## DEPARTMENT OF THE INTERIOR <br> CANADA

## PUBLICATIONS

OF THE

# Dominion Observatory 

OTTAWA<br>R. Meldrum Stewart, M.A., Director

Vol. VIII, No. 7

# Photometry with a 6-Inch Doublet 

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Fig. 1-Camera Hut


Fig. 4-Telescope and Cameras

## PHOTOMETRY WITH A 6-INCH DOUBLET

## PHOTOGRAPHIC EQUATORIAL

When the photographic telescope ${ }^{i}$ of the Dominion Observatory was mounted in a separate building (Fig. 1), the 6 -inch doublet then purchased was figured for stellar photometry by the extra-focal method of Parkhurst and Jordan. ${ }^{2}$ Both the 6 -inch and 8 -inch doublets give excellent negatives in stellar photography but the discs formed by the 8inch, when the plate is within or without the focus, are too uneven to permit of accurate measurements of their densities. The 6 -inch being figured with a view to extra-focal work gives fairly even dises when the plate is set at least 5 mm . outside the focus. If the plate is closer to the focus the discs are too uneven to measure, a light centre making it almost impossible to get accurate measurements. This is a very unfortunate condition as it means the out-of-focus images must be at least 1 mm . in diameter and this necessitates, for stars below the seventh magnitude, an exposure so long that the plates will be fogged by the city lights. In other words, the 6 -inch is not suitable for extra-focal photometry of the fainter stars. This difficulty was soon realized and the work embraced in this article was carried out, having in mind a focal method by which the fainter stars might be reached.


The 6 -inch doublet was thoroughly tested for spherical and chromatic aberration by the Hartmann ${ }^{3}$ method. Fig. 2 shows a maximum spherical aberration of slightly over 0.4 mm . and Fig. 3 gives the colour curve. The field of the doublet is reasonably flat,


Fig. 3-Colour Curve of 6-inch Doublet
good definition being obtainable on focal plates over a field of about $9^{\circ}$ diameter. For extra-focal work, however, the curvature of the field necessitates a correction which will

[^0]be dealt with in detail in a subsequent paragraph. This correction limits the available field to a radius of about $3^{\circ}$; adapters are therefore fitted in place of the 8 by 10 -inch plate holders and 4 by 5 -inch plates used. The 4 by 5 -inch plate holders can be moved 25 mm . in declination either way from the central position so that a series of exposures can be made on one plate.

The guiding telescope with a focal length of 52.5 inches and aperture of 4.5 inches is sufficiently powerful to permit of very accurate guiding, even for focal plates. This is, of course, very necessary as the instrument is used for direct photography of star fields and comets. There are also two 8 -inch objective prisms of $15^{\circ}$ and $25^{\circ}$ angles. These can be mounted, separately or together, on the 8 -inch doublet and are used for photographing spectra of comets and star fields. The combined prisms give a spectrum slightly over one-half inch between $H_{\beta}$ and $K$. The guiding telescope can be moved in declination, but not far enough to guide directly on the object whose spectrum is being photographed. The eye-piece can also be moved in any direction, linear and circular scales on the eye-end of the tube providing a check on any setting should it be necessary to repeat the observation at another date. This shifting of the eye-piece is especially useful in photographing comets with tails of a length greater than the radius of the plate. The telescope and mounting are shown in Fig. 4.

## PHOTOMETRIC METHOD

## Sensitometer Box

The sensitometer box (Fig. 5) is similar to those used in other observatories but perhaps a brief description might be given. There are twenty light brass tubes, each 75 mm . long and 10 mm . in diameter, set parallel in a brass box 129 mm . by 101 mm . by 80 mm . Over each end of the box is a thin brass plate pierced with circular holes opposite the centre of each tube. The holes in the back plate are 0.8 mm . diameter. Those in the front plate vary from 0.739 mm . to 4.360 mm . In each tube are two diaphragms to prevent reflection of light from the walls of the tubes, and the front and back plates and interior of each tube are coated with a dull black paint to further reduce reflection.

The sides of the box extend 3 mm . beyond the back plate, thus forming a holder for the photographic plate. A light-tight cover fits over the end of the box and inside this cover are two springs which press the photographic plate tightly against the back plate.

A metal framework (see Fig. 6) which can be rotated by an electric motor holds the sensitometer in such a position that the front end points toward the pole through an opening in a window of the dark room. A fixed frame in front of the box contains several sheets of opal glass which render the illumination of the front plate openings more uniform, and the rotation of the box during exposure eliminates, to a great extent, irregular illumination due to lack of uniformity in the thickness of the opal glass sheets.

The light passes through the openings in the front and back plates and strikes the photographic plate, producing thereon a circular image of the same size as the openings in the back plate. The relative densities of these images depend on the relative diameters of the openings in the front plate. These diameters were measured several times in two coorrdinates and the mean is given in the second column of Table I. The third column


Fra. 5-Sensitometer Box



Fig. 7-Microphotometer
gives $\log \mathrm{D}^{2}$, the logarithm of the relative area, hence the logarithm of the relative amount of light admitted by each hole. Column four gives the relative amount of light expressed in magnitudes. Column five is 4.00 minus column four, thus expressing the relative magnitudes of the images produced through the sensitometer openings in a form convenient for use in stellar work. The application of these relative magnitudes to the star images on the plates will be fully explained in a later paragraph.

TABLE I


Exposure and Development of Plates
Seed 30, Gilt Edge, plates have been used for all photometric work as they are fast and comparatively free from chemical fog. The holders are loaded in the dark (no red light) and wrapped in black cloth until the telescope is ready. The dome is kept dark during exposure, only a 2 c.p. lamp enclosed in a wooden tube being used. It was originally intended to expose each plate in the sensitometer box on the following day, just before developing, but for reasons which will be given later this practice was soon given up and only a certain number of plates of each emulsion exposed in the sensitometer box.

Hydrochinone developer has been used in all the work. The formula as given by Prof. Parkhurst follows:-

## A.

B.

Water.................... . . 64 oz. Water...................... . . 64 oz.
Sulphite of soda, dry.... 2 oz. Sulphite of Soda, dry.... 2 oz.
Hydrochinone.......... 2 $2 \frac{1}{2} \mathrm{oz}$. Potassium Carbonate..... 8 oz.
Sulphuric Acid c.p...... 2 drs. Potassium Bromide...... 200 grs.
Equal parts A and B.
A wooden tank 18 by 8 by 8 inches, lined with block tin, is used to control the temperature of the developer. In the winter this tank is filled with water and an electric heating element controlled by a contact thermometer, whose bulb is in the water, keeps the temperature of the water at $20^{\circ} \mathrm{C}$. In the summer the water from the tap runs around the tank, the flow being regulated according to the temperature of the room. The developer is put in an Eastman developing tank which is then put in the temperature bath and
the plates immersed as the timer is started. The developer is kept in 16 -oz. bottles which stand in one end of the temperature tank so that the developer is always at the required temperature. The time of development is eight minutes. The plates are then fixed for twenty minutes on edge in a hypo bath, to which has been added Velox liquid hardener. This has proved to be an excellent fixer both for clearness of plates and keeping properties of the fixer. There is some doubt as to the effect of developing from one to six plates in the same quantity of developer. Whether there would be any change in the form of the reduction curve has not been investigated.

## Measurement of Plates

The densities of the sensitometer images and the out-of-focus images of the stars are measured with a Hartmann microphotometer, shown in Fig. 7. This instrument is similar to that used by Prof. Parkhurst and fully described in Astrophysical Journal, Vol. 10, p. 321. A and B are microscope objectives through which the light shines from source P., two mirrors reflecting the light into these objectives. C is a Lummer-Brodhun cube, in the centre of which a small silvered portion reflects the light from $B$ to the eye-piece $F$, while the remaining surface of the cube $C$ permits the light from $A$ to pass directly to $F$. The photographic plate to be measured is placed on the table $K$ and adjusted by means of screws $L$ and $M$ until the star image is directly beneath $B$. In this way the intensity of the light through $B$ is controlled by the density of the star image. Now in the centre of the field of view of $F$ we have the light coming through the image whose density we wish to measure. Around this we have the light from $A$. To equalize the two parts of the field of view a photographic wedge $W$ is placed in front of A. This wedge can be moved across the field of $A$ by the knurled head $D$ until the light through $A$ just equals that through B. A millimetre scale to the right of A gives the position of the wedge for each setting.

The eye-piece G , together with the $45^{\circ}$ prism H , gives a clear view of the plate through the objective B , only a very small part in the centre of the field being obscured by the silver spot on C. By means of the plate carrier $K$, controlled by screws $L$ and $M$, one can quickly bring any part of the photographic plate within the field of the objective B . In this way it is very easy to set the silver spot on the desired star image. The lens E magnifies the scale on the wedge carrier, thus giving quick and accurate readings to one-tenth of a millimetre. $O$ and $R$ are mirrors for reflecting the light from the source $P$ to the scale. The source $P$ is a 40 -watt Mazda lamp, frosted. The light passes through ground glass before being reflected to objectives A and B .

The wedge $W$ was very kindly furnished by the late Professor E. C. Pickering. The plates used being Seed 30 and the wedge being made from Seed 23 , the difference in grain is very apparent when wedge and plate are in focus. This trouble was eliminated by adjusting objectives A and B so that the plate and wedge were both 2.0 mm . out of focus.

Three settings are made on each image and the mean taken as the scale reading. When the instrument was first adjusted an extra-focal plate of the Pleiades was measured several times and the mean of these measures is used to check up the instrument from time to time. In this way any change due to moving of the wedge or lamp, or defects in the mirrors, will be readily detected. Excellent agreement has always been obtained in repeating measures at irregular intervals.

Reduction of Measurements
The first step in the reduction of the scale readings of the microphotometer to relative star magnitudes is the construction of the so-called reduction curve. A plate which has been exposed in the sensitometer box before developing is placed in the instrument and the sensitometer images measured. These measures or scale readings are plotted against the relative magnitudes of the openings in the front plate of the sensitometer box, as given in the last column of Table I. A smooth curve through the plotted points gives the desired reduction curve. By means of this curve all wedge readings for star images may be converted to relative magnitudes.

It was at first intended to expose each plate in the sensitometer box and so have a separate reduction curve for each plate. This would require extra measuring but would provide for individual characteristics of all plates. However, even after much experimenting the sensitometer images often failed to give a satisfactory reduction curve. Lack of uniformity due to differences in the time of exposure in the sensitometer box was eliminated by cutting down the light so that the exposure was never less than one minute. The chief difficulty, however, was a sudden increase or decrease in density between successive rows of images, this change being lengthwise, crosswise or radial, The first produced a change in the slope of the curve for each row of images, the second gave a change in the height of the curve for each row while the last caused a bending of the curve for each row. A large percentage of the plates gave satisfactory curves but the number which gave useless curves was such as to lead to other methods. Moreover, a sudden change in the brightness of the sky while one was in the dark room often led to over or under exposure of the plate. Consequently it was decided to measure from eight to a dozen plates for each emulsion and take the mean curve. This was done for several emulsions and there has been such good agreement among the curves of the various emulsions that all measures to date have been re-examined and reduced by a curve formed from the means of the emulsions. Fig. 8 shows this curve. In view, however, of the experience of other observers regarding the change of the reduction curve with the change of emulsion a few trial curves are made for each emulsion. To date, however, the mean curve has been quite satisfactory.

## Correction for Sky Fog on Plates

So far the reduction curve referred to is one constructed from measures on plates whose film measures have never been more than $6 \cdot 0$ on the microphotometer scale. This film measure is a setting made on the plate close to the star image under measurement. Such settings are made beside every image measured to detect any irregularities or defects around the image and also to determine the amount of fog over the surface of the plate. Where these film readings are more than 6.0 a change is produced in the form of the reduction curve, the lower end of the curve being raised. Knowing this fog effect before drawing up the specifications of the sensitometer box, the openings were so planned as to group them about the bend of the reduction curve but in the drilling of the plate the drills available did not permit of this being done to the extent desired. The following procedure serves to give any change in the reduction curve due to sky fog. Two exposures, one about five times the other, are made of the same star field on the one plate. This


Fig. 8-Reduction Curve
gives dense images and faint images of the same stars and the difference between these dense and faint images, expressed in magnitudes, should be the same for each pair. The denser images fall on the straight part of the curve which is unaffected by sky fog. The lower part of the curve, on which the measures of the fainter images fall, is then adjusted until there is the same difference for all pairs. This gives the correct reduction curve for any particular film reading of the plate. When the sky fog is so dense as to give a film reading beyond 10.5 the effect on the reduction is such as to render it useless for accurate reductions. Consequently, all plates with film readings greater than 10.5 are discarded. Any exposure sufficiently long to give measurable images of the fainter stars fogs the plate well beyond film reading $10 \cdot 5$, so it will be readily seen that this method is not suitable for photometric work at this observatory.

## Correction for Curvature of Field of Camera

Since the focus of the centre of the field of the camera is longer than that of the outer parts of the field, the centre of the plate is not so far out of focus as are the surrounding parts. Consequently, the size of the star image increases according to its distance from the optical centre. This increase in the size of the image means that the image of a star will be more dense when it is in the centre of the plate than if it were out some distance. In order that we may have the relative magnitudes of the stars on the plate it is necessary to apply a correction dependent on the distance of the star from the centre of the field. This correction is determined in the following manner. The telescope is set so that Polaris or some other star near it is in the centre of the field, a star near the pole being chosen so that there will be no marked change in zenith distance during the exposure. After an exposure sufficient to give a good image the telescope is moved about 20 minutes in declination and another exposure made. This is repeated across the plate to a distance of about 3 degrees each way from the centre. Care must be taken to have the exposure times as nearly the same as possible, and also the sky must be uniformly clear during the entire series of exposures. The densities of the resulting images are measured and converted to relative magnitudes from the reduction curve.

These relative magnitudes are subtracted from the magnitude of the central image and the resulting differences plotted against the distances of the respective images from the centre. The curve thus formed (Fig. 9) gives the corrections necessary to reduce all measures to the centre of the plate. Table II gives these corrections in tabulated form. Any errors in the curve due to wrong exposure time or uneven sky are reduced to a minimum by taking the mean of a large number of plates.

## Atmospheric Absorption

As the effective field of the 6 -inch doublet as used in photometric work has a diameter of nearly 6 degrees the zenith distances of the stars on a plate differ. If the field being photographed is far south or far east or west of the meridian, this difference in zenith distance means a difference in the relative magnitudes due to a difference in the atmospheric absorption. The zenith distance of the centre of the plate at the middle of the exposure_and also the angle pole-star-zenith are measured directly from a globe and the differences in zenith distance, $\Delta Z$, between the centre star and the others are then read directly from the plate by a graphic method of Prof. Parkhurst's. Using the extinction


Fig. 9-Correction Curve for Distance from Centre of Plate
curve of $\mathrm{Wirtz}^{1}$ the change in magnitude, $\Delta M$, due to the difference in zenith distance, $\Delta Z$, is determined. Table III gives the quantity, $\frac{\Delta M}{\Delta Z}$ for various zenith distances as derived from the Wirtz curve. This quantity multiplied by $\Delta Z$ gives the required $\Delta M$.

TABLE II
CORRECTIONS FOR DISTANGE FROM CENTRE OF FIELD

| $\begin{gathered} \rho \\ \text { Distance } \\ \text { from } \\ \text { centre } \end{gathered}$ | Correction* | $\rho$ Distance from centre | Correction* | $\rho$ <br> Distance from centre | Correction* | $\rho$ <br> Distance from centre | Correction* |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| - | $M$ | 0 | $M$ | - | M | 0 | M |
| 0.1 | 0.00 | 0.9 | 0.03 | 1.7 | $0 \cdot 09$ | $2 \cdot 5$ | 0.18 |
| $0 \cdot 2$ | 0.00 | $1 \cdot 0$ | 0.03 | $1 \cdot 8$ | $0 \cdot 10$ | $2 \cdot 6$ | 0-19 |
| $0 \cdot 3$ | 0.00 | $1 \cdot 1$ | 0.04 | 1.9 | 0.11 | $2 \cdot 7$ | 0.20 |
| 0.4 | $0 \cdot 01$ | $1 \cdot 2$ | 0.05 | $2 \cdot 0$ | $0 \cdot 12$ | $2 \cdot 8$ | $0 \cdot 22$ |
| $0 \cdot 5$ | 0.01 | 1.3 | 0.06 | $2 \cdot 1$ | 0.13 | $2 \cdot 9$ | 0.23 |
| 0.6 | 0.01 | $1 \cdot 4$ | 0.06 | $2 \cdot 2$ | $0 \cdot 14$ | $3 \cdot 0$ | 0.24 |
| 0.7 | $0 \cdot 02$ | 1.5 | 0.07 | $2 \cdot 3$ | 0.15 | $3 \cdot 1$ | $0 \cdot 26$ |
| $0 \cdot 8$ | $0 \cdot 02$ | 1.6 | 0.08 | $2 \cdot 4$ | $0 \cdot 17$ | $3 \cdot 2$ | $0 \cdot 27$ |

*This correction is necessarily negative as the distance out of focus increases with distance from centre; hence the images are larger and less dense, and the star would appear to be fainter than it really is. To correct for this apparent faintness we must increase its magnitude, that is, apply a negative correction.
${ }^{1}$ A. N., Vol. 154, p. 349, 1900.

TABLE III

| Zenith distance | $\frac{\Delta M}{\Delta Z}$ | Zenith distance | $\frac{\Delta M}{\Delta Z}$ | Zenith distance | $\frac{\Delta M}{\Delta Z}$ | Zenith distance | $\frac{\Delta M}{\Delta Z}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| - | M | - | M | - | M | - | M |
| 10 | 0.001 | 37 | 0.007 | 50 | 0.013 | 58 | $0 \cdot 020$ |
| 15 | 0.002 | 40 | 0.008 | 51 | 0.014 | 59 | 0.021 |
| 20 | 0.002 | 42 | 0.009 | 52 | 0.015 | 60 | 0.023 |
| 25 | 0.003 | 44 | 0.010 | 53 | 0.016 | 61 | 0.025 |
| 30 | 0.005 | 46 | 0.010 | 54 | 0.017 | 62 | 0.028 |
| 34 | 0.006 | 47 | 0.011 | 55 | 0.018 | 63 | 0.030 |
| 35 | 0.006 | 48 | 0.011 | 56 | 0.019 | 64 | 0.032 |
| 36 | 0.007 | 49 | 0.012 | 57 | 0.019 | 65 | 0.035 |

The following sample reduction of some stars on plate No. 517, as given in Table IV, will make clear the method of measurement and reduction of the star images.

TABLE IV
Plate 517 (part)
H.A. $=2^{\text {h. }} \cdot 8 \mathrm{~W} ; z=36^{\circ} \cdot 5 ; q=128^{\circ} \cdot 5 ; \frac{\Delta M}{\Delta Z}=.007$

| Star | Scale <br> Reading | Rel. Mag. | $\rho$ | $\Delta Z$ | Corrn. for $\rho$ | $\Delta M$ | Corr'd. <br> Rel. <br> Mag. | Park. Mag. -Corr'd. Rel. Mag. | Final Mag. | Observed Mag. -Park. Mag. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| B.D. |  |  |  |  |  |  |  |  |  |  |
| $77^{\circ} 641$ | $46 \cdot 8$ | $1 \cdot 19$ | 0.5 | $\pm 0 \cdot 1$ | -. 01 | . 00 | $1 \cdot 18$ | $5 \cdot 42$ | $6 \cdot 53$ | -. 02 |
| $77 \quad 634$ | 54.9 | $0 \cdot 86$ | $1 \cdot 1$ | $-0.3$ | -. 04 | . 00 | 0.82 | $5 \cdot 54$ | $6 \cdot 22$ | -. 14 |
| 78562 | $25 \cdot 1$ | $2 \cdot 09$ | 1.3 | -0.8 | -. 06 | -. 01 | $2 \cdot 02$ | $5 \cdot 47$ | $7 \cdot 42$ | $-.07$ |
| $77 \quad 627$ | $25 \cdot 1$ | $2 \cdot 09$ | 1.7 | -0.9 | -. 09 | -. 01 | 1.99 | $5 \cdot 44$ | $7 \cdot 39$ | -. 04 |
| 79511 | $21 \cdot 6$ | $2 \cdot 30$ | 1.4 | -1.3 | -. 06 | -. 01 | $2 \cdot 23$ | $5 \cdot 27$ | $7 \cdot 63$ | $+.13$ |
| 80 | $20 \cdot 8$ | $2 \cdot 36$ | $2 \cdot 2$ | $-1.9$ | -. 14 | -. 01 | $2 \cdot 21$ | $5 \cdot 32$ | $7 \cdot 61$ | +.08 |
| $79 \quad 540$ | $25 \cdot 7$ | 2.06 | 1.5 | $0 \cdot 0$ | -. 07 | . 00 | 1.99 | $5 \cdot 36$ | 7-39 | +.04 |

[^1]While the most outstanding sources of error have doubtless been taken care of by the methods described there are still possible sources of minor errors. The variation in the thickness of the glass in the photographic plate must produce errors which are classed as accidental along with all other irregularities of the film not revealed by the film readings. The sky fog is taken care of up to a certain density beyond which it is well to discard the plate. Also much greater accuracy is assured by discarding all measures of star images below 20 and above 55 as the reduction curve is much more uncertain beyond these points and there is a lack of agreement between successive settings of the wedge.

## TABLE OF EXPOSURES

TABLE V

|  | Date |  |  |  |  | Julian Day | Exposure |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1917- <br> April | d21 | h <br> 15 | m | s <br> 55 |  | h m |  |
| 267 |  |  |  |  |  | 2421340-6617 | 0 |  |
| 268. |  |  | 16 | 17 | 55 | $340 \cdot 6791$ |  | 10 |
| 269. |  |  | 17 | 18 | 55 | $340 \cdot 7215$ |  | 10 |
| 270. |  |  | 17 | 46 | 55 | $340 \cdot 7409$ |  |  |
| 276. | $\begin{gathered} \text { May } \\ 1919-2 \end{gathered}$ | 14 | 15 | 51 | 56 | 363-6610 | $0 \quad 10$ |  |
|  |  |  |  |  |  |  |  |  |
| 517. | July | 24 | 16 | $47 \quad 00$ |  | 2422164-6993 | 015 |  |
| 518. | Sept. |  | 17 | 1600 |  | 164.7194 | 015 |  |
| 530. |  | 26 | 14 | 01 | 30 | $228 \cdot 5844$ | 0 |  |
| 536. | Oct. <br> 1920 | 29 | 15 | 2130 |  | 261 -6399 | $0 \quad 15$ |  |
|  |  |  |  | $1920-$ |  |  |  |  |
| 539. | May | 10 | 14 | 50 | 00 | $455 \cdot 6181$ | 0 | 15 |
| 540. |  |  | 16 | 03 | 00 | $455 \cdot 6687$ | 0 | 15 |
| 541. |  |  | 16 | 33 | 00 | $455 \cdot 6896$ | 0 | 15 |
| 542. | June | 7 | 15 | 00 | 00 | $483 \cdot 6250$ | 0 |  |
| 543. |  |  | 15 | 56 | 35 | $483 \cdot 6642$ | 0 |  |
| 544. |  |  | 16 | 26 | 30 | $483 \cdot 6851$ | 0 | 15 |
| 545. | June | 11 | 15 | 52 | 00 | $487 \cdot 6611$ | 0 | 8 |
| 546. |  |  | 16 | 12 | 30 | $487 \cdot 6753$ | 0 | 15 |
| 547. | June | 13 | 15 | 50 | 30 | $489 \cdot 6601$ | 0 | 15 |
| 548. |  |  | 16 | 16 | 00 | $489 \cdot 6778$ | 0 | 8 |
|  | 1921- |  |  |  |  |  |  |  |
| 585. | Mar. | 3 | 17 | 32 | 00 | $752 \cdot 7306$ | 0 |  |
| 586. |  |  | 18 | 17 | 33 | 752-7622 | 0 |  |
| 587. | April | 1 | 17 | 16 | 00 | 781-7194 |  |  |
| 588. |  |  | 17 | 59 | 00 | $781 \cdot 7493$ | 0 |  |
| 589. | April | 5 | 17 | 25 | 30 | $785 \cdot 7260$ |  |  |
| 590. |  |  |  | 56 | 00 | 785.7472 |  |  |
| 591. |  |  |  |  | 00 | - 785.7799 | 1 | 00 |

## CATALOGUE OF RESULTS

| Star B.D. |  | Plate | Position, 1900 |  | Spec. | Magnitude |  | P.E. | O-P |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | R.A. | Dec. |  |  |  |  |  |
| - |  |  |  | h m | - |  |  |  |  |  |
| 77 | 27 | 536 | $00 \quad 43 \cdot 6$ | $77 \quad 25$ | $\mathrm{A}_{6}$ |  | $7 \cdot 10$ |  | $+20$ |
| 85 | 19 | 589 | $00 \quad 55 \cdot 0$ | 8543 | $\mathrm{K}_{0}$ | $5 \cdot 55$ |  |  |  |
|  |  | 590 |  |  |  | $5 \cdot 54$ | 5•54 | . 00 | $+.07$ |
| 88 | 4 | 587 | $00 \quad 55 \cdot 6$ | 8830 | $\mathrm{A}_{2}$ | $6 \cdot 32$ |  |  |  |
|  |  | 588 |  |  |  | $6 \cdot 34$ |  |  |  |
|  |  | 589 |  |  |  | $6 \cdot 36$ |  |  |  |
|  |  | 590 |  |  |  | $6 \cdot 37$ | 6-35 | . 01 | -. 08 |
| 73 | 51 | 536 | $\begin{array}{ll}00 & 57.6\end{array}$ | $\begin{array}{ll}73 & 50\end{array}$ | $\mathrm{A}_{0}$ |  | $6 \cdot 87$ |  | +.12 |
|  | 17 | 589 | $00 \quad 59 \cdot 1$ | $86 \quad 37$ | $\mathrm{K}_{0}$ | $7 \cdot 31$ |  |  |  |
|  |  | 590 |  |  |  | $7 \cdot 28$ |  |  |  |
|  |  | 591 |  |  |  | $7 \cdot 27$ | $7 \cdot 29$ | . 01 | -. 06 |
| 76 | 40 | 536 | $01 \quad 12 \cdot 0$ | 7702 | $\mathrm{G}_{5}$ |  | $7 \cdot 24$ |  | +.01 |
| 75 | 58 | 536 | $\begin{array}{lll}01 & 13.8\end{array}$ | $76 \quad 11$ | $\mathrm{K}_{0}$ |  | 7.99 |  | $+\cdot 10$ |
| 73 | 66 | 536 | $\begin{array}{lll}01 & 13.8\end{array}$ | 74 | $\mathrm{A}_{2}$ |  | $7 \cdot 26$ |  | $-.03$ |
| 75 | 59 | 536 | $\begin{array}{lll}01 & 13.8\end{array}$ | $75 \quad 43$ | $\mathrm{A}_{3}$ |  | $6 \cdot 68$ |  | +.06 |
| 77 | 49 | 536 | $\begin{array}{lll}01 & 15 \cdot 0\end{array}$ | $78 \quad 12$ | $\mathrm{A}_{2}$ |  | $6 \cdot 45$ |  | +.14 |
| 73 | 75 | 536 | $01 \quad 21.0$ | 7341 | $\mathrm{G}_{5}$ |  | $7 \cdot 58$ |  | $-.16$ |
| 73 | 81 | 536 | $\begin{array}{ll}01 & 29.2\end{array}$ | $\begin{array}{ll}73 & 47\end{array}$ | $\mathrm{B}_{8}$ |  | 6.46 |  | $-.07$ |
| 77 | 58 | 536 | $\begin{array}{ll}01 & 31.6\end{array}$ | $77 \quad 28$ | $\mathrm{B}_{9}$ |  | $6 \cdot 58$ |  | -. 06 |
| 75 | 72 | 536 | $\begin{array}{ll}01 & 36 \cdot 0\end{array}$ | $\begin{array}{ll}75 & 22\end{array}$ | $\mathrm{F}_{0}$ |  | $7 \cdot 24$ |  | -. 13 |
| 74 | 84 | 536 | $\begin{array}{lll}01 & 42 \cdot 7\end{array}$ | 7506 | $\mathrm{F}_{5}$ |  | $7 \cdot 13$ |  | -. 12 |
| 75 | 76 | 536 | $01 \quad 46 \cdot 2$ | $\begin{array}{ll}75 & 44\end{array}$ | $\mathrm{A}_{5}$ |  | 7-10 |  | -. 10 |
| 74 | 87 | 536 | $\begin{array}{lll}01 & 48.7\end{array}$ | $\begin{array}{ll}74 & 50\end{array}$ | $\mathrm{G}_{6}$ |  | $7 \cdot 51$ |  | -. 01 |
| 86 | 51 | 589 | $\begin{array}{ll}03 & 33 \cdot 9\end{array}$ | $86 \quad 20$ | $\mathrm{F}_{5}$ | $6 \cdot 22$ |  |  |  |
|  |  | 590 |  |  |  | $6 \cdot 12$ | $6 \cdot 17$ | . 03 | $+.04$ |
|  | 13 | 587 | $07 \quad 58.0$ | $88 \quad 56$ | $\mathrm{A}_{3}$ | $7 \cdot 19$ |  |  |  |
|  |  | 588 |  |  |  | $7 \cdot 08$ |  |  |  |
|  |  | 589 |  |  |  | $7 \cdot 15$ |  |  |  |
|  |  | 590 |  |  |  | $7 \cdot 15$ |  |  |  |
|  |  | 591 |  |  |  | $7 \cdot 19$ | $7 \cdot 15$ | . 01 | $+\cdot 03$ |
|  | 328 | 267 | $10 \quad 05 \cdot 8$ | $79 \quad 27$ | $\mathrm{A}_{0}$ | 6.87 |  |  |  |
|  |  | 539 |  |  |  | 6.88 | $6 \cdot 87$ | . 00 | -. 08 |
|  | 343 | 539 | $\begin{array}{ll}10 & 25 \cdot 7\end{array}$ | 8101 | $\mathrm{G}_{5}$ |  | $7 \cdot 52$ |  | +.05 |
|  | 393 | 267 | $10 \quad 26 \cdot 6$ | $76 \quad 14$ | $\mathrm{G}_{5}$ | 5.89 |  |  |  |
|  |  | 539 |  |  |  | $5 \cdot 96$ | 5.92 | . 02 | +.05 |
|  | 406 | 539 | $\begin{array}{ll}10 & 32.9\end{array}$ | $77 \quad 45$ | $\mathrm{A}_{0}$ |  | $7 \cdot 37$ |  |  |
|  | 349 | 267 | $10 \quad 33 \cdot 6$ | $80 \quad 57$ | $\mathrm{A}_{0}$ | $6 \cdot 77$ |  |  |  |
|  |  | 539 |  |  |  | $6 \cdot 73$ | $6 \cdot 75$ | . 01 | +.04 |
|  | 359 | 539 | $10 \quad 34 \cdot 5$ | $77 \quad 56$ | B9 |  | $7 \cdot 32$ |  | -. 25 |
|  | 402 | 539 | $\begin{array}{lll}10 & 43 \cdot 5\end{array}$ | $76 \quad 32$ | $\mathrm{A}_{3}$ |  | 7-26 |  | -. 01 |
|  | 347 | 539 | $\begin{array}{ll}10 & 50 \cdot 7\end{array}$ | 80 | $\mathrm{F}_{3}$ |  | $7 \cdot 71$ |  | +.03 |
|  | 406 | 539 | $10 \quad 51.5$ | $\begin{array}{ll}76 & 15\end{array}$ | Fs |  | $7 \cdot 80$ |  | -. 01 |
| 78 | ¢ 67 | 539 | $10 \quad 52 \cdot 0$ | $78 \quad 18$ | $\mathrm{G}_{5}$ |  | 7-19 |  | -.01 |
|  | 64 | 587 | $11 \quad 04 \cdot 2$ | $88 \quad 11$ | $\mathrm{B}_{8}$ | 7.36 |  |  |  |
|  |  | 588 |  |  |  | $7 \cdot 28$ |  |  |  |
|  |  | 590 |  |  |  | $7 \cdot 42$ |  |  |  |
|  |  | 591 |  |  |  | $7 \cdot 38$ | $7 \cdot 36$ | . 02 | $+.09$ |
|  | 385 | 539 | $11 \quad 16.0$ | $77 \quad 55$ | $\mathrm{F}_{5}$ |  | $7 \cdot 72$ |  |  |
|  | 370 | 585 | $\begin{array}{ll}11 & 54 \cdot 5\end{array}$ | $80 \quad 09$ | $\mathrm{F}_{8}$ |  | $8 \cdot 17$ |  |  |
| 87 | 101 | 588 | $11 \quad 54 \cdot 6$ | $\begin{array}{ll}87 & 33\end{array}$ | $\mathrm{A}_{2}$ |  | $7 \cdot 78$ |  |  |
|  | 389 | 585 | $11 \quad 55 \cdot 1$ | 8128 | Ma |  | 7.98 |  |  |

CATALOGUE OF RESULTS-Continued


CATALOGUE OF RESULTS-Continued


CATALOGUE OF RESULTS-Continued

| Star B.D. | Plate | Position, 1900 |  | Spec. | Magnitude | P.E. | O-P |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | R.A. | Dec. |  |  |  |  |
| - , |  | h m | - , |  | $\begin{array}{ll}7 \cdot 37 & \\ 7 \cdot 41 & 7 \cdot 41\end{array}$ | . 01 |  |
|  | 544 |  |  |  |  |  | -. 02 |
|  | 546 |  |  |  |  |  |  |
| 80519 | 517 | $16 \quad 37 \cdot 7$ | $80 \quad 00$ | $\mathrm{G}_{0}$ | $7 \cdot 62$ | . 03 |  |
|  | 544 |  |  |  | $7 \cdot 52 \quad 7 \cdot 57$ |  | $+.04$ |
| 77628 | 517 | $16 \quad 37 \cdot 8$ | $77 \quad 53$ | $\mathrm{A}_{2}$ | $7 \cdot 70$ | .02 |  |
|  | 543 |  |  |  | $7 \cdot 76$ |  | -. 06 |
|  | 544 |  |  |  | $7 \cdot 61$ |  |  |
|  | 546 |  |  |  | $7 \cdot 68 \quad 7 \cdot 69$ |  |  |
| 78562 | 517 | $\begin{array}{ll}16 & 39.9\end{array}$ | $77 \quad 57$ | $\mathrm{F}_{8}$ | $7 \cdot 43$ |  |  |
|  | 543 |  |  |  | $7 \cdot 52$ |  |  |
|  | 544 |  |  |  | $7 \cdot 38$ | . 02 |  |
|  | 546 |  |  |  | $7 \cdot 41$ |  |  |
| 79508 | 544 | $\begin{array}{ll}16 & 41.8\end{array}$ | $79 \quad 24$ | $\mathrm{F}_{2}$ | 7.98 |  | $+.08$ |
|  | 546. . |  |  |  | $8.03 \quad 8.00$ | . 02 |  |
| 79511 | 517. | $\begin{array}{ll}16 & 43 \cdot 6\end{array}$ | 7906 | $\mathbf{K}_{0}$ | $7 \cdot 64$ | . 02 |  |
|  | 544 |  |  |  | $7 \cdot 52$ |  |  |
|  | 546 |  |  |  | $7 \cdot 58 \quad 7 \cdot 58$ |  |  |
| 74680 | 543 | $16 \quad 44 \cdot 2$ | 74.04 | $A_{2}$ | $7 \cdot 02$ |  |  |
|  | 545 |  |  |  | 7.01 |  |  |
|  | 548 |  |  |  | $6.97 \quad 7.00$ | . 01 | $+.01$ |
| 77634 | 276. | $16 \quad 47 \cdot 5$ | 7741 | $\mathrm{F}_{2}$ | $6 \cdot 27$ | . 02 |  |
|  | 517 |  |  |  | 6.23 |  |  |
|  | 543 |  |  |  | 6.40 |  | $\begin{array}{r} -.03 \\ +.06 \end{array}$ |
|  | 544 | ........ |  |  | 6.44 |  |  |
|  | 545 | ............ |  |  | 6.27 |  |  |
|  | 546 | . ......... |  |  | $6 \cdot 36$ |  |  |
|  | 548. |  |  |  | $6 \cdot 31 \quad 6.33$ |  |  |
| 75608 | 543 | $16 \quad 56 \cdot 0$ | $75 \quad 33$ | $\mathrm{F}_{0}$ | $7 \cdot 09$ |  |  |
| 77639 | 517 | $16 \quad 56.8$ | 7701 | $\mathrm{F}_{0}$ | $7 \cdot 58$$7 \cdot 60$ |  |  |
|  | 543 |  |  |  |  |  | -. 03 |
|  | 544 |  |  |  | $7 \cdot 57$ |  |  |
|  | 546 |  |  |  | $\begin{array}{ll}7 \cdot 57 & 7 \cdot 58\end{array}$ |  |  |
| 77641 | 517 | $17 \quad 00 \cdot 9$ | $77 \quad 48$ | $A_{0}$ | $6 \cdot 59$ | . 02 |  |
|  | 544 |  |  |  | $6 \cdot 67$ |  | $+\cdot 05$ |
|  | 546 |  |  |  | $\begin{array}{ll}6.69 & 6.65\end{array}$ |  |  |
| 79540 | 517 | $17 \quad 25 \cdot 8$ | $79 \quad 24$ | $\mathrm{A}_{6}$ | $7 \cdot 40$ |  |  |
|  | 530 |  |  |  | $7 \cdot 35$ |  | $+\cdot 03$ |
|  | 544 |  |  |  | $7 \cdot 43$ | . 01 |  |
|  | 546 |  |  |  | $\begin{array}{ll}7 \cdot 34 & 7 \cdot 38\end{array}$ |  |  |
| $80 \cdot 544$ | 517 | $17 \quad 27 \cdot 2$ | $80 \quad 14$ | $\mathrm{K}_{2}$ | $7 \cdot 65$ | . 03 |  |
|  | 518 |  |  |  | $7 \cdot 35$ |  |  |
|  | 530 |  |  |  | $7 \cdot 51$ |  | $\pm \cdot 19$ |
|  | 544 |  |  |  | $7 \cdot 55$ |  |  |
|  | 546 |  |  |  | $\begin{array}{ll}7 \cdot 49 & 7 \cdot 51\end{array}$ |  |  |
| 79556 | 518 | $17 \quad 44 \cdot 2$ | $79 \quad 16$ | $\mathrm{F}_{2}$ | $7 \cdot 54$ | . 05 | $-.06$ |
|  | 530 |  |  |  | $\begin{array}{ll}7 \cdot 69 & 7 \cdot 61\end{array}$ |  |  |
| 79564 | 518 | $17 \quad 55 \cdot 6$ | $79 \quad 21$ | $\mathrm{F}_{2}$ | $7 \cdot 76$ | . 00 | -. 01 |
|  | 530 |  |  |  | $\begin{array}{ll}7.77 & 7.76\end{array}$ |  |  |
| 78616 | 518 | $17 \quad 55 \cdot 8$ | $78 \quad 19$ | $\mathrm{K}_{5}$ | $7 \cdot 86$ | . 03 | $+10$ |
|  | 530 |  |  |  | $\begin{array}{ll}7 \cdot 78 & 7 \cdot 82\end{array}$ |  |  |
| 78621 | 518 | $18 \quad 00 \cdot 1$ | 78. 41 | $\mathrm{F}_{3}$ | $7 \cdot 79$ |  |  |

## GATALOGUE OF RESULTS-Concluded

| Star B.D. | Plate | Position, 1900 |  | Spec. | Magnitude | P.E. | O-P |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | R.A. | Dec. |  |  |  |  |
| - ' |  | h m | - , |  |  |  |  |
| 86272 | 530 |  |  |  | $7 \cdot 71 \quad 7 \cdot 75$ | . 03 | $-.06$ |
|  | 587 | $18 \quad 07.8$ | 8700 | $\mathrm{A}_{3}$ | $5 \cdot 86$ |  |  |
|  | 589 |  |  |  | $5 \cdot 79$ |  |  |
|  | 590 |  |  |  | $\begin{array}{ll}5.88 & 5.84\end{array}$ | . 02 | $-.07$ |
| 79587 | 530 | $18 \quad 30 \cdot 6$ | 7909 | $\mathrm{K}_{0}$ | 7.85 |  | $+.06$ |
| 79 590a | 518 | $18 \quad 33 \cdot 1$ | $79 \quad 33$ | $\mathrm{A}_{5}$ | $7 \cdot 56$ |  |  |
|  | 530 | . |  |  | $7 \cdot 62 \quad 7 \cdot 59$ | . 02 | +.01 |
| 77699 | 518 | $18 \quad 34 \cdot 6$ | $77 \quad 28$ | $\mathrm{K}_{0}$ | 6.98 |  |  |
|  | 530 |  |  |  | $7.04 \quad 7.01$ | . 02 | $+.09$ |
| 77702 | 518 | $18 \quad 42 \cdot 3$ | $77 \quad 35$ | $\mathrm{F}_{0}$ | $7 \cdot 19$ |  |  |
|  | 530 |  |  |  | $7 \cdot 20 \quad 7 \cdot 19$ | . 00 | $-.06$ |
| 88112 | 588 | $19 \quad 22.5$ | $88 \quad 59$ | Mb | 7.97 |  |  |
|  | 591 |  |  |  | $7.92 \quad 7.94$ | . 02 | $-.15$ |
| 87205 | 589 | $22 \quad 24 \cdot 2$ | $87 \quad 34$ | $\mathrm{A}_{2}$ | $7 \cdot 34$ |  |  |
|  | 590 | ........... |  |  | 7-34 |  |  |
|  | 591 | 23 4 | 85 | ............ | $\begin{array}{ll}7 \cdot 38 & 7 \cdot 35\end{array}$ | . 01 | $-\cdot 13$ |
| 85399 | $589$ | $23 \quad 24 \cdot 4$ | $85 \quad 52$ | $\mathrm{A}_{6}$ | $6 \cdot 78$ |  |  |
|  | $590$ | $\mid \ldots . . . . . .$ |  | ............... | 6.75 |  |  |
|  | 591 |  |  | ............ | $6.79 \quad 6.77$ | . 01 | $-.02$ |
| 85401 | 591 | $\begin{array}{ll}23 & 27 \cdot 5\end{array}$ |  |  | $7 \cdot 46$ |  |  |
| 86344 | $589$ | $\begin{array}{ll}23 & 27.8\end{array}$ | 8645 | $\mathrm{A}_{4}$ | $5 \cdot 67$ |  |  |
|  | 590 589 |  |  |  | $\begin{array}{ll}5 \cdot 64 & 5 \cdot 65\end{array}$ | . 01 | $+\cdot 03$ |
| 85403 | 589 590 | $23 \quad 30 \cdot 4$ | $85 \quad 38$ | ............ | $7 \cdot 22$ 7.13 |  |  |
|  | 591 |  |  |  | 7-19 7 7.18 | . 02 |  |
| 85409 | 589 | $23 \quad 54 \cdot 8$ | $86 \quad 09$ | ........... | $6 \cdot 71$ |  |  |
|  | $590$ |  |  | ............ | $6 \cdot 64$ |  |  |
|  | 591 |  |  | ............ | $6.67 \quad 6.67$ | . 01 |  |

Column (1) gives the B.D. number of the star.
Column (2) gives the number of each plate on which each star was measured, the date of exposure of each plate being given in Table V.
Columns (3) and (4) give the position for 1900.
Column (5) gives the Harvard spectral type.
Column (6) gives the magnitude derived from each plate and also the mean magnitude for each star.
Column (7) gives the probable error of the mean magnitude.
Column (8) gives the difference between the Ottawa magnitude and that contained in Yerkes Actinometry.
The probable errors given in column (7) were plotted against the distance, $\rho$, of each star from the centre of the plate as a check on the values given in Table II. The resulting curve of the normal places was a line practically parallel to the $\rho$ ordinate, so that the probable error is evidently in no way dependent on the position of the star image on the plate.

Similarly it was shown that there was no connection between the probable error and the spectral type.

The residuals in column (8) were plotted against spectral type, distance of star from centre of plate and magnitude, respectively, no apparent relation existing in any case.

All the plates listed in Table V were measured at least twice and the average taken, the measures being practically identical. The question of obtaining measurable plates, however, has been a problem owing to the proximity of the city lights. Where the exposure exceeded fifteen minutes there were at least five bad plates for every good one. The results, however, agree very closely with the magnitudes of the Yerkes Actinometry, as published by Prof. Parkhurst. The writer had the privilege of studying photometric work under the direction of Prof. Parkhurst and has followed his method as closely as possible.

Dominion Observatory,
Ottama, Canada, September, 1924.


[^0]:    1 Jour. R.A.S.C., Sept.-Oct., 1914.
    ${ }^{2}$ A. J., Vol. 26, p. 244, 1907.
    ${ }^{3}$ Zeitschrift für Instrumentenkunde, Vol. 24, pp. 1, 33 and 97.1904.
    86602-21

[^1]:    H.A. is the hour angle of the centre of the plate at the middle of exposure.
    $z$ is the zenith distance of the centre of the plate at the middle of exposure.
    $q$ is the angle pole-star-zenith and is measured directly from a globe. This angle is necessary in order that $\Delta Z$ may be read graphically from the plates.
    $\frac{\Delta M}{\Delta Z}$ as stated above is from Wirtz's extinction curve and its value, depending on the zenith distance, is given in Table III.
    Column (1) gives the B.D. number of the star.
    Column (2) gives the density of the star image in terms of the scale on the microphotometer.
    Column (3) gives the relative magnitude of each star as read from the mean reduction curve.
    Column (4) gives the distance of each star from the centre of the plate.
    Column (5) gives the difference in zenith distance between each star and the centre of the plate.
    Column (6) gives the correction for reducing each measure to the centre of the plate, being read directly from Table II.
    Column (7) gives the correction for atmospheric absorption being derived from $\Delta Z$ and Table III, which gives $\frac{\Delta M}{\Delta Z}$ for
    Column (8) gives relative magnitudes to which the corrections have been applied.
    Column (9) gives difference between Parkhurst's magnitudes and the relative corrected magnitudes. The mean of the quantities in column (9) gives the quantity to be added to column (8) to give the final magnitudes as in column (10). For this plate the mean of column (9) was $5 \cdot 43$.

    Column (10) gives the residuals, observed magnitudes minus Parikhurst's magnitudes.

