1334 | 3223 | 0012 | 3223 | 2334 | 3544 | 3231 | 3765 | 5433 | 3745 | 3322 | 3765 | 5433 |
| 31 | 2811 | 2230 | 3232 | 2432 | 2132 | 2110 | 3232 | 2432 |  |  |  |  |  |  |  |  |


| May | D |  | H |  | Z |  | K |  | D |  | H |  | Z |  | June |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 1 | 2421 | 0110 | 3333 | 1212 | 2443 | 0010 | 3443 | 1212 | 2211 | 1110 | 3202 | 2222 | 2222 | 1010 | 3222 | 2222 |
| 2 | 1213 | 3352 | 2235 | 5343 | 1234 | 4233 | 2235 | 5353 | 0231 | 2111 | 1241 | 2222 | 0251 | 2002 | 1251 | 2222 |
| 3 | 0332 | 2111 | 2354 | 3223 | 0453 | 3211 | 2454 | 3223 | 1011 | 1211 | 2110 | 1112 | 1111 | 1012 | 2111 | 1212 |
| 4 | 0321 | 0120 | 2222 | 2212 | 1212 | 0111 | 2322 | 2222 | 1131 | 2100 | 2222 | 3212 | 1142 | 3111 | 2242 | 3212 |
| 5 | 1001 | 1211 | 3203 | 3222 | 3002 | 3112 | 3203 | 3222 | 1102 | 1210 | 2212 | 1111 | 2112 | 1110 | 2212 | 1211 |
| 6 | 1320 | 1100 | 2421 | 1112 | 2531 | 2001 | 2531 | 2112 | 0001 | 1210 | 1100 | 1122 | 0000 | 0111 | 1101 | 1222 |
| 7 | 1121 | 0000 | 2155 | 0001 | 1243 | 0000 | 2255 | 0001 | 1112 | 3210 | 2113 | 4212 | 1123 | 4202 | 2123 | 4212 |
| 8 | 0110 | 0201 | 1110 | 2212 | 1120 | 0102 | 1120 | 2212 | 1232 | 1321 | 1332 | 1333 | 1333 | 1123 | 1333 | 1333 |
| 9 | 0132 | 1122 | 1244 | 2123 | 0254 | 2102 | 1254 | 2123 | 2112 | 2142 | 3212 | 3344 | 2201 | 2242 | 3212 | 3344 |
| 10 | 1231 | 2110 | 3353 | 2212 | 2353 | 1100 | 3353 | 2212 | 1133 | 2210 | 4353 | 3322 | 2343 | 2100 | 4353 | 3322 |
| 11 | 1122 | 1110 | 1112 | 1121 | 0023 | 0010 | 1123 | 1121 | 1232 | 1131 | 2243 | 2223 | 1243 | 1002 | 2243 | 2233 |
| 12 | 0010 | 1122 | 1001 | 0133 | 0001 | 0113 | 1011 | 1133 | 3543 | 2231 | 5755 | 3222 | 4553 | 2211 | 5755 | 3232 |
| 13 | 3455 | 5423 | 5676 | 7436 | 3366 | 6524 | 5676 | 7536 | 1512 | 2232 | 3632 | 3323 | 2521 | 3323 | 3632 | 3333 |
| 14 | 5533 | 2245 | 6555 | 3357 | 5645 | 2345 | 6655 | 3357 | 2352 | 5322 | 4374 | 6324 | 2362 | 4213 | 4374 | 6324 |
| 15 | 8556 | 8644 | 5768 | 8766 | 8757 | 8645 | 8768 | 8766 | 1123 | 3221 | 3224 | 4232 | 2224 | 4221 | 3224 | 4232 |
| 16 | 5576 | 4010 | 6787 | 6223 | 5676 | 5002 | 6787 | 6223 | 1345 | 2222 | 3376 | 4323 | 2345 | 3313 | 3376 | 4323 |
| 17 | 1353 | 2111 | 3473 | 3124 | 3453 | 2103 | 3473 | 3124 | 4332 | 2220 | 5444 | 1332 | 4344 | 1211 | 5444 | 2332 |
| 18 | 3254 | 2331 | 5366 | 2333 | 4455 | 2112 | 5466 | 2333 | 1000 | 1101 | 2210 | 1211 | 1000 | 0110 | 2210 | 1211 |
| 19 | 2012 | 2220 | 3123 | 4323 | 2012 | 3111 | 3123 | 4323 | 0021 | 1111 | 1222 | 2223 | 0133 | 1111 | 1233 | 2223 |
| 20 | 2222 | 1110 | 3231 | 1222 | 1331 | 1112 | 3332 | 1222 | 3332 | 1111 | 3355 | 3222 | 2355 | 3111 | 3355 | 3222 |
| 21 | 1235 | 3111 | 2335 | 4423 | 2335 | 3312 | 2335 | 4423 | 0223 | 2120 | 2122 | 2212 | 1123 | 2010 | 2223 | 2222 |
| 22 | 1224 | 4120 | 2225 | 5322 | 1135 | 5210 | 2235 | 5322 | 0001 | 0110 | 0100 | 1211 | 0001 | 0000 | 0101 | 1211 |
| 23 | 0032 | 3221 | 3233 | 4221 | 1134 | 4110 | 3234 | 4221 | 0002 | 1210 | 1222 | 1212 | 0001 | 1122 | 1222 | 1222 |
| 24 | 0431 | 1221 | 2742 | 3323 | 1533 | 2212 | 2743 | 3323 | 3312 | 3221 | 3333 | 3212 | 2333 | 3112 | 3333 | 3222 |
| 25 | 2111 | 1110 | 5101 | 0222 | 4121 | 0011 | 5111 | 1222 | 0022 | 2221 | 2222 | 2333 | 1122 | 2122 | 2222 | 2333 |
| 26 | 0001 | 1110 | 1112 | 1111 | 1003 | 1001 | 1113 | 1111 | 2002 | 2210 | 3113 | 2212 | 2103 | 3301 | 3113 | 3312 |
| 27 | 0000 | 1110 | 1010 | 1112 | 0000 | 0001 | 1010 | 1112 | 1111 | 1000 | 2212 | 2112 | 2202 | 2002 | 2212 | 2112 |
| 28 | 0232 | 2201 | 2233 | 2212 | 0122 | 1100 | 2233 | 2212 | 0000 | 0010 | 2101 | 0012 | 1011 | 0010 | 2111 | 0012 |
| 29 | 0011 | 1121 | 1011 | 2123 | 0000 | 1012 | 1011 | 2123 | 0011 | 0110 | 2211 | 2322 | 0010 | 1111 | 2211 | 2322 |
| 30 | 0123 | 3311 | 2244 | 4313 | 1254 | 4201 | 2254 | 4313 | 0111 | 1210 | 1110 | 1222 | 0010 | 0111 | 1111 | 1222 |
| 31 | 1432 | 2121 | 3433 | 3123 | 1533 | 3111 | 3533 | 3123 |  |  |  |  |  |  |  |  |
| July | D |  | H |  | Z |  | K |  | D |  | H |  | Z |  | August$\mathbf{K}$ |  |
| 1 | 1152 | 3221 | 2273 | 3333 | 1163 | 3222 | 2273 | 3333 | 0011 | 0000 | 2112 | 1122 | 1001 | 1000 | 2112 | 1122 |
| 2 | 2221 | 0001 | 2231 | 1112 | 2332 | 0100 | 2332 | 1112 | 0012 | 1111 | 1001 | 2222 | 0000 | 0001 | 1012 | 2222 |
| 3 | 0001 | 0121 | 1101 | 1111 | 0100 | 1001 | 1101 | 1121 | 0322 | 3232 | 3213 | 2333 | 1102 | 1113 | 3323 | 3333 |
| 4 | 0000 | 1011 | 0100 | 0112 | 0000 | 0000 | 0100 | 1112 | 2323 | 1111 | 4424 | 2323 | 2424 | 2111 | 4424 | 2323 |
| 5 | 0001 | 1101 | 2101 | 2111 | 0001 | 1001 | 21012 | 2111 | 0312 | 2211 | 2434 | 4111 | 2433 | 4000 | 2434 | 4211 |
| 6 | 0001 | 1010 | 1101 | 1212 | 0000 | 0000 | 1101 | 1212 | 1211 | 0101 | 2101 | 0012 | 2210 | 0001 | 2211 | 0112 |
| 7 | 1001 | 1310 | 2201 | 2212 | 0112 | 1002 | 2212 | 2312 | 0321 | 1120 | 2221 | 2123 | 0120 | 0012 | 2321 | 2123 |
| 8 | 1001 | 1121 | 2200 | 1122 | 1100 | 0002 | 2201 | 1122 | 1033 | 2111 | 3125 | 2218 | 2034 | 4012 | 3135 | 4213 |
| 9 | 1121 | 1221 | 2231 | 1122 | 2231 | 1020 | 2231 | 1222 | 1231 | 2120 | 3321 | 2222 | 3331 | 2112 | 3331 | 2222 |
| 10 | 1112 | 1110 | 2213 | 2213 | 2213 | 1201 | 2213 | 2213 | 1234 | 2100 | 2155 | 1100 | 1254 | 2210 | 2255 | 2210 |
| 11 | 0021 | 1110 | 2110 | 1122 | 0111 | 0112 | 2121 | 1122 | 0001 | 1120 | 0111 | 2122 | 0000 | 0001 | 0111 | 2122 |
| 12 | 2231 | 1111 | 3353 | 1234 | 2353 | 1112 | 33531 | 1234 | 2443 | 3320 | 3456 | 5433 | 3456 | 4221 | 3456 | 5433 |
| 13 | 1433 | 2231 | 3654 | 2233 | 2655 | 1121 | 3655 | 2233 | 1133 | 1011 | 3343 | 0122 | 1155 | 1001 | 3355 | 1122 |
| 14 | 1322 | 2221 | 2433 | 4222 | 1434 | 3111 | 2434 | 4222 | 0133 | 2120 | 2154 | 3110 | 0144 | 3100 | 2154 | 3120 |
| 15 | 0022 | 2110 | 2122 | 3212 | 0132 | 2001 | 2132 | 3212 | 0021 | 2111 | 0020 | 1112 | 0020 | 0001 | 0021 | 2112 |
| 16 | 1213 | 2221 | 2115 | 1222 | 0215 | 2111 | 2215 | 2222 | 0002 | 1121 | 1012 | 1212 | 0002 | 1101 | 1012 | 1222 |
| 17 | 1211 | 1110 | 2211 | 1211 | 1111 | 0010 | 2211 | 1211 | 1331 | 1111 | 2231 | 0121 | 1210 | 0000 | 2331 | 1121 |
| 18 | 0012 | 0010 | 1012 | 2211 | 0003 | 1000 | 1013 | 2211 | 1001 | 1221 | 2112 | 3212 | 1101 | 2111 | 2112 | 3222 |
| 19 | 0111 | 0118 | 1121 | 0211 | 0022 | 0000 | 1122 | 0211 | 1333 | 2322 | 2334 | 2334 | 1233 | 2012 | 2334 | 2334 |
| 20 | 0100 | 1100 | 2111 | 1211 | 0000 | 0110 | 2111 | 1211 | 2231 | 1211 | 3462 | 3322 | 1142 | 1101 | 3462 | 3322 |
| 21 | 0000 | 1211 | 2010 | 2212 | 0000 | 1111 | 2010 | 2212 | 0311 | 2220 | 1200 | 2212 | 0100 | 0001 | 1311 | 2222 |
| 22 | 1121 | 1211 | 2221 | 1112 | 0121 | 0102 | 2221 | 1212 | 0101 | 2221 | 2100 | 1133 | 1001 | 0101 | 2101 | 2233 |
| 23 | 0001 | 0111 | 2112 | 0222 | 2001 | 1012 | 2112 | 0222 | 1223 | 3211 | 3324 | 2223 | 1212 | 2111 | 3324 | 3223 |
| 24 | 0010 | 0100 | 1120 | 1111 | 2010 | 0110 | 2120 | 1111 | 1212 | 2221 | 2202 | 2123 | 1001 | 1001 | 2212 | 2223 |
| 25 | 1220 | 0101 | 2220 | 1222 | 1220 | 0000 | 2220 | 1222 | 2110 | 1121 | 2100 | 1112 | 0011 | 0000 | 2110 | 1122 |
| 26 | 1213 | 3212 | 2203 | 4225 | 1211 | 4313 | 2213 | 4325 | 0024 | 3221 | 1116 | 3224 | 0014 | 2001 | 1126 | 3224 |
| 27 | 5563 | 2111 | 7584 | 4232 | 7573 | 3121 | 7584 | 4232 | 4534 | 2221 | 5745 | 3122 | 2533 | 1110 | 5745 | 3222 |
| 28 | 0031 | 0100 | 2252 | 1111 | 0042 | 0000 | 2252 | 1111 | 1311 | 1131 | 2311 | 2021 | 1311 | 1001 | 2311 | 2131 |
| 29 | 0010 | 0100 | 1110 | 0111 | 0000 | 0000 | 1110 | 0111 | 0001 | 2221 | 2000 | 1122 | 0000 | 0000 | 2001 | 2222 |
| 30 | 1000 | 1342 | 2111 | 2444 | 0000 | 1122 | 2111 | 2444 | 0031 | 2121 | 1121 | 1112 | 0110 | 0000 | 1131 | 2122 |
| 31 | 0001 | 1111 | 2211 | 1222 | 2111 | 1010 | 2211 | 1222 | 1131 | 2221 | 1031 | 1211 | 0021 | 0000 | 1131 | 2221 |

THREE-HOUR RANGE INDICES, MEANOOK, 1969

| September |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | D |  | H |  | 2 |  | K |  |
| 1 | 1011 | 2121 | 1110 | 1211 | 1011 | 0000 | 1111 | 2221 |
| 2 | 0111 | 1111 | 1011 | 1200 | 0000 | 0000 | 1111 | 1211 |
| 3 | 0001 | 0221 | 1100 | 0112 | 0000 | 0000 | 1101 | 0222 |
| 4 | 1100 | 1110 | 0100 | 0112 | 0000 | 0000 | 1100 | 1112 |
| 5 | 0000 | 1122 | 2000 | 1124 | 0000 | 0102 | 2000 | 1124 |
| 6 | 2433 | 2221 | 4557 | 2322 | 2444 | 0011 | 4557 | 2322 |
| 7 | 1033 | 2222 | 2144 | 3223 | 0033 | 1011 | 2144 | 3223 |
| 8 | 2565 | 2220 | 3576 | 2211 | 1453 | 1000 | 3576 | 2221 |
| 9 | 0142 | 2210 | 1242 | 3212 | 0031 | 1100 | 1242 | 3212 |
| 10 | 2200 | 1121 | 2210 | 2121 | 1000 | 0000 | 2210 | 2121 |
| 11 | 3232 | 1222 | 2233 | 2121 | 1122 | 1000 | 3233 | 2222 |
| 12 | 1313 | 1111 | 2212 | 1110 | 0211 | 0000 | 2313 | 1111 |
| 13 | 0012 | 1110 | 0012 | 0001 | 0001 | 1000 | 0012 | 1111 |
| 14 | 1112 | 1223 | 1112 | 0224 | 0001 | 0011 | 1112 | 1224 |
| 15 | 5353 | 3331 | 5353 | 4332 | 4231 | 2220 | 5353 | 4332 |
| 16 | 1321 | 1110 | 2231 | 2012 | 1121 | 0000 | 2331 | 2112 |
| 17 | 0003 | 3231 | 1004 | 3232 | 0003 | 2110 | 1004 | 3232 |
| 18 | 2232 | 3321 | 2323 | 3333 | 1121 | 2111 | 2333 | 3333 |
| 19 | 2412 | 1111 | 2313 | 2112 | 1212 | 0000 | 2413 | 2112 |
| 20 | 1112 | 2210 | 2154 | 2212 | 0032 | 1110 | 2154 | 2212 |
| 21 | 0121 | 0111 | 1121 | 1111 | 1231 | 1000 | 1121 | 1111 |
| 22 | 1131 | 0211 | 1021 | 0011 | 0020 | 0000 | 1131 | 0211 |
| 23 | 0010 | 1211 | 1001 | 2212 | 0000 | 1101 | 1011 | 2212 |
| 24 | 0222 | 1111 | 2212 | 0122 | 0111 | 0000 | 2222 | 1122 |
| 25 | 0231 | 1221 | 1231 | 1212 | 0120 | 0101 | 1231 | 1222 |
| 26 | 0032 | 1110 | 2013 | 0012 | 0012 | 0000 | 2033 | 1112 |
| 27 | 0000 | 1113 | 0000 | 1113 | 0000 | 0001 | 0000 | 1113 |
| 28 | 3226 | 5332 | $\$ 237$ | 7434 | 1115 | 4212 | $3 \times 37$ | 7434 |
| 29 | 1355 | 4444 | 2377 | 6635 | 1255 | 3414 | 2377 | 6645 |
| 30 | 6577 | 5332 | 7678 | 7343 | 5555 | 5111 | 7678 | 7343 |
| 31 |  |  |  |  |  |  |  |  |


| November |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | D |  | H |  | Z |  | K |
| 1 | 1022 | 1221 | 1112 | 2311 | 0022 | 1200 | 1122 | 2311 |
| 2 | 1122 | 1111 | 1112 | 2322 | 1133 | 1102 | 1133 | 2322 |
| 3 | 1432 | 2211 | 2355 | 2322 | 2344 | 1211 | 2455 | 2322 |
| 4 | 0122 | 1110 | 1223 | 1212 | 1224 | 1000 | 1224 | 1212 |
| 5 | 1100 | 1200 | 1111 | 2201 | 01.02 | 1100 | 1112 | 2201 |
| 6 | 0110 | 0011 | 1020 | 0112 | 0010 | 0000 | 1120 | 0112 |
| 7 | 2233 | 2211 | 2232 | 4222 | 0144 | 1111 | 2244 | 4222 |
| 8 | 0231 | 2332 | 1231 | 1333 | 1141 | 1222 | 1241 | 2333 |
| 9 | 1545 | 4532 | 2667 | 6682 | 2657 | 5621 | 2667 | 6632 |
| 10 | 1545 | 4530 | 2465 | 7442 | 0455 | 5432 | 2565 | 7542 |
| 11 | 1122 | 1210 | 2123 | 2322 | 1122 | 1211 | 2123 | 2322 |
| 12 | 2212 | 1200 | 2222 | 0211 | 1012 | 0000 | 2222 | 1211 |
| 13 | 0022 | 1200 | 1122 | 2211 | 1022 | 1101 | 1122 | 2211 |
| 14 | 0000 | 0000 | 1100 | 0001 | 1000 | 0000 | 1100 | 0001 |
| 15 | 0000 | 0010 | 0000 | 0111 | 0000 | 0000 | 0000 | 0111 |
| 16 | 0001 | 0121 | 0011 | 0111 | 0001 | 0000 | 0011 | 0111 |
| 17 | 0000 | 0111 | 1000 | 0211 | 0000 | 0000 | 1000 | 0211 |
| 18 | 0000 | 0110 | 1111 | 1211 | 0001 | 0111 | 1111 | 1211 |
| 19 | 0021 | 2111 | 0021 | 2222 | 0021 | 1001 | 0021 | 2222 |
| 20 | 1011 | 0000 | 2101 | 0001 | 1001 | 0000 | 2111 | 0001 |
| 21 | 0000 | 0100 | 0000 | 1100 | 0000 | 0000 | 0000 | 1100 |
| 22 | 0321 | 1121 | 3321 | 1121 | 0220 | 0001 | 3321 | 1121 |
| 23 | 0000 | 0110 | 1001 | 0312 | 0000 | 0001 | 1001 | 0312 |
| 24 | 0002 | 1210 | 1013 | 1211 | 0012 | 1001 | 1013 | 1211 |
| 25 | 0021 | 2211 | 1022 | 3211 | 0012 | 2111 | 1022 | 3211 |
| 26 | 3320 | 0320 | 2231 | 1332 | 1220 | 0220 | 3331 | 1332 |
| 27 | 0445 | 4331 | 1458 | 5422 | 0356 | 3312 | 1458 | 5422 |
| 28 | 1232 | 1121 | 2143 | 1212 | 1133 | 1001 | 2143 | 1222 |
| 29 | 1032 | 3221 | 2032 | 4333 | 1122 | 3233 | 2132 | 4333 |
| 30 | 4333 | 2321 | 3444 | 2321 | 4544 | 1221 | 4544 | 2321 |




[^0]:    $\dagger_{\text {Système international. }}$

[^1]:    $\dagger_{\text {e.g. }}$ Stratton, 1941, p. 18.

[^2]:    $\dagger$ In analogy to Maxwell's electrostatic and magnetic pairs, Treatise, Art. 621.

[^3]:    This notation has been suggested by G.V. Haines, Div. of Geomagnetism, Earth Fhysics Branch, EMR, Ottawa, Can.
    $\dagger_{\text {The Haines male-female rule. }}$

[^4]:    $\dagger_{A}$ consequence of using $P$ and $M$ is that $E$ and $H$ now represent the space-average fields.

[^5]:    $\dagger_{\text {For ferromagnetic materials }} H_{I}$ is not sufficient to explain the very strong spontaneous magnetization existing in the domains, The actual explanation is based on exchange integrals and belongs to quantum mechanics.

[^6]:    

[^7]:    $\dagger_{\text {Introduced by Maxwell. }}$

[^8]:    *Browne, I.M. and A.P. Crary. The movement of ice in the Arctic Ocean. In Arctic Sea Ice (ed. W.R. Thurston), N.R.C. Publ 598, 191-209, Nat. Acad. Sci, Washington, D.C.

[^9]:    *Requests for these charts (price $\$ 1.00$ each) may be made to: Hydrographic Chart Distribution Office, Canadian Hydrographic Service, 615 Booth Street, Ottawa, Canada.

[^10]:    *Sheridan, R.E., and C.L. Drake. 1968. Seaward extensions of the Canadian Appalechians. Can. J. Earth ScL, 5, 337-373.

[^11]:    *Published with the permission of the Deputy Minister, Department of Natural Resources, Quebec.
    **Considered by Cooke (1937) and Riordon (1954) as part of the Caldwell group or series and by St. Julien (1965) as part of the Caldwell group and part of the St. Daniel formation.

[^12]:    Mapped by Cooke (1937) as part of the Caldwell series and by Riordon (1954) as part of the Middle Ordovician Beauceville group (formation).

[^13]:    *All the chemical analyses of ultramafic rocks illustrated graphically in the present paper, including trace element data, have been adjusted for effects of serpentinization on the "constant composition" model by converting $\mathrm{Fe}_{2} \mathrm{O}_{3}$ to FeO (except for an arbitrary 0.5 per cent such as generally is found in unaltered ultramafic rocks) and normaliaing to 100 per cent without $\mathrm{H}_{2} \mathrm{O}$ and $\mathrm{CO}_{2}$. Most of the analyzed rocks are only partly serpentinized, and a comparison with the primary mineralogy shows good correlation between $\mathrm{Mg} /\left(\mathrm{Mg}+\mathrm{Fe}^{+2}\right)$ variations of the primary olivine and the adjusted analysea, and between original modal compositions as inferred partly from textures and calculated modes based on a "spinel peridotite norm" in which $\mathrm{Al}_{2} \mathrm{O}_{3}$ is assigned to chromite (with $\mathrm{Cr}_{2} \mathrm{O}_{3}$ ) and the pyroxenes.

[^14]:    *An alternative interpretation is that the clinopyroxene and the critical part of the $\mathrm{Al}_{2} \mathrm{O}_{3}$ content of the chromite were derived from Ca-Tschermaks "molecule" in solid solution in orthopyroxene by reaction with olivine:
    $\mathrm{CaAl}_{2} \mathrm{SiO}_{6}+\mathrm{Mg}_{2} \mathrm{SiO}_{4} \rightarrow \mathrm{CaMgSi}_{2} \mathrm{O}_{6}+\mathrm{MgAl}_{2} \mathrm{O}$, However, this is not supported by textural relationships in that the clinopyroxene and spinel appear quite independent of the orthopyroxene. Also, there is no clear correlation between either the amount of CaO or the composition of the spinel and the amount of orthopyroxene in the rocks.

    In the preferred interpretation, it is considered that the rock must initially have contained some chromite because its $\mathrm{Cr}_{2} \mathrm{O}_{3}$ content is generally more than four times the common solubility limit of $\mathrm{Cr}_{2} \mathrm{O}_{3}$ in basaltic magmas (Figure 6A) and therefore probably far exceeded the amount that could have been contained in the postulated interstitial liquid.

[^15]:    *For example, the discussion here assumes that the system was "closed". It is not unlikely, however, that there was some migration of the liquid while it was solidifying.

[^16]:    *Circumpacific magma compositions are represented by analyses from the North American Cordilleran and Aleutian arc compiled from a number of sources by Dr. T.N. Irvine. The original references are to be found in Irvine and Baragar (in press).

[^17]:    *Total Fe calculated as FeO
    Column 1. Estimated bulk composition of Dundonald sill after Naldrett and Mason (1968).
    2. Estimated composition of liquid portion of Dundonald sill magma at the time of intrusion (Naldrett and Mason, 1968).
    3. Estimated composition of Munro Lake sill apart from peridotite (after MacRae, 1969).
    4. High lime basic silicate liquid, recalculated to eliminate $\mathrm{H}_{2} \mathrm{O}$, aftor Drever and Johnston (1966), Table 1, analysis 5.
    5. Average composition of quench rocks from Dundonald township after Naldrett and Mason (1968).
    6. Composition of experimental charge from Preenall (1966).

[^18]:    *Total Fe calculated as FeO.

[^19]:    Note: $\Psi \mathrm{E}$, the angle between geographic and geomagnetic meridians at a station is measured eastward from the geographic meridian.

[^20]:    * 1113. MAG 5.0 TO 6.1

[^21]:    Absolute observations were made twice a week, on the average. Baseline values for the vertical intensity were computed from the readings of the proton precession magnetometer and the earth inductor by the formula $Z=F \sin I^{5}$

